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CS4192- Deep Learning

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# **Table of Contents** 3 Tensor Functions 4 **3.2 Subtraction** \_\_\_\_\_\_ 5 3.6 Elementwise Division 6 3.9 TORCH.NUMEL 9 3.10 Elementwise Exponential 9 3.13 Elementwise less than and Greater than 10 3.14 Calculate the determinate of a Matrix. **3.21 TORCH.PERMUTE.** 16 3.25 TORCH.AUTOGRAD.GRAD. References 20

# 1 What is TORCH.TENSOR?

A torch. Tensor is a multi-dimensional matrix which containing elements of single data. According to the PyTorch documentation, tensors are defined as a data structure which are really similar to the arrays and matrices. In PyTorch tensors used to encode the inputs and outputs of the model and model's parameters. Tensors are similar to NumPy's and ndarrays except they can run on GPUs and hardware accelerators.

# 2 Tensor Data Types

Torch defines there are 10 types with CPU and GPU variants.

The following table is taken from the PyTorch Documentation.

Data type	dtype	CPU tensor	GPU tensor
32-bit floating point	torch.float32 Or torch.float	torch.FloatTensor	torch.cuda.FloatTensor
64-bit floating point	torch.float64 Or torch.double	torch.DoubleTensor	torch.cuda.DoubleTensor
16-bit floating point	torch.float16 Or torch.half	torch.HalfTensor	torch.cuda.HalfTensor
16-bit floating point	torch.bfloat16	torch.BFloat16Tensor	torch.cuda.BFloat16Tensor
32-bit complex	torch.complex32 <b>or</b> torch.chalf		
64-bit complex	torch.complex64 Or torch.cfloat		
128-bit complex	torch.complex128 <b>Or</b> torch.cdouble		
8-bit integer (unsigned)	torch.uint8	torch.ByteTensor	torch.cuda.ByteTensor
8-bit integer (signed)	torch.int8	torch.CharTensor	torch.cuda.CharTensor
16-bit integer (signed)	torch.int16 Or torch.short	torch.ShortTensor	torch.cuda.ShortTensor
32-bit integer (signed)	torch.int32 Or torch.int	torch.IntTensor	torch.cuda.IntTensor
64-bit integer (signed)	torch.int64 Or torch.long	torch.LongTensor	torch.cuda.LongTensor
Boolean	torch.bool	torch.BoolTensor	torch.cuda.BoolTensor
quantized 8-bit integer	torch.quint8	torch.ByteTensor	/
(unsigned)			
quantized 8-bit integer	torch.qint8	torch.CharTensor	/
(signed)			
quantized 32-bit integer	torch.qint32	torch.IntTensor	/
(signed)			
quantized 4-bit integer (unsigned)	torch.quint4x2	torch.ByteTensor	/

# **3 Tensor Functions**

To perform several tensor functions, first two tensors called tensor a and tensor b was created.

#### 3.1 Addition

Using torch.add() function, addition operation was performed on above created tensors.

In here first element of tensor\_a matrix and first element of tensor\_b (number 1 and 5) are added and given as 6. Subsequently, four elements in tensor\_a and four elements in tensor\_b are added and given as [6, 8] and [10, 12] as addition\_result tensor.

```
1 #Creating Tensors
2 tensor_a = torch.tensor([[1,2],[3,4]])
3 tensor_b = torch.tensor(P[5,64,[7,8]))
```

#### 3.2 Subtraction

Using torch.sub() function subtraction was performed on above tensors.

```
# Subtraction
2  subtraction_results = torch.sub(tensor_a,tensor_b)
3  print(f'Subtraction of the Tensor A and Tensor B is: ',subtraction_results)

Subtraction of the Tensor A and Tensor B is: tensor([[-4, -4], [-4, -4]])
```

Similarly to addition, subtraction going through first element of tensor\_a and first element of tensor b, then subsequently goes through other elements of the tensors.

# 3.3 Elementwise Multiplication

Using torch.mul() function, multiplies the corresponding elements of tensor\_a and tensor\_b.

## 3.4 Matrix Multiplication

Consider tensor a and tensor b as matrix format mathematically.

$$A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \quad B = \begin{bmatrix} 5 & 6 \\ 7 & 8 \end{bmatrix}$$

When perform torch.mm() function on tensor\_a and tensor\_b the mat\_mul\_result tensor perform matrix multiplication on tensor\_a and tensor\_b as follows. Let's consider the results stored in variable C.

$$C = \begin{bmatrix} (1.5 + 2.7) & (1.6 + 2.8) \\ (3.5 + 4.7) & (3.6 + 4.8) \end{bmatrix}$$

#### 3.5 Transpose

Torch.transpose(tensor a,0,1) change the dimension of the tensor a

For simplicity transpose function behave like bellow,

$$A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \to A^T = \begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix}$$

#### 3.6 Elementwise Division

Divide corresponding elements of two tensors.

#### 3.7 TORCH.ARANGE

Returns 1-D tensor of size  $\left[\frac{end-start}{step}\right]$  with values from the interval [start, end) taken with common difference step beginning from the start

As an example, let's take torch.arrange(5),

```
1 # TORCH.ARANGE
2 torch.arange(5)
tensor([0, 1, 2, 3, 4])
```

When we consider the size of the 1-D tensor,

Start = 0, end = 5 and step=1 (gap between adjacent points)

Therefore, size of the tensor is,  $size = \left[\frac{5-0}{1}\right] = 5$ 

As few examples bellow,

```
3 torch.arange(1,10)

Hensor([1, 2, 3, 4, 5, 6, 7, 8, 9])
```

```
4 torch.arange(1,10,0.5)

tensor([1.0000, 1.5000, 2.0000, 2.5000, 3.0000, 3.5000, 4.0000, 4.5000, 5.0000, 5.5000, 6.0000, 6.5000, 7.0000, 7.5000, 8.0000, 8.5000, 9.0000, 9.5000])
```

# 3.8 TORCH.SPRACE\_COO\_TENSOR

This function is used to create a sparse tensor in the Coordinate Format (COO). These sparse tensors are useful when dealing with a large matrix which containing many zero elements, they cause to increase the significant amount of memory usage and computational time.

Following example which contained in PyTorch documentation explain the behavior of the sprace function.

```
i = torch.tensor([[0, 1, 1],
                     [2, 0, 2]])
     v = torch.tensor([3, 4, 5], dtype=torch.float32)
 3
 4
     # Create a sparse COO tensor with specified size [2, 4]
 5
     sparse coo tensor 1 = torch.sparse coo tensor(i, v, [2, 4])
 7
     print("Sparse COO Tensor 1:")
 9
     print(sparse_coo_tensor_1)
10
     # Create a sparse COO tensor without specifying size
11
12
     sparse_coo_tensor_2 = torch.sparse_coo_tensor(i, v)
     print("\nSparse COO Tensor 2:")
13
     print(sparse_coo_tensor_2)
14
15
Sparse COO Tensor 1:
tensor(indices=tensor([[0, 1, 1],
                      [2, 0, 2]]),
      values=tensor([3., 4., 5.]),
      size=(2, 4), nnz=3, layout=torch.sparse_coo)
Sparse COO Tensor 2:
tensor(indices=tensor([[0, 1, 1],
                       [2, 0, 2]]),
      values=tensor([3., 4., 5.]),
      size=(2, 3), nnz=3, layout=torch.sparse_coo)
```

- 1. "i" is the tensor which containing non-zero elements. In this example "i" has 2 rows and 3 columns.
- 2. "v" tensor containing the values corresponding to the non-zero elements at the specified indices. The values are of type float32.
- 3. "torch.sparse\_coo\_tensor(i, v, [2, 4])" this part creates a sparse COO tensor using the provided indices 'i' values. And the specified size [2,4], which means given sparse tensor have 2 rows and 4 columns. The non-zero values are placed at specified indices with corresponding value.

#### For the second sparse tensor,

1. The 'i' tensor contains the indices of non-zero elements. In the given example, the maximum index values along each dimension are 2 and 2.

- 2. When creating the sparse COO tensor using torch.sparse\_coo\_tensor(i, v), PyTorch infers the size of the sparse tensor based on the maximum index values in 'i'.
- 3. The resulting sparse\_coo\_tensor\_2 will have a size that is large enough to accommodate the maximum index values. In this case, the inferred size will be [3, 3] because the maximum indices are 2 along both dimensions.

#### 3.9 TORCH.NUMEL

```
1 # TORCH.NUMEL
2 tensor_c =torch.randn(1,100)
3 torch.numel(tensor_c)
100
```

Using this function we can return the number of elements in the certain tensor. For an example tensor\_c was created using rand function which can contain 100 random elements. torch.numel function returns the number of elements in the tensor c.

# 3.10 Elementwise Exponential

This function returns the elementwise exponential values of each element.

# 3.11 Concatenation

This function concatenates the tensors along with specified dimensions.

$$A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \quad B = \begin{bmatrix} 5 & 6 \\ 7 & 8 \end{bmatrix}$$

$$C = \begin{bmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{bmatrix}$$

$$7 \quad 8$$

# 3.12 Reshape the Tensor

This function reshapes the tensor in to new shape.

```
1 # Reshape tensor
2 reshaped_result = tensor_a.view(-1)
3 print(f'reshaped_result :',reshaped_result )
reshaped_result : tensor([1, 2, 3, 4])
```

## 3.13 Elementwise less than and Greater than

These functions subsequently perform elementwise greater than and elementwise less than comparison. As a result, they output True or False.

#### 3.14 Calculate the determinate of a Matrix.

First recreated the tensor a and tensor b with data type float32.

```
[47] 1 tensor_a = torch.tensor([[1, 2], [3, 4]], dtype=torch.float32)
2 tensor_b = torch.tensor([[5, 6], [7, 8]], dtype=torch.float32)
```

```
#Matrix determinant
matrix_determinant = torch.det(tensor_a)
print("Matrix Determinant:")
print(matrix_determinant)

Matrix Determinant:
tensor(-2.)
```

This function calculates the determinant of the tensor a and save it into matrix determinant tensor.

#### 3.15 TORCH.FULL

This function creates a tensor for the given size and filled with the given value. Tensor's data type will infer from the fill value.

```
1 #TORCH.FULL
2 torch.full((2,2),5)
tensor([[5, 5],
[5, 5]])
```

# 3.16 TORCH.MASKED SELECTED

To get an idea about this function, first 2X2 tensor was created and named as tensor\_d. Then create a mask to get the values greater than 0.5. These masks contained Boolean format data. Then a selected value variable was created and using the function torch.masked\_selected() all the values which are greater than 0.5 were stored in the tensor.

# 3.17 Batch Matrix Multiplication

```
1 # Batch matrix multiplication
     2 batched_matrix_a = torch.rand(3, 2, 2)
     3 batched_matrix_b = torch.rand(3, 2, 2)
     4 print(batched_matrix_a,'\n',batched_matrix_b,'\n')
     5 batched_matrix_multiply_result = torch.bmm(batched_matrix_a, batched_matrix_b)
     6 print("\nBatch Matrix Multiplication Result:")
     7 print(batched_matrix_multiply_result)

→ tensor([[[0.8176, 0.9138],
             [0.2785, 0.1611]],
            [[0.9226, 0.8993],
             [0.0601, 0.2610]],
            [[0.2041, 0.5310],
             [0.8635, 0.5005]]])
     tensor([[[0.7942, 0.3209],
             [0.1028, 0.8022]],
            [[0.4398, 0.6017],
             [0.8370, 0.5187]],
            [[0.0945, 0.6098],
             [0.7600, 0.8448]]])
    Batch Matrix Multiplication Result:
    tensor([[[0.7432, 0.9955],
             [0.2377, 0.2186]],
            [[1.1584, 1.0215],
             [0.2449, 0.1715]],
            [[0.4228, 0.5730],
             [0.4620, 0.9493]])
```

Two tensors were created calling batch\_matrix\_a and batch\_matrix\_b. each tensor containing 3 matrices, size of 2x2. **torch.bmm** perform batch matrix multiplication between two batches. Each 2x2 matrix in batched\_matrix\_a multiply with corresponding 2x2 matrices in batched\_matrix\_b. The result matrix named batch\_matrix\_multiplication\_result containg 3, 2x2 matrices.

#### 3.18 TORCH.VSPLIT

```
1 # TORCH.VSPLIT
    # Create a 4x4 tensor
 3
    t = torch.arange(16.0).reshape(4, 4)
    print(t)
    # Split the tensor into two along the rows
    split_result_1 = torch.vsplit(t, 2)
8 print(split_result_1)
10 # Split the tensor into three along the rows with specified indices
split_result_2 = torch.vsplit(t, [3, 6])
12 print(split_result_2)
tensor([[ 0., 1., 2., 3.], [ 4., 5., 6., 7.],
       [ 8., 9., 10., 11.],
       [12., 13., 14., 15.]])
(tensor([[0., 1., 2., 3.],
       [4., 5., 6., 7.]]), tensor([[ 8., 9., 10., 11.], [12., 13., 14., 15.]]))
```

First created a 4x4 tensor which contained values ranging from 0 to 15. **torch.vslpit(t,2)** function splits the tensor t in to 2 tensors along with the rows and save it as split\_result\_1. Then second variable named split\_result\_2 created and using the **torch.vslpit(t,[3,6])** function, it split in to 3 tensors along with rows and split points are specified as 3 and 6.

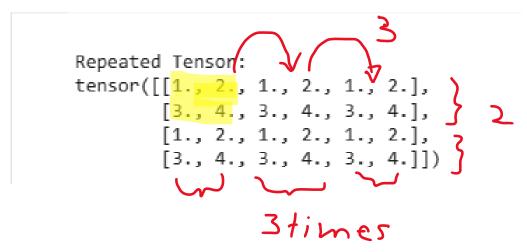
#### 3.19 Repeat Tensor Along with the Dimension

$$A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$
 Tensor\_a is 2x2 tensor.

The 'tensor a.repeat(2, 3)' will be perform as bellow,

1. The first dimension (rows) is repeated 2 times, and the second dimension (columns) is repeated 3 times.

2. The resulting tensor has a shape of (4, 6) because 2 times 2 along the rows and 3 times 2 along the columns.



## 3.20 Cumulative Product along the Dimension

- Along the specified dimension (dim=1), the cumulative product is computed for each row.
- For the first row [2, 3, 4], the cumulative product along the columns is [2, 2\*3, 2\*3\*4] resulting in [2, 6, 24].
- For the second row [5, 2, 1], the cumulative product along the columns is [5, 5\*2, 5\*2\*1] resulting in [5, 10, 10].

#### 3.21 TORCH.PERMUTE.

```
# TORCH.PERMUTE
 2
    x = torch.randn(2, 3, 5)
 3 print(x)
    print(x.size(),'\n')
 5
    torch.permute(x, (2, 0, 1))
tensor([[[ 1.5880, 0.7639, 0.5755, 0.2814, -0.2978],
         [ 0.5198, -0.9649, -0.7114, -0.7560, 0.8767],
        [-0.3643, 0.2914, 1.1468, 0.7619, -0.7350]],
       [[ 0.2616, 1.0866, 0.5497, 0.8726, -0.6225],
        [ 0.6467, 0.6140, -0.2402, 0.7382, -0.1878],
        [ 0.8570, -0.4697, 0.6649, -0.3207, 1.0428]]])
torch.Size([2, 3, 5])
tensor([[[ 1.5880, 0.5198, -0.3643],
        [ 0.2616, 0.6467, 0.8570]],
       [[ 0.7639, -0.9649, 0.2914],
        [ 1.0866, 0.6140, -0.4697]],
       [[ 0.5755, -0.7114, 1.1468],
        [ 0.5497, -0.2402, 0.6649]],
       [[ 0.2814, -0.7560, 0.7619],
        [ 0.8726, 0.7382, -0.3207]],
       [[-0.2978, 0.8767, -0.7350],
         [-0.6225, -0.1878, 1.0428]]])
```

## torch.permute(x, (2, 0, 1)).size()

This uses **torch.permute** to permute the dimensions of the tensor. The argument (2, 0, 1) specifies the new order of dimensions. The result is a tensor with dimensions [5, 2, 3].

So, the original tensor x has dimensions [2, 3, 5], and after permuting the dimensions using (2, 0, 1), the resulting tensor has dimensions [5, 2, 3]. The order of dimensions is changed accordingly.

#### 3.22 TORCH.WHERE

- torch.where is used for element-wise conditional selection in PyTorch.
- The function takes three arguments: **condition**, **x**, and **y**.
  - **condition**: A boolean tensor of the same shape as **x** and **y**. The values of **x** are selected where **condition** is **True**, and the values of **y** are selected where **condition** is **False**.
  - x: The tensor whose elements are selected where the condition is **True**.
  - y: The tensor whose elements are selected where the condition is **False**.
  - The result tensor has the same shape as **condition**, **x**, and **y**

- The condition tensor has the values [[True, False], [False, True]].
- The elements of x are selected where **condition** is **True**, and the elements of y are selected where **condition** is **False**.
- The resulting tensor is [[1, 6], [7, 4]], where [1, 6] corresponds to selecting elements from x, and [7, 4] corresponds to selecting elements from y based on the condition.

#### 3.23 TORCH.NN.FUNCTIONAL.PAD

- **torch.nn.functional.pad** takes two arguments: the input tensor and a tuple specifying the padding for each dimension.
- In the example, the input tensor is a 2x3 tensor.
- The tuple (1, 2) indicates padding of 1 element on the left and 2 elements on the right along the second dimension.
- The resulting padded tensor will have a shape of (2, 3 + 1 + 2) = (2, 6)
- Zeros are added on the left and right sides of each row to achieve the specified padding.
- The first and last columns are padded with zeros according to the specified padding configuration.

```
tensor([[0, 1, 2, 3, 0, 0], [0, 4, 5, 6, 0, 0]])
```

## 3.24 TORCH.ARGMAX

- torch.argmax returns the indices of the maximum values in a tensor.
- By default, it returns a single index corresponding to the flattened array of the input tensor. This is useful when you want the index of the overall maximum value.

```
# Create a tensor
input_tensor = torch.tensor([[3, 1, 4], [1, 5, 9]])

# Find the indices of the maximum values along a specified axis (default: last axis)
max_indices = torch.argmax(input_tensor)
print(max_indices)

tensor(5)
```

#### 3.25 TORCH.AUTOGRAD.GRAD

```
# Define a tensor and create a computation graph
    x = torch.tensor(2.0, requires_grad=True)
    y = x ** 2
    z = y + 3

# Compute the gradient of z with respect to x using torch.autograd.grad
    gradient = torch.autograd.grad(z, x)
    print("Gradient:", gradient[0].item())

Gradient: 4.0
```

- torch.autograd.grad is used to compute the gradient of a scalar-valued tensor (z in this case) with respect to other tensors (x in this case).
- The input to torch.autograd.grad is the target tensor (z) and the source tensor (x).
- The result is a tuple containing the gradient with respect to each source tensor. In this example, **gradient[0]** contains the gradient with respect to **x**.
- The requires grad=True flag is set on x to track operations for automatic differentiation.
- The gradient of  $z = x^2 + 3$  with respect to x is 2 \* x = 2 \* 2 = 4.0

# References

[1]

 $\hbox{``torch--- PyTorch\ 1.12\ documentation,''} \ \underline{\textit{https://pytorch.org/docs/stable/torch.html}}$ 

[2]

"Tensor Math Operations - Deep Learning with PyTorch 4," www.youtube.com. https://www.youtube.com/watch?v=Ta3z9vZaoMc&t=167s (accessed Mar. 08, 2024).

# **Appendix**

Colab Code