

The calendar indicates which script chapters you should study in conjunction with each lecture. The exercises are designed to enhance your understanding of the lecture material and prepare you for the mini-tests and the final exam. Additional exercises can be found at the end of each chapter in the script.

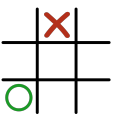
The difficulty of an exercise on the sheet is determined by the number of annotated 'X' and 'O' marks in the tic-tac-toe field, with four levels (1-4) increasing by one mark per level.

## 1 MIPS

### Exercise 3.1:

Write two assembler programs which both compute *powers of three*. The  $n$ -th power of three is defined by:

$$3^n = \begin{cases} 1 & \text{if } n = 0 \\ 3 \cdot 3^{(n-1)} & \text{if } n > 0 \end{cases}$$



Example:

$$3^4 = 3 \cdot 3^3 = \dots = 3 \cdot (3 \cdot (3 \cdot (3 \cdot 1))) = 81$$

The first program `pow3_rec` shall compute the  $n$ -th power of three recursively as in the recursive definition above. To this end, the program calls itself. The second variant `pow3_iter` must compute the  $n$ -th power of three without calling other subroutines by using a loop. Consider the additional precautions (setting up the call frame, saving registers, etc.) which the recursive definition requires. The parameter  $n$  is passed via register `$a0`, the result must be passed back to the caller via register `$v0`.

*Hint:* Remember the example program from the lecture which calculates the factorial.

### Solution

Recursive version:

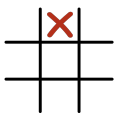
```
1 .text
2     .globl pow3_rec
3
4 pow3_rec:
5     addi $sp, $sp, -8           # allocate some space in the stack
6     sw $ra, 4($sp)             # store the address where we need to jump back
7     sw $a0, 0($sp)             # store n
8
9     beq $a0, $zero, base_case  # base case if $a0 is zero
10    addi $a0, $a0, -1           # we call pow3_(n-1)
11    jal pow3_rec
12
13    mul $v0, $v0, 3              # multiply current result by 3
14
15    lw $a0, 0($sp)              # load n stored before
16    lw $ra, 4($sp)              # load return address stored before
17    addi $sp, $sp, 8            # reset stack pointer
18    jr $ra                      # return to caller
19
20 base_case:
21    li $v0, 1                   # (could be avoided and code shortened)
22                                # base case
23    lw $a0, 0($sp)              # load n stored before
24    lw $ra, 4($sp)              # load return address stored before
25    addi $sp, $sp, 8            # reset stack pointer
26    jr $ra                      # return to caller
```

Iterative version:

```
1 .text
2     .globl pow3_iter
3
4 pow3_iter:
5     li $v0, 1           # start at 1
6     li $t0, 0           # initialize loop counter
7
8 loop:
9     beq $t0, $a0, end    # end if loop counter $t0 equals $a0
10    mul $v0, $v0, 3       # multiply by 3
11    addi $t0, $t0, 1      # increase loop counter
12    j loop               # loop
13
14 end:
15    jr $ra               # return to return address
```

### Exercise 3.2:

Konrad Klug has been assigned the task to carry out a complex mathematical calculation. Since he will often need the first  $n$  Fibonacci numbers for this task, he wants to store as many of them as possible in an array so that he does not need to recompute them from scratch each time. Unfortunately, he does not know how to implement this yet. The Fibonacci numbers are calculated as follows:



$$\begin{aligned} F_0 &:= 0 \\ F_1 &:= 1 \\ F_n &:= F_{n-1} + F_{n-2} \quad \text{for } n \in \mathbb{N} \wedge n \geq 2 \end{aligned}$$

Help Konrad Klug by implementing the storage of the Fibonacci numbers in a *word* array. You are given the base address of the array in register  $\$a0$  and the address one word behind the last element of the array in register  $\$a1$ .

### Solution

```
1 .text
2     .globl fib
3     # a0 Base address of the array
4     # a1 One past-the-end address
5
6 fib:
7     # replace first element
8     li $t0, 0
9     sw $t0, 0($a0)
10    # replace second element
11    li $t0, 1
12    sw $t0, 4($a0)
13    # increase address
14    addiu $a0, $a0, 8
15
16 loop:
17    # loop condition
18    bge $a0, $a1, end
19    # load previous elements
20    lw $t0, -4($a0)
21    lw $t1, -8($a0)
22    # calculate next element
23    addu $t0, $t0, $t1
```

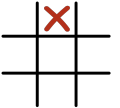
```

24     # store new element
25     sw $t0 0($a0)
26     # increase address
27     addiu $a0 $a0 4
28     j loop
29
30 end:
31     jr $ra

```

### Exercise 3.3:

Look at the following code implementing insertion sort.



1. Fill in the gaps such that swap swaps two elements in an array. The addresses of the elements to be swapped are passed via the registers \$a0 and \$a1.

```

1 .text
2 swap:
3     # $a0, $a1 addresses of the elements to be swapped
4     lw ---- ----
5     lw ---- ----
6     sw ---- ----
7     sw ---- ----
8     jr $ra

```

2. Now fill in the gaps such that insertion\_sort follows the calling convention.

```

1 insertion_sort:
2     # $a0 base address of the array
3     # $a1 last address of the array
4     beq $a0 $a1 end
5     move $t0 $a0
6
7     loop:
8         addiu $t0 $t0 4
9         bgt $t0 $a1 end
10        lw $t5 ($t0)
11        move $t1 $t0
12
13    loop_2:
14        beq $t1 $a0 loop
15
16        addiu $t2 $t1 -4
17        lw $t6 ($t2)
18        ble $t6 $t5 loop
19
20        addiu $sp $sp -32
21        sw ---- ----
22        sw ---- ----
23        sw ---- ----
24        sw ---- ----
25        sw ---- ----
26        sw ---- ----
27        sw ---- ----
28        sw ---- ----
29
30        move $a0 $t1
31        move $a1 $t2
32

```

```

33     jal swap
34
35     lw ---- ----
36     lw ---- ----
37     lw ---- ----
38     lw ---- ----
39     lw ---- ----
40     lw ---- ----
41     lw ---- ----
42     lw ---- ----
43     addiu $sp $sp 32
44
45     addiu $t1 $t1 -4
46     b loop_2
47
48 end:
49     jr $ra

```

## Solution

```

1 # a)
2 .text
3 swap:
4 # $a0, $a1 addresses of elements to be swapped
5 lw $t0 ($a0)
6 lw $t1 ($a1)
7 sw $t0 ($a1)
8 sw $t1 ($a0)
9 jr $ra
10
11 # b)
12 insertion_sort:
13 # $a0 base address of the array
14 # $a1 last address of the array
15 beq $a0 $a1 end
16 move $t0 $a0
17
18 loop:
19     addiu $t0 $t0 4
20     bgt $t0 $a1 end
21     lw $t5 ($t0)
22     move $t1 $t0
23
24 loop_2:
25     beq $t1 $a0 loop
26
27     addiu $t2 $t1 -4
28     lw $t6 ($t2)
29     ble $t6 $t5 loop
30
31     addiu $sp $sp -32
32     sw $a0 0($sp)
33     sw $a1 4($sp)
34     sw $t0 8($sp)
35     sw $t1 12($sp)
36     sw $t2 16($sp)
37     sw $t5 20($sp)
38     sw $t6 24($sp)
39     sw $ra 28($sp)
40

```

```

41     move $a0 $t1
42     move $a1 $t2
43
44     jal swap
45
46     lw $a0 0($sp)
47     lw $a1 4($sp)
48     lw $t0 8($sp)
49     lw $t1 12($sp)
50     lw $t2 16($sp)
51     lw $t5 20($sp)
52     lw $t6 24($sp)
53     lw $ra 28($sp)
54     addiu $sp $sp 32
55
56     addiu $t1 $t1 -4
57     b loop_2
58
59 end:
60     jr $ra

```

### Exercise 3.4: Nested Function calls

Take a look at the following MIPS program.

```

.text
.globl confusion
confusion:

...

and     $t0 $t0 $zero
or      $t0 $t0 $a0
add     $t1 $a1 $t0
or      $s1 $t0 $t1

move    $s0 $t0

...

jal     mystery

...

add     $t0 $t1 $v0
add     $v0 $a0 $t0

...

jr      $ra

```

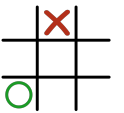


Figure 1: A program disregarding calling conventions.

Complete the program following the calling conventions. Be memory efficient, thus only store necessary registers.

## Solution

```
.text
.globl confusion
confusion:
    # prologue
    add    $sp $sp -8
    sw     $s0 ($sp)
    sw     $s1 4($sp)

    and    $t0 $t0 $zero
    or     $t0 $t0 $a0
    add    $t1 $a1 $t0
    or     $s1 $t0 $t1

    move   $s0 $t0

    # store the registers
    add    $sp $sp -12
    sw     $t1 ($sp)
    sw     $a0 4($sp)
    sw     $ra 8($sp)

    jal    mystery

    # load back the registers
    lw     $t1 ($sp)
    lw     $a0 4($sp)
    lw     $ra 8($sp)
    add    $sp $sp 12

    add    $t0 $t1 $v0
    add    $v0 $a0 $t0

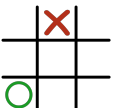
    # epilogue
    lw     $s0 ($sp)
    lw     $s1 4($sp)
    add    $sp $sp 8

    jr     $ra
```

## Exercise 3.5:

In this exercise you must find the errors in a MIPS program (see *buggy.zip*). Find the errors and correct them. There are two errors per exercise. First, try to solve the exercise without using MARS.

1. In `buggyProgram1.asm`, all numbers in an array are supposed to be added and the results should be printed to the console.
2. A fellow student asks for your help. He tried to write down the faculty program from the lecture by himself, but for some reason it does not work. His attempt can be found in `buggyProgram2a.asm` and `buggyProgram2b.asm`.



*Remark:* To test these programs in MARS, copy them into the same directory and select the options *Assemble all files in directory* and *Initialize Program Counter to global 'main' if defined* in the settings of MARS.

## Solution

1. The end address of the array is incorrect. A word is four bytes, to access the last element of the array we need to point to the address behind the fourth word, i.e. address of the first word plus  $4 * 4 = 16$ .

```
1 addiu $a2 $a1 4      # wrong
2 addiu $a2 $a1 16     # correct
```

The data is stored as words, but is loaded as bytes. To load words, one must use `lw` instead of `lb`.

```
1 lb $t0 0($a1)        # wrong
2 lw $t0 0($a1)        # correct
```

2. The subroutine `fac` did not make its definition visible to external programs, therefore it cannot be used by `main`.

```
1 .globl fac           # insert below .text
```

The loop counts from `n` to 0, which causes the result to be always zero.

```
1 bgez $a0 loop        # wrong
2 bgtz $a0 loop        # correct
```

## 2 Introduction to C

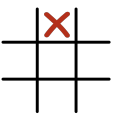
### Exercise 3.6:

1. Write a C program which declares two variables of type `int`, assigns arbitrary values to these variables, and then prints both variable values to the console. To this end, create a file `main.c` and implement the `main` function.

Create an executable file `prog` and execute the program.

2. Extend the file `main.c` from part a) with a function `max` which receives two `int` arguments and returns the maximum of both values.
3. Extract the function written in b) into its own translation unit `max.c`. Create a header file `max.h` to make the signature of the function available to `main`.

Create an executable `prog` and execute the program.



## Solution

1. Program:

```
1 #include <stdio.h>
2
3 int main() {
4     int a = 10;
5     int b = 20;
6
7     printf("a: %d\n", a);
8     printf("b: %d\n", b);
9
10    return 0;
11 }
```

Create an executable and run it:

```
1$ cc -o main.o -c main.c
2$ cc -o prog main.o
3$ ./prog
```

In short:

```
1$ cc main.c -o prog
2$ ./prog
```

## 2. Function max:

```
1#include <stdio.h>
2
3int max(int x, int y) {
4    if(x > y) {
5        return x;
6    } else {
7        return y;
8    }
9}
10
11int main() {
12    int a = 10;
13    int b = 20;
14
15    int res = max(a, b);
16
17    printf("Maximum of a and b: %d\n", res);
18
19    return 0;
20}
```

Create executable: Same as above.

## 3. With a header file:

max.h

```
1#ifndef MAX_H
2#define MAX_H
3
4int max(int x, int y);
5
6#endif
```

max.c

```
1#include "max.h"
2
3int max(int x, int y) {
4    if(x > y) {
5        return x;
6    } else {
7        return y;
8    }
9}
```

main.c

```
1#include <stdio.h>
2#include "max.h"
3
4int main() {
5    int a = 10;
```



```

6     int b = 20;
7
8     int res = max(a, b);
9
10    printf("Maximum of a and b: %d\n", res);
11
12    return 0;
13}

```

Create executable and run it:

```

1$ cc -o main.o -c main.c
2$ cc -o max.o -c max.c
3$ cc -o prog main.o max.o
4$ ./prog

```

In short:

```

1$ cc main.c max.c -o prog
2$ ./prog

```

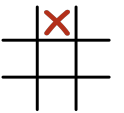
### Exercise 3.7:

Analyze and understand the following C program:

```

1#include <stdio.h>
2
3int main() {
4    for (int i = 1; i < 10; i++) {
5        if ((i % 2) == 0) {
6            printf("The number %i is ... \n", i);
7        } else {
8            printf("The number %i is ... \n", i);
9        }
10    }
11    return 0;
12}

```



1. What is the program output? How can you reasonably replace the ellipses (...) in the printf statements?
2. Modify the program such that it prints the numbers in range 0 to 20 (inclusive).
3. Can you modify the loop in such a way that the numbers from subtask (2.) are printed in reverse order?

### Solution

1. The first ellipsis should be replaced with “even” and the second ellipsis with “odd”. The program then prints the following:

```

1 The number 1 is odd.
2 The number 2 is even.
3 The number 3 is odd.
4 The number 4 is even.
5 The number 5 is odd.
6 The number 6 is even.
7 The number 7 is odd.
8 The number 8 is even.
9 The number 9 is odd.

```

## 2. Modified program:

```
1#include <stdio.h>
2
3int main() {
4    for (int i = 0; i <= 20; i++) {
5        if ((i % 2) == 0) {
6            printf("The number %i is even\n", i);
7        } else {
8            printf("The number %i is odd\n", i);
9        }
10    }
11    return 0;
12}
```

## 3. With print order reversed:

```
1#include <stdio.h>
2
3int main() {
4    for (int i = 20; i >= 0; i--) {
5        if ((i % 2) == 0) {
6            printf("The number %i is even\n", i);
7        } else {
8            printf("The number %i is odd\n", i);
9        }
10    }
11    return 0;
12}
```

## Exercise 3.8:

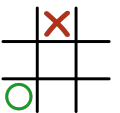
Konrad Klug wants to compute some integer calculations, but he lost his calculator.

He has already found some code that reads the inputs from the user and outputs the result, but he doesn't know how to implement the calculation.

Help him, by implementing the `calculate` function. The function receives two integers (`x` and `y`) and a character `op` representing the operation.

Your calculator should support addition (+), subtraction (-), multiplication (\*) and division (/).

```
1#include <stdio.h>
2#include <stdlib.h>
3#include <string.h>
4
5int calculate(int x, char op, int y) {
6    // Add your code here
7    return 0;
8}
9
10int main(int argc, char* argv[]) {
11    int x = 0;
12    int y = 0;
13    char op = 0;
14    char* s = calloc(64, sizeof(char));
15
16    printf("Please enter the expression to be calculated: ");
17    scanf("%d%c%d", &x, &op, &y);
18
19    sprintf(s, "%d%c%d=", x, op, y );
```



```

20     int slen = strlen(s);
21     s += slen;
22
23     if (!((op == '+') || (op == '-') || (op == '*') || (op == '/'))) {
24         sprintf(s - slen, "Invalid input!");
25     } else {
26         sprintf (s, "%d", calculate(x, op, y));
27     }
28
29     s -= slen;
30     printf( "%s\n", s);
31
32     free(s);
33     return 0;
34 }

```

## Solution

```

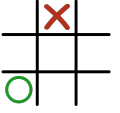
1 #include <stdio.h>
2 #include <stdlib.h>
3 #include <string.h>
4
5 int calculate(int x, char op, int y) {
6     switch(op){
7         case '+':
8             return (x + y);
9         case '-':
10            return (x - y);
11        case '*':
12            return (x * y);
13        case '/':
14            return (x / y);
15        default:
16            return -1;
17    }
18 }
19
20 int main(int argc, char* argv[]) {
21     int x = 0;
22     int y = 0;
23     char op = 0;
24     char* s = calloc(64, sizeof(char));
25
26     printf("Please enter the expression to be calculated: ");
27     scanf("%d%c%d", &x, &op, &y);
28
29     sprintf (s,"%d%c%d=", x, op, y );
30     int slen = strlen(s);
31     s += slen;
32
33     if (!((op == '+') || (op == '-') || (op == '*') || (op == '/'))) {
34         sprintf(s - slen, "Invalid input!");
35     } else {
36         sprintf (s, "%d", calculate(x, op, y));
37     }
38
39     s -= slen;
40     printf( "%s\n", s);
41
42     free(s);

```

```
43     return 0;
44 }
```

### Exercise 3.9:

This exercise is all about dealing with a variety of pesky error messages one might encounter while programming in C.



1. Analyse the following error messages and describe the issue or what could have triggered them.

(a) `main.c:9:7: error: assignment of read-only variable 'a'`

(b) `main.c:12:5: error: too few arguments to function 'g'`

(c) `main.c:16:5: error: called object 'b' is not a function  
or function pointer`

(d) `main.c:19:5: warning: implicit declaration of function 'h'  
[-Wimplicit-function-declaration]  
/usr/bin/ld: /tmp/ccsVArgH.o: in function 'main':  
main.c:(.text+0x3c): undefined reference to 'h'  
collect2: error: ld returned 1 exit status`

(e) `main.c:23:8: error: lvalue required as left operand of assignment`

(f) `main.c:26:6: error: #error "The cake is a lie!"`

(g) `/usr/bin/ld: /tmp/cctUcBj6.o: in function 'foo':  
foo.c:(.text+0x0): multiple definition of 'foo';  
/tmp/cc01IbiT.o:main.c:(.text+0x0): first defined here  
/usr/bin/ld: /tmp/cckGDjLC.o: in function 'foo':  
bar.c:(.text+0x0): multiple definition of 'foo';  
/tmp/cc01IbiT.o:main.c:(.text+0x0): first defined here  
/usr/bin/ld: /tmp/cckGDjLC.o: in function 'bar':  
bar.c:(.text+0xf): multiple definition of 'bar';  
/tmp/cc01IbiT.o:main.c:(.text+0xf): first defined here  
collect2: error: ld returned 1 exit status`

2. For each error, write a small program that generates such a compiler message.

### Solution

1. (a) Constant expressions, for example constant variables or literals, can not be assigned new values.
- (b) Calling functions with the wrong number of arguments will result in an error. One exception to this are variadic functions, i.e. functions that allow for an arbitrary amount of arguments to be passed.
- (c) This error is generated when you try to call something as a function that is not callable, for example when the name of a variable is confused with that of a function.
- (d) An undefined reference means that the definition of an object can not be found. While the problem could simply be a misspelling, more commonly this occurs if files are not linked properly.
- (e) Some operators require (modifiable) lvalues as arguments, which are expressions that designate an object (e.g. a variables). Providing rvalues (e.g. literals or temporary return values) instead will result in this error.
- (f) It is possible to show user-defined diagnostics with the `#error` and `#warning` preprocessor directives.

- (g) Multiple definitions are usually the consequence of definitions occurring in header as opposed to source files. If such a header file is included more than once, such definitions will exist more than once because the `#include` directive just pastes the contents of the supplied header file.

```
2. #include <stdio.h>

int g(int arg) { return arg; }

int main()
{
    // 1
    const int a = 1;
    a = 2;

    // 2
    g();

    // 3
    int b = 42;
    b(42);

    // 4
    h();

    // 5
    int c = 1;
    42 = c;

    // 6
    #error "The cake is a lie!"

    return 0;
}
```

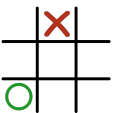
### Exercise 3.10: FooBar Game

1. The rules of the game are as follows:

- (a) Before the game starts, two parameters are set.
- (b) The goal of the game is to count upwards starting from 1 trying to reach as high a number as possible.
- (c) Each round the game asks for input and the player has to enter either the next number, `foo`, `bar` or `foobar`.
- (d) Which of these depends on the current number:
  - i. If the current number is only divisible by the first parameter, the player has to enter `foo`
  - ii. If it is only divisible by the second parameter, the player has to enter `bar`
  - iii. If it is divisible by both, the player has to enter `foobar`
  - iv. Otherwise, the current number must be entered.
- (e) The game ends as soon as the player makes a mistake.

For example, if the parameters are 3 and 4 the first few steps would be

```
Please provide your input: 1
Please provide your input: 2
Please provide your input: foo
Please provide your input: bar
Please provide your input: 5
```



2. Implement the following function, where x and y serve as the parameters of the game.

```
1#include <stdio.h>
2#include <memory.h>
3
4void foobar(int x, int y){
5    /* TODO: Implement FooBarGame */
6}
```

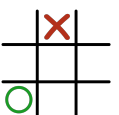
## Solution

```
1#include <stdio.h>
2#include <memory.h>
3
4void foobar(int x, int y){
5    int current = 1;
6    char input[10];
7    char expected[10];
8    printf("FooBar-Game\nParameters: %d and %d\n", x, y);
9    while(1){
10        printf("Please provide your input: ");
11        scanf("%s", input);
12        if (current % x == 0 && current % y == 0){
13            strcpy(expected, "foobar");
14        }
15        else if (current % x == 0){
16            strcpy(expected, "foo");
17        }
18        else if (current % y == 0){
19            strcpy(expected, "bar");
20        }
21        else {
22            snprintf(expected, 10, "%d", current);
23        }
24        if (strcmp(input, expected)){
25            printf("Failure-Expected: %s", expected);
26            return;
27        }
28        current += 1;
29    }
30}
```

## Exercise 3.11:

Dieter Schlau just saw this C program online and wants to find out, what exactly it does. Help him by creating an execution trace for the program and calculate what it outputs by hand. You can use a computer afterwards to verify your result

```
1#include <stdio.h>
2
3char func1(int arg1, int arg2) {
4    int res = 0;
5    int i = arg1;
6    while (i > 0) {
7        res = res + arg2;
8        i = i - 1;
9    }
10    return res;
11}
```



```

12
13 int main(int argc, char* argv[]) {
14     int a;
15     int b;
16     a = 3;
17     b = 7;
18     // b = 8;
19     int c;
20     int d;
21     c = (5 - 3) + (a - 2);
22     d = b + b;
23     a = func1(c, d);
24     printf("The answer is %d!\n", a);
25     return 0;
26 }

```

## Solution

Output of the program:

Step	Line	a	b	c	d	side effect
1	14	-	-	-	-	
2	15	?	-	-	-	
3	16	?	?	-	-	
4	17	3	?	-	-	
5	18	3	7	-	-	
6	19	3	7	-	-	
7	20	3	7	?	-	
8	21	3	7	?	?	
9	22	3	7	3	?	
10	23	3	7	3	14	call func1 ->
11	24	42	7	3	14	
12	25	42	7	3	14	print a
13	26	42	7	3	14	termination

Table 1: Call to main

Step	Line	arg1	arg2	res	i	side effect
1	4	3	14	-	-	
2	5	3	14	0	-	
3	6	3	14	0	3	
4	7	3	14	0	3	
5	8	3	14	14	3	
6	9	3	14	14	2	
7	6	3	14	14	2	
8	7	3	14	14	2	
9	8	3	14	28	2	
10	9	3	14	28	1	
11	6	3	14	28	1	
12	7	3	14	28	1	
13	8	3	14	42	1	
14	9	3	14	42	0	
15	6	3	14	42	0	
16	10	3	14	42	0	return with 42

Table 2: Call to func1