Algorithm 1: tGMM

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Input:
           x \in R^{T \times d}: the time-series data.
          \mu^0 \in R^{d \times c}: an initial guess at the means. \Sigma^0 \in R^{d \times d \times C}: an initial guess at the covariances.
          \pi \in R^{T \times C}: \sum_{c \in [C]} \pi[., c] = 1: pi-vector indicating the weighted contributions of each
           tol > 0: the tolerance for defining convergence.
     Result:
           \mu^n \in \mathbb{R}^{d \times c}: the tGMM estimated means.
           \Sigma^n \in \mathbb{R}^{d \times d \times c}: the tGMM estimated true covariance matrices.
  1 ll = loglikelihood(x, \mu^0, \Sigma^0, \pi)
  \mathbf{2} converged = FALSE
 \mathbf{3} while converged = FALSE do
           // E step
           for t in 1:T do
  4
                for c in 1:C do
 5
                 \tilde{w}_{tc} = \frac{1}{s} \pi_{tc} \mathcal{N}(x_t, \mu_c \Sigma_c)
 6
                \mathbf{end}
  7
          \mathbf{end}
 8
          \bar{\tilde{w}} = \sum_{c=1}^{C} \tilde{w}(.,c)
w_{tc} = \bar{\tilde{w}}^{-1} \tilde{w}_{tc}
  9
10
          \hat{\tilde{w}} = \sum_{t=1}^{T} \tilde{w}(t,.)
11
           // M step
           for c in 1:C do
12
               \mu_c = \hat{\tilde{w}}^{-1} w_c^T x
13
             \Sigma_c = \sum_{t=1}^{T} \hat{\tilde{w}}^{-1} w_{tc} (x_t - \mu_c)^T (x_t - \mu_c)
14
15
           newll = loglikelihood(x, \mu, \Sigma, \pi)
16
           if newll - ll > tol then
17
               ll = newll
18
19
           else
               converged = TRUE
20
          end
21
22 end
23 loglikelihood(x, \theta^i) \leftarrow \sum_{i=1}^{nt} \sum_{c=1}^{nc} log(\pi_{ic}) + log(\mathcal{N}(x_i|\mu_c^i, \Sigma_c^i))
```