Jerk, Snap, Crackle & Pop.

Big Picture:

Map the problem onto an *image recognition/classification problem* that we know how to solve using a convolutional neural network or some other deep learning technique.

Key Insight: The following analogy gives a mapping

telematics problem → handwriting association/classification' problem.

- A trip can be represented as a trajectory on an image contained in a grid of P×P pixels.
- Each trajectory/image represents a collection of time-stamped coordinates $\{(x_t, y_t)\}$ of the positions of the car collected during a trip.
- Consider a dataset that consists of trips taken by N individuals, indexed by i.
- Each individual, i, makes K trips, with each trip indexed by (i, k). So $k = 1, \dots, K$, and $i = 1, \dots, N$, giving a total of KN trips.
- A demon goes through the each individual's trips and randomly removes a fraction α_i and replaces them with decoys.
- Your task is to build a system which, given an image, reveals the identity of the trip's driver.

- A handwriting sample is represented by an image contained in a grid of P × P pixels.
- Each image represents a collection of time-stamped coordinates $\{(x_t, y_t)\}$ of the positions of the pen collected while the handwriting sample was made.
- Consider a data set that consists of handwriting samples taken from N individuals, indexed by i.
- Each individual, i, provides K handwriting samples, with each sample indexed by (i,k). So $k=1,\cdots,K$, and $i=1,\cdots,N$, giving a total of KN samples.
- A demon goes through the each individual's samples and randomly removes a fraction α_i and replaces them with forgeries.
- Your task is to build a system which, given an image, reveals the identity of the image's author.

We know that a version of the handwriting problem consisting of the first three elements of the list on the right can be solved by a deep neural network. So, we can be confident that placing a similar constraint on the *telematics* problem should allow a deep neural network solution.

So the real twist here is how to deal with the problem posed by the nasty demon.

Proposed strategy:

Assume that the dataset is close to being ideal in the sense that the demon's actions are a small enough perturbation to a probabilistic solution to the ideal problem.

In other words, find a probabilistic solution to the $\alpha=0$ problem, and then interpret any samples with low probability outcomes as outliers corresponding to the demon's perturbation.

Notation

- Let N = total number of drivers, and K = total number of trips per driver.
- Let T denote the duration of the longest trip in the data-set.
- Let $i = 1, \dots, N$, $k = 1, \dots, K$, and $t = 1, \dots, T$.
- We will implement a mapping

data corresponding to
$$\text{the } k^{\text{th}} \text{ trip} \qquad \longleftrightarrow \quad \text{a } \textit{multi-channel} \text{ image } D^{(i,k)}$$
 made by driver i

- Each multi-channel image has *C* channels representing *C* categories of features, and each feature, *c*, is represented by *T* data-points.
 - Thus each multi-channel image $D^{(i,k)}$ has the structure $\left[D^{(i,k)}_{c,t}\right]_{c=1,t=1}^{C}$
 - We will represent each $D^{(i,k)}$ as a numpy ndarray of shape (1, C, T).
- Finally, we will pack all trips by a given driver, say driver i into a data structure $D^{(i)} = \left[D^{(i,k)}\right]_{k=1}^{K}$ represented by a numpy ndarray of shape (K,C,T).

Feature Engineering

- Each "example" in the training set consists of a collection of "time-stamped" spatial coordinates (x(t), y(t)), with $0 \le t \le T 1$. We will always transform our data so that \sqrt{T} is an integer.
- Begin by first mapping "time into space" by defining a transformation that maps each time $t=0,\cdots,T-1$ to spatial coordinates (p_t,q_t) given by

$$p_t \equiv \frac{t - (t \mod \sqrt{T})}{\sqrt{T}}, \qquad q_t \equiv t \mod \sqrt{T}$$

- We will implement a neural network with an input layer of CT neurons, where
 - C is the number of feature categories extracted from the data, and
 - each feature category will be labeled using a "channel index" $c=0,\cdots$, C-1.
- An input neuron representing feature category c at time t is represented by a unit in channel c located at (p(t), q(t)) and receives input $I_c(t)$ where

$$I_c(t) = \begin{cases} \frac{d^c}{dt^c} x(t) & \text{if } c \bmod 2 \equiv 0\\ \frac{d^c}{dt^c} y(t) & \text{if } c \bmod 2 \equiv 1 \end{cases}$$

■ The 0th & 1st features are positions, the 2nd & 3rd features are velocities, the 4th & 5th features are accelerations, the 6th & 7th features are jerks, the 8th & 9th features are snaps, the 10th & 11th features are crackles, and the 12th & 13th features are pops. A sample of the data format is given below.

\overline{t}	X	y	V_X	V_X	$a_{\scriptscriptstyle X}$	a_y	jх	j y	S_{χ}	Sy	C_X	c_y	p_x	p_y
0	-0.05	-3.56	0.24	0.24	0.27	0.63	0.29	0.17	0.32	0.04	0.30	0.31	0.27	0.53
1	-0.04	-3.57	0.25	0.31	0.28	0.33	0.32	-0.02	0.33	0.28	0.30	0.59	0.29	0.34
÷	i		:	:	:	:	i	i	:	:	:	:	:	i

- 1. So, each driving record $D^{(i,k)}$ is associated with C=14 channels, with each channel represented by a vector with \mathcal{T} non-zero components corresponding to non-zero input neuron activations in the input image map associated with that channel.
- 2. During training, the set of GPS coordinates $\{x^{(i,k)}(t)\}_{t=1}^T$ gives rise to activity in 14 channels that are to be classified as belonging to driver i. In other words, each class label i has 200 sample images indexed by k, with each image having 14 channels. Of these images, a fraction α_i are mislabeled, and the task is to identify them.
- 3. At the outset, we arbitrarily split the data into a training set and a test set in a 4:1 ratio.
- 4. The pair of objects $(D^{(i,k)}, i)$ will serve as the input, target pairs to our network during training.
- 5. These are fed into the input layer of a neural network with the structure

- 6. The network utilizes dropout during training.
- 7. In the testing phase, we interpret the response of the most active network output as the response to the input, i.e. if we use $\{O_j\}$ to denote output activities, then on feeding an image $D^{(i,k)}$ as input, we interpret $\{O_j\}$ as the network's prediction for the class label.

..... To Be Completed