Practice Quiz

Part 1:

Prove that the following two sentences are sentences of propositional logic.

1. $((\neg P \supset Q) \supset R)$

2. ¬¬(A ∨ B)

Part 2:

For the following translation task, use the following translation key.

- I = Antonio is Italian.
- P = Antonio loves pasta.
- L = Jingyi loves linguistics.

Translate the following three sentences into propositional logic.

- 3. Antonio loves pasta, if Antonio is Italian
- 4. Antonio loves pasta only if Antonio is Italian.
- 5. Either Jingyi doesn't love linguistics or Antonio loves pasta.

Part 3:

Using truth tables, identify whether the following arguments are valid.

Be sure to fill out the truth table for each sentence in the argument.

6. $(A \lor B) \supset B$ A $\therefore B$

А	В	(Α	٧	В)	⊃	В	А	∴ В
Т	Т									
Т	F									
F	Т									
F	F									

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7.
$$(A \lor B) \equiv B$$

$$\neg B$$

$$\therefore A \land \neg B$$

А	В	(А	V	В)	=	В	Г	В	<i>:</i> .	А	٨	¬В
Т	T													
Т	F													
F	Т													
F	F													

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Part 4

For the following questions, show that the conclusion is a logical consequence of the given premises by constructing a derivation of the conclusion from the premises. If there are no premises, derive the conclusion from the no premises.

8.
$$(X \lor Y) \supset Z$$
X

9. Derive:
$$\neg(A \land \neg A)$$

Challenge question:

10. Using the following premises:

a.
$$(A \lor B) \supset \neg C$$

b. $D \supset (\neg F \land \neg G)$

Derive:
$$(A \lor D) \supset \neg(C \land F)$$