First Order Logic



Project description

After the high-profile lawsuit in which you succeeded to bring RealityMan to justice after proving that distributing his Nintendo emulator was a criminal act, everyone wants to hire you! From disputes over tech patents, to lawsuits on questions of privacy in social media, to suits on liability issues with self-driving cars, to disputes between Hollywood celebrities and their agents or producers, you are just running out of time and energy to run all these cases by hand like we have done in the lectures.

Because of the highly sensitive nature of the cases you handle, and because of the extremely high monetary amounts involved, you cannot trust any existing. You thus decide to create your own, ultra-optimized inference engine.

After much debating, you decide that the knowledge bases which you will create to handle each case will contain sentences with the following defined operators:

```
NOT X \sim X X OR Y X | Y
```

You will use **first-order logic resolution** to solve this problem.

Format for input.txt:

```
<NQ = NUMBER OF QUERIES>
<QUERY 1>
...
<QUERY NQ>
<NS = NUMBER OF GIVEN SENTENCES IN THE KNOWLEDGE BASE>
<SENTENCE 1>
...
<SENTENCE NS>
```

where

- Each query will be a single literal of the form Predicate(Constant) or ~Predicate(Constant).
- Variables are all single lowercase letters.
- All predicates (such as Sibling) and constants (such as John) are case-sensitive alphabetical strings that begin with an uppercase letter.
- Each predicate takes at least one argument. Predicates will take at most 100 arguments. A given predicate name will not appear with different number of arguments.
- There will be at most 100 queries and 1000 sentences in the knowledge base.
- See the sample input below for spacing patterns.
- You can assume that the input format is exactly as it is described. There will be no syntax errors in the given input.

Format for output.txt:

For each query, determine if that query can be inferred from the knowledge base or not, one query per line:

```
<answer 1>
...
<answer no>
```

where each answer should be either TRUE if you can prove that the corresponding query sentence is true given the knowledge base, or FALSE if you cannot.

Notes and hints:

- If you decide that the given statement can be inferred from the knowledge base, every variable in each sentence used in the proving process should be unified with a Constant (i.e., unify variables to constants before you trigger a step of resolution).
- All variables are assumed to be universally quantified. There is no existential quantifier. There is no need for Skolem functions or Skolem constants.
- Operator priorities apply (negation has higher priority than disjunction). There will be no parentheses in the sentences, other than around arguments of predicates.
- The knowledge base that you will be given is consistent. So there are no contracting rules or facts in the knowledge base.
- If you run into a loop and there is no alternative path you can try, report FALSE. An example for this would be having two rules (1) ~A(x) | B(x) and (2) ~B(x) | A(x) and wanting to prove A(John). In this case your program should report FALSE.

Example 1:

For this input.txt:

```
F(Joe)
H (John)
~H(Alice)
~H(John)
G(Joe)
G(Tom)
14
\sim F(x) \mid G(x)
\sim G(x) \mid H(x)
\sim H(x) \mid F(x)
\sim R(x) \mid H(x)
\sim A(x) \mid H(x)
\sim D(x,y) \mid \sim H(y)
\sim B(x,y) \mid \sim C(x,y) \mid A(x)
B(John, Alice)
B(John, Joe)
\sim D(x,y) \mid \sim Q(y) \mid C(x,y)
D(John, Alice)
Q(Joe)
D(John, Joe)
R(Tom)
your output.txt should be:
FALSE
TRUE
TRUE
FALSE
FALSE
TRUE
Example 2:
For this input.txt:
Ancestor (Liz, Billy)
Ancestor(Liz, Joe)
Mother (Liz, Charley)
Father (Charley, Billy)
\simMother(x,y) | Parent(x,y)
\simFather(x,y) | Parent(x,y)
~Parent(x,y) | Ancestor(x,y)
\simParent(x,y) | \simAncestor(y,z) | Ancestor(x,z)
```

your output.txt should be:

TRUE FALSE

Example 3:

For this input.txt:

```
1
Criminal(West)
6
~American(x) | ~Weapon(y) | ~Sells(x,y,z) | ~Enemy(z,America) |
Criminal(x)
Owns(Nono,M1)
Missile(M1)
~Missile(x) | ~Owns(Nono,x) | Sells(West,x,Nono)
~Missile(x) | Weapon(x)
Enemy(Nono,America)
```

your output.txt should be:

TRUE