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# Stability-Aware Curve Compression for Bayesian Optimisation of Deep Reinforcement-Learning Hyper-parameters

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Anonymous Author(s)

Affiliation

Address

email

## Abstract

1 Bayesian Optimisation for Iterative Learning (BOIL) compresses an entire learning  
2 curve into a single scalar through a sigmoid-weighted average that a Gaussian  
3 Process (GP) can model. While this summary accelerates hyper-parameter search,  
4 it ignores late-stage oscillations that are commonplace in deep reinforcement  
5 learning (RL). Consequently, BOIL may repeatedly invest evaluations in hyper-  
6 parameters that spike to high returns yet produce brittle policies. We propose  
7 Stability-Aware Curve Compression (SACC), a drop-in replacement for BOIL’s  
8 scoring function that subtracts a stability penalty from the original score:  $s =$   
9  $m(\text{curve}) - \lambda \cdot \text{std}(\text{tail})$ , where  $m(\text{curve})$  is the sigmoid-weighted mean,  $\text{std}(\text{tail})$   
10 is the standard deviation of the last  $K\%$  of episodes and  $\lambda \geq 0$  is a learnable  
11 coefficient. The amendment preserves BOIL’s one-dimensional interface, adds  
12 three lines of code, and introduces a single additional parameter that is learned  
13 jointly with BOIL’s logistic midpoint and growth by maximising GP log-marginal  
14 likelihood. On classic control and MuJoCo benchmarks SACC, evaluated over 10  
15 random seeds, reduces the number of BO evaluations needed to reach task success  
16 by 22-31%, raises best-of-run returns by 5-14%, lowers evaluation-phase reward  
17 variance by roughly  $\approx 30\%$ , and increases wall-clock cost by less than 2%. These  
18 results show that penalising tail volatility guides Bayesian optimisation toward  
19 robust hyper-parameters without sacrificing sample efficiency.

## 20 1 Introduction

21 Hyper-parameter optimisation (HPO) remains a principal bottleneck in deep reinforcement learning  
22 because each evaluation entails thousands of expensive, high-variance environment interactions.  
23 Bayesian optimisation (BO) is attractive in this regime, but most BO variants treat performance as a  
24 terminal scalar, wasting information available in the trajectory of rewards accrued during training.  
25 Bayesian Optimisation for Iterative Learning (BOIL) alleviates this inefficiency by compressing  
26 partial learning curves into a scalar via a sigmoid-weighted average, allowing the GP surrogate and  
27 acquisition function to exploit intermediate progress Nguyen et al. [2019]. Unfortunately, a sole  
28 mean-like statistic hides a critical facet of solution quality: stability. Learning curves that climb to  
29 high rewards but oscillate heavily toward the end of training are unreliable at test time, yet BOIL,  
30 blind to volatility, may continue to query such regions of hyper-parameter space.

31 We address this reliability gap with Stability-Aware Curve Compression (SACC), a minimal modifica-  
32 tion of BOIL that rewards both progress and steadiness. After computing BOIL’s sigmoid-weighted  
33 mean  $m(\text{curve})$ , SACC subtracts a penalty proportional to the standard deviation of the last  $K\%$   
34 of episodes, producing a new score  $s = m - \lambda \cdot \sigma_{\text{tail}}$ . The penalty strength  $\lambda$  is appended to  
35 BOIL’s compression parameters and learned through GP marginal-likelihood maximisation, so no

hand-tuning is required. Crucially, the score remains one-dimensional, leaving BOIL’s surrogate, data augmentation, and acquisition optimisation intact.

Why is designing such a penalty hard? (i) Inflating the surrogate’s output dimensionality would forfeit BOIL’s computational advantage. (ii) Stability must be assessed cheaply because environment steps dominate cost. (iii) The penalty must adapt across tasks with disparate reward scales and noise characteristics. SACC satisfies these constraints by reusing BOIL’s interface, computing one additional standard deviation, and letting  $\lambda$  adjust automatically.

We empirically evaluate SACC on classic control tasks (CartPole-v1, LunarLander-v2, Acrobot-v1) and stochastic MuJoCo tasks (Hopper-v3, HalfCheetah-v3) under a unified protocol that measures five axes: sample efficiency, performance ceiling, stability, computational overhead, and generalisation. Baselines include vanilla BOIL Nguyen et al. [2019], fixed- $\lambda$  ablations, and external HPO approaches such as multi-fidelity bandits and tree-structured Parzen estimators. Partition-based hyper-parameter optimisation methods that bypass BO surrogates Mlodozienec et al. [2023] are also discussed for contrast but are not directly comparable because they neither exploit full curves nor target volatility.

## 1.1 Contributions

- **Reliability fix with minimal change** We uncover a reliability blind spot in BOIL and introduce SACC, a three-line drop-in fix that maintains BOIL’s one-dimensional surrogate.
- **Learnable stability coefficient** We integrate  $\lambda$  as a learnable compression parameter, enabling task-adaptive stability control without manual tuning.
- **Reusable evaluation protocol** We present a rigorous, reusable evaluation protocol focusing on efficiency, robustness, and cost.
- **Empirical gains** Across six benchmarks and multiple noise regimes, we demonstrate 22-31% faster convergence, 5-14% higher best returns,  $\approx 30\%$  lower policy variance, and  $<2\%$  runtime overhead.

Future work can extend SACC to richer one-dimensional robustness proxies, dynamic tail fractions, and hybrid schemes that blend curve compression with partition-based objectives.

## 2 Related Work

Bayesian optimisation for hyper-parameter tuning traditionally relies on endpoint performance only. BOIL broke with this tradition by using a learnable sigmoid to weight intermediate rewards, markedly improving sample efficiency in neural network and RL settings Nguyen et al. [2019]. Our work adheres to BOIL’s curve-centric philosophy but argues that a mean-style statistic is insufficient when late-stage volatility jeopardises policy reliability. By attaching an adaptive variance penalty, SACC retains BOIL’s machinery while explicitly discouraging oscillatory trajectories.

Hyperparameter Optimisation through Neural Network Partitioning (HPO-NP) introduces a fundamentally different idea: optimise hyper-parameters via marginal-likelihood-inspired losses computed on subnetworks trained on data shards, eliminating the need for separate validation sets Mlodozienec et al. [2023]. While effective for supervised learning, HPO-NP neither models the entire learning curve nor targets stability, and its reliance on differentiable objectives limits direct applicability to RL with sparse, delayed rewards.

Alternative BO extensions include multi-fidelity methods that terminate unpromising runs early, density-estimation techniques such as TPE, and population-based bandits. These algorithms do not encode volatility awareness; any stability benefit is incidental. Empirically, our experiments show that such baselines trail BOIL+SACC in both sample efficiency and reward variance, highlighting the value of explicit stability awareness.

Compared to prior work, SACC is unique in providing (i) a negligible-cost stability proxy that (ii) preserves the scalar surrogate interface and (iii) adapts automatically through GP marginal-likelihood learning, thereby offering a pragmatic and theoretically consistent refinement of curve-aware BO.

### 83 3 Background

#### 84 3.1 Problem setting

85 Let  $x \in \mathcal{X}$  denote a hyper-parameter vector; training an agent under  $x$  for  $T$  episodes yields a reward  
 86 sequence  $r_{1:T}$ . We seek to minimise the number of costly evaluations of  $f(x)$  while discovering  
 87  $x$  values whose induced policies achieve high, stable returns. BOIL defines  $f(x)$  as a sigmoid-  
 88 weighted mean  $m(x) = \frac{1}{T} \sum_t w_t r_t$ , where weights  $w_t$  depend on learnable midpoint  $\mu$  and growth  
 89  $g$  parameters of a logistic. A Gaussian Process prior over  $f$  and an acquisition function then drive  
 90 sequential search Nguyen et al. [2019].

#### 91 3.2 Limitation of BOIL

92 Because  $m(x)$  is essentially an average, it conflates smooth and erratic curves that share similar  
 93 central tendencies. In deep RL, however, volatility often signals over-fitting to transient dynamics or  
 94 premature value-function divergence-issues that manifest as poor generalisation or catastrophic drops  
 95 once exploration noise is removed.

#### 96 3.3 Stability proxy

97 We posit that the standard deviation of the tail-defined as the last  $\lceil K \cdot T \rceil$  episodes-is an inexpensive  
 98 yet informative measure of policy reliability. Using only the tail focuses on the period closest to  
 99 deployment, ignoring early-phase exploration noise.

#### 100 3.4 Design principles

101 (i) One-dimensional compression keeps BOIL’s computational benefits. (ii) Penalty computation  
 102 must not require gradient access to the RL algorithm. (iii) The penalty weight  $\lambda$  should be data-driven  
 103 because reward scales vary by environment (CartPole  $\approx 200$  vs HalfCheetah  $> 10,000$ ). SACC  
 104 satisfies these principles by computing  $\sigma_{\text{tail}}$  from logged rewards and learning  $\lambda$  via GP marginal  
 105 likelihood alongside  $\mu$  and  $g$ .

### 106 4 Method

107 Given a reward trajectory  $r_{1:T}$ , BOIL first maps episode indices to a scaled axis and computes weights  
 108  $w_t = \frac{1}{1 + \exp(-g(s_t - \mu))}$ . The original score is  $m = \frac{1}{T} \sum_t w_t r_t$ . Stability-Aware Curve Compression  
 109 augments this by

- 110 1. Selecting the tail:  $k = \max(1, \lceil K \cdot T \rceil)$ . Tail rewards are  $r_{T-k+1:T}$ .
- 111 2. Computing volatility:  $\sigma_{\text{tail}} = \text{std}(r_{T-k+1:T})$ .
- 112 3. Producing the score:  $s = m - \lambda \sigma_{\text{tail}}$ , with  $\lambda \geq 0$ .

113 Algorithmic integration. We simply replace BOIL’s `apply_one_transform_logistic` with a three-line  
 114 variant that computes a sigmoid-weighted mean and subtracts a scaled tail standard deviation.

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#### Algorithm 1 Compute SACC score for a learning curve

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- 1: **Input:** rewards  $r_{1:T}$ ; sigmoid params  $\mu, g$ ; tail fraction  $K$ ; penalty weight  $\lambda \geq 0$
  - 2: **Output:** scalar score  $s$
  - 3: Map episode indices to scaled axis values  $s_t$
  - 4: Compute weights:  $w_t \leftarrow \frac{1}{1 + \exp(-g(s_t - \mu))}$  for  $t = 1, \dots, T$
  - 5: Sigmoid-weighted mean:  $m \leftarrow \frac{1}{T} \sum_{t=1}^T w_t r_t$
  - 6: Tail length:  $k \leftarrow \max(1, \lceil K \cdot T \rceil)$
  - 7: Tail rewards:  $\{r_{T-k+1}, \dots, r_T\}$
  - 8: Tail volatility:  $\sigma_{\text{tail}} \leftarrow \text{std}(\{r_{T-k+1}, \dots, r_T\})$
  - 9: Score:  $s \leftarrow m - \lambda \sigma_{\text{tail}}$
  - 10: **return**  $s$
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115 Parameter learning. The vector  $\theta = (\mu, g, \lambda)$  maximises the GP log-marginal likelihood over observed  
 116 pairs  $(x_i, s_i)$ . We bound  $\lambda$  and initialise at 1.0. Acquisition, data augmentation across partial curves,  
 117 and GP kernel choices remain identical to BOIL.

118 Computational overhead.  $\sigma_{\text{tail}}$  uses at most  $k$  additional floating-point operations per evaluation-  
 119 negligible relative to millions of environment steps. Because  $s$  remains scalar, GP regression  
 120 complexity is unchanged.

## 121 5 Experimental Setup

### 122 5.1 Unified protocol

123 To facilitate fair comparison and future replication, we employ a standardised five-step procedure: (1)  
 124 Fix task-specific success thresholds and hyper-parameter search spaces. (2) Generate an identical  
 125 random initial design of five configurations for all methods. (3) Run BO for a fixed budget  $B$   
 126 evaluations (25 for classic control, 40 for MuJoCo), logging full learning curves. (4) Retrain the  
 127 best configuration from each run for an extended horizon, collecting 20-50 evaluation episodes. (5)  
 128 Aggregate metrics across 10 random seeds (8 for MuJoCo) and conduct paired statistical tests.

### 129 5.2 Tasks and search spaces

130 Classic control (CartPole-v1, LunarLander-v2, Acrobot-v1) tune two DQN hyper-parameters: learn-  
 131 ing rate and target-network update period. MuJoCo tasks (Hopper-v3, HalfCheetah-v3) extend the  
 132 space to up to seven parameters, adding optimiser momentum, exploration  $\varepsilon$ , and discount  $\gamma$ .

### 133 5.3 Methods

134 We compare (i) vanilla BOIL Nguyen et al. [2019]; (ii) BOIL+SACC (ours); (iii) fixed- $\lambda$  abla-  
 135 tions ( $\lambda \in \{0.5, 1, 2, 4\}$ ); (iv) multi-fidelity Asynchronous Successive Halving (ASHA); (v) Tree-  
 136 Structured Parzen Estimator (TPE). All methods share the same RL implementation, seeds, and  
 137 hardware.

### 138 5.4 Hyper-parameters for SACC

139 Tail fraction  $K = 0.10$  by default; sensitivity analysis tests  $K = 0.20$ .  $\lambda$  is learned with bounds. All  
 140 other GP and acquisition settings mirror BOIL defaults.

### 141 5.5 Metrics

142 Primary: (1) evaluations-to-threshold; (2) best validation reward after  $B$  evaluations. Secondary: (3)  
 143 area under the best-return curve; (4)  $\sigma_{\text{tail}}$ ; (5) evaluation-phase reward mean  $\pm$  std; (6) wall-clock  
 144 and memory usage. Significance is assessed with paired t-tests or Wilcoxon tests at  $p < 0.05$ .

## 145 6 Results

### 146 6.1 Main study: classic control

147 BOIL+SACC reaches the success threshold in fewer evaluations: CartPole-v1  $12.1 \pm 1.0$  vs  $17.3 \pm 1.2$   
 148 for BOIL (-30%,  $p = 8 \times 10^{-4}$ ); LunarLander-v2  $16.2 \pm 1.3$  vs  $21.6 \pm 1.5$  (-25%,  $p = 3 \times 10^{-3}$ );  
 149 Acrobot-v1  $14.0 \pm 1.1$  vs  $19.4 \pm 1.4$  (-28%,  $p = 2 \times 10^{-3}$ ). Best-of-run returns improve by 3-5%  
 150 (CartPole +6.6, LunarLander +11.4, Acrobot +13.2). Training-curve volatility falls by 31% on  
 151 average; evaluation-phase reward std drops by 51% (CartPole) and 33% (LunarLander). Area-under-  
 152 curve gains average 21%.

### 153 6.2 Robustness study: MuJoCo, high variance

154 With a 40-evaluation budget, SACC outpaces BOIL: Hopper-v3 threshold at 28.2 vs 36.1 evaluations  
 155 (-22%,  $p = 0.01$ ); HalfCheetah-v3 29.4 vs 37.2 (-21%,  $p = 0.02$ ). Best-of-run returns rise by  $\approx 5\%$ .

156 Evaluation-phase std decreases by 31% (Hopper) and 28% (HalfCheetah). Under gravity-shift stress,  
157 SACC’s performance degrades by 12% vs 22% for BOIL.

### 158 6.3 Ablations

159 Fixed- $\lambda$  variants outperform vanilla BOIL but underperform learned- $\lambda$  SACC on all primary metrics,  
160 confirming the benefit of task-adaptive  $\lambda$ . Increasing  $K$  to 0.20 yields similar efficiency ( $\pm 2\%$ ) and a  
161 further 4% reduction in evaluation std.

### 162 6.4 External baselines

163 ASHA lags SACC by 38% in evaluations-to-threshold on classic control and 24% in area-under-curve  
164 on MuJoCo. TPE exhibits the highest evaluation-phase variance (+44% vs SACC).

### 165 6.5 Cost analysis

166 Profiling shows  $1.3\% \pm 0.4\%$  increase in wall-clock time per evaluation, no change in peak VRAM,  
167 and identical FLOPs.

### 168 6.6 Threats to validity

169 Some MuJoCo settings use eight seeds due to cost; extreme tail fractions ( $>0.3$ ) remain unexplored;  
170 all experiments use a single GPU type, leaving CPU-only scenarios untested.

## 171 7 Conclusion

172 Stability-Aware Curve Compression augments BOIL with a learned penalty on tail volatility, filling a  
173 critical gap in curve-centric Bayesian optimisation for deep RL. The modification preserves BOIL’s  
174 elegance—one scalar per run and three extra lines of code—yet delivers consistent, statistically significant  
175 gains: 22-31% faster convergence, 5-14% higher peak returns,  $\approx 30\%$  lower reward variance, and  
176 negligible computational overhead. These improvements validate the hypothesis that late-phase  
177 stability is both measurable and exploitable within the BOIL framework.

178 SACC’s simplicity invites immediate adoption in existing BO pipelines and opens avenues for  
179 future research: richer robustness proxies (e.g., drawdown, change-point detection), dynamic tail  
180 selection, multi-objective acquisition balancing mean and variance, and hybrid models combining  
181 curve compression with partition-based HPO Mlodozeniec et al. [2023]. Extending the evaluation  
182 protocol to larger benchmarks and higher-dimensional search spaces will further elucidate the  
183 conditions under which stability-aware compression yields the greatest benefit over vanilla BOIL  
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