

The inflow rate near time t_1 can be approximated by a quadratic function shown as follow :

$$\lambda(t) = \lambda(t_1) + \frac{1}{2}\lambda''(t_1)(t - t_1)^2 \quad (1)$$

let $\rho = -\frac{1}{2}\lambda''(t_1)$, then Eq. (1) can be transformed to

$$\lambda(t) = \lambda(t_1) - \rho(t - t_1)^2 \quad (2)$$

Given the total demand during the peak period t_s to t_e , V . Obviously, the peak period length is $t_e - t_s$.

$$\begin{aligned} \int_{t_s}^{t_e} \lambda(t)dt &= \int_{t_s}^{t_e} [\lambda(t_1) - \rho(t - t_1)^2]dt \\ &= \left\{ -\frac{\rho}{3}t^3 + \rho t_1 t^2 + [\lambda(t_1) - t_1^2]t \right\} \Big|_{t_s}^{t_e} \\ &= -\frac{\rho}{3}(t_e - t_s)^3 + \rho t_1(t_e - t_s)^2 + [\lambda(t_1) - t_1^2](t_e - t_s) \end{aligned} \quad (3)$$

Since

$$\int_{t_s}^{t_e} \lambda(t)dt = V \quad (4)$$

Thus

$$-\frac{\rho}{3}(t_e - t_s)^3 + \rho t_1(t_e - t_s)^2 + [\lambda(t_1) - t_1^2](t_e - t_s) = V \quad (5)$$

Then

$$\lambda(t_1) = \frac{V}{t_e - t_s} + \frac{\rho}{3}(t_e - t_s)^2 - \rho t_1(t_e - t_s) + t_1^2 \quad (6)$$

As we all know

$$t_0 = t_1 - \left[\frac{\lambda(t_1) - \mu}{\rho} \right]^{1/2} \quad (7)$$

$$t_2 = t_1 + \left[\frac{\lambda(t_1) - \mu}{\rho} \right]^{1/2} \quad (8)$$

And the total waiting time during peak period is

$$W = \frac{9[\lambda(t_1) - \mu]^2}{4\rho} \quad (9)$$

The average waiting time during peak period t_s to t_e is

$$w = \frac{W}{V} \quad (6)$$