



$$A_1 = \begin{bmatrix} \cos(q_1) & -\sin(q_1)\cos(q_0) & \sin(q_1)\sin(q_0) & 0 \\ \sin(q_1) & \cos(q_1)\cos(q_0) & -\cos(q_1)\sin(q_0) & 0 \\ 0 & \sin(q_0) & \cos(q_0) & L_1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

	Z	X		
i	q_i	d_i	a_i	alpha_i
1	q <sub>1</sub>	L <sub>1</sub>	0	90°
2	q <sub>2</sub>	0	L <sub>2</sub>	0
3	q <sub>3</sub>	0	L <sub>3</sub>	0
4	q <sub>4</sub>	0	L <sub>4</sub>	0

$$A_1 = \begin{bmatrix} \cos(q_1) & 0 & \sin(q_1) & 0 \\ \sin(q_1) & 0 & -\cos(q_1) & 0 \\ 0 & 1 & 0 & 0.8 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$A_2 = \begin{bmatrix} \cos(q_2) & -\sin(q_2)\cos(1) & \sin(q_2)\sin(1) & L_2 \cos(q_2) \\ \sin(q_2) & \cos(q_2)\cos(1) & \sin(q_2)\cos(1) & L_2 \sin(q_2) \\ 0 & \sin(0) & \cos(0) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$A_2 = \begin{bmatrix} \cos(q_2) & -\sin(q_2) & 0 & 0.9 \cos(q_2) \\ \sin(q_2) & \cos(q_2) & 0 & 0.9 \sin(q_2) \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$A_3 = \begin{bmatrix} \cos q_3 & -\sin q_3 & 0 & 0,3 \cos q_3 \\ \sin q_3 & \cos q_3 & 0 & 0,3 \sin q_3 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$A_4 = \begin{bmatrix} \cos q_4 & -\sin q_4 & 0 & 0,3 \cos q_4 \\ \sin q_4 & \cos q_4 & 0 & 0,3 \sin q_4 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$T = A_1 * A_2 * A_3 * A_4$$

$$T = \begin{bmatrix} \cos(q_1 + q_2 + q_3 + q_4) \\ \sin(q_1 + q_2 + q_3 + q_4) \end{bmatrix}$$

$$T = \begin{bmatrix} \frac{\cos(q_1 + q_2 + q_3 + q_4) + \cos(q_1 - q_2 - q_3 - q_4)}{2} & \frac{\sin(q_1 + q_2 + q_3 + q_4) - \sin(q_1 - q_2 - q_3 - q_4)}{2} \\ \frac{\sin(q_1 + q_2 + q_3 + q_4) + \sin(q_1 - q_2 - q_3 - q_4)}{2} & \frac{\cos(q_1 + q_2 + q_3 + q_4) - \cos(q_1 - q_2 - q_3 - q_4)}{2} \\ \sin(q_2 + q_3 + q_4) & \cos(q_2 + q_3 + q_4) \\ 0 & 0 \\ \sin q_1 & 0,1 \cos(q_1) (3 \cos(q_2 + q_3 + q_4) + 3 \cos(q_2 + q_3) + 9 \cos q_2) \\ -\cos q_1 & 0,1 \sin(q_1) (3 \cos(q_2 + q_3 + q_4) + 3 \cos(q_2 + q_3) + 9 \cos q_2) \\ 0 & 0,1 (3 \sin(q_2 + q_3 + q_4) + 3 \sin(q_2 + q_3) + 9 \sin q_2 + 8) \\ 0 & 1 \end{bmatrix}$$

Simplifying,

$$\begin{array}{llll} \cos(\theta_1) \cos(\theta_2 + \theta_3 + \theta_4) & - \cos(\theta_1) \sin(\theta_2 + \theta_3 + \theta_4) & \sin(\theta_1) & (\cos(\theta_1)(0.4 \cos(\theta_2) + 0.3 \cos(\theta_2 + \theta_3) + 0.3 \cos(\theta_2 + \theta_3 + \theta_4)) \\ \sin(\theta_1) \cos(\theta_2 + \theta_3 + \theta_4) & - \sin(\theta_1) \sin(\theta_2 + \theta_3 + \theta_4) & - \cos(\theta_1) & \sin(\theta_1)(0.4 \cos(\theta_2) + 0.3 \cos(\theta_2 + \theta_3) + 0.3 \cos(\theta_2 + \theta_3 + \theta_4)) \\ \sin(\theta_2 + \theta_3 + \theta_4) & \cos(\theta_2 + \theta_3 + \theta_4) & 0 & 0.4 \sin(\theta_2) + 0.3 \sin(\theta_2 + \theta_3) + 0.3 \sin(\theta_2 + \theta_3 + \theta_4) \\ 0 & 0 & \cancel{0} & \cancel{0} \end{array}$$

## Matrix Jacobians

$$\begin{bmatrix}
 - (0.4 \cos(q_2) + 0.3 \cos(q_2 + q_3) + 0.3 \cos(q_2 + q_3 + q_4)) \sin(q_1) & - (0.4 \sin(q_2) + 0.3 \sin(q_2 + q_3) + 0.3 \sin(q_2 + q_3 + q_4)) \cos(q_1) & -0.3 (\sin(q_2 + q_3) + \sin(q_2 + q_3 + q_4)) \cos(q_1) & -0.3 \sin(q_2 + q_3 + q_4) \cos(q_1) \\
 0 & \sin(q_1) & \sin(q_1) & \sin(q_1) \\
 (0.4 \cos(q_2) + 0.3 \cos(q_2 + q_3) + 0.3 \cos(q_2 + q_3 + q_4)) \cos(q_1) & - (0.4 \sin(q_2) + 0.3 \sin(q_2 + q_3) + 0.3 \sin(q_2 + q_3 + q_4)) \sin(q_1) & -0.3 (\sin(q_2 + q_3) + \sin(q_2 + q_3 + q_4)) \sin(q_1) & -0.3 \sin(q_1) \sin(q_2 + q_3 + q_4) \\
 0 & -\cos(q_1) & -\cos(q_1) & -\cos(q_1) \\
 0 & 0.4 \cos(q_2) + 0.3 \cos(q_2 + q_3) + 0.3 \cos(q_2 + q_3 + q_4) & 0.3 \cos(q_2 + q_3) + 0.3 \cos(q_2 + q_3 + q_4) & 0.3 \cos(q_2 + q_3 + q_4) \\
 1 & 0 & 0 & 0
 \end{bmatrix}$$