

Figure 1: A Wumpus Wonderland

1 Discussion-Based Warm Ups

- (a) Given the following, can you prove that the unicorn is mythical? How about magical? Horned?

If the unicorn is mythical, then it is immortal, but if it is not mythical, then it is a mortal mammal. If the unicorn is either immortal or a mammal, then it is horned. The unicorn is magical if it is horned.

Do not attempt to formalize your solution here. Rather, turn to the people around you and reason through this question. How many possible worlds would we have to enumerate to give a formal answer?

- (b) Determine which of the following are correct, and explain your reasoning:

- (i) $(A \wedge B) \models (A \iff B)$
- (ii) $A \iff B \models A \vee B$
- (iii) $A \iff B \models \neg A \vee B$
- (iv) $(A \wedge B) \implies C \models (A \implies C) \vee B \implies C$
- (v) $(A \vee B) \wedge \neg(A \implies B)$ is satisfiable.

- (c) What is the difference between satisfiability and entailment (think about the purpose and requirements of each)?

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function HYBRID-WUMPUS-AGENT(percept) returns an action
  inputs: percept, a list, [stench,breeze,glitter,bump,scream]
  persistent: KB, a knowledge base, initially the atemporal “wumpus physics”
    t, a counter, initially 0, indicating time
    plan, an action sequence, initially empty

  TELL(KB, MAKE-PERCEPT-SENTENCE(percept, t))
  TELL the KB the temporal “physics” sentences for time t
  safe  $\leftarrow \{[x, y] : \text{ASK}(KB, OK_{x,y}^t) = \text{true}\}$ 
  if ASK(KB, Glittert) = true then A
    plan  $\leftarrow [\text{Grab}] + \text{PLAN-ROUTE}(\text{current}, \{[1,1]\}, \text{safe}) + [\text{Climb}]$ 
  if plan is empty then B
    unvisited  $\leftarrow \{[x, y] : \text{ASK}(KB, L_{x,y}^{t'}) = \text{false} \text{ for all } t' \leq t\}$ 
    plan  $\leftarrow \text{PLAN-ROUTE}(\text{current}, \text{unvisited} \cap \text{safe}, \text{safe})$ 
  if plan is empty and ASK(KB, HaveArrowt) = true then C
    possible_wumpus  $\leftarrow \{[x, y] : \text{ASK}(KB, \neg W_{x,y}) = \text{false}\}$ 
    plan  $\leftarrow \text{PLAN-SHOT}(\text{current}, \text{possible\_wumpus}, \text{safe})$ 
  if plan is empty then // no choice but to take a risk D
    not_unsafe  $\leftarrow \{[x, y] : \text{ASK}(KB, \neg OK_{x,y}^t) = \text{false}\}$ 
    plan  $\leftarrow \text{PLAN-ROUTE}(\text{current}, \text{unvisited} \cap \text{not\_unsafe}, \text{safe})$ 
  if plan is empty then E
    plan  $\leftarrow \text{PLAN-ROUTE}(\text{current}, \{[1, 1]\}, \text{safe}) + [\text{Climb}]$ 
  action  $\leftarrow \text{POP}(\text{plan})$ 

  TELL(KB, MAKE-ACTION-SENTENCE(action, t))
  t  $\leftarrow t + 1$ 
  return action

function PLAN-ROUTE(current,goals,allowed) returns an action sequence
  inputs: current, the agent’s current position
    goals, a set of squares; try to plan a route to one of them
    allowed, a set of squares that can form part of the route

  problem  $\leftarrow \text{ROUTE-PROBLEM}(\text{current}, \text{goals}, \text{allowed})$ 
  return A*-GRAPH-SEARCH(problem)

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Figure 2: Hybrid-Wumpus-Agent from AIMIA 3rd ed. It uses a propositional knowledge base to infer the state of the world, and a combination of problem-solving search and domain-specific code to decide what actions to take.

2 Wandering in Wumpus World

We bring together what we have learned in lecture as well as the ideas of search so far in order to construct wumpus world agents that use propositional logic. The first step is to enable the agent to deduce, to the extent possible, the state of the world given its percept history. This requires writing down a complete logical model of the effects of actions. We also show how the agent can keep track of the world efficiently without going back into the percept history for each inference. Finally, we show how the agent can use logical inference to construct plans that are guaranteed to achieve its goals.

Try it out: <http://thiagodnf.github.io/wumpus-world-simulator/>

Throughout this question, we will present several screenshots from the Wumpus World simulator linked previously. In each of these, assume that you *do* have an arrow on hand (as an extra exercise, consider how the answers might be different if you did not have an arrow). Also, note that the location of the explorer can be ignored. We just tried to place him somewhere where he wouldn't be blocking the text!

- (a) Consider the following Wumpus World state:

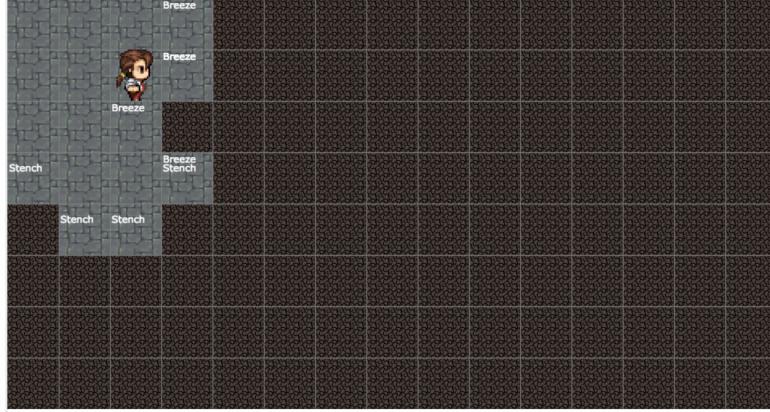


Figure 3: Entailment versus Satisfiability?

Based on our previous discussion around entailment and satisfiability, identify locations where our knowledge base entails that there must be a Wumpus, Pit, or safe path. Additionally, identify locations where Wumpuses, Pit, and safe paths are not entailed but could be satisfied.

- (b) Now, refer to Figure 2 from Page 2, and take a moment to familiarize yourself with the pseudocode to understand how we might decide to act in Wumpus World. You'll notice that we have labeled the key decision-making portions of this code, and that different decisions need to be made given the state of our knowledge-base.

Match each of the following states to one of the labeled code chunks in the pseudocode, and explain your reasoning.



Figure 4: Which code chunk is applicable for each of these states?

3 Axioms & Arrows

Up until now we have assumed that the plans we create always make sure that an actions preconditions are satisfied. Let us now investigate what propositional successor-state axioms such as $\text{HaveArrow}^{t+1} \iff (\text{HaveArrow}^t \wedge \neg \text{Shoot}^t)$ have to say about actions whose preconditions are not satisfied.

- (a) First, let us consider what successor-state axioms are. How do they differ from action axioms, and why might we choose to use them?
- (b) Show that the axioms predict that nothing will happen when an action is executed in a state where its preconditions are not satisfied.
- (c) Consider a plan p that contains the actions required to achieve a goal but also includes illegal actions.
Is it the case that
$$\text{initial state} \wedge \text{successor-state axioms} \wedge p \models \text{goal}$$

We recommend that you write a truth table and ask yourself the following questions when looking at the truth table

- Can I shoot if I don't have an arrow?
- If I do shoot without an arrow will I end up with an arrow?
- If I shoot with an arrow **could** I still have an arrow?