

Gilbert_Nathaniel_329_Final_Project

2025-03-17

In this report we will be analyzing the hitters dataset from the ISLR library, we will be attempting to create a linear regression model in order to predict a hitters salary.

```
head(Hitters)
```

```
##           AtBat Hits HmRun Runs RBI Walks Years CAtBat CHits CHmRun
## -Andy Allanson    293   66     1   30  29   14     1    293   66     1
## -Alan Ashby       315   81     7   24  38   39   14   3449   835   69
## -Alvin Davis      479  130    18   66  72   76    3   1624   457   63
## -Andre Dawson     496  141    20   65  78   37   11   5628  1575  225
## -Andres Galarraga  321   87    10   39  42   30    2    396   101   12
## -Alfredo Griffin  594  169     4   74  51   35   11   4408  1133   19
##           CRuns CRBI CWalks League Division PutOuts Assists Errors
## -Andy Allanson     30   29    14      A        E     446     33    20
## -Alan Ashby        321  414   375      N        W     632     43    10
## -Alvin Davis       224  266   263      A        W     880     82    14
## -Andre Dawson      828  838   354      N        E     200     11     3
## -Andres Galarraga   48   46    33      N        E     805     40     4
## -Alfredo Griffin   501  336   194      A        W     282    421    25
##           Salary NewLeague
## -Andy Allanson      NA      A
## -Alan Ashby        475.0     N
## -Alvin Davis       480.0     A
## -Andre Dawson      500.0     N
## -Andres Galarraga   91.5     N
## -Alfredo Griffin   750.0     A
```

The dataset features a number of baseball statistics, both for the previous year (1986) and career for a number of baseball players, it also tells the salary for each player.

Nearly every variable is a discrete numerical variable, with the exception of league, division, and NewLeague which are categorical variables. Additionally salary is a continuous numerical variable.

```
is.na(Hitters)
```

The dataset does have null values, all in the salary column. As that is our response variable we must remove any columns with a null value

```
hitters= na.omit(Hitters)
```

```
str(hitters)
```

```
## 'data.frame':   263 obs. of  20 variables:
```

```
## $ AtBat : int 315 479 496 321 594 185 298 323 401 574 ...
## $ Hits : int 81 130 141 87 169 37 73 81 92 159 ...
## $ HmRun : int 7 18 20 10 4 1 0 6 17 21 ...
## $ Runs : int 24 66 65 39 74 23 24 26 49 107 ...
## $ RBI : int 38 72 78 42 51 8 24 32 66 75 ...
## $ Walks : int 39 76 37 30 35 21 7 8 65 59 ...
## $ Years : int 14 3 11 2 11 2 3 2 13 10 ...
## $ CAtBat : int 3449 1624 5628 396 4408 214 509 341 5206 4631 ...
## $ CHits : int 835 457 1575 101 1133 42 108 86 1332 1300 ...
## $ CHmRun : int 69 63 225 12 19 1 0 6 253 90 ...
## $ CRuns : int 321 224 828 48 501 30 41 32 784 702 ...
## $ CRBI : int 414 266 838 46 336 9 37 34 890 504 ...
## $ CWalks : int 375 263 354 33 194 24 12 8 866 488 ...
## $ League : Factor w/ 2 levels "A","N": 2 1 2 2 1 2 1 2 1 1 ...
## $ Division : Factor w/ 2 levels "E","W": 2 2 1 1 2 1 2 2 1 1 ...
## $ PutOuts : int 632 880 200 805 282 76 121 143 0 238 ...
## $ Assists : int 43 82 11 40 421 127 283 290 0 445 ...
## $ Errors : int 10 14 3 4 25 7 9 19 0 22 ...
## $ Salary : num 475 480 500 91.5 750 ...
## $ NewLeague: Factor w/ 2 levels "A","N": 2 1 2 2 1 1 1 2 1 1 ...
## - attr(*, "na.action")= 'omit' Named int [1:59] 1 16 19 23 31 33 37 39 40 42 ...
## ..- attr(*, "names")= chr [1:59] "-Andy Allanson" "-Billy Beane" "-Bruce Bochte" "-Bob Boone" ...
```

All of the variables are stored as the correct type.

Next we will do some numerical analysis on the data

```
summary(hitters)
```

```
##           AtBat           Hits           HmRun           Runs
## Min.      : 19.0   Min.      : 1.0   Min.      : 0.00   Min.      : 0.00
## 1st Qu.:282.5   1st Qu.: 71.5   1st Qu.: 5.00   1st Qu.: 33.50
## Median :413.0   Median :103.0   Median : 9.00   Median : 52.00
## Mean     :403.6   Mean     :107.8   Mean     :11.62   Mean     : 54.75
## 3rd Qu.:526.0   3rd Qu.:141.5   3rd Qu.:18.00   3rd Qu.: 73.00
## Max.     :687.0   Max.     :238.0   Max.     :40.00   Max.     :130.00
##           RBI           Walks           Years           CAtBat
## Min.      : 0.00   Min.      : 0.00   Min.      : 1.000   Min.      : 19.0
## 1st Qu.: 30.00   1st Qu.: 23.00   1st Qu.: 4.000   1st Qu.: 842.5
## Median : 47.00   Median : 37.00   Median : 6.000   Median :1931.0
## Mean     : 51.49   Mean     : 41.11   Mean     : 7.312   Mean     :2657.5
## 3rd Qu.: 71.00   3rd Qu.: 57.00   3rd Qu.:10.000   3rd Qu.:3890.5
## Max.     :121.00   Max.     :105.00   Max.     :24.000   Max.     :14053.0
##           CHits           CHmRun           CRuns           CRBI
## Min.      : 4.0   Min.      : 0.00   Min.      : 2.0   Min.      : 3.0
## 1st Qu.: 212.0   1st Qu.: 15.00   1st Qu.: 105.5   1st Qu.: 95.0
## Median : 516.0   Median : 40.00   Median : 250.0   Median : 230.0
## Mean     : 722.2   Mean     : 69.24   Mean     : 361.2   Mean     : 330.4
## 3rd Qu.:1054.0   3rd Qu.: 92.50   3rd Qu.: 497.5   3rd Qu.: 424.5
## Max.     :4256.0   Max.     :548.00   Max.     :2165.0   Max.     :1659.0
##           CWalks           League           Division           PutOuts           Assists
## Min.      : 1.0   A:139   E:129   Min.      : 0.0   Min.      : 0.0
## 1st Qu.: 71.0   N:124   W:134   1st Qu.: 113.5   1st Qu.: 8.0
## Median : 174.0           Median : 224.0   Median : 45.0
```

```
## Mean      : 260.3          Mean      : 290.7      Mean      :118.8
## 3rd Qu.: 328.5          3rd Qu.: 322.5      3rd Qu.:192.0
## Max.      :1566.0        Max.      :1377.0    Max.      :492.0
##           Errors          Salary          NewLeague
## Min.      : 0.000      Min.      : 67.5      A:141
## 1st Qu.: 3.000      1st Qu.: 190.0      N:122
## Median : 7.000      Median : 425.0
## Mean      : 8.593      Mean      : 535.9
## 3rd Qu.:13.000      3rd Qu.: 750.0
## Max.      :32.000      Max.      :2460.0
```

The summary shows us there is a very wide range for salaries, additionally it shows there are roughly equal amount of players in each league and division.

```
numeric_hitters <-hitters[, sapply(hitters, is.numeric)]
cor(numeric_hitters)
```

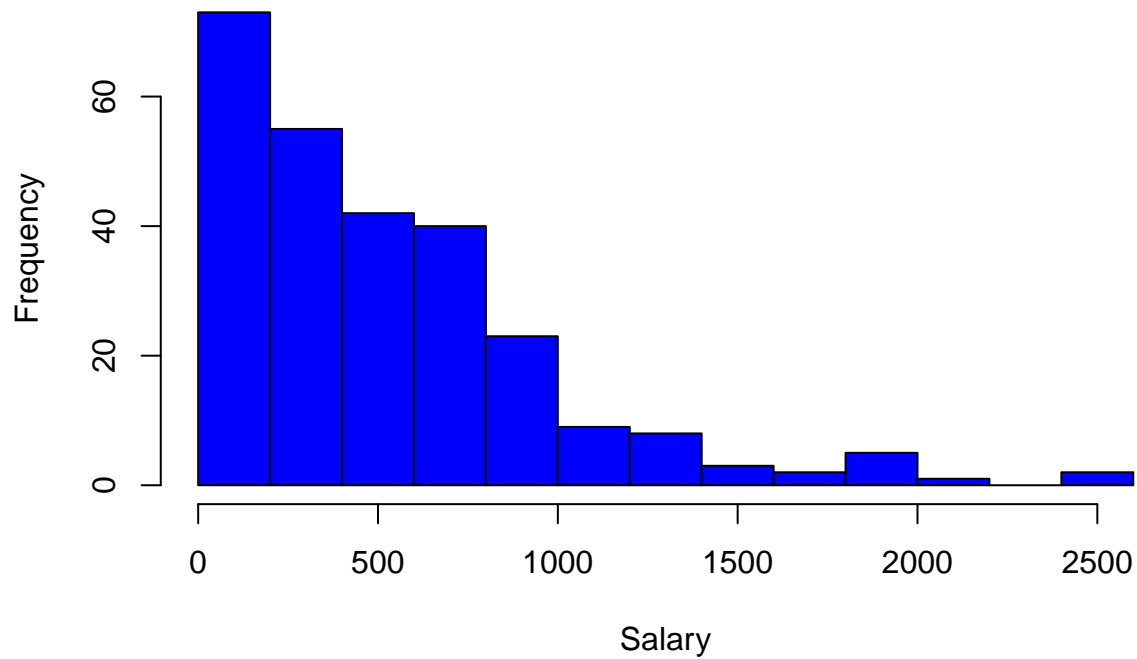
```
##           AtBat      Hits      HmRun      Runs      RBI      Walks
## AtBat      1.0000000 0.96396913 0.555102154 0.89982910 0.79601539 0.6244481
## Hits       0.9639691 1.00000000 0.530627358 0.91063014 0.78847819 0.5873105
## HmRun      0.5551022 0.53062736 1.000000000 0.63107588 0.84910743 0.4404537
## Runs       0.8998291 0.91063014 0.631075883 1.00000000 0.77869235 0.6970151
## RBI        0.7960154 0.78847819 0.849107434 0.77869235 1.00000000 0.5695048
## Walks      0.6244481 0.58731051 0.440453717 0.69701510 0.56950476 1.0000000
## Years      0.0127255 0.01859809 0.113488420 -0.01197495 0.12966795 0.1347927
## CAtBat     0.2071663 0.20667761 0.217463613 0.17181080 0.27812591 0.2694500
## CHits      0.2253415 0.23560577 0.217495691 0.19132697 0.29213714 0.2707951
## CHmRun     0.2124215 0.18936425 0.492525845 0.22970104 0.44218969 0.3495822
## CRuns      0.2372778 0.23889610 0.258346846 0.23783121 0.30722616 0.3329766
## CRBI       0.2213932 0.21938423 0.349858379 0.20233548 0.38777657 0.3126968
## CWalks     0.1329257 0.12297073 0.227183183 0.16370021 0.23361884 0.4291399
## PutOuts    0.3096075 0.29968754 0.250931497 0.27115986 0.31206456 0.2808555
## Assists    0.3421174 0.30397495 -0.161601753 0.17925786 0.06290174 0.1025226
## Errors     0.3255770 0.27987618 -0.009743082 0.19260879 0.15015469 0.0819372
## Salary     0.3947709 0.43867474 0.343028078 0.41985856 0.44945709 0.4438673
##           Years      CAtBat      CHits      CHmRun      CRuns
## AtBat      0.01272550 0.207166254 0.22534146 0.21242155 0.23727777
## Hits       0.01859809 0.206677608 0.23560577 0.18936425 0.23889610
## HmRun      0.11348842 0.217463613 0.21749569 0.49252584 0.25834685
## Runs      -0.01197495 0.171810798 0.19132697 0.22970104 0.23783121
## RBI        0.12966795 0.278125914 0.29213714 0.44218969 0.30722616
## Walks      0.13479270 0.269449974 0.27079505 0.34958216 0.33297657
## Years      1.00000000 0.915680692 0.89784449 0.72237071 0.87664855
## CAtBat     0.91568069 1.000000000 0.99505681 0.80167609 0.98274694
## CHits      0.89784449 0.995056810 1.00000000 0.78665204 0.98454184
## CHmRun     0.72237071 0.801676089 0.78665204 1.00000000 0.82562483
## CRuns      0.87664855 0.982746941 0.98454184 0.82562483 1.00000000
## CRBI       0.86380936 0.950730141 0.94679739 0.92790264 0.94567701
## CWalks     0.83752373 0.906711655 0.89071842 0.81087827 0.92776846
## PutOuts    -0.02001921 0.053392514 0.06734799 0.09382223 0.05908718
## Assists    -0.08511772 -0.007897271 -0.01314420 -0.18888646 -0.03889509
## Errors     -0.15651196 -0.070477521 -0.06803583 -0.16536941 -0.09408054
## Salary     0.40065699 0.526135310 0.54890956 0.52493056 0.56267771
```

##		CRBI	CWalks	PutOuts	Assists	Errors
##	AtBat	0.22139318	0.13292568	0.30960746	0.342117377	0.325576978
##	Hits	0.21938423	0.12297073	0.29968754	0.303974950	0.279876183
##	HmRun	0.34985838	0.22718318	0.25093150	-0.161601753	-0.009743082
##	Runs	0.20233548	0.16370021	0.27115986	0.179257859	0.192608787
##	RBI	0.38777657	0.23361884	0.31206456	0.062901737	0.150154692
##	Walks	0.31269680	0.42913990	0.28085548	0.102522559	0.081937197
##	Years	0.86380936	0.83752373	-0.02001921	-0.085117725	-0.156511957
##	CAtBat	0.95073014	0.90671165	0.05339251	-0.007897271	-0.070477521
##	CHits	0.94679739	0.89071842	0.06734799	-0.013144204	-0.068035829
##	CHmRun	0.92790264	0.81087827	0.09382223	-0.188886464	-0.165369407
##	CRuns	0.94567701	0.92776846	0.05908718	-0.038895093	-0.094080542
##	CRBI	1.00000000	0.88913701	0.09537515	-0.096558877	-0.115316131
##	CWalks	0.88913701	1.00000000	0.05816016	-0.066243445	-0.129935875
##	PutOuts	0.09537515	0.05816016	1.00000000	-0.043390143	0.075305857
##	Assists	-0.09655888	-0.06624345	-0.04339014	1.000000000	0.703504693
##	Errors	-0.11531613	-0.12993587	0.07530586	0.703504693	1.000000000
##	Salary	0.56696569	0.48982204	0.30048036	0.025436136	-0.005400702
##	Salary					
##	AtBat	0.394770945				
##	Hits	0.438674738				
##	HmRun	0.343028078				
##	Runs	0.419858559				
##	RBI	0.449457088				
##	Walks	0.443867260				
##	Years	0.400656994				
##	CAtBat	0.526135310				
##	CHits	0.548909559				
##	CHmRun	0.524930560				
##	CRuns	0.562677711				
##	CRBI	0.566965686				
##	CWalks	0.489822036				
##	PutOuts	0.300480356				
##	Assists	0.025436136				
##	Errors	-0.005400702				
##	Salary	1.000000000				

The correlation matrix shows how well all of the numeric variables are correlated. At Bats is very correlated with many offensive totals. Additionally it seems Salary does not have a super strong correlation with any individual variable. Next we will do some visual analysis

```
hist(hitters$Salary, main="Distribution of Player Salaries", xlab="Salary", col="blue")
```

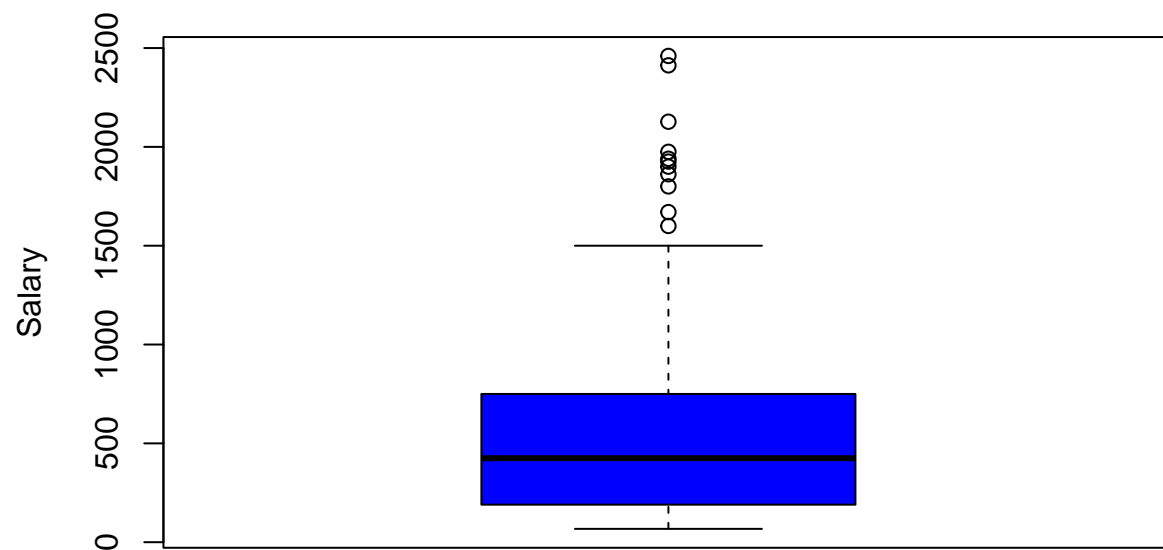
Distribution of Player Salaries



This graph shows that player salaries are heavily skewed right, and a majority of players had a salary under 500,000 dollars.

```
boxplot(hitters$Salary, main="Boxplot of Player Salaries", ylab="Salary", col="blue")
```

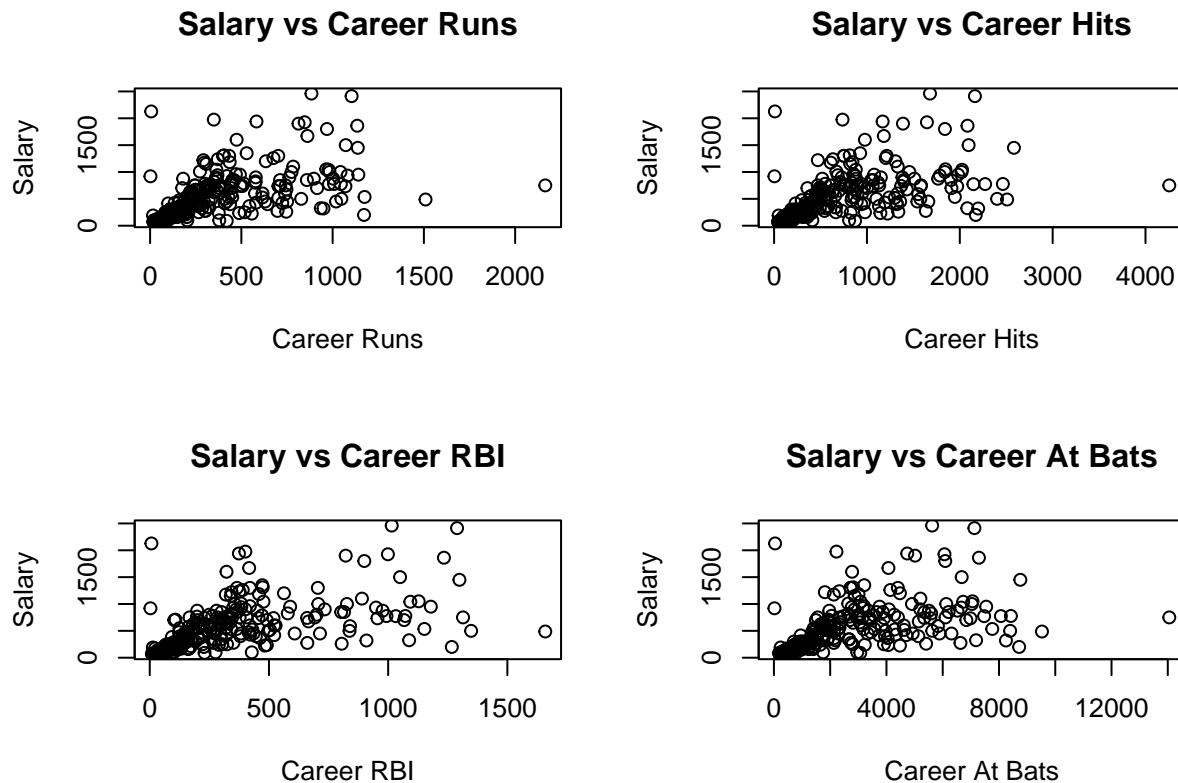
Boxplot of Player Salaries



In fact, using a boxplot we can see there are an unusually large number of outliers on the high end of salaries. We can also see the average is around 500,000 a year.

```
par(mfrow=c(2,2))
plot(hitters$CRuns, hitters$Salary, main="Salary vs Career Runs", xlab="Career Runs", ylab="Salary")
```

```
plot(hitters$CHits, hitters$Salary, main="Salary vs Career Hits", xlab="Career Hits", ylab="Salary")
plot(hitters$CRBI, hitters$Salary, main="Salary vs Career RBI", xlab="Career RBI", ylab="Salary")
plot(hitters$CAtBat, hitters$Salary, main="Salary vs Career At Bats", xlab="Career At Bats", ylab="Salary")
```



Finally, we plot the salary in comparison to the variables that it had the 4 strongest correlation with. All of these graphs look very similar and clearly show a moderate positive correlation between the variable and salary.

Next, we will be training a regression model in order to predict a hitters salary.

```
model <- lm(Salary~.,data=hitters)
summary(model)
```

```
##
## Call:
## lm(formula = Salary ~ ., data = hitters)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -907.62  -178.35   -31.11   139.09  1877.04
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  163.10359    90.77854   1.797  0.073622 .
## AtBat        -1.97987     0.63398  -3.123  0.002008 **
## Hits         7.50077     2.37753   3.155  0.001808 **
## HmRun         4.33088     6.20145   0.698  0.485616
## Runs        -2.37621     2.98076  -0.797  0.426122
## RBI          -1.04496     2.60088  -0.402  0.688204
```

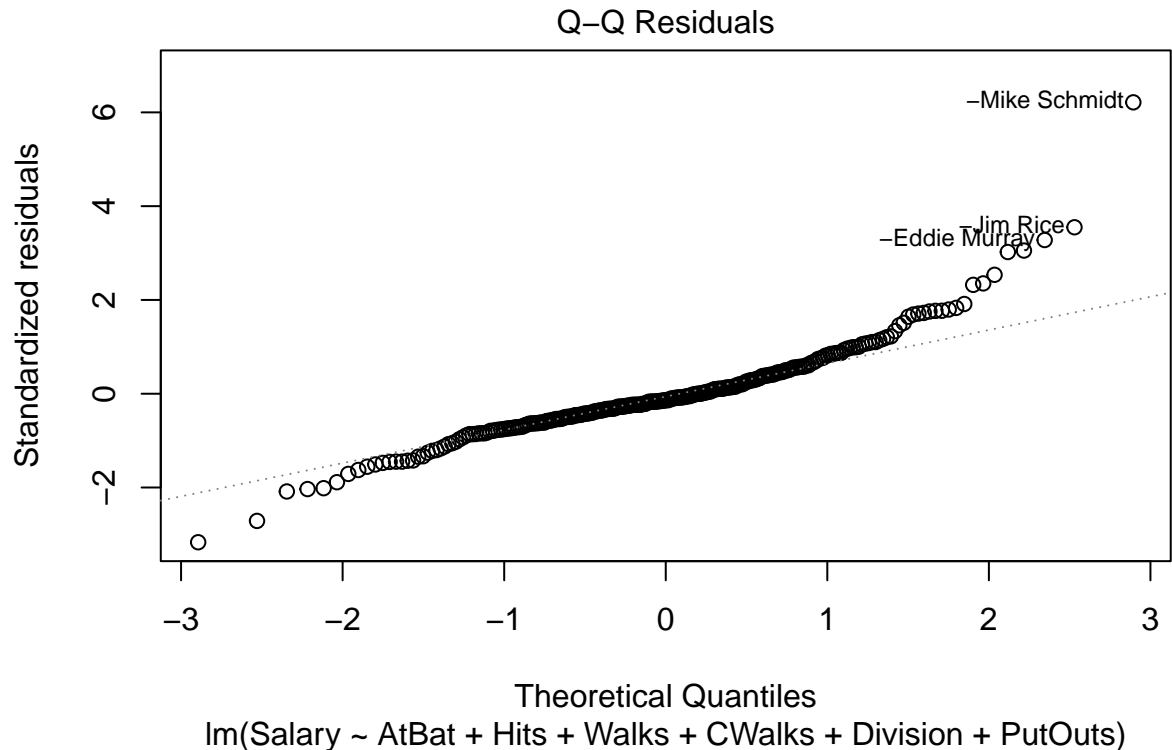
```
## Walks      6.23129    1.82850    3.408 0.000766 ***
## Years     -3.48905   12.41219   -0.281 0.778874
## CAtBat    -0.17134    0.13524   -1.267 0.206380
## CHits      0.13399    0.67455    0.199 0.842713
## CHmRun    -0.17286    1.61724   -0.107 0.914967
## CRuns      1.45430    0.75046    1.938 0.053795 .
## CRBI       0.80771    0.69262    1.166 0.244691
## CWalks    -0.81157    0.32808   -2.474 0.014057 *
## LeagueN    62.59942   79.26140    0.790 0.430424
## DivisionW -116.84925   40.36695   -2.895 0.004141 **
## PutOuts     0.28189    0.07744    3.640 0.000333 ***
## Assists     0.37107    0.22120    1.678 0.094723 .
## Errors     -3.36076    4.39163   -0.765 0.444857
## NewLeagueN -24.76233   79.00263   -0.313 0.754218
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 315.6 on 243 degrees of freedom
## Multiple R-squared:  0.5461, Adjusted R-squared:  0.5106
## F-statistic: 15.39 on 19 and 243 DF,  p-value: < 2.2e-16
```

AtBat, Hits, Walks, CWalks, Division, and PutOuts are all significant at a 95% confidence level so these are the variables we will be using.

```
model <-lm(Salary~AtBat+Hits+Walks+CWalks+Division+PutOuts, data=hitters)
```

Next, we need to check the five assumptions of linearity, we will do that using the diagnostic plots from our model. We will start with normality.

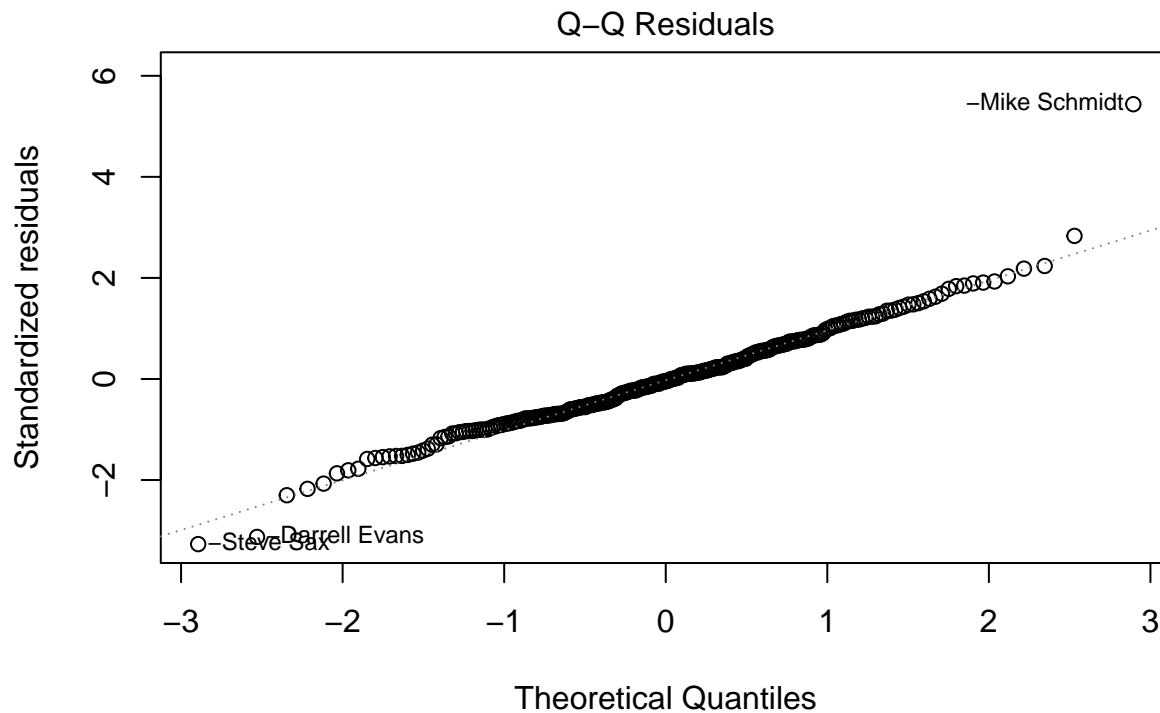
```
plot(model, which=2)
```



From

the Q-Q Residual plot we can see that the normality assumption of our model is violated, we can fix this by modifying the response variable.

```
model <-lm(sqrt(Salary)~AtBat+Hits+Walks+CWalks+Division+PutOuts, data=hitters)
plot(model, which=2)
```

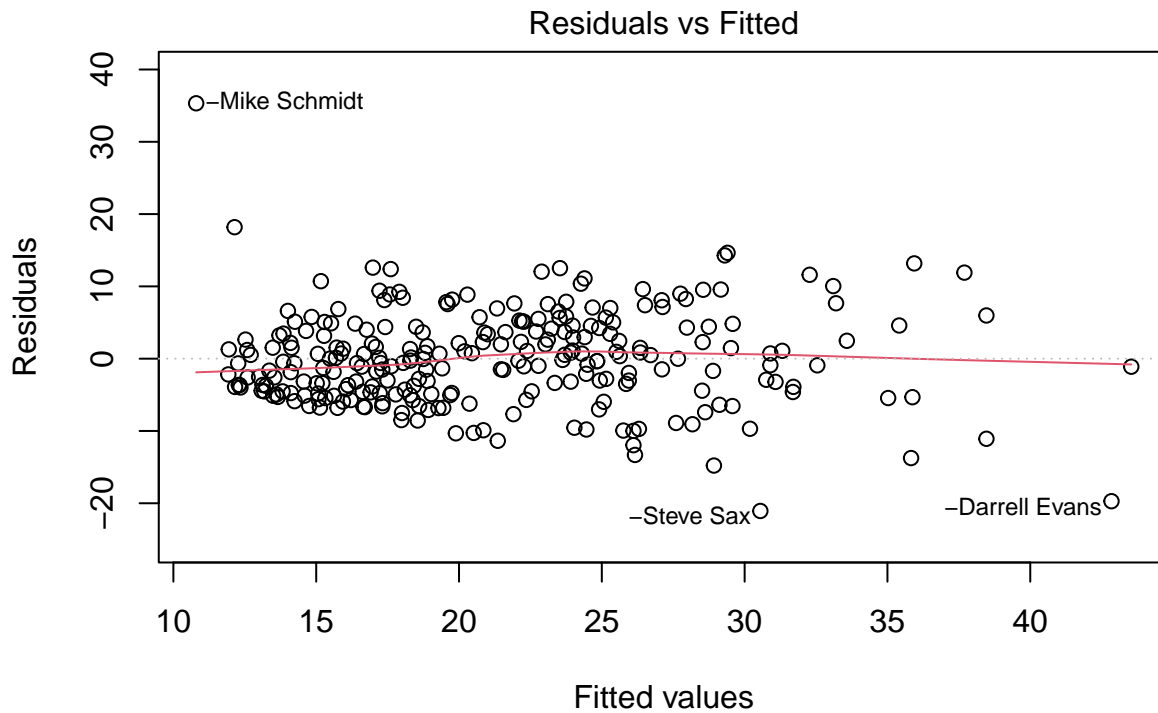


$\text{lm}(\text{sqrt}(\text{Salary}) \sim \text{AtBat} + \text{Hits} + \text{Walks} + \text{CWalks} + \text{Division} + \text{PutOuts})$

By

taking the square root of Salary we fix the normality of our data, next we will see if the linearity of the data holds.

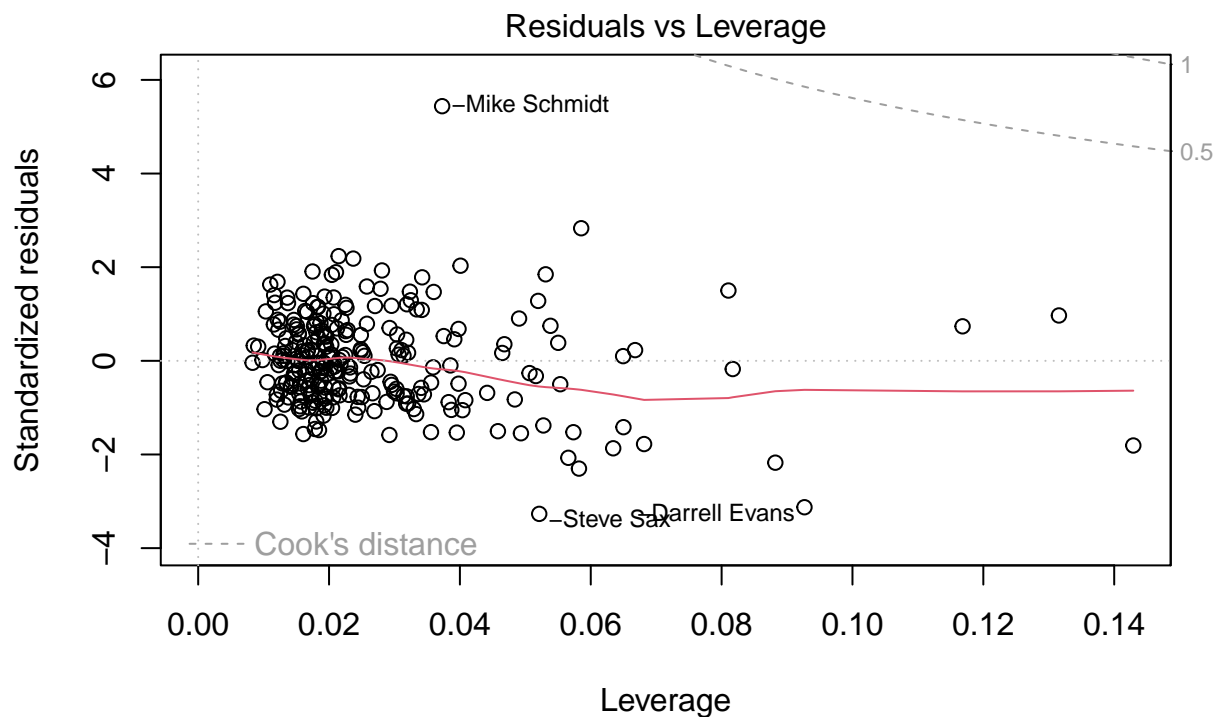
```
plot(model, which=1)
```

$\text{lm}(\text{sqrt}(\text{Salary}) \sim \text{AtBat} + \text{Hits} + \text{Walks} + \text{CWalks} + \text{Division} + \text{PutOuts})$

There does not seem to be a pattern in the residuals and the red line stays mostly flat through zero so our data does not violate the linearity assumption. Next we will check the data for outliers.

```
plot(model, which=5)
```



$\text{lm}(\text{sqrt}(\text{Salary}) \sim \text{AtBat} + \text{Hits} + \text{Walks} + \text{CWalks} + \text{Division} + \text{PutOuts})$

Mike Schmidt is a massive outlier (as his career stats in the dataset are incorrect), Steve Sax and Darrell Evans are also big outliers and all three should be removed.

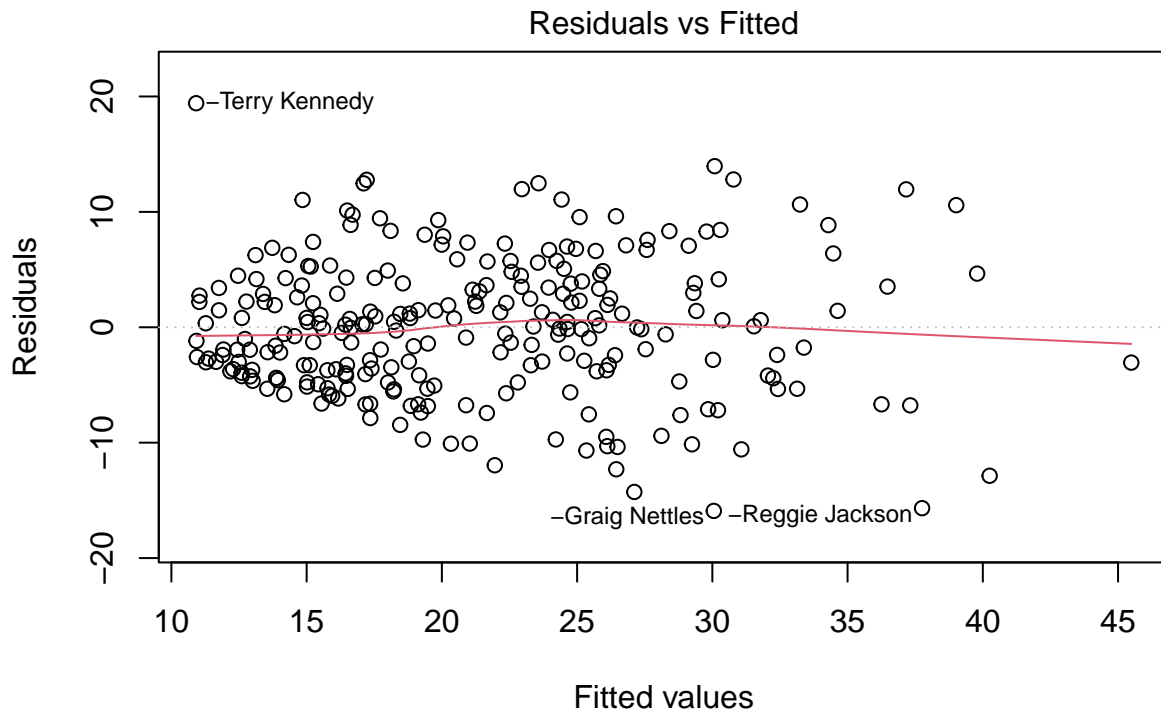
```
Schmidt <- which(hitters$AtBat == 20 & hitters$CRBI == 7)
Sax <-which(hitters$AtBat==633)
Evans <-which(hitters$AtBat==507)
remove <-c(Schmidt, Sax, Evans)
```

Since the dataset does not have row indices and uses player names(which are not numeric and therefore not compatible with slice) I found the index using the which function of the players I want to remove

```
hitters <- hitters %>% slice(-remove)
model <-lm(sqrt(Salary)~AtBat+Hits+Walks+CWalks+Division+PutOuts, data=hitters)
```

Finally, we have to check the homoscedasticity of the model.

```
plot(model, which=1)
```



$\text{lm}(\text{sqrt}(\text{Salary}) \sim \text{AtBat} + \text{Hits} + \text{Walks} + \text{CWalks} + \text{Division} + \text{PutOuts})$

The

Residuals vs Fitted plot show that homoscedasity holds for the regression model.

So our final model is

```
model <-lm(sqrt(Salary)~AtBat+Hits+Walks+CWalks+Division+PutOuts, data=hitters)
```

```
summary(model)
```

```
##
## Call:
## lm(formula = sqrt(Salary) ~ AtBat + Hits + Walks + CWalks + Division +
##     PutOuts, data = hitters)
##
```

```
## Residuals:
##      Min       1Q   Median       3Q      Max
## -15.912  -4.083  -0.034   3.806  19.415
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  8.825795   1.252646   7.046 1.74e-11 ***
## AtBat        -0.027482   0.010016  -2.744 0.006509 **
## Hits          0.162585   0.031677   5.133 5.70e-07 ***
## Walks         0.018217   0.024561   0.742 0.458953
## CWalks        0.017788   0.001619  10.990 < 2e-16 ***
## DivisionW    -1.524899   0.749062  -2.036 0.042818 *
## PutOuts       0.004987   0.001403   3.554 0.000452 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5.966 on 253 degrees of freedom
## Multiple R-squared:  0.5709, Adjusted R-squared:  0.5608
## F-statistic: 56.11 on 6 and 253 DF,  p-value: < 2.2e-16
```

With an Adjusted R Squared of 0.5608 show that our model does a moderately good job at correctly predicted player salaries. The intercept is 8.8258, while our coefficients are -0.028, 0.163, 0.018, 0.018, -1.525, and 0.005.

Overall, we cleaned out the dataset by omitting null values, then preformed exploratory data analysis to try and find potential relationships within the data and get a better feel for the dataset. We then plotted the distribution of salaries and its relationship with othere variables to help visualize the salary variable. Then we created a regression model. First by finding the variables that had the strongest signifcance, then by checking the regression assumptions and modifying our model to ensure the assumptions are kept. One thing that seemed unusual while doing the project is the statistics for Mike Schmidt were incorrect, but the salary was correct causing him to be a massive outlier, it does call into question how accurate the rest of the dataset was.