



$$\sum_{i=2}^{\frac{n}{2}} (n-i)! \quad \frac{n}{2} - 1 \text{ terms}$$

$$= (n-2)! + (n-3)! + (n-4)! + \dots + (n-\frac{n}{2})!$$

$$= 1 \times 2 \times 3 \times \dots \times (n-3) \times (n-2) + 1 \times 2 \times 3 \times \dots \times (n-3) \times 1 + 1 \times 2 \times 3 \times \dots \times (n-\frac{n}{2})$$

$$= 1 \times 2 \times 3 \times \dots \times \underbrace{(n-\frac{n}{2})}_{\frac{n}{2}} + \dots + 1 \times 2 \times 3 \times \dots \times \underbrace{(n-\frac{n}{2})}_{\frac{n}{2}} \times \dots \times (n-3) \times (n-2)$$

$$= \frac{n}{2}! + \frac{n}{2}! \times (\frac{n}{2}+1) + \frac{n}{2}! \times (\frac{n}{2}+1) \times (\frac{n}{2}+2) + \dots + \frac{n}{2}! \times (\frac{n}{2}+1) \times (\frac{n}{2}+2) \times \dots \times (n-2)$$

$$= \frac{n}{2}! \left[1 + (\frac{n}{2}+1) + (\frac{n}{2}+1)(\frac{n}{2}+2) + \dots + (\frac{n}{2}+1)(\frac{n}{2}+2) \dots (n-2) \right]$$

$$= \frac{n}{2}! \left[1 + (\frac{n}{2}+1) \left[1 + (\frac{n}{2}+2) + \dots \right] \right]$$