

CANTHO UNIVERSITY

Chapter 3: Basic Sort and Search

Part 3.2: Searching

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Agenda

- Introduction
- Linear search
- Binary search
- Summary

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What is searching?

- The process of finding an element with a special property in a collection
 - Search a record in a database
 - Search a word in a dictionary
 - Search an element in a list (array)
 - ...
- Problem
 - Input:
 - A sequence of n elements: $\langle a_0, a_1, \dots, a_{n-1} \rangle$
 - An item x
 - Output: Position of x in the sequence

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Search in an array

- Give an array A, find the first occurrence of an item x
- Example: A = [7, 2, 5, 3, 2]: search(x = 2, A) → 1
- Algorithm
 - Start from the first position, compare the element at that position to x.
 - If equal, return that position
 - Else, move the next position

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Algorithm on array

```
#Find an item in an array A of n elements
ALGORITHM linearSearch(x, A, n):
    for pos = 0 to n-1:
        if A[pos].key == x # Compare
            return pos
    return -1 #not found
```

- Complexity
 - In the worst case, there are n comparisons: $T(n) = O(n)$

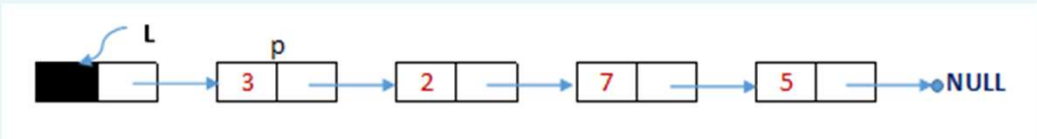
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Search in a linked list


- Give a linked list L, return pointer referring to the first node whose value is x
- Example: search($x = 2$, L) \rightarrow p



- Algorithm
 - Start from the first node's pointer p, compare the node referred by p->next to x.
 - If equal, return p
 - Else, move the next position

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Algorithm on linked list

```

#Find an item x in a linked list
ALGORITHM linearSearch(x, L):
    p = L
    while p->next != NULL:
        if p->next->data == x: #Compare
            return p
        p = p->next


    return p #the pointer of the last node

```

- Complexity
 - In the worst case, there are n comparisons: $T(n) = O(n)$

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Binary search

- Give an ascending sorted array of size n , find the position of a given item x .
- **Intuition:** Compare the target value to the middle element:
 - If equal, return the middle position
 - If not, a half of the array that the target can not lie is eliminated, repeat searching on the other side

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Example 1


Search

Result

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Example 1

Search

Result

start


mid

end

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Example 1


Search Result

start mid end

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Example 1


Search Result

start mid end

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Example 1


Search 45 Result

start 6 mid 8 end 11

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Example 1


Search 45 Result

start 9 mid 5 end 11

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Example 1


Search 45 Result

start 9 mid 10 end 11

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Example 1


Search 45 Result 10

start 9 mid 10 end 11

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Example 2


Search

Result

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Example 2

Search

Result

start


mid

end

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Example 2


Search Result

start mid end

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Example 2


Search Result

start mid end

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Example 2


Search Result

start mid end

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Example 2


Search Result

start mid end

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Example 2


Search Result

start mid end

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Example 2


Search Result

start mid end

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Example 2

Search

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Result

-1

start

0

mid

0


end

-1

5	9	13	16	18	28	31	35	37	38	45	48
0	1	2	3	4	5	6	7	8	9	10	11

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Iterative algorithm

```


ALGORITHM binarySearch(x, A, start, end):
    while start <= end:
        mid = (start + end)/2
        if A[mid].key == x:
            return mid
        else if A[mid].key < x:
            end = mid - 1
        else:
            start = mid + 1
    return -1

```

- Each iteration: one comparison, eliminate a half of elements
- In the worst case: $\sim \log n$ comparisons $\rightarrow T(n) = O(\log n)$

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Recursion version

```

ALGORITHM binarySearch(x, A, start, end):
    if start <= end:
        mid = (start + end)/2
        if x == A[mid]:
            return mid
        else if x < A[mid]:
            return binarySearch(x, A, start, mid - 1)
        else:
            return binarySearch(x, A, mid + 1, end)
    else:
        return -1
  
```

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Recursion tree


Search	45	Result	
--------	----	--------	--

start	0	mid		end	11
-------	---	-----	--	-----	----

n	5	9	13	16	18	28	31	35	37	38	45	48
---	---	---	----	----	----	----	----	----	----	----	----	----

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Recursion tree

Search 45 Result


start 0 mid 5 end 11

n

5	9	13	16	18	28	31	35	37	38	45	48
---	---	----	----	----	----	----	----	----	----	----	----

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Recursion tree

Search 45 Result

start 6 mid 5 end 11

n


5	9	13	16	18	28	31	35	37	38	45	48

n/2

5	9	13	16	18	28	31	35	37	38	45	48
---	---	----	----	----	----	----	----	----	----	----	----

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Recursion tree


Search 45 **Result**

start 6 **mid** 8 **end** 11

n	5	9	13	16	18	28	31	35	37	38	45	48
$n/2$	5	9	13	16	18	28	31	35	37	38	45	48

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Recursion tree


Search 45 **Result**

start 9 **mid** 8 **end** 11

n	5	9	13	16	18	28	31	35	37	38	45	48
$n/2$	5	9	13	16	18	28	31	35	37	38	45	48
$n/4$	5	9	13	16	18	28	31	35	37	38	45	48

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Recursion tree

Search 45

Result

start 9


mid 10

end 11

n	5	9	13	16	18	28	31	35	37	38	45	48
n/2	5	9	13	16	18	28	31	35	37	38	45	48
n/4	5	9	13	16	18	28	31	35	37	38	45	48

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Recursion tree

Search 45

Result 10

start 9


mid 10

end 11

n	5	9	13	16	18	28	31	35	37	38	45	48
n/2	5	9	13	16	18	28	31	35	37	38	45	48
n/4	5	9	13	16	18	28	31	35	37	38	45	48

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Recursion tree

Search 45

Result 10

start 9

mid 10

end 11


n	5	9	13	16	18	28	31	35	37	38	45	48
n/2	5	9	13	16	18	28	31	35	37	38	45	48
n/4	5	9	13	16	18	28	31	35	37	38	45	48

~logn
calls

~ logn function calls, each costs $O(1) \rightarrow T(n) = O(\log n)$

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Summary

- Linear search
 - Can be done in either on array or linked list
 - Takes $O(n)$ time
- Binary search
 - Can only be done on array
 - Takes $O(\log n)$ time

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Q&A

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