



Homework 5 Solutions

2.5.6 (a) AB = AC ~ A-1(AB) = A-1(AC) ~> (A'A)B=(A'A)C~>IB=IC~>B=C if A is invertible.

(b) Here, A is not invertible. In general, [1] [ab]= = [a+c b+d], For example, we would get AB=O if $B = \begin{bmatrix} ab \end{bmatrix}$ has a = -c, b = -d: $\begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} a \\ -a - b \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$

For example: [1] [-10] = [1] [01] You could pick two possible choices for B and C

Infinitely many choicks for a, b.

2.5.11 Many possible solutions. Here are some simple ones: (a) A=[0] and B=[0] are invertible, but A+B=[0] unot. (b) [10] and [00] are not invertible, but A+B=[10] is.

$$\begin{bmatrix} B \mid T \end{bmatrix} = \begin{bmatrix} 2 & -1 & -1 \mid 1 & 0 & 0 \\ -1 & 2 & -1 & 1 & 0 & 0 \\ -1 & -1 & 2 & 0 & 0 & 1 \end{bmatrix} \xrightarrow{Row 3 + \frac{1}{2}Row 1} \begin{bmatrix} 2 & -1 & -1 & | & 1 & 0 & 0 \\ 0 & 3/2 & -3/2 & | & 1/2 & 1 & 0 \\ 0 & -3/2 & 3/2 & | & 1/2 & 0 & 1 \end{bmatrix}$$

Row of 0's means that we connot eliminate all the way to I, which means that B is not invartible-



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$$S_0 A^{-1} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$5x5 \cos 2: A = \begin{bmatrix} 1 - 1 & 1 - 1 & 1 \\ 0 & 1 - 1 & 1 - 1 \\ 0 & 0 & 1 - 1 \end{bmatrix} \quad \text{Guess } A^{-1} = \begin{bmatrix} 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

Gross
$$H_1 = \begin{bmatrix} 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

Multiply to confirm:
$$\begin{bmatrix}
1 & 0 & 0 & 0 \\
0 & 1 & 1 & 0 \\
0 & 0 & 1 & 1 \\
0 & 0 & 0 & 1 \\
0 & 0 & 0 & 1
\end{bmatrix} = \begin{bmatrix}
1 & -1+1 & 1-1 & -1+1 & 1-1 \\
0 & 1 & -1+1 & 1-1 \\
0 & 0 & 0 & 1 & -1+1 \\
0 & 0 & 0 & 1 & -1+1 \\
0 & 0 & 0 & 0 & 1
\end{bmatrix}$$

Now solve
$$A\hat{x} = \begin{bmatrix} 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 2 \end{bmatrix} = \begin{bmatrix} 2 \\ 2 \\ 1 \end{bmatrix}$$





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2.6.8
$$A = L = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\$$

2.6.16
$$L = b$$
: $c_1 = 4$
 $c_1 + c_2 = 5 \rightarrow c_2 = 5 - c_1 = 1$
 $c_1 + c_2 + c_3 = 6 \rightarrow c_3 = 6 - c_1 - c_2 = 1$
 $c_1 + c_2 + c_3 = 6 \rightarrow c_3 = 6 - c_1 - c_2 = 1$
 $A = c = x_1 + x_2 + x_3 = 1 \rightarrow x_2 = 1 - x_3 = 0$
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Solve $AX = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 2 & -1 & 0 & 0 \\ -1 & 2 & -1 & 0 \\ 0 & 0 & -1 & 2 & -1 \\ 0 & 0 & -1 & 2 & -1 \end{bmatrix}$



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From coefficients:
$$\begin{bmatrix} -1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 \end{bmatrix}$$

First solve
$$L^{2} = \begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix}$$
 $\begin{cases} y_{1} + y_{2} \\ y_{1} + y_{2} + y_{3} \\ y_{1} - y_{3} + y_{4} = 4 \end{cases} = 3 \rightarrow y_{3} = 3 - 1 - 1 = 1$

Now solve
$$U = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$
: $x_1 + x_2 + x_3 + x_4 = 1 \rightarrow x_1 = 1 - 0 - (-\frac{1}{2}) - (-1) = \frac{5}{2}$
 $-2x_2 - 2x_3 = 1 \rightarrow x_3 = \frac{1}{2}(1 + 2(-\frac{1}{2})) = 0$
 $-2x_3 - 2x_4 = 1 \rightarrow x_3 = \frac{1}{2}(1 + 2(-1)) = -\frac{1}{2}$
 $-4x_4 - 4 \rightarrow x_4 = -1$

$$50 \Rightarrow -\begin{pmatrix} 5/2 \\ 0 \\ -1/2 \\ -1 \end{pmatrix}$$

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