(a) The speed of rotation of this generator's shaft is

$$n_{\text{sync}} = \frac{120 f_{\text{se}}}{P} = \frac{120 (50 \text{ Hz})}{20} = 300 \text{ r/min}$$

(b) The per-unit phase voltage at rated conditions is $V_{\phi} = 1.0 \angle 0^{\circ}$ and the per-unit phase current at rated conditions is $I_{A} = 1.0 \angle -25.8^{\circ}$ (since the power factor is 0.9 lagging), so the per-unit internal generated voltage is

$$\begin{split} \mathbf{E}_{A} &= \mathbf{V}_{\phi} + R_{A} \mathbf{I}_{A} + j X_{S} \mathbf{I}_{A} \\ \mathbf{E}_{A} &= 1 \angle 0^{\circ} + \big(0.1\big) \big(1 \angle -25.8^{\circ}\big) + j \, \big(0.9\big) \big(1 \angle -25.8^{\circ}\big) \\ \mathbf{E}_{A} &= 1.69 \angle 27.4^{\circ} \text{ pu} \end{split}$$

The base phase voltage is

$$V_{4 \text{ base}} = 12 \text{ kV} / \sqrt{3} = 6928 \text{ V}$$

so the internal generated voltage is

$$E_A = (1.69 \angle 27.4^{\circ} \text{ pu})(6928 \text{ V}) = 11,710 \angle 27.4^{\circ} \text{ V}$$

- (c) The torque angle of the generator is $\delta = 27.4^{\circ}$.
- (d) The base impedance of the generator is

$$Z_{\text{base}} = \frac{3 \ V_{\phi, \text{base}}^2}{S_{\text{base}}^2} = \frac{3 \left(6928 \ \text{V}\right)^2}{200,000,000 \ \text{VA}} = 0.72 \ \Omega$$

Therefore the synchronous reactance is

$$X_s = (0.9)(0.72 \Omega) = 0.648 \Omega$$

and the armature resistance is

$$R_A = (0.1)(0.72 \Omega) = 0.072 \Omega$$

(e) If the field current is held constant (and the armature resistance is ignored), the power out of this generator is given by

$$P = \frac{3V_{\phi}E_{A}}{X_{S}}\sin\delta$$

The max power is given by

$$P_{\text{max}} = \frac{3V_{\phi}E_A}{X_S}\sin 90^\circ = \frac{3(6928 \text{ V})(11,710 \text{ V})}{0.648 \Omega} = 376 \text{ MW}$$

Since the full load power is P = (200 MVA)(0.85) = 170 MW, this generator is supplying 45% of the maximum possible power at full load conditions.

(f) At the maximum power possible, the torque angle $\delta = 90^{\circ}$, so the phasor \mathbf{E}_A will be at an angle of 90° , and the current flowing will be

$$\begin{split} \mathbf{E}_{A} &= \mathbf{V}_{\phi} + R_{A} \mathbf{I}_{A} + j X_{S} \mathbf{I}_{A} \\ \\ \mathbf{I}_{A} &= \frac{\mathbf{E}_{A} - \mathbf{V}_{\phi}}{R_{A} + j X_{S}} \\ \\ \mathbf{I}_{A} &= \frac{11,710 \angle 90^{\circ} \text{ kV} - 6298 \angle 0^{\circ} \text{ kV}}{0.072 + j 0.648 \ \Omega} = 20,400 \angle 34.6^{\circ} \text{ A} \end{split}$$

The impedance angle $\theta = -34.6^{\circ}$, and the reactive power supplied by the generator is

$$Q = 3V_{\phi}I_{A}\sin\theta = 3(6298 \text{ V})(20,400 \text{ A})\sin(-34.6^{\circ}) = -219 \text{ Myar}$$

