

1.

At a location in Europe, it is necessary to supply 1000 kW of 60-Hz power. The only power sources available operate at 50 Hz. It is decided to generate the power by means of a motor-generator set consisting of a synchronous motor driving a synchronous generator. How many poles should each of the two machines have in order to convert 50-Hz power to 60-Hz power?

2.

A six-pole, 60-Hz synchronous machine has a peak fundamental air-gap flux density of 1.23 T. The rotor length is 1.97 m, the rotor radius is 58 cm, and the air-gap length = 3.15 cm. It consists of one full-pitch, 11-turn coil per pole pair, with the coils connected in series to form the phase winding. If the machine is operating at rated speed.

- (a) What is the rated operating speed in r/min?
- (b) Calculate the corresponding flux per pole.
- (c) Calculate the rms generated voltage per phase.

Homework 6

1. motor has P_1 poles,
generator has P_2 poles

$$\frac{P_1}{2} = \frac{50\text{Hz}}{f_1}, \quad \frac{P_2}{2} = \frac{60\text{Hz}}{f_1}$$

$$\Downarrow$$
$$\frac{P_1}{P_2} = \frac{5}{6}$$

Since P_1, P_2 must be even number

$$\frac{P_1}{P_2} = \frac{10}{12} = \begin{cases} P_1 = 10N \\ P_2 = 12N \end{cases}, N \in \mathbb{N}^*$$

2. (a) $\frac{n}{60} = \frac{6}{\frac{P_1}{2}}$

$$n = 1200 \text{ r/min}$$

(b) $\Phi = \int B ds$

$$= \frac{2}{\mu} 2lBr$$

$$= \frac{2}{6} \times 2 \times 1.97 \times 1.23 \times 0.58$$

$$= 0.9369 \text{ V}$$

(c) $V = \frac{\sqrt{2}}{2} 2\pi f N \Phi$

$$= 4.44 \times 60 \times 11 \times 0.9369$$

$$= 2745 \text{ V}$$