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the Rain Classroom

Department of Electrical Engineering
Tsinghua University

High Voltage Engineering

Spring 2025, Lecture 4

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March 13, 2025

Chapter 2 Insulation Characteristics of Air under Different Voltage Waveforms

- 2.1** Analysis of electric field distribution and field adjustment
- 2.2** Insulation characteristics of air under continuous applied voltage
- 2.3** Insulation characteristics of air under lightning impulse voltage
- 2.4** Insulation characteristics of air under switching impulse voltage
- 2.5** Measures to increase gas gap breakdown voltage

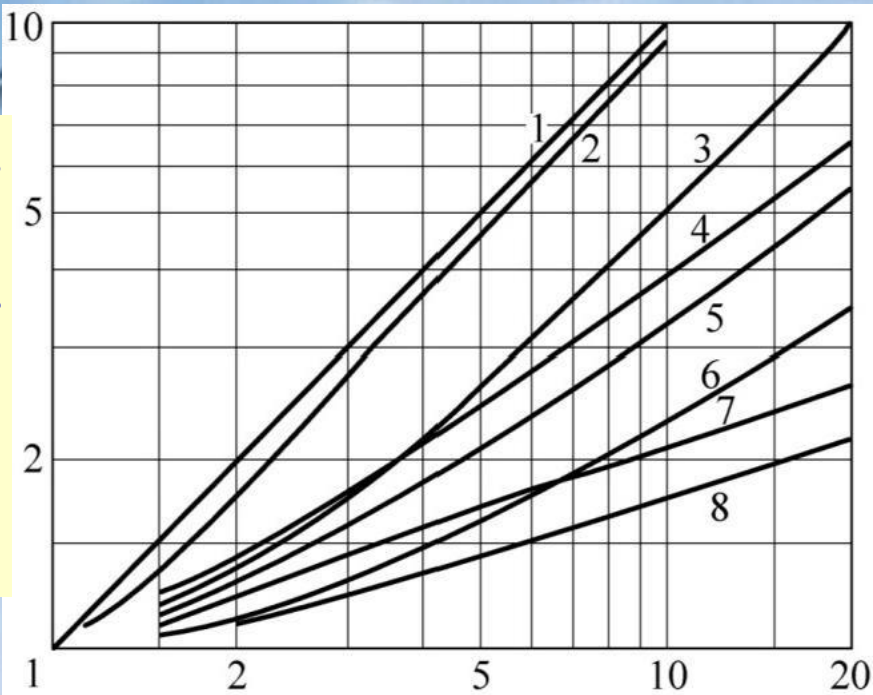
Core concepts of this chapter:

high voltage and high electric stress, non-uniform field, electric field control, lightning and switching impulse voltage, 50% breakdown voltage, v-t characteristics, breakdown strength of air, high vacuum insulation, SF₆ insulation

What is the difference on the focus of Chat 1 & 2?

Chat 1: Internal physical process, discharge mechanism, how discharge happens? What is the criterion of discharge? What is the factor which may influence the discharge?.....

Chat 2: Apply above principle to actual situation, guide the design and predict or analyze the possible results



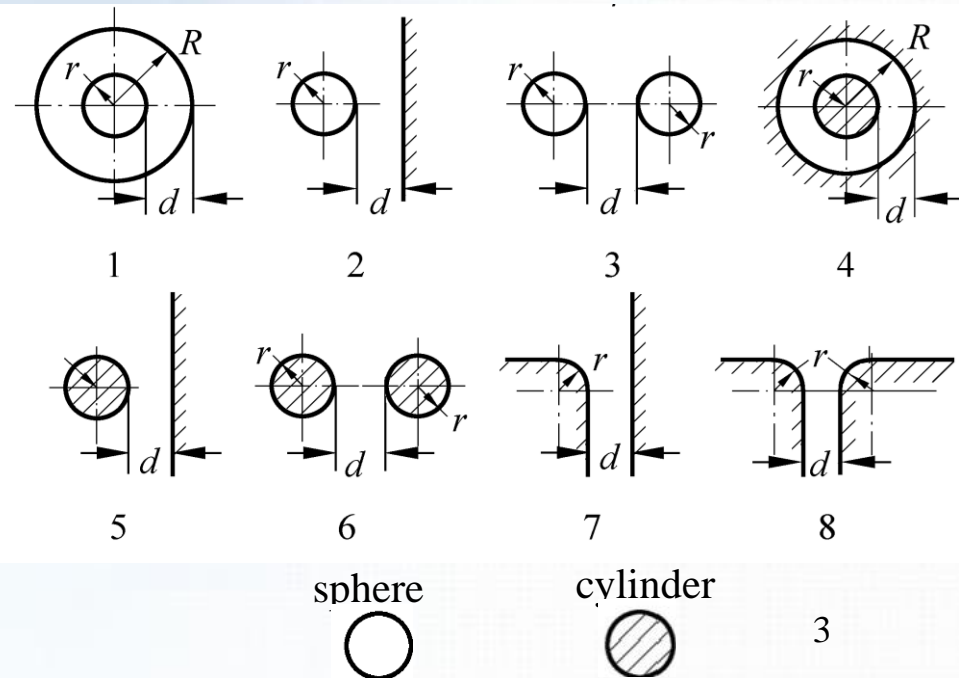
Geometric characteristic factor

$$p = \frac{r+d}{r}$$

- Under the same size, **symmetric field is more uniform than asymmetric one**

2.1 Analysis of electric field distribution and field adjustment

- Under the same size, **field on cylindrical surfaces are more uniform than spherical surfaces**



2.2 Insulation characteristics of air under continuous applied voltage (AC & DC)

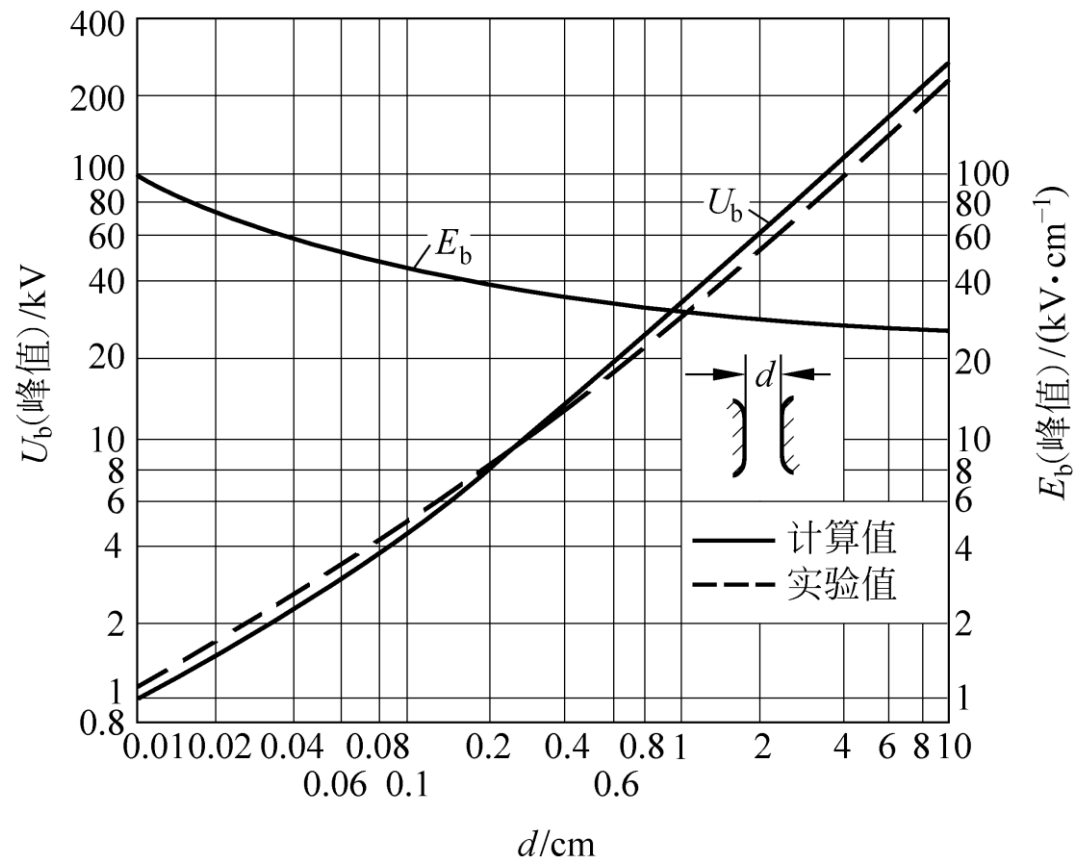
2.2.1 Insulation characteristics of air gaps in a uniform electric field

$$U_b = 24.22\delta d + 6.08 \sqrt{\delta d} \text{ (peak)}$$

The breakdown strength of air under various voltages in a uniform electric field is almost the same, roughly equal to **30kV/cm (peak)**

It is difficult to realize large scale uniform electric field in engineering practice

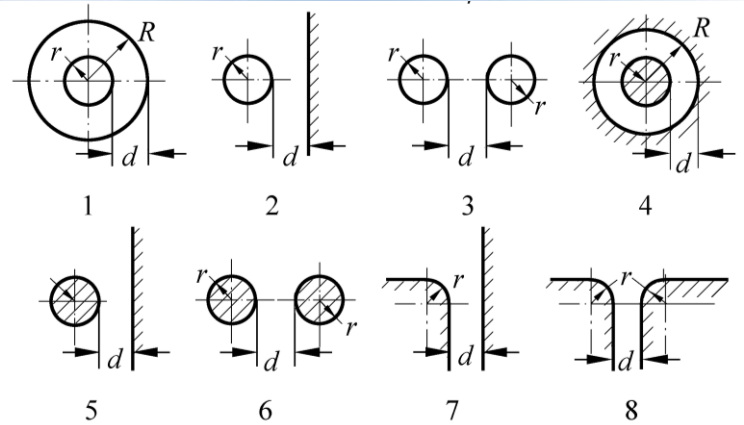
In electrical equipment, the distance of a uniform electric field is not long



2.2 Insulation characteristics of air under continuous applied voltage (AC&DC)

2.2.2 Insulation characteristics of air gaps in slightly non-uniform electric fields

$$U = E_{\max} \frac{d}{f} \quad U_b = U_c = E_0 \frac{d}{f}$$



- Slightly non-uniform field: **no obvious corona phenomenon** before breakdown. When the highest field stress E_{\max} reaches the corona inception stress E_0 , the applied voltage U is the corona inception voltage U_c , and is also the breakdown voltage U_b
- For slightly non-uniform fields, **field non-uniformity** has a significant impact on the discharge/breakdown voltage
- Slightly non-uniform fields are often estimated using simplified typical electrodes using the empirical formula in Table 2-1.

- Table 2-1 presents the corona inception stress formula for several typical electrode configurations, in peak value
- **Digital calculation** of field distribution is very helpful and powerful now!
- If no available empirical formula to obtain the E_0 , **then 30kV/cm can be used** at the beginning



2.2 Insulation characteristics of air under continuous applied voltage (AC&DC)

2.2.3 Insulation characteristics of air gaps in extremely non-uniform electric fields

- For extremely non-uniform fields, the field non-uniformity has limited or little effect on the breakdown voltage.
- Obvious corona before breakdown, big difference between corona inception voltage and gap breakdown voltage.
- The empirical formula in Table 2-1 can also estimate the corona inception voltage/stress, but cannot estimate the gap breakdown voltage of extremely non-uniform fields!

The gap breakdown voltage of extremely non-uniform fields is mainly obtained through experiments (1:1 experiment), or by referring to curves obtained under similar experiment conditions.

The breakdown voltage cannot be calculated from discharge theory!

Extremely non-uniform fields classified into rod-rod (symmetric) and rod-plane (asymmetric)
voltage polarity: positive or negative polarity

Symmetrical and voltage polarity are the two most important factors influence breakdown

2.2 Insulation characteristics of air under continuous applied voltage

2.2.3 Insulation characteristics of air gaps in extremely non-uniform electric fields

Positive rod-plane: $E_b \approx 4.5 \text{ kV/cm}$

Negative rod-plane: $E_b \approx 10 \text{ kV/cm}$

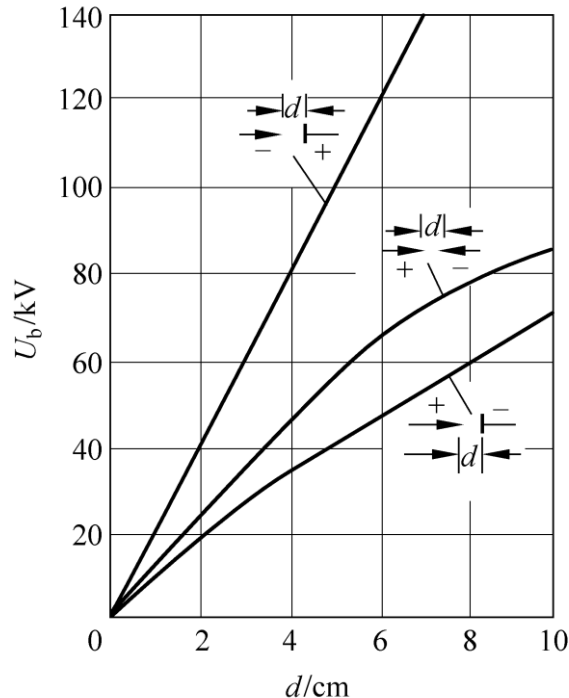


Figure 2-12 Relation between DC breakdown voltage and air gap distance of point-plane and point-point

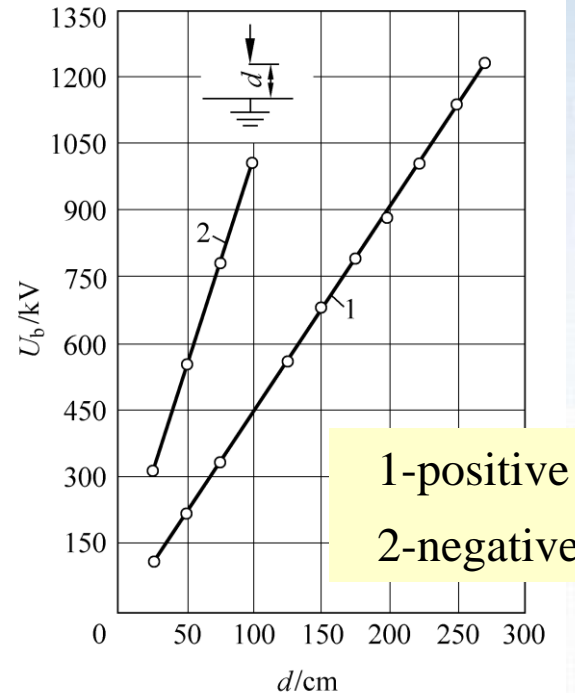


Figure 2-13 Relation between DC breakdown voltage and gap distance of rod-plane air gap

Symmetrical and voltage polarity are the two most important factors influence breakdown

- U_b cannot be calculated, **can be obtained from experiment**
- Qualitative and rough judgment and analysis are also important

2.2 Insulation characteristics of air under continuous applied voltage

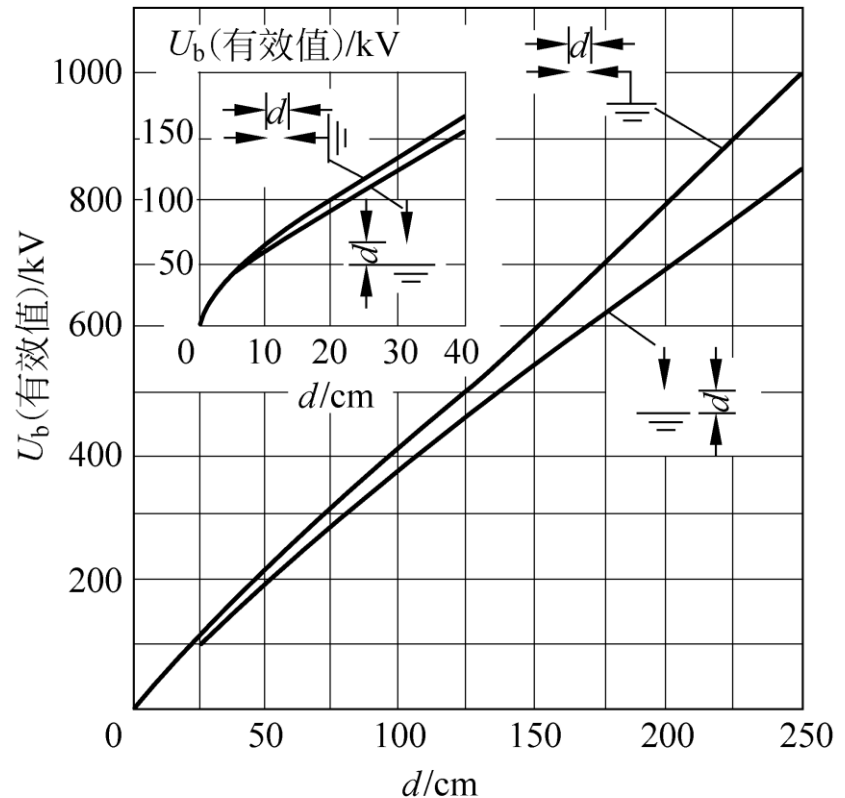
2.2.3 Insulation characteristics of air gaps in extremely non-uniform electric fields

Rod-rod: $E_b \approx 4.0 \text{ kV/cm (rms)}$
 $\approx 5.66 \text{ kV/cm (peak)}$

Rod-plane: $E_b \approx 3.7 \text{ kV/cm (rms)}$
 $\approx 5.23 \text{ kV/cm (peak)}$

Breakdown voltage U_b can be
obtained from experiment

Gap breakdown under AC voltage
occurs in the positive half wave



Extremely non-uniform fields classified into **rod-rod** (symmetric) and **rod-plane** (asymmetric)
voltage polarity: positive or negative polarity

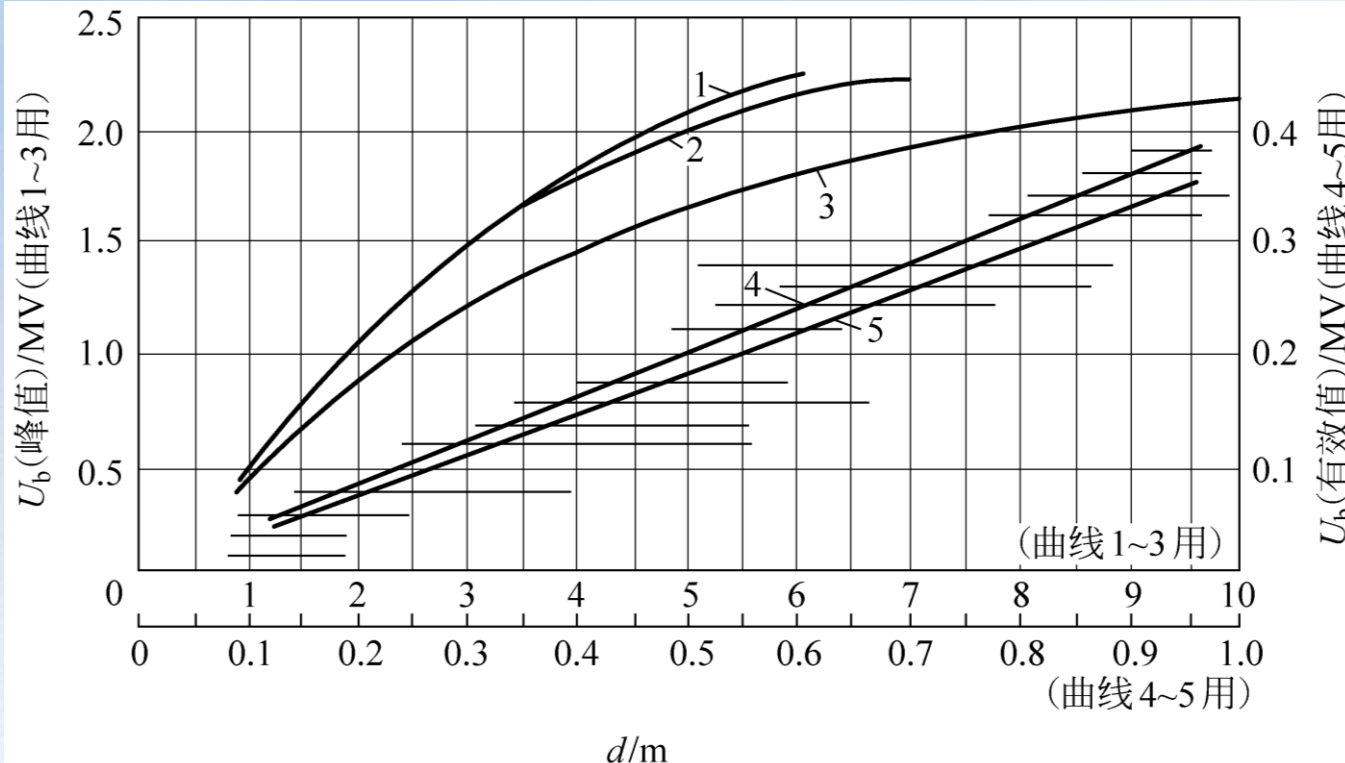
Symmetrical and voltage polarity are the two most important factors influence breakdown

2.2 Insulation characteristics of air under continuous applied voltage

2.2.3 Insulation characteristics of air gaps in extremely non-uniform electric fields

Long gap rod-plane:

$d = 10\text{m}$, $E_b \approx 210 \text{ kV/m}$ (peak)
or $\approx 150 \text{ kV/m}$ (rms)



The saturation of gap breakdown voltage with increasing gap distance is the significant characteristics of long air gap under AC voltage

Symmetrical and voltage polarity are the two most important factors influence breakdown **for extremely non-uniform electric field**

Chapter 2 Insulation Characteristics of Air under Different Voltage Waveforms

- 2.1 Analysis of electric field distribution and field adjustment
- 2.2 Insulation characteristics of air under continuous applied voltage
- 2.3 Insulation characteristics of air under lightning impulse voltage
- 2.4 Insulation characteristics of air under switching impulse voltage
- 2.5 Measures to increase gas gap breakdown voltage

Core concepts of this chapter:

high voltage and high electric stress, non-uniform field, electric field control, lightning and switching impulse voltage, 50% breakdown voltage, v-t characteristics, breakdown strength of air, high vacuum insulation, SF₆ insulation

2.3 Insulation characteristics of air under lightning impulse voltage

2.3.1 Formation and waveform of lightning impulse voltage

- ✚ Cloud to cloud lightning, inner-cloud lightning, and cloud to ground lightning, as well as the accumulation and distribution of electric charges inside thunderclouds
- ✚ Polarity of lightning, Upward and downward thunder
- ✚ The development process and the stepped leader, main discharge; Component of lightning;
- ✚ The field strength between thunder cloud and the ground;
- ✚ The potential of thunder cloud and the potential of the object being struck;
- ✚ The discharge current and electricity of lightning to the ground.
- ✚ The destructive power of lightning strikes



2.3 Insulation characteristics of air under lightning impulse voltage

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- ✚ The discharge current and electricity of lightning to the ground.
- ✚ The destructive power of lightning strikes
- ✚ Waveform of lightning impulse voltage



What are the key points when we discussing the lightning impulse voltage in Chapter 2?

2.3 Insulation under light

- ## (1) Standard waveform

(2) Time lag of discharge

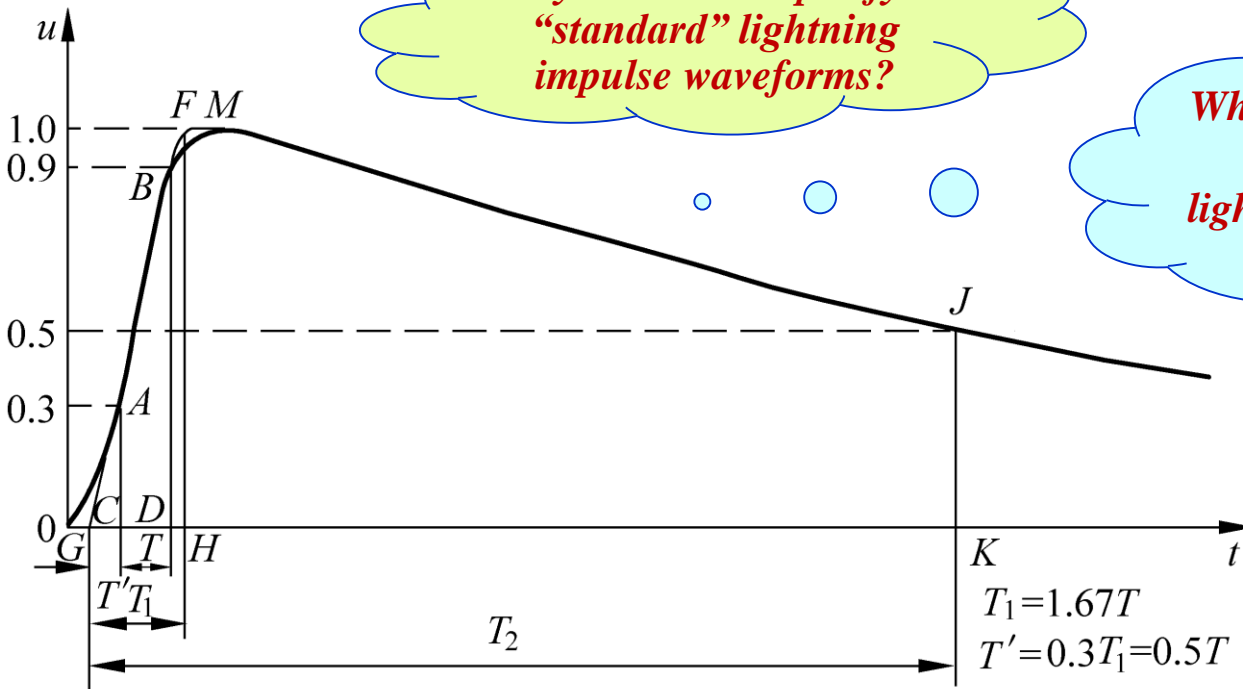
(3) 50% breakdown voltage

(4) v-t characteristic

Why we need to specify a “standard” lightning impulse waveforms?

What is the relation between laboratory standard lightning strikes and natural lightning strikes?

Think about the similarities and differences between "simulation" and "reproduction"



The full waveform of lightning impulse voltage

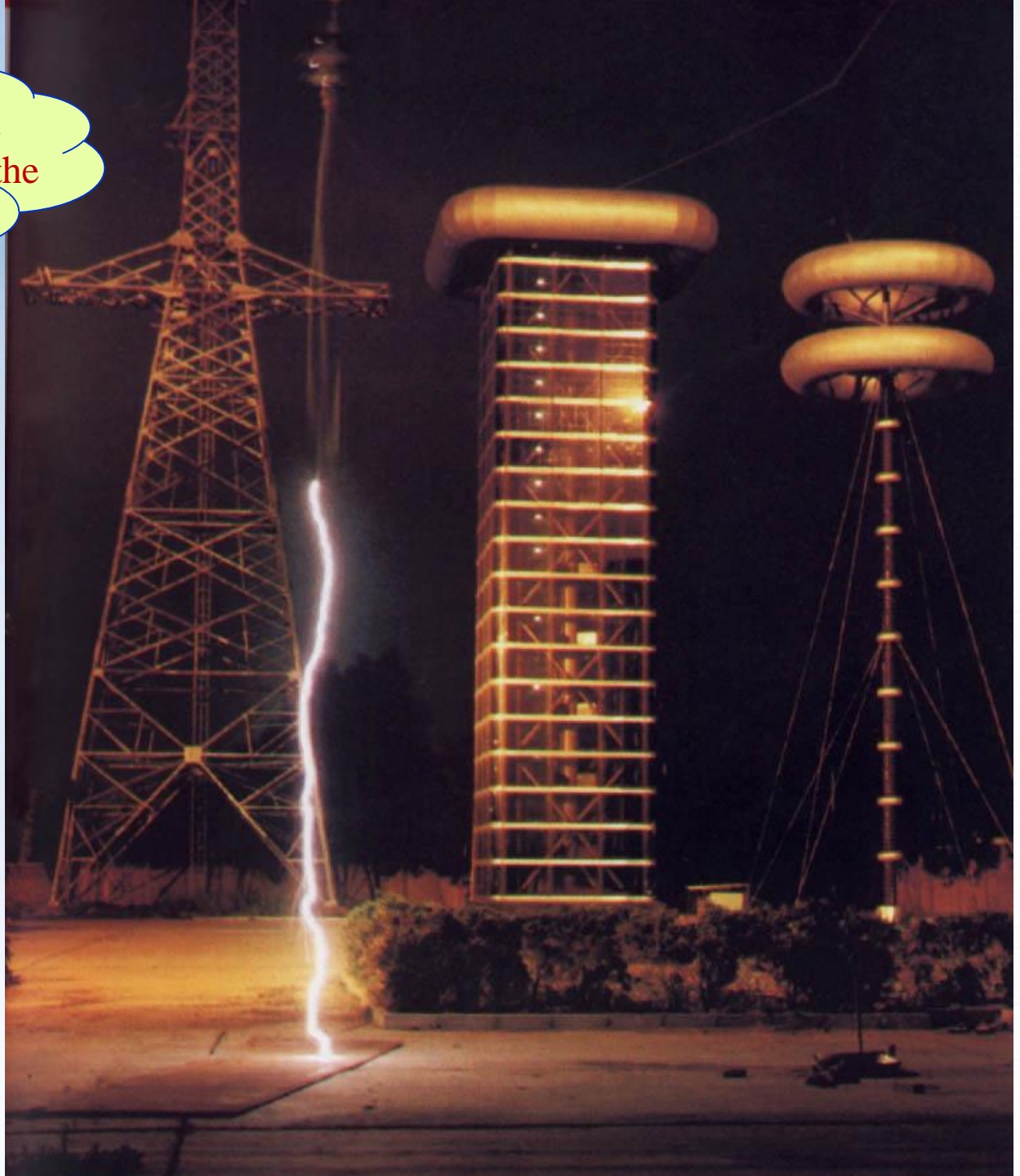
Standard waveform 1. 2/50 μ s
(1. 2 \pm 30%、 50 \pm 20%)

Is laboratory "standard" lightning impulse a "standard amplitude" impulse?

How to generate simulated lightning impulse voltage in the laboratory? See Chapt 6

The air gap breakdown under artificially simulated lightning impulse voltage

Think about the similarities and differences between "simulation" and "reproduction"



2.3 Insulation characteristics of air under lightning impulse voltage

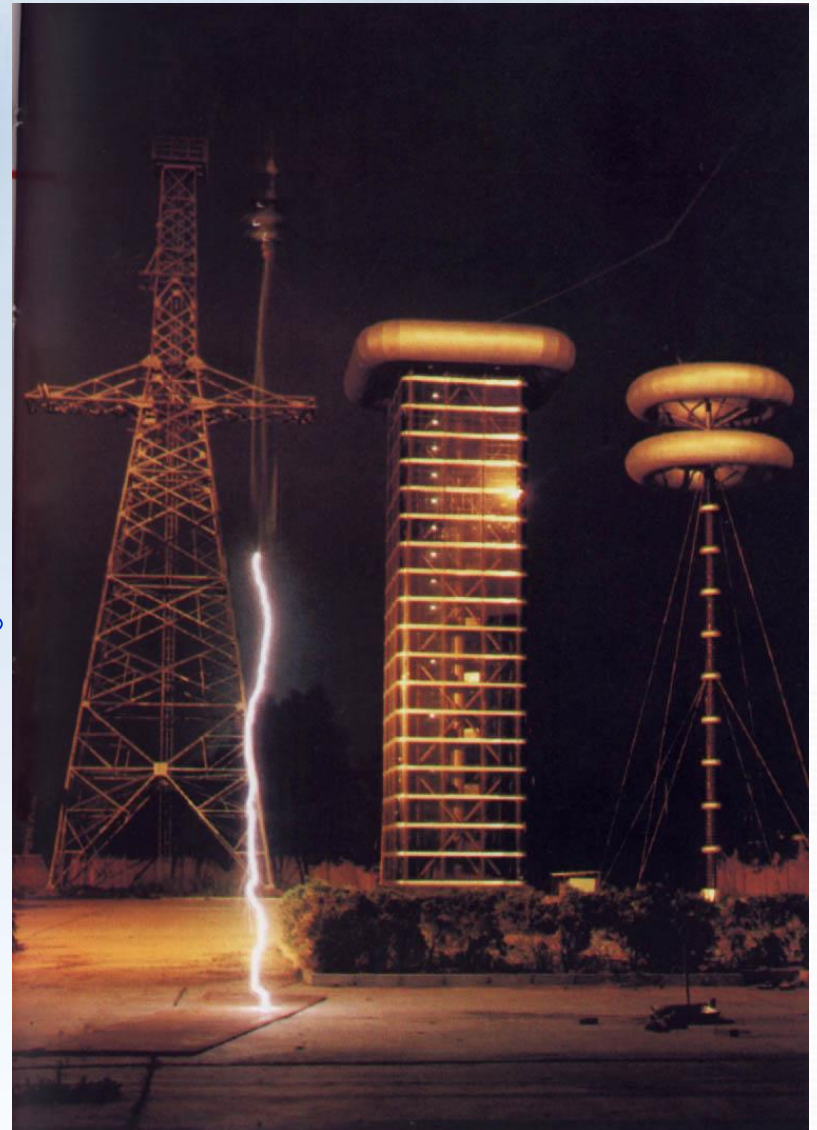
(1) Standard waveform

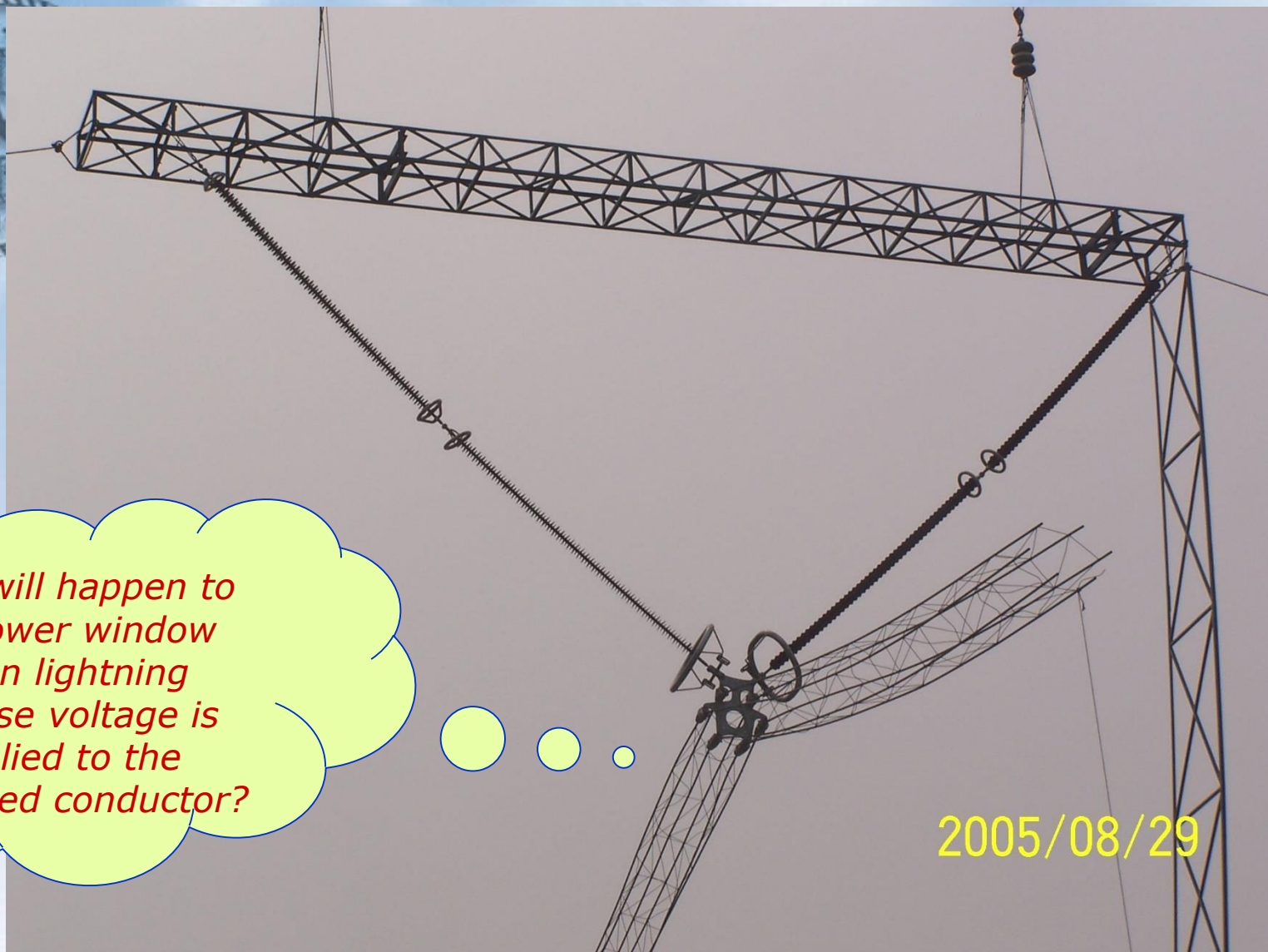
- (2) Time lag of discharge
- (3) 50% breakdown voltage
- (4) v-t characteristic

When a standard impulse voltage applied to an air gap, what is the measured voltage waveform of the gap if breakdown occurs

What is the measured voltage waveform if there is no breakdown

How to define the breakdown voltage?





*What will happen to
the tower window
when lightning
impulse voltage is
applied to the
simulated conductor?*

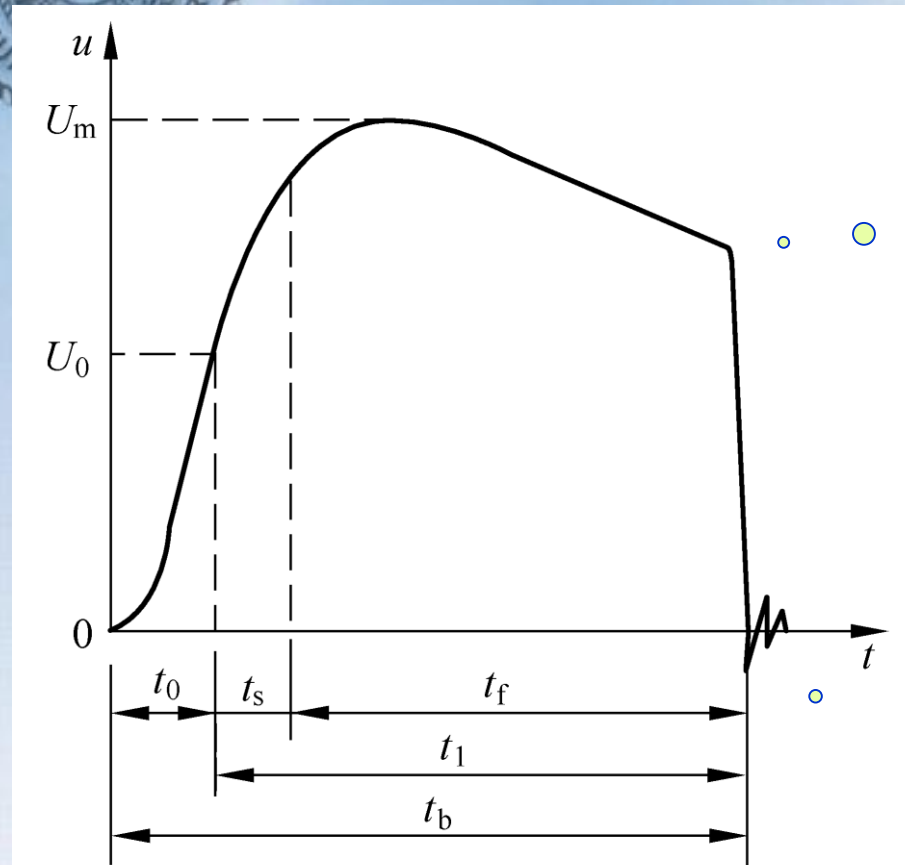
Simulated tower window and simulated conductor



Typical lightning impulse discharge path

2.3 Insulation characteristics of air under lightning impulse voltage

- (1) Standard waveform
- (2) Time lag of discharge
- (3) 50% breakdown voltage
- (4) v-t characteristic



How to define the breakdown voltage?

Why is there a discharge time lag in impulse voltage?

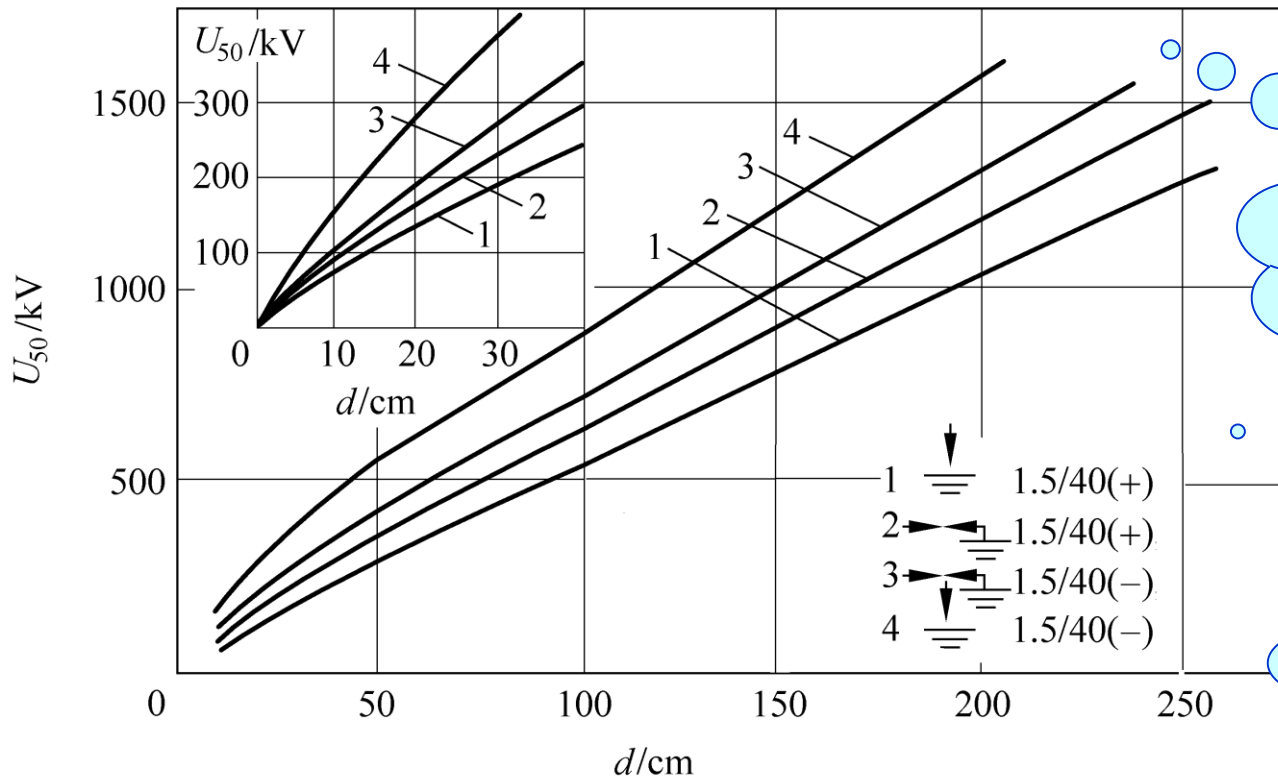
What's the influence of field distribution to time lag, and time lag to breakdown voltage?

Time lag of discharge $t_d = \text{statistical time lag } t_s + \text{formation time lag } t_f$

Uniform/slightly non-uniform electric fields are dominated by t_s with short time lag, while extremely non-uniform electric fields are dominated by t_f with long time lag

2.3 Insulation characteristics of air under lightning impulse voltage

- (1) Standard waveform
- (2) Time lag of discharge
- (3) 50% breakdown voltage U_{50}
- (4) v-t characteristic



When several standard LI voltage applied to an air gap, how to define the U_b ?

*What is U_{50} ?
Why to use U_{50} ?
How to obtain U_{50} ?*

Figure 2-22 Relation between lightning impulse 50% breakdown voltage and gap distance of rod-rod and rod-plane air gap

1-1.5/40(+), $d > 40\text{cm}$, $U_b = 40 + 5d$; 2-1.5/40(+), $d > 40\text{cm}$, $U_b = 75 + 5.56d$
 3-1.5/40(-), $d > 40\text{cm}$, $U_b = 110 + 6d$; 4-1.5/40(-), $d > 40\text{cm}$, $U_b = 215 + 6.7d$

2.3 Insulation characteristics of air under lightning impulse voltage

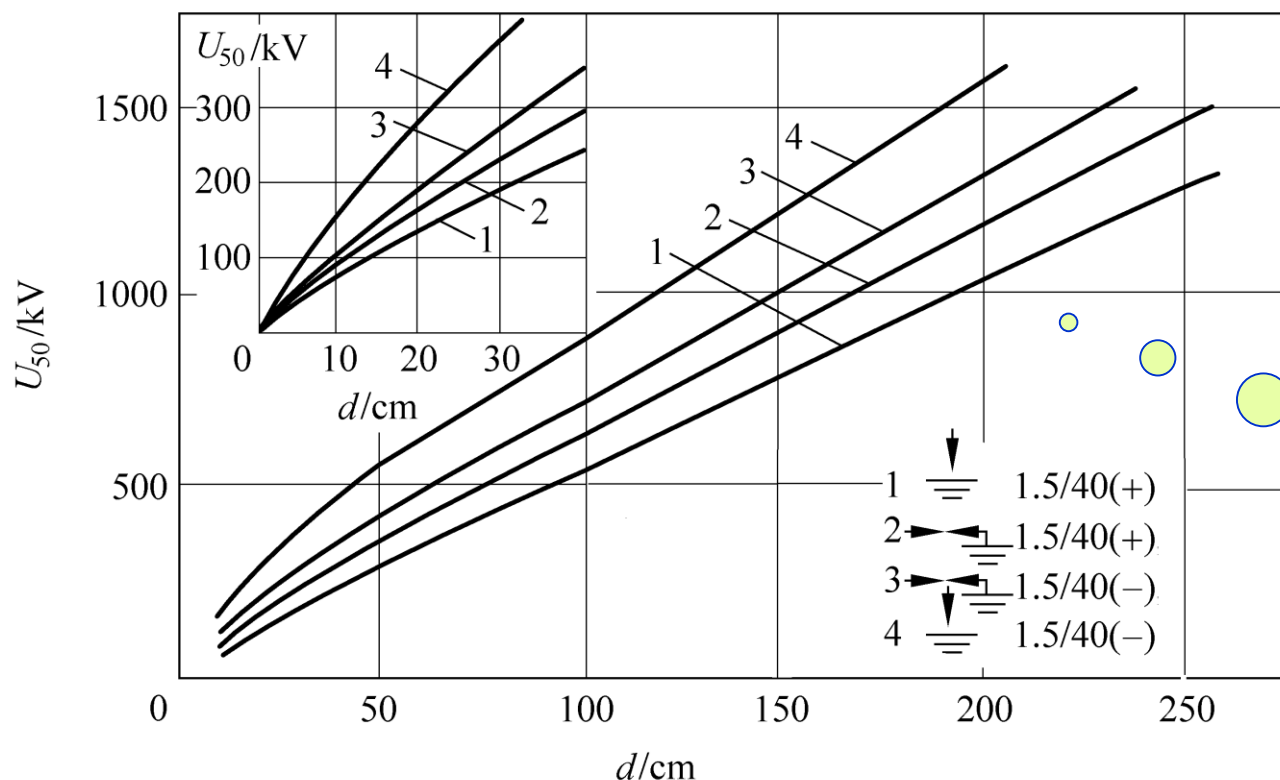
- For impulse voltage, **50% breakdown voltage U_{50}** is generally used to represent the insulation characteristics of a gap
 - **The simplest method** to determine the U_{50} for a gap: Keeping the standard waveform unchanged, stepwise increase the voltage magnitude, apply per level of voltage for 10 times, until 4-6 breakdown occurs, then this voltage can be used as the approximate U_{50} of the gap
 - The more impulse in each voltage level is applied, the more accurate the U_{50} will be
 - **Another method** to obtain U_{50} by experiment is called “Up-and-Down”(Chapter 7)
- When using U_{50} to determine gap insulation distance, necessary margin should be left
 - The discharge probability of impulse voltage is generally considered to follow a Gauss distribution, and the relative standard deviation σ of lightning impulse voltage is $\approx 3\%$
 - **$U_{50} (1-1.3\sigma) = 0.96U_{50}$ is commonly used as the withstand voltage for self recoverable outdoor insulation gaps**, with a withstand probability of **90%**. For occasions with higher safety requirements, **$U_{50} (1-3\sigma) = 0.91U_{50}$** can be used as the withstand voltage of the gap with a withstand probability of **99.85%**.

Gas insulation can be quickly self-recovered (self-restoring insulation)

2.3 Insulation characteristics of air under lightning impulse voltage

50% breakdown voltage U_{50}
(generally believed to follow a
Gauss distribution)

$$U_{\text{withstand}} = U_{50} (1 - n\sigma)$$



*Lightning impulse
voltage ($\sigma \approx 3\%$)*

*The breakdown voltage
curve of impulse
voltage is a strip-
shaped area*

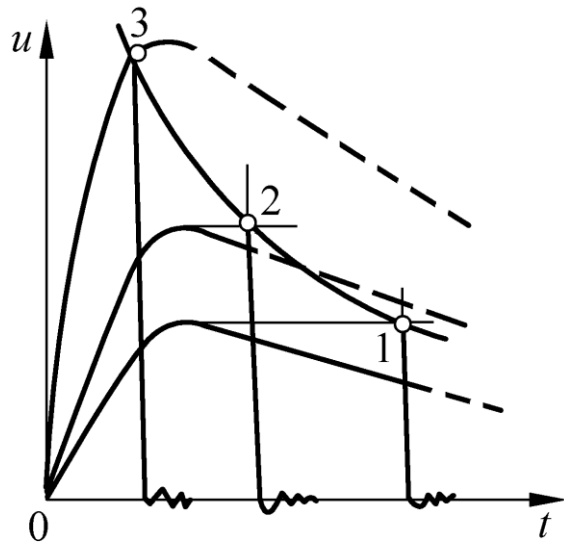
Figure 2-22 Relationship between lightning impulse 50% breakdown voltage and gap distance of rod-rod and rod-plane air gap

1-1.5/40(+), $d > 40$ cm, $U_b = 40 + 5d$; 2-1.5/40(+), $d > 40$ cm, $U_b = 75 + 5.56d$
3-1.5/40(-), $d > 40$ cm, $U_b = 110 + 6d$; 4-1.5/40(-), $d > 40$ cm, $U_b = 215 + 6.7d$

2.3 Insulation characteristics of air under lightning impulse voltage

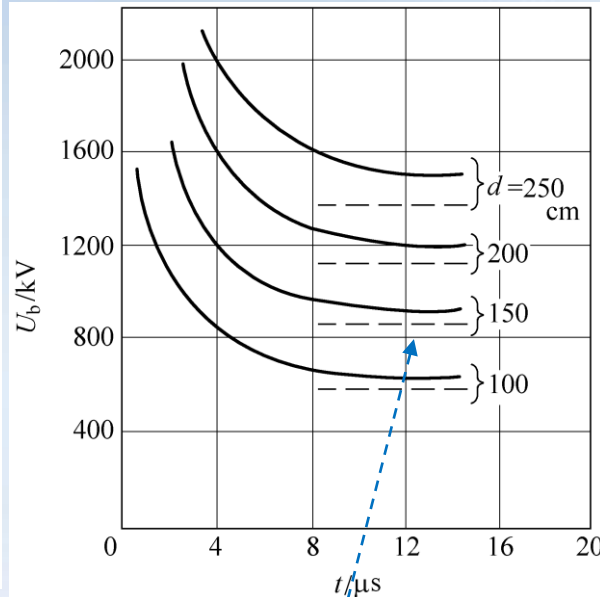
Due to the influence of time lag, the v-t curve of a uniform field are relatively flat, but tend to increase significantly when time decrease for an extremely non-uniform field

- (1) Standard waveform
- (2) Time lag of discharge
- (3) 50% breakdown voltage
- (4) v-t characteristic**



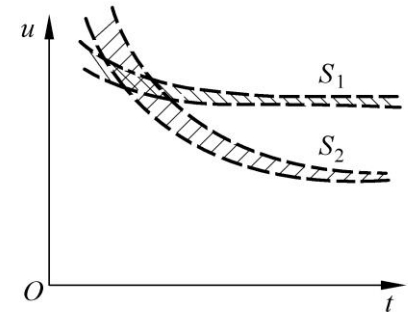
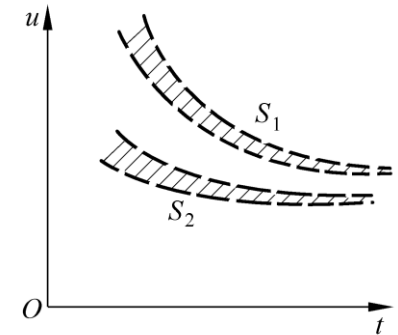
Obtaining the voltage-time characteristic curve

Lightning protection in
Chapter 9



v-t curve of rod-rod air gap

(dotted line represents the power frequency breakdown voltage of the gap)

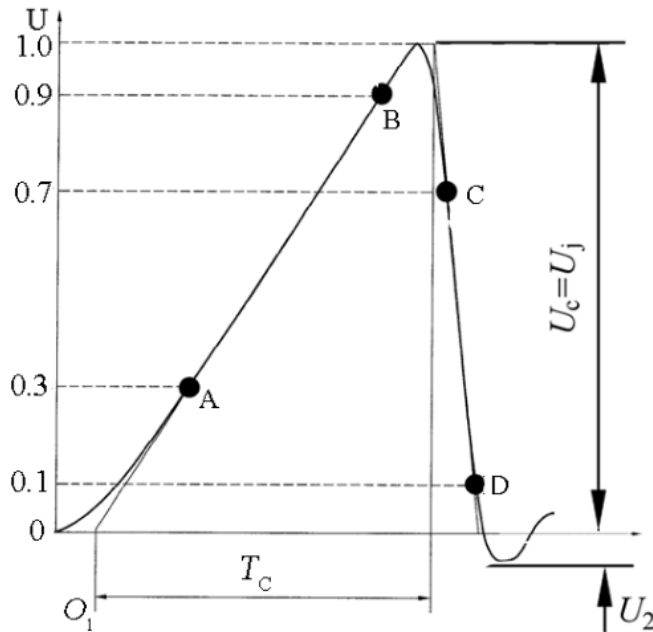


v-t curves of two parallel gap clearances

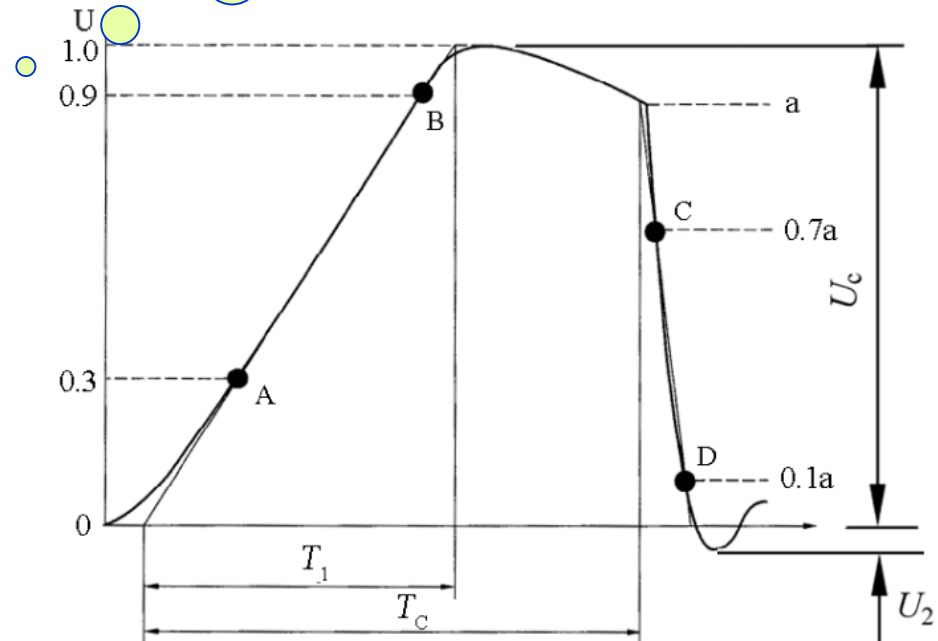
2.3 Insulation characteristics of air under lightning impulse voltage

Standard waveform of **chopped impulse voltage**

Some internal insulation of electrical equipment, such as transformers and motor windings, are more afraid of chopped-wave impulse and **require chopped-wave tests**



(a)



(b)

Schematic waveform diagram of chopped lightning impulse voltage

(a) Wave chopped at front

(b) Wave chopped at tail

Insulation is normally punctured by the amplitude of applied voltage.
But in some case, steepness of applied voltage is the most important factor.

Chapter 2 Insulation Characteristics of Air under Different Voltage Waveforms

- 2.1 Analysis of electric field distribution and field adjustment
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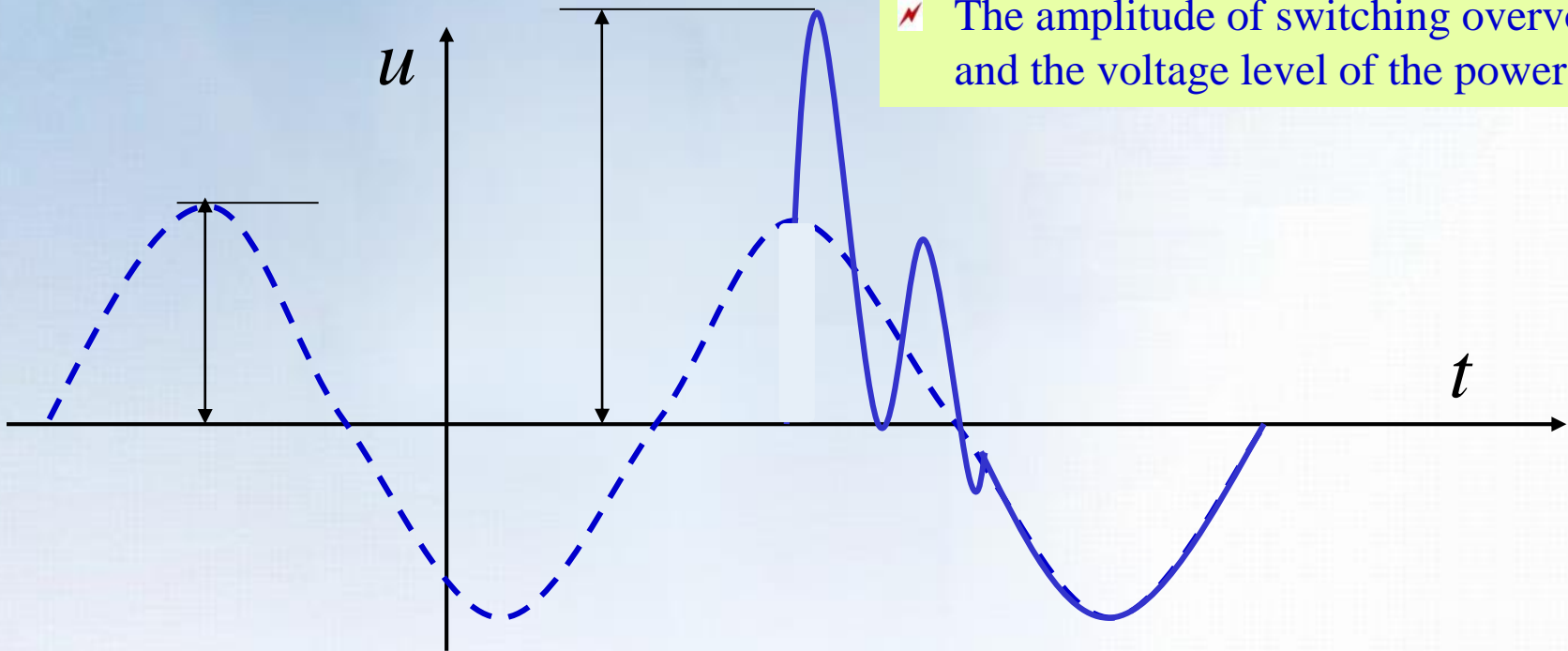
Core concepts of this chapter:

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2.4 Insulation characteristics of air under switching impulse voltage

2.4.1 Occurrence of switching impulse voltage and its waveform

- ⚡ Transition process and switching overvoltage in power system
- ⚡ Waveform of switching overvoltage
- ⚡ The amplitude of switching overvoltage and the voltage level of the power grid



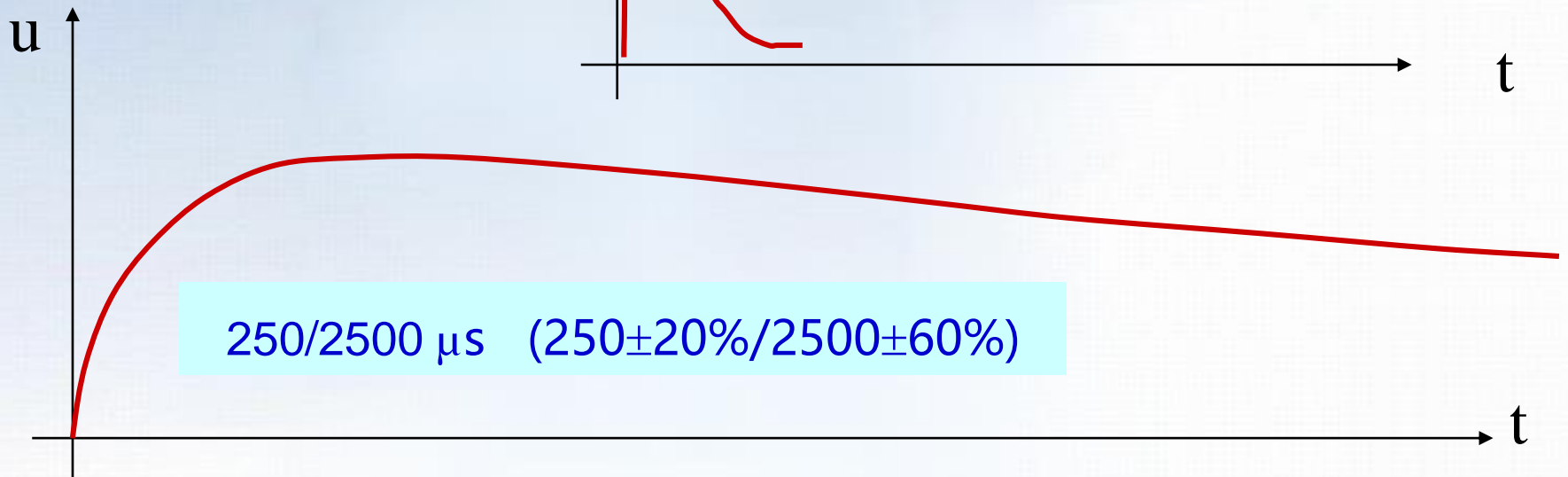
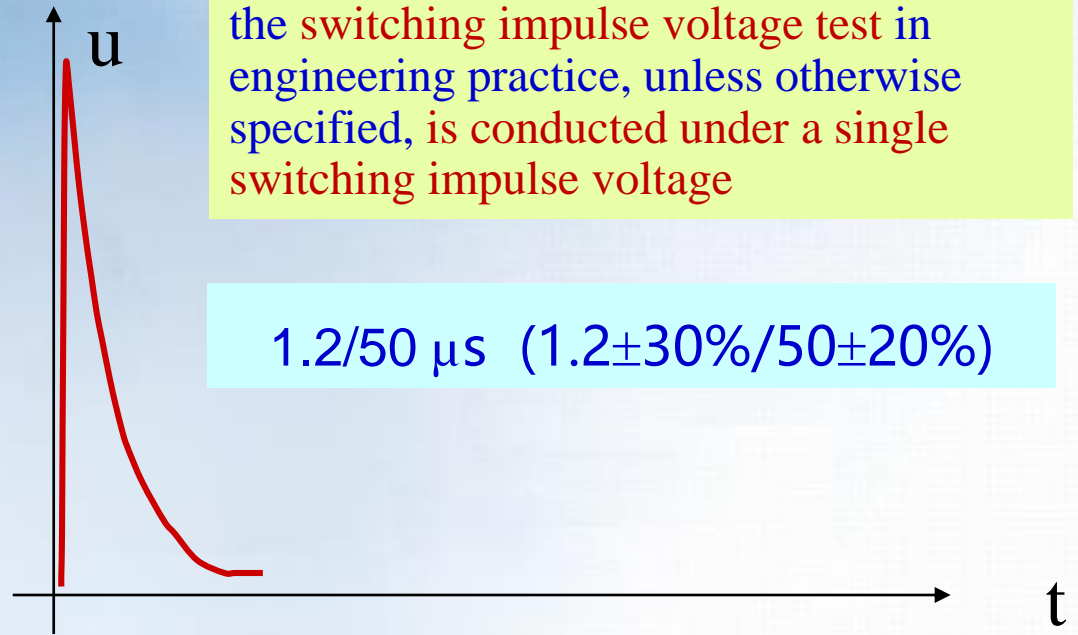
Using which type of tests to **simulate switching impulse voltage**, and **insulation characteristics** of air gaps under simulated switching impulse voltage are the main concerns in this section.

Switching overvoltage protection is described in Chapter 10.



Waveform comparison:
standard lightning
impulse voltage
and
standard switching
impulse voltage

Although the actual switching overvoltage in the power system is superimposed on different phases of the AC voltage, the switching impulse voltage test in engineering practice, unless otherwise specified, is conducted under a single switching impulse voltage

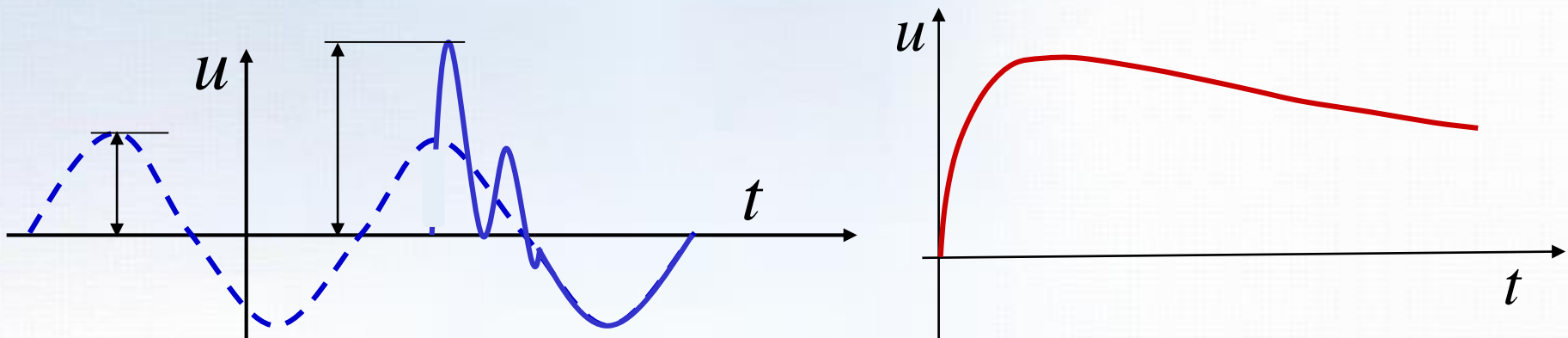


2.4.2 Characteristics of switching impulse voltage

Although the actual switching overvoltage in the power system is superimposed on different phases of the AC voltage, the **switching impulse voltage test** in engineering practice, unless otherwise specified, is **conducted under a single switching impulse voltage**

- (1) U-shaped curves
- (2) Polarity effect of asymmetric electric field
- (3) The saturation phenomenon of long air gaps
- (4) 50% breakdown voltage and dispersion
- (5) Effect of nearby earthed object
- (6) Empirical formula for minimum air gap breakdown voltage

Think about the similarities and differences between "simulation" and "reproduction"



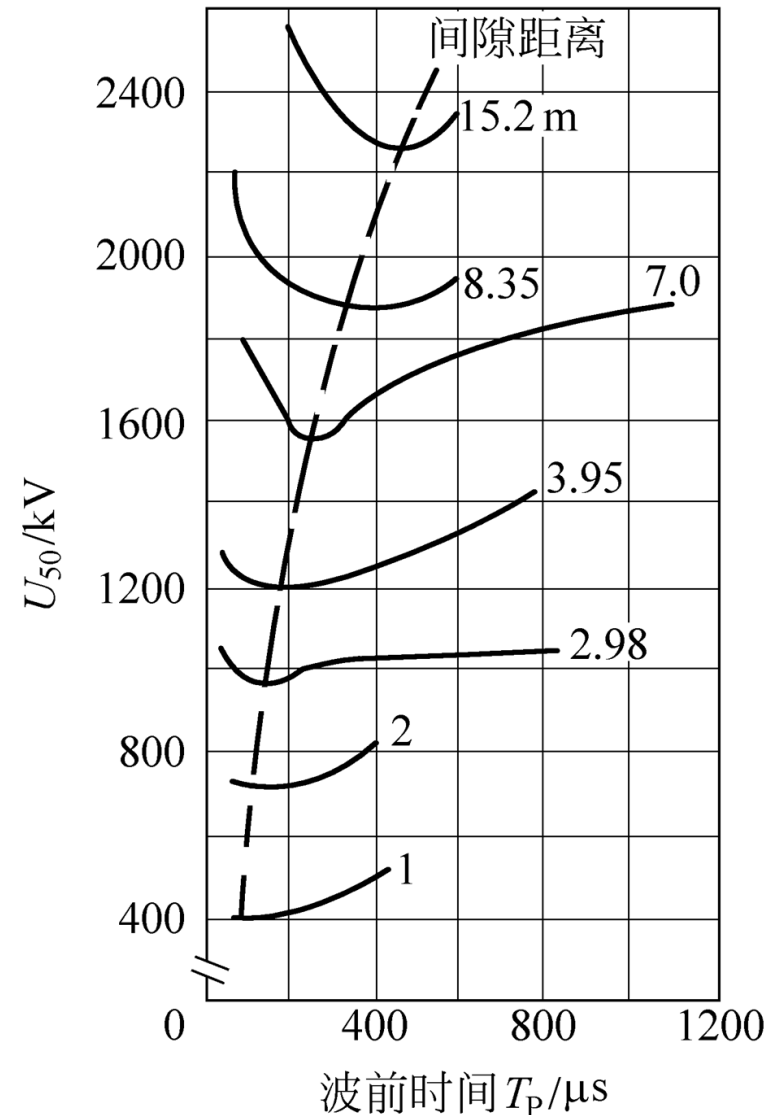
2.4.2 Characteristics of switching impulse voltage

Positive rod-plane air gap switching impulse voltage

The critical wavefront time increases with the increase of gap distance.

For gaps distance $< 7\text{m}$, the critical wave front time is between $100\text{-}300\ \mu\text{s}$

U-shaped curves



2.4.2 Characteristics of switching impulse voltage

Positive rod-plane air gap switching impulse voltage

The critical wavefront time increases with the increase of gap distance.

For gaps distance $< 7\text{m}$, the critical wave front time is between $100\text{-}300\ \mu\text{s}$

Therefore, a long gap requires a long wave front switching impulse voltage test, which cannot be done with only 250/2500 standard wave

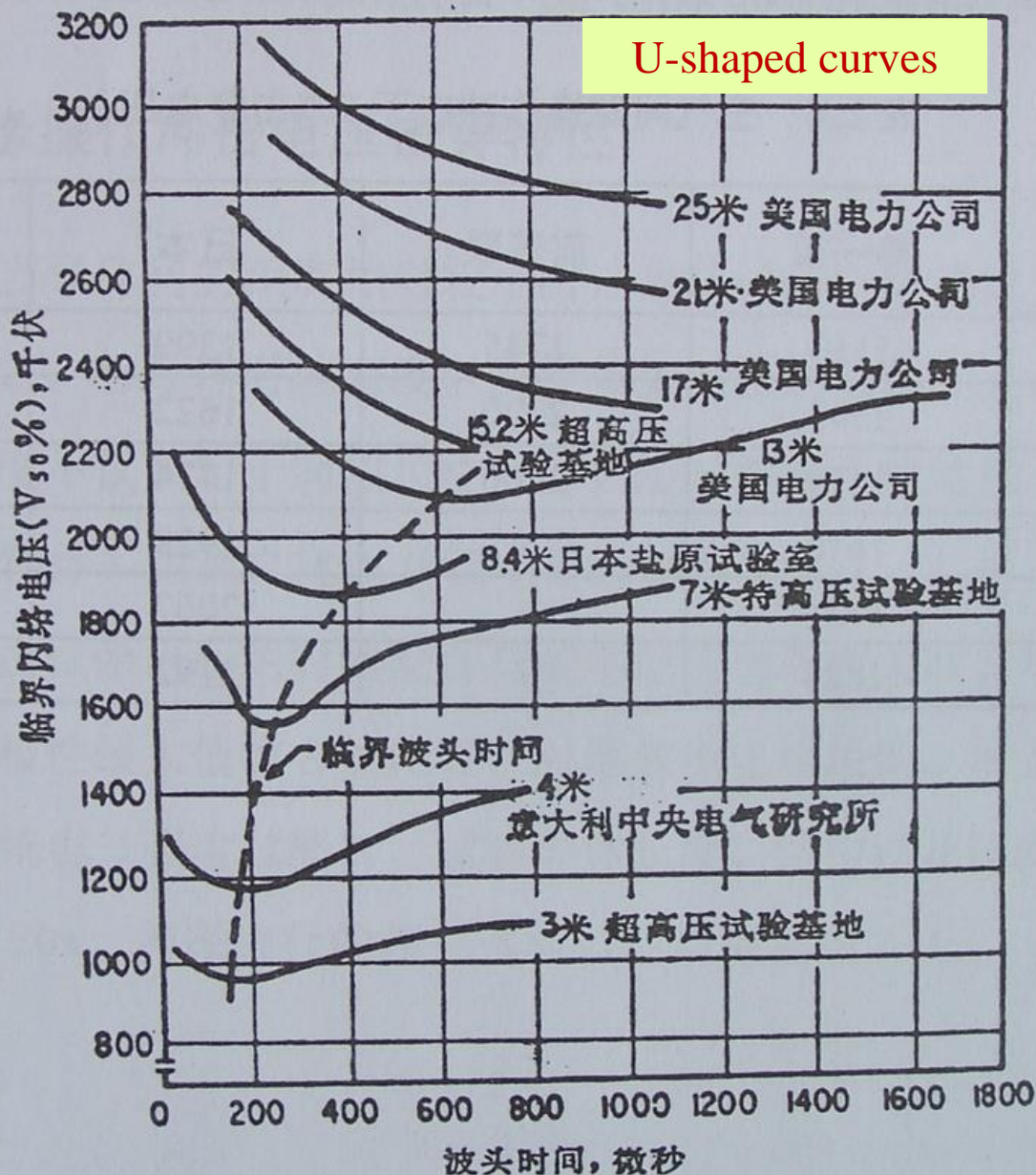


图 2-2 棒—板间隙临界闪络电压

2.4.2 Characteristics of switching impulse voltage

Positive rod-plane air gap switching impulse voltage

Therefore, a long gap requires a long wave front switching impulse voltage test, which cannot be done with only 250/2500 standard wave

The switching impulse breakdown voltage of the rod-plane gap is sometimes lower than the peak breakdown voltage at power frequency

U-shaped curves

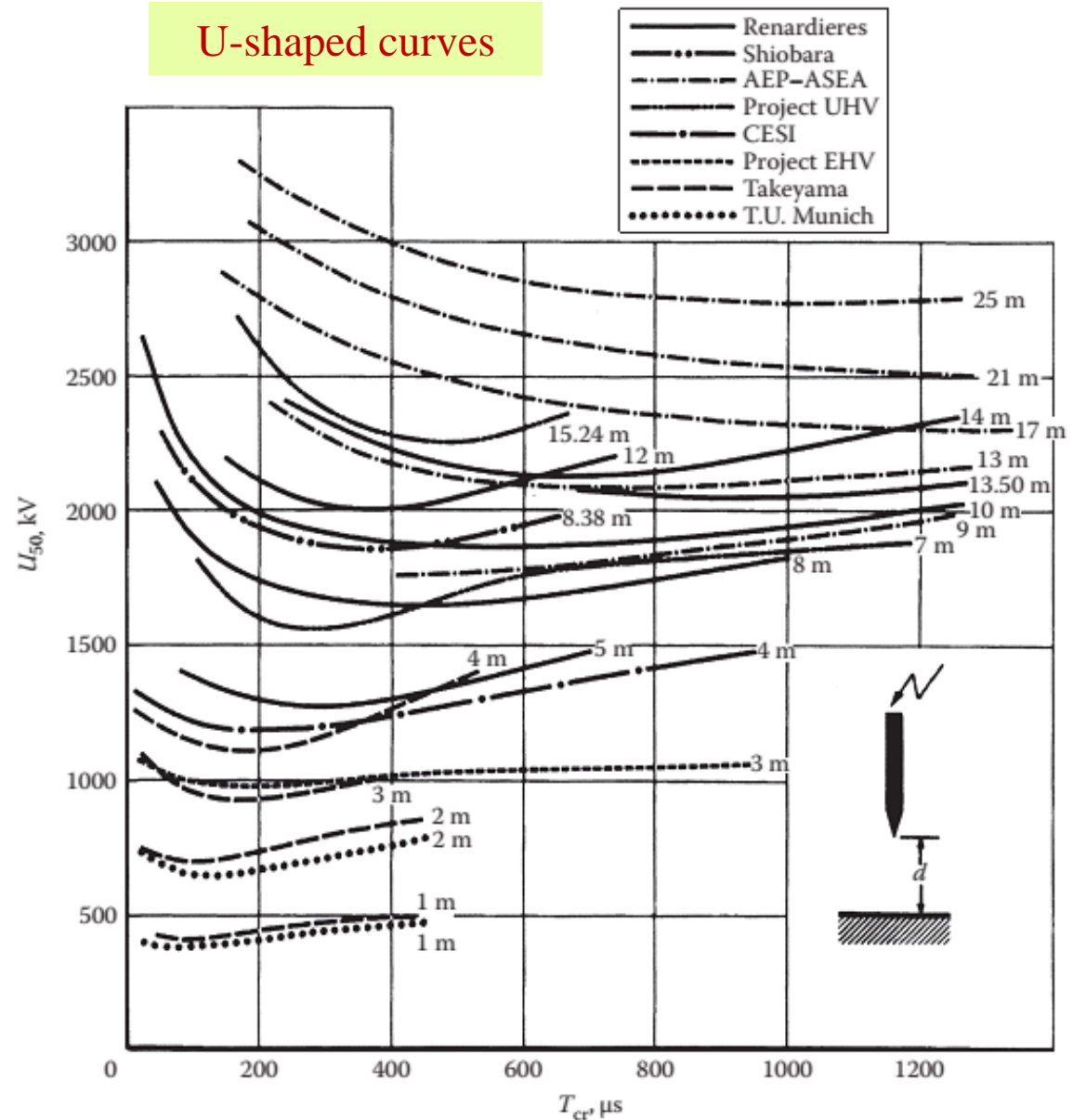


FIGURE 5.6 Data collection of 50% positive switching impulse breakdown voltage as a function of time to crest of rod-plane configuration for different spacings. (From Leroy, G., Recent developments in the physics and engineering of high voltage breakdown, in: *IEE Gas Discharge Conference* (Review Lecture, Opening Session), London, U.K., September 1974.)

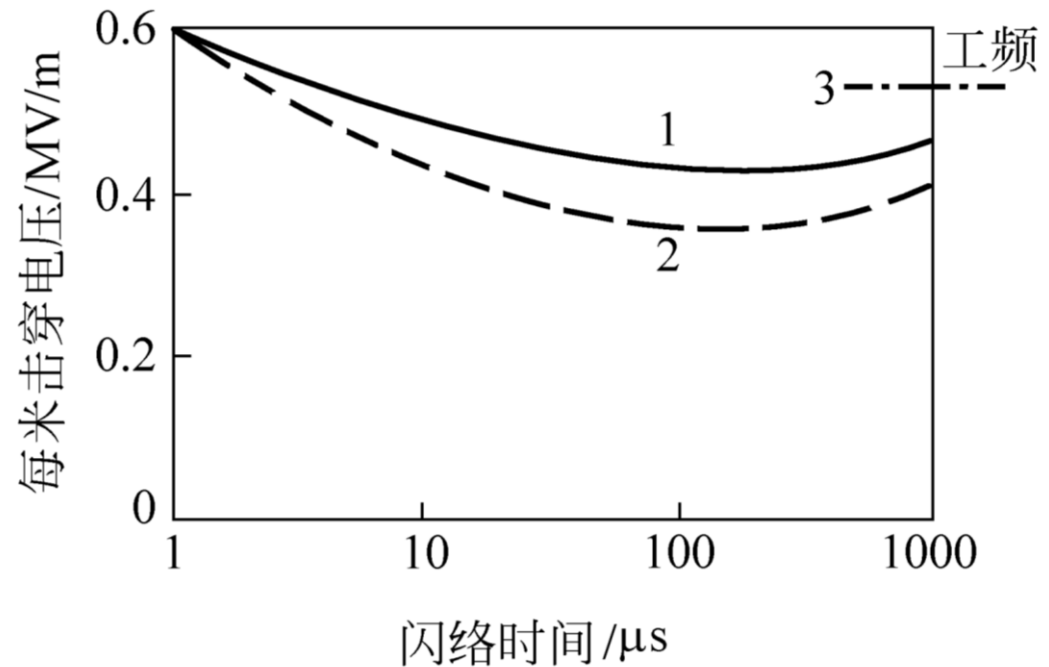
2.4.2 Characteristics of switching impulse voltage

Positive rod-plane air gap switching impulse voltage

The switching impulse breakdown voltage of the rod-plane gap is sometimes lower than the peak breakdown voltage at power frequency

- How to understand the U-shaped curve of long air gap under switching impulse voltage?
- How to understand the switching impulse breakdown voltage is lower than that of under power frequency?

U-shaped curves



Relation between switching impulse breakdown voltage and wave front time in rod-plane gap

1--Rod-rod gap; 2--Conductor-plane gap;
3--Power frequency breakdown voltage

2.4.2 Characteristics of switching impulse voltage

U_{50} , polarity effect, saturation phenomenon

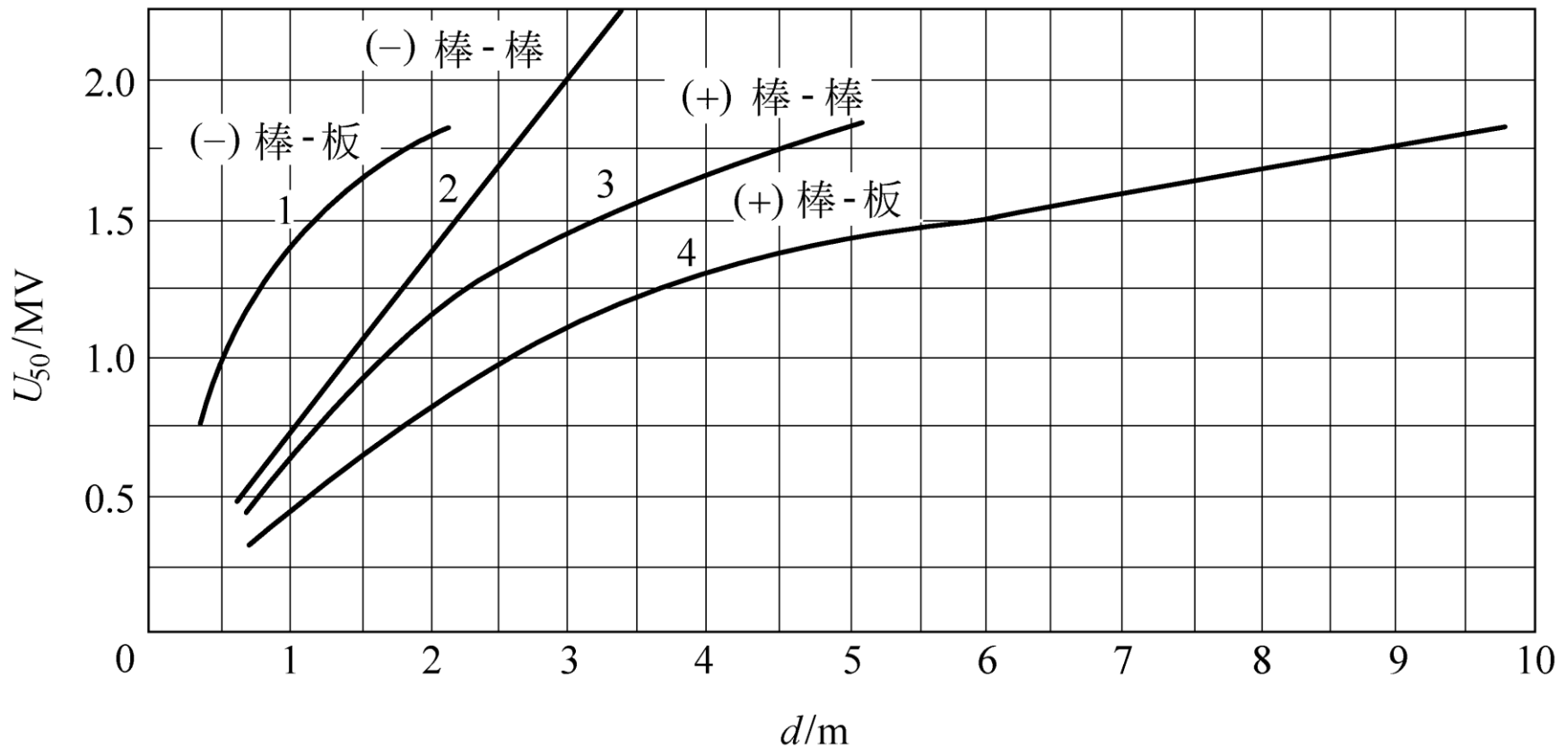


Figure 2-33 Relation between 50% breakdown voltage and gap distance in rod-plane and rod-rod air gap under switching impulse voltage (500 μ s/5000 μ s)

- 1- Rod-plane, negative polarity; 2- Rod-rod, negative polarity;
3- Rod-rod, positive polarity; 4- Rod-plane, positive polarity

2.4.2 Characteristics of switching impulse voltage

polarity effect,
saturation phenomenon

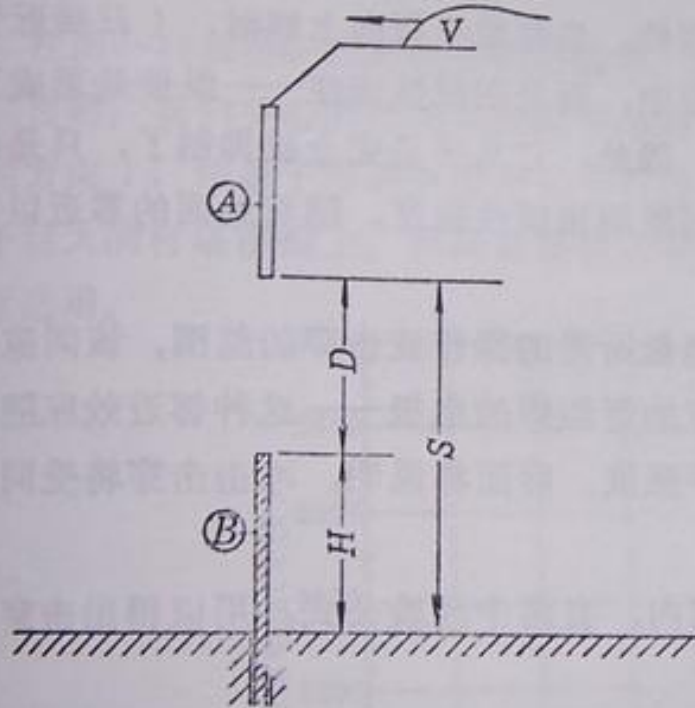


图 6-9 垂直棒对棒间隙和棒对板间隙
($H=0$) 的基本间隙几何

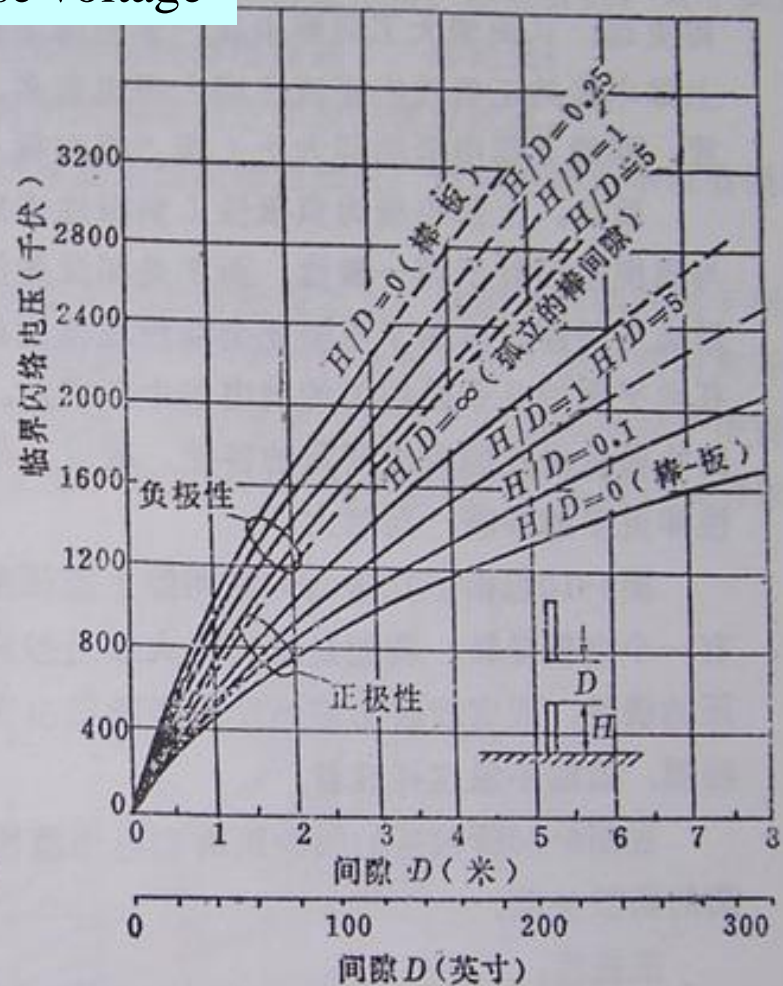


图 6-10 棒对棒和棒对板间隙的
操作波闪络强度

(波头100~200微秒, 蒸汽压力 ≈ 0.5 英寸水银柱)

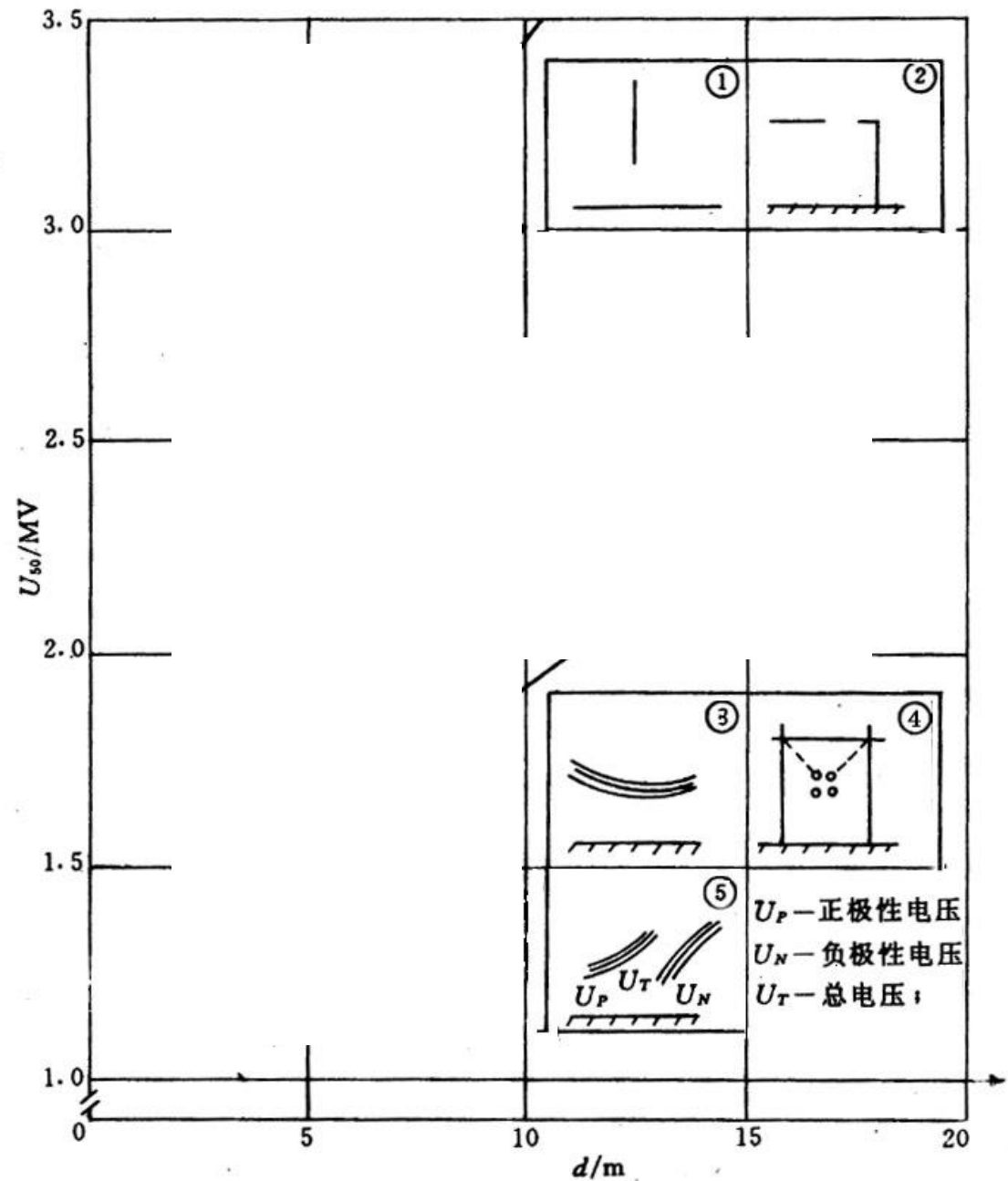
Rod-plane and rod-rod gap, switching impulse voltage curve

2.4.2 Characteristics of switching impulse voltage

The influence of different electrode structures

The analysis of extremely non-uniform electric fields mainly focuses on:

- Electric field is symmetric or not:
rod-rod, rod-plane
- Voltage polarity:
positive or negative



2.4.2 Characteristics of switching impulse voltage

The influence of different electrode structures

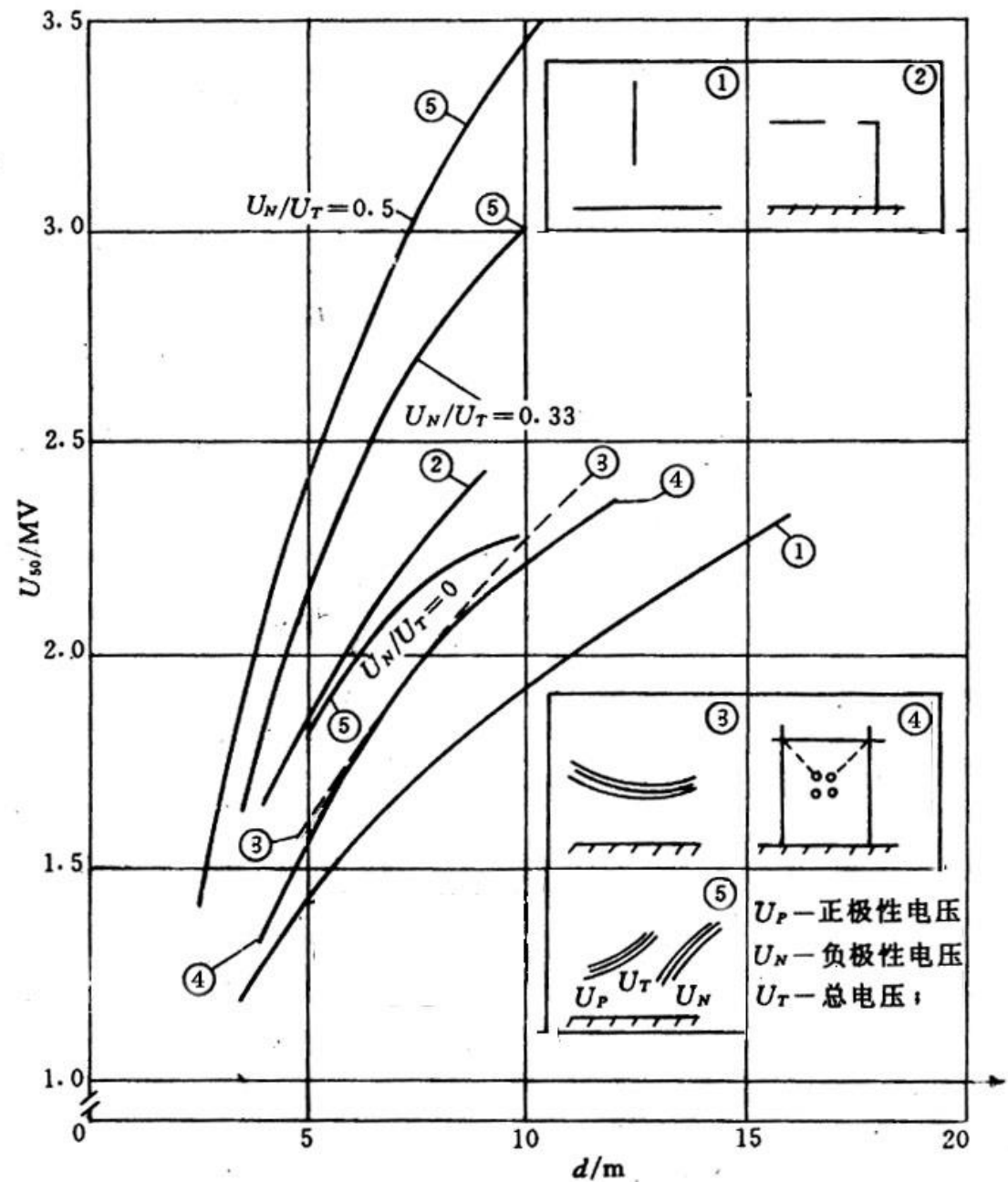
Figure 2-34 Positive polarity switching impulse voltage curve

Positive rod-plane gap

$$1280/5=256\text{kV/m}$$

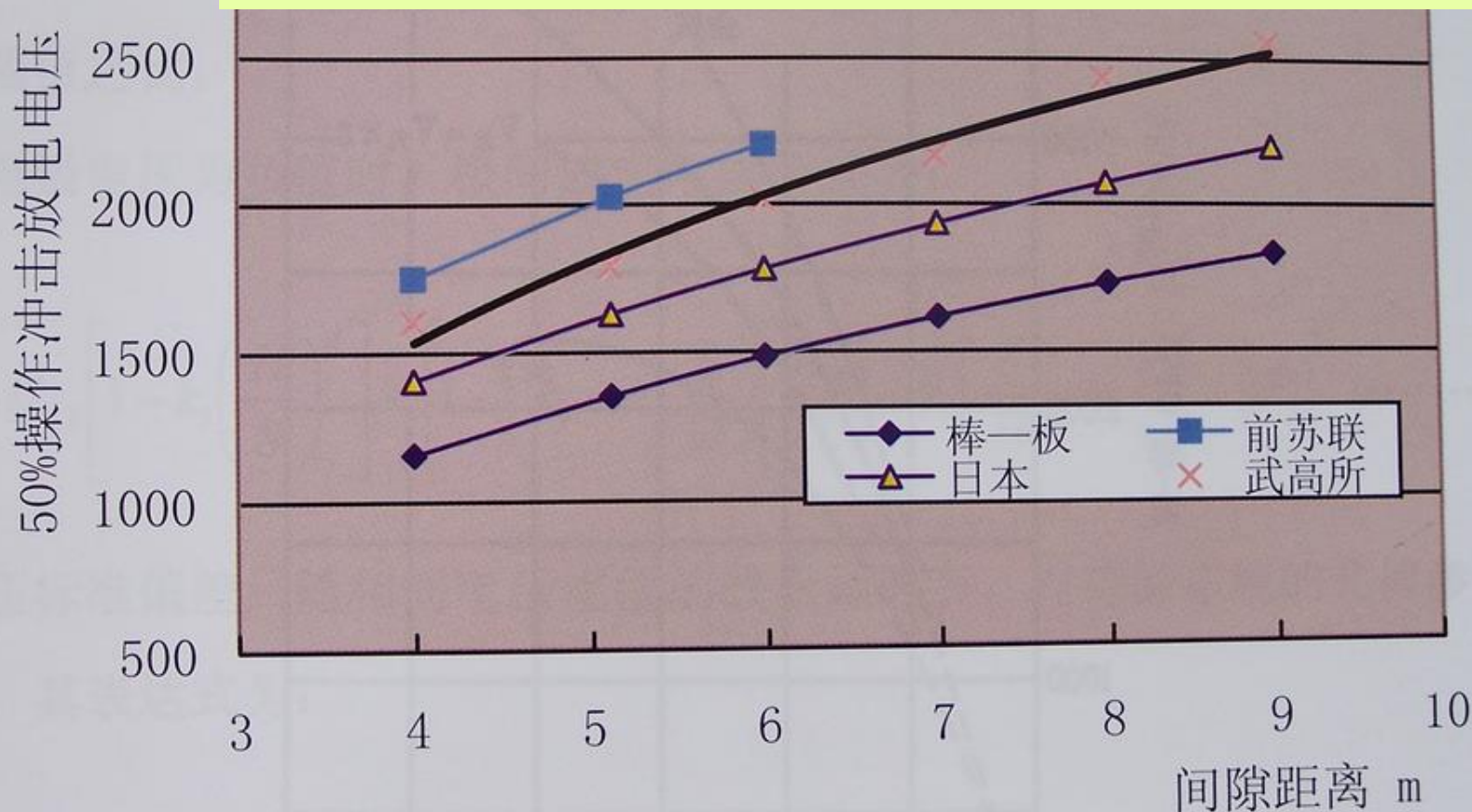
$$1860/10=186\text{kV/m}$$

$$2220/15=148\text{kV/m}$$



2.4.2 Characteristics of switching impulse voltage

U_{50} , saturation phenomenon, pay attention to differences in laboratory test conditions



Positive polarity switching impulse voltage curve of conductor- tower

$$1200/4 = 300\text{kV/m}, \quad 1500/6 = 250\text{kV/m}, \quad 1800/9 = 200\text{kV/m}$$

Lightning impulse discharge almost always follows the shortest path to air gap clearance



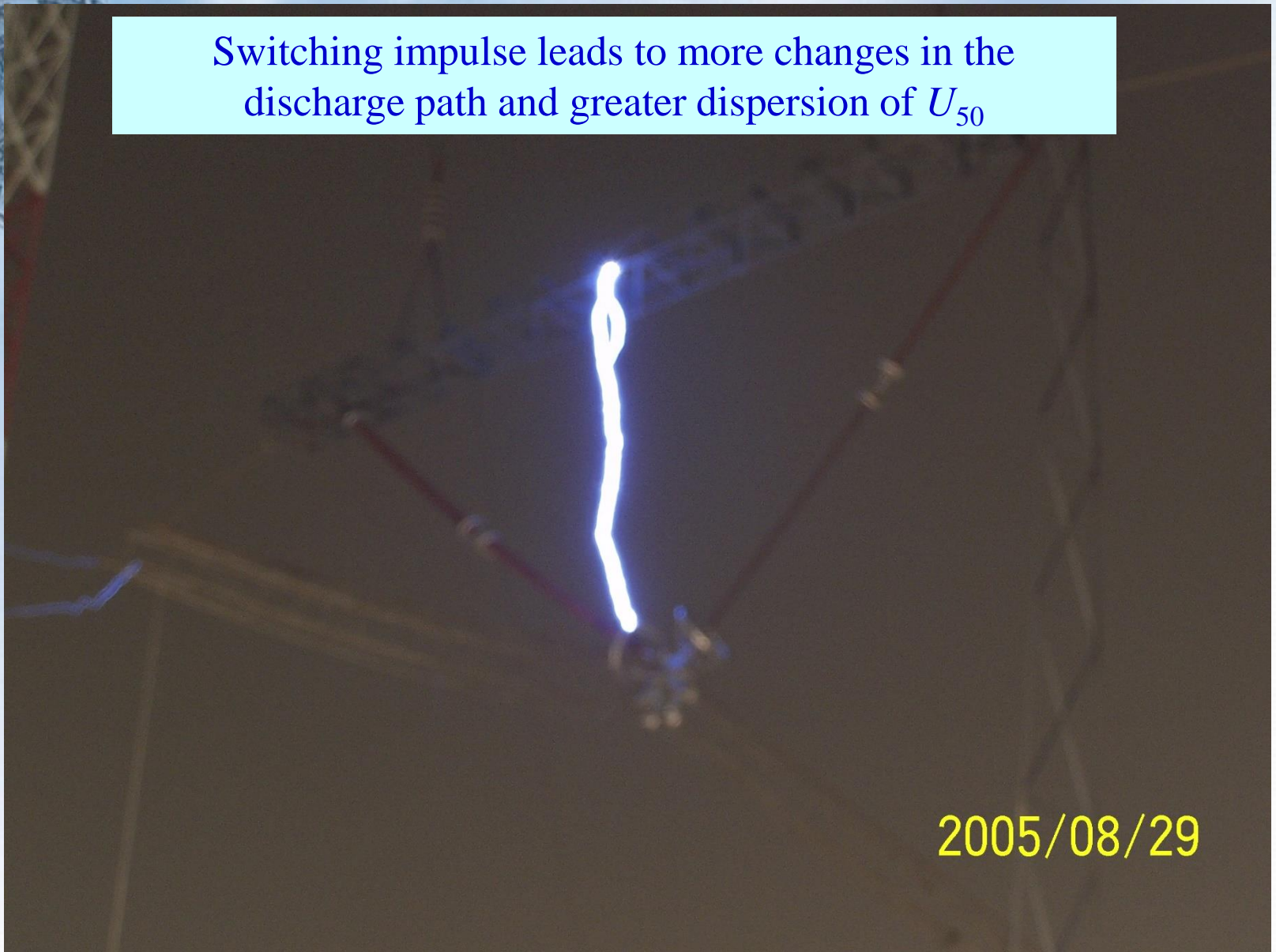
Typical lightning impulse discharge path

Switching impulse leads to more changes in the discharge path and greater dispersion of U_{50}



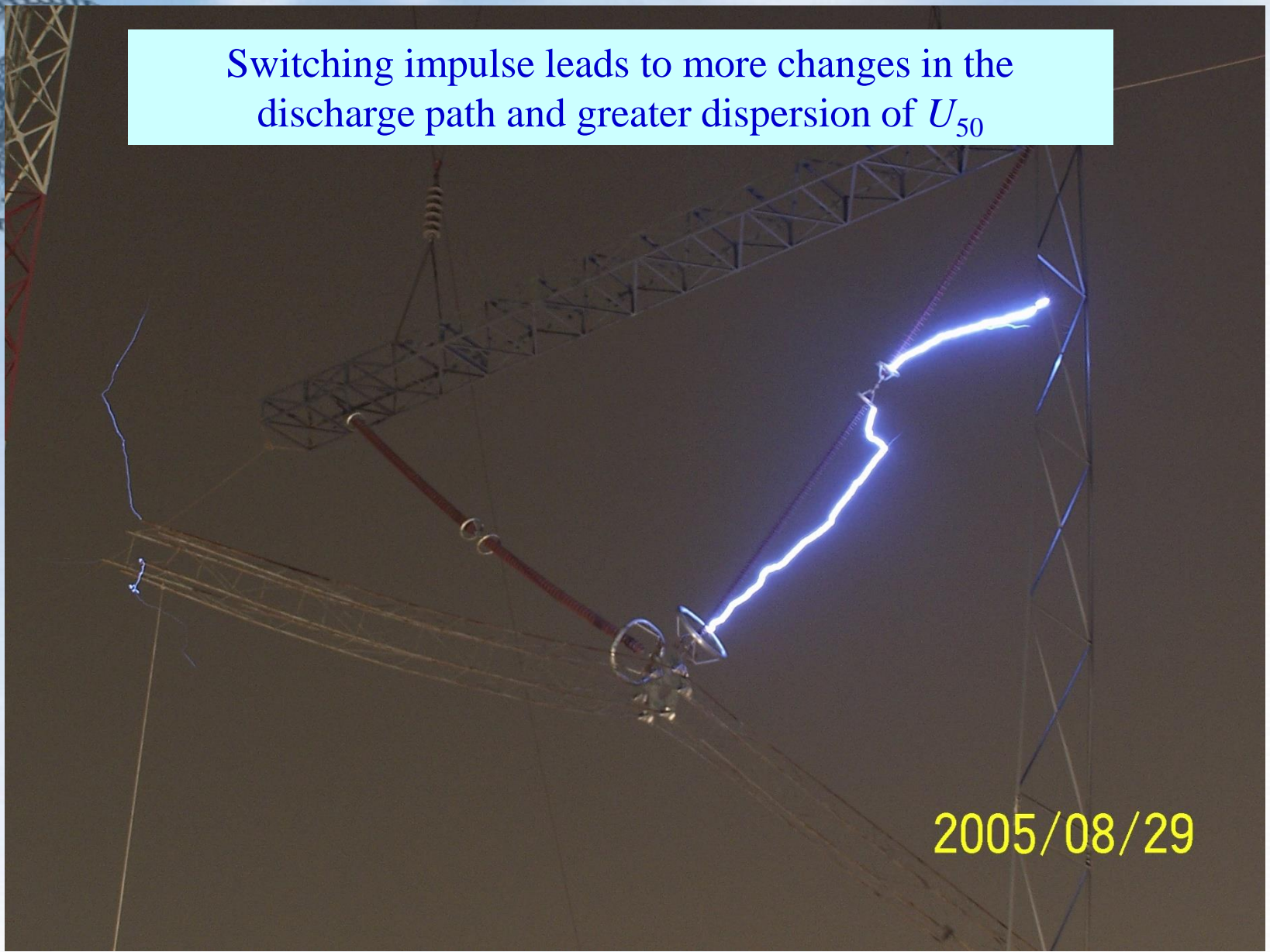
Typical lightning impulse discharge path 1

Switching impulse leads to more changes in the discharge path and greater dispersion of U_{50}



Typical lightning impulse discharge path 2

Switching impulse leads to more changes in the discharge path and greater dispersion of U_{50}



Typical lightning impulse discharge path 3



图 7-8 特高压酒杯塔边相 I 串间隙
操作冲击电压试验

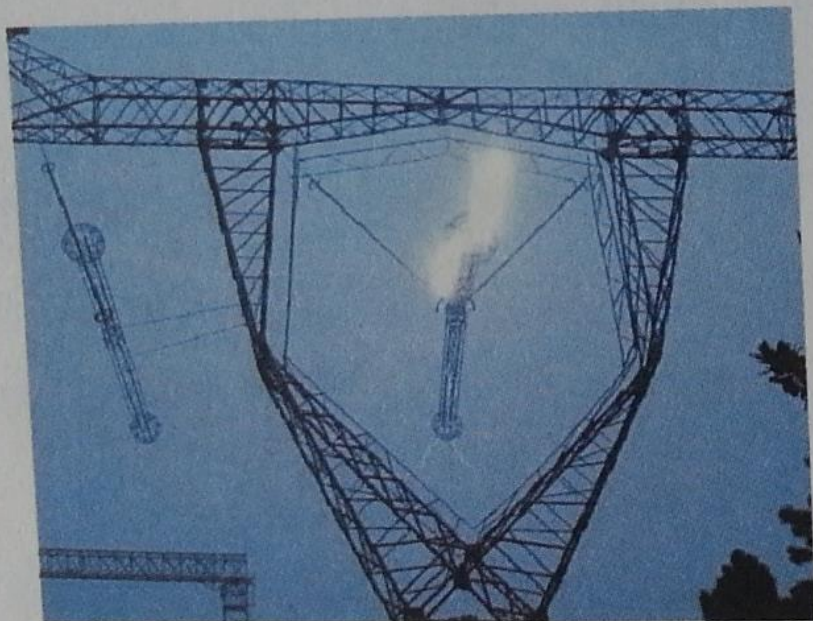


图 7-10 特高压酒杯塔中相塔窗操作
冲击电压试验



4850kV switching impulse discharge



The analysis of extremely non-uniform electric fields mainly focuses on:
electric field is symmetric or not: rod-rod, rod-plane,
and voltage polarity: positive or negative

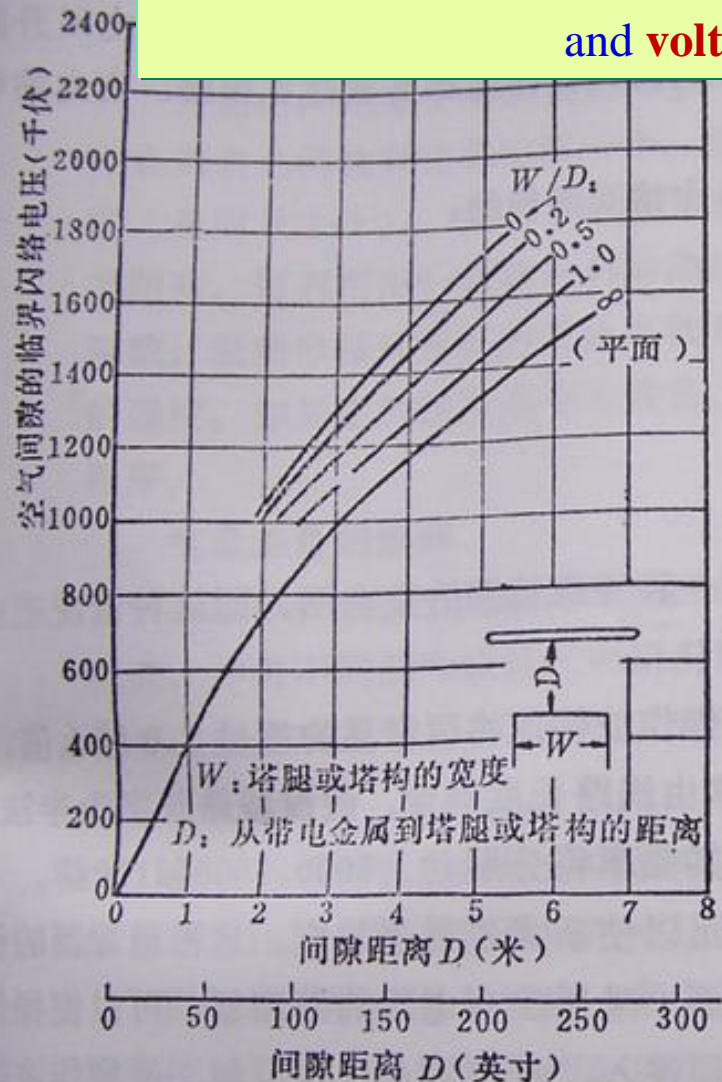
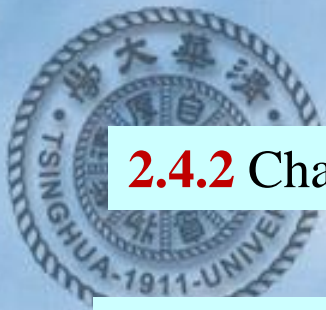


图 6-45 导线对塔腿（或塔构）空气
 间隙的干态正极性操作波强度



Conductor-tower positive switching impulse
 voltage curve

$$1000/3 = 333\text{kV/m}, 1480/6 = 247\text{kV/m}$$



2.4.2 Characteristics of switching impulse voltage

- (1) U-shaped curves
- (2) Polarity effect of asymmetric electric field
- (3) The saturation phenomenon of long air gaps
- (4) 50% breakdown voltage and dispersion
- (5) Effect of nearby earthed object
- (6) Empirical formula for minimum air gap breakdown voltage

$$U_{50, \min} = \frac{3400}{1 + \frac{8}{d}}$$

$(d < 20\text{m})$

Electrical strength of air gaps in extremely non-uniform fields

Lightning impulse:

Positive rod-plane: $\approx 500\text{kV/m}$ Negative rod-plane: $\approx 750\text{kV/m}$

Switching impulse:

Positive rod-plane: $\approx 400\text{kV/m}$ (2m) Negative rod-plane: $\approx 900\text{kV/m}$ (2m)

Long positive rod-plane gap: $\approx 195\text{kV/m}$ (8-10m)

DC voltage:

Positive rod-plane: $\approx 4.5\text{kV/cm}$ Negative rod-plane: $\approx 10\text{kV/cm}$

Relatively long rod-rod gap: $\approx 4.8\text{-}5.0\text{kV/cm}$

AC voltage:

Rod-rod: 5.66kV/cm (peak) Rod-plane: $\approx 5.23\text{kV/cm}$ (peak)

long rod-plane gap: $\approx 210\text{kV/m}$ (peak)