

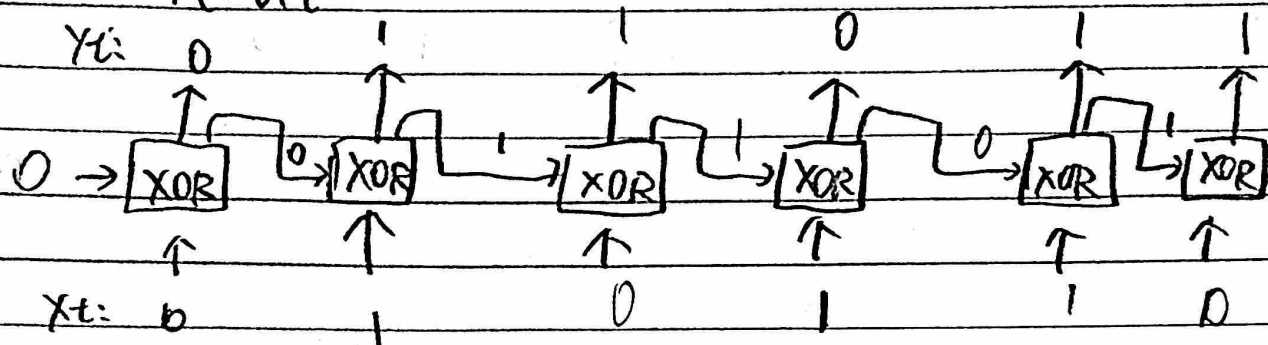
1. Design a sequence parity function with vanilla RNN. we can use XOR

input  $x = [0, 1, 0, 1, 1, 0]$  and output is  $y = [0, 1, 1, 0, 1, 1]$   
the hidden units can be written as:

$$h_0 = 0$$

$$h_t = h_{t-1} \text{ XOR } x_t$$

$$y_t = h_t$$



XOR can be represented as  $\text{XOR}(a, b) = \bar{a} \cdot \bar{b} + a \cdot b$

$$\text{XOR}(0, 0) = 0$$

$$\text{XOR}(1, 0) = 1$$

$$\text{XOR}(0, 1) = 1$$

$$\text{XOR}(1, 1) = 0$$

In our RNN, we have

$y_{t-1}$	$x_t$	$y_t$
0	0	0
0	1	1
1	1	0
1	0	1