

# Integrated Circuit Design

**Pham Thanh Huyen**

University of Transport and Communications, Vietnam

## Chapter 3: **ANALOG CMOS CIRCUITS**

- Basic CMOS amplifier
- MOSFET Cascode Stage
- MOSFET Current Mirror
- MOSFET Differential Amplifiers

# Basic CMOS amplifier

# MOSFET Amplifier Design

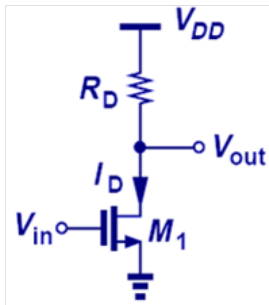
A MOSFET amplifier circuit should be designed to ensure that the MOSFET operates in the saturation region, allow the desired level of DC current to flow, and couple to a small-signal input source and to an output “load”.

Proper “DC biasing” is required! (*DC analysis using large-signal MOSFET model*)

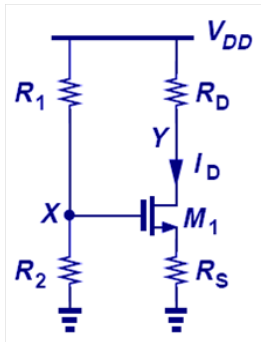
Key amplifier parameters: (*AC analysis using small-signal MOSFET model*)

- **Voltage gain**  $A_v = v_{out}/v_{in}$ .
- **Input resistance**  $R_{in}$ : resistance seen between the input node and ground (with output terminal floating).
- **Output resistance**  $R_{out}$ : resistance seen between the output node and ground (with input terminal grounded).

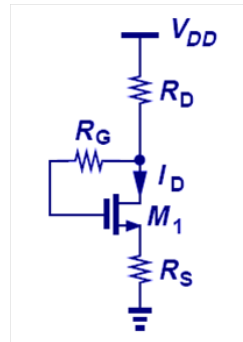
# MOSFET biasing



Mạch khuếch đại chế độ B



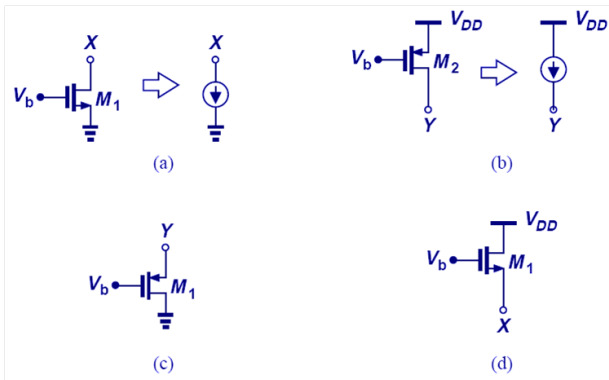
Mạch khuếch đại chế độ A



# MOSFETs as Current Sources

A MOSFET behaves as a current source when it is operating in the saturation region.

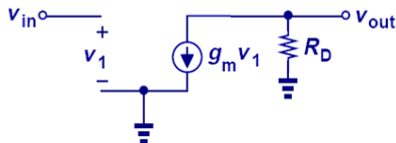
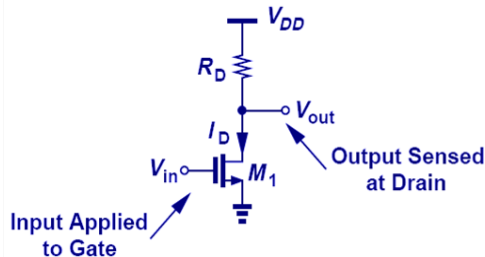
An NMOSFET draws current from a point to ground (“sinks current”), whereas a PMOSFET draws current from  $V_{DD}$  to a point (“sources current”).



## Common-Source Stage



# Common-Source Stage: $\lambda = 0$

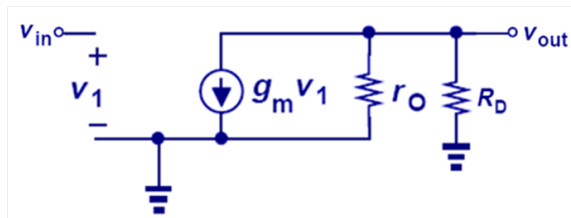


$$A_v = -g_m R_D = -\sqrt{2\mu_n C_{ox} \frac{W}{L} I_D} R_D$$

$$R_{in} = \infty$$

$$R_{out} = R_D$$

## Common-Source Stage: $\lambda \neq 0$

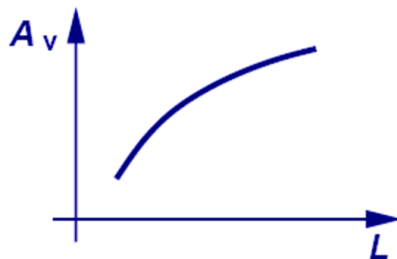
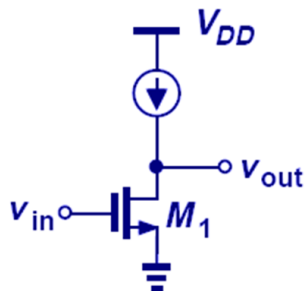


$$A_v = -g_m (R_D \parallel r_O)$$

$$R_{in} = \infty$$

$$R_{out} = R_D \parallel r_O$$

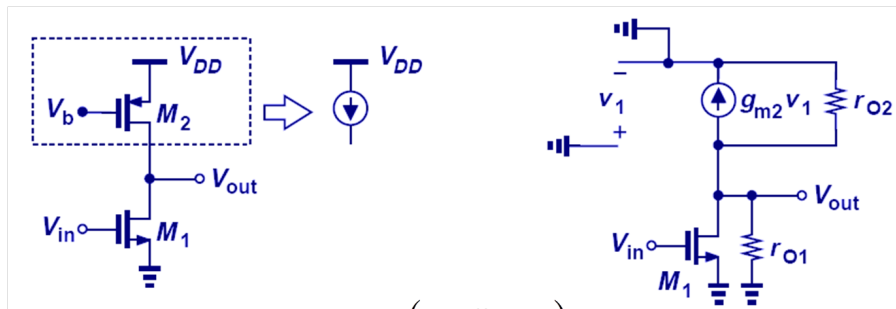
# CS Gain Variation with L



$$|A_v| = g_m r_o = \frac{\sqrt{2\mu_n C_{ox} \frac{W}{L} I_D}}{\lambda_D} \propto \sqrt{\frac{2\mu_n C_{ox} W L}{I_D}}$$

# CS Stage with Current-Source PMOS Load

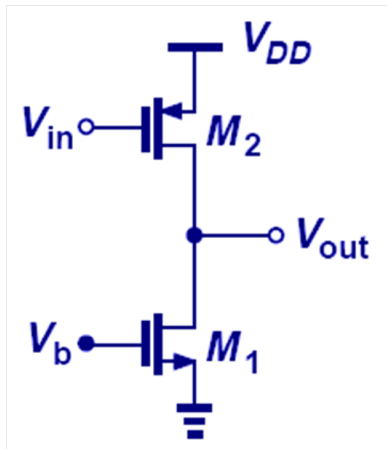
Recall that a PMOSFET can be used as a current source from  $V_{DD}$ . Use a PMOSFET as a load of an NMOSFET CS amplifier.



$$A_v = -g_{m1}(r_{O1} \parallel r_{O2})$$

$$R_{out} = r_{O1} \parallel r_{O2}$$

# PMOS CS Stage with NMOS Load

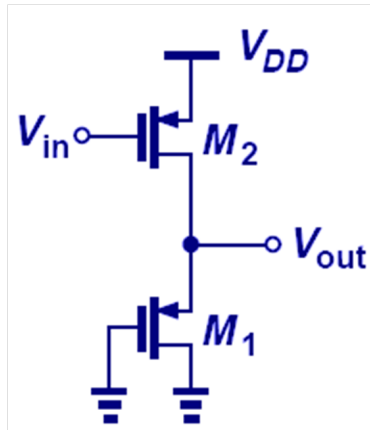
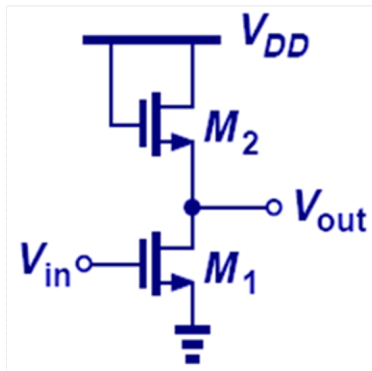


$$A_v = -g_{m2}(r_{O1} \parallel r_{O2})$$

$$R_{out} = r_{O1} \parallel r_{O2}$$

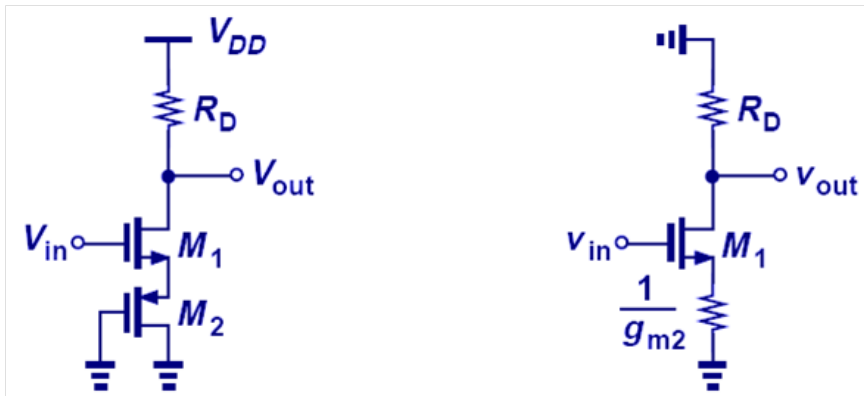
# CS Stage with Diode-Connected Load

$$A_v = ? \quad R_{out} = ?$$



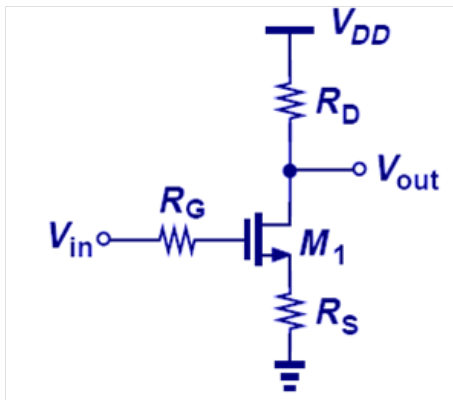
# Problem 1

$$A_v = ?$$



## Problem 2

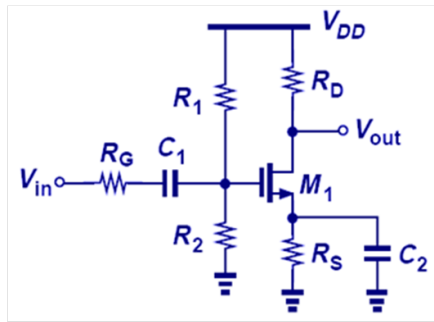
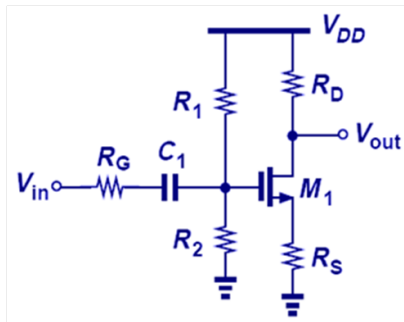
$$A_v = ?$$





# Problem 3

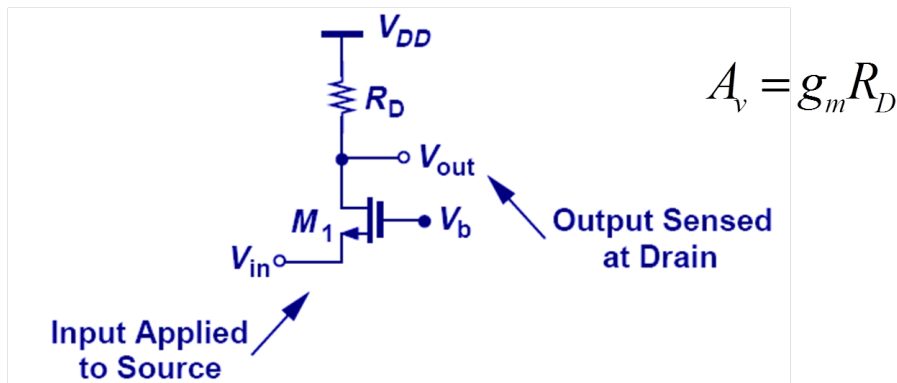
$$A_V = ?$$



## Common-gate Stage

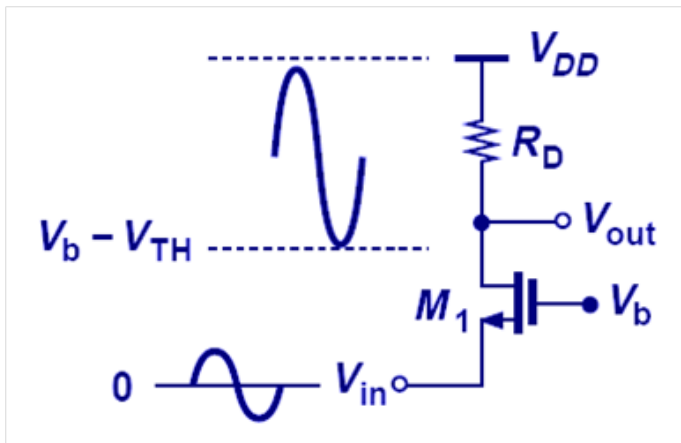
# Common-Gate Amplifier Stage

An increase in  $V_{in}$  decreases  $V_{GS}$  and hence decreases  $I_D$ .  
The voltage drop across  $R_D$  decreases  $\Rightarrow V_{out}$  increases.  
The small-signal voltage gain ( $A_v$ ) is positive.



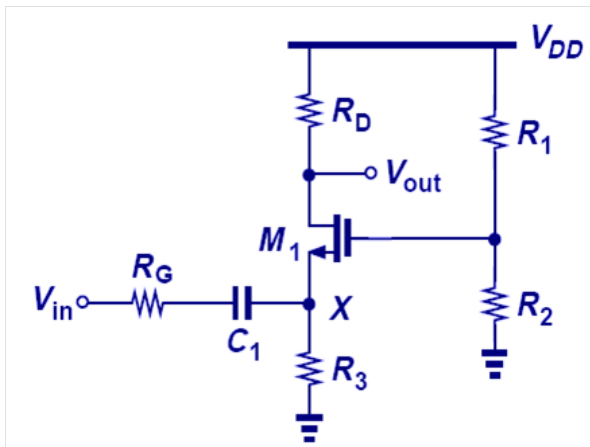
## CG: Operation in Saturation Region

For  $M_1$  to operate in saturation,  $V_{out}$  cannot fall below  $V_b - V_{TH}$ .  $\Rightarrow$  Trade-off between headroom and voltage gain.



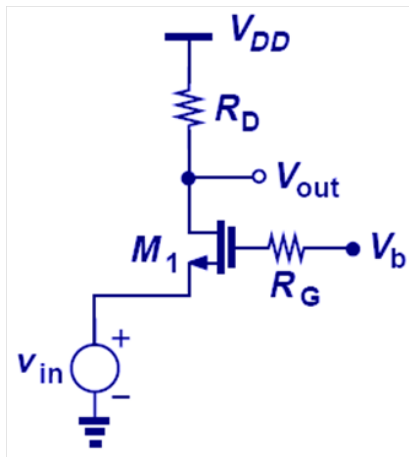
# Problem 1

$$A_v = ?$$



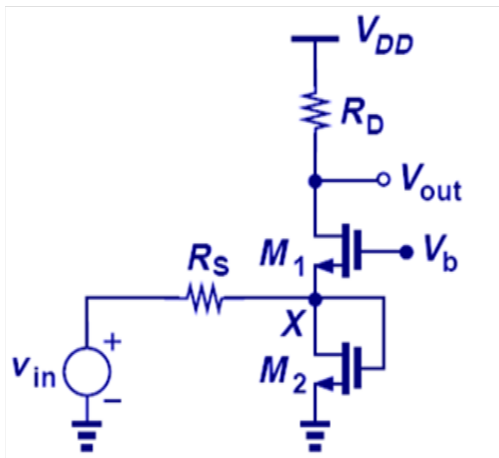
## Problem 2

$$A_v = ?$$



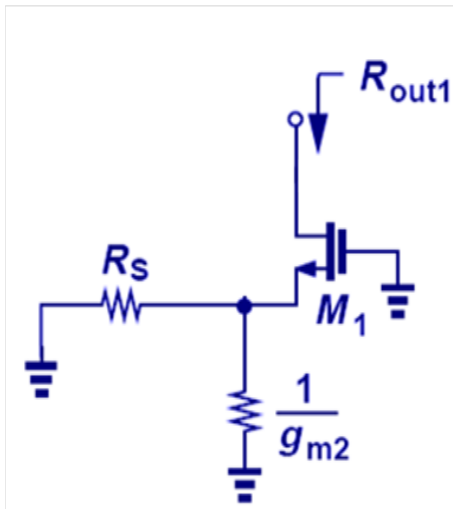
## Problem 3

$$A_v = ?$$



## Problem 4

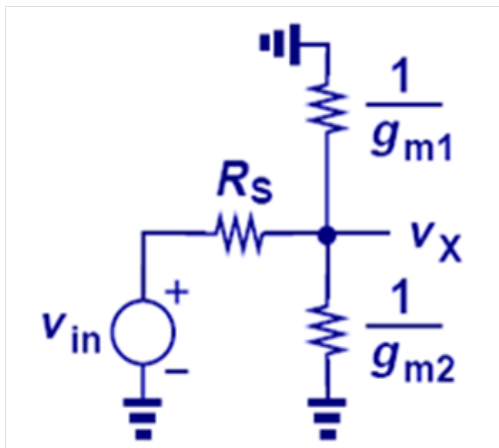
$$A_v = ?$$





## Problem 5

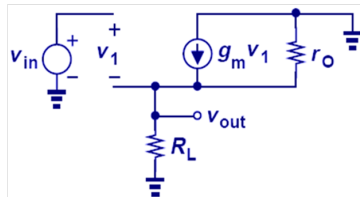
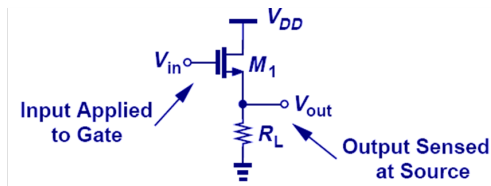
$$A_v = ?$$



## Source Follower Stage

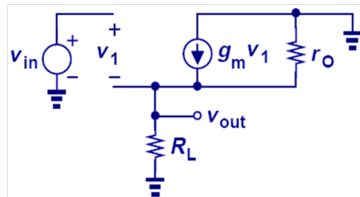
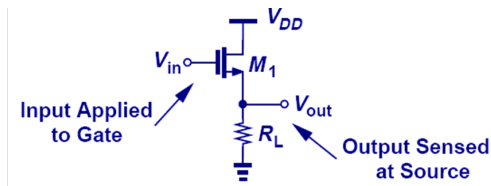
# Source Follower Stage

Amplifier Circuit and Small-signal analysis circuit for determining voltage gain,  $A_v$ .



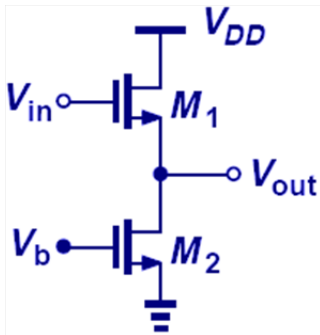
# Source Follower Stage

Amplifier Circuit and Small-signal analysis circuit for determining voltage gain,  $A_v$ .



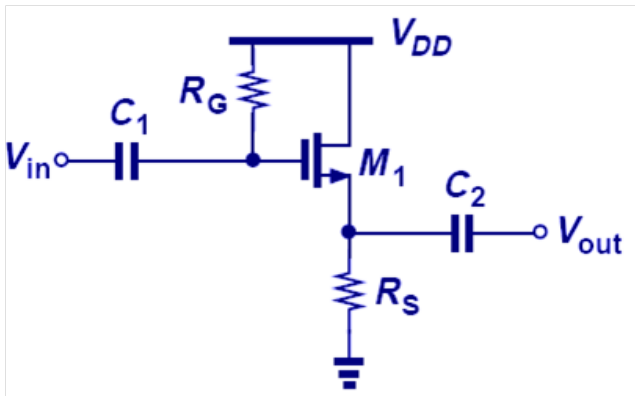
# Example

M2 acts as a current source.



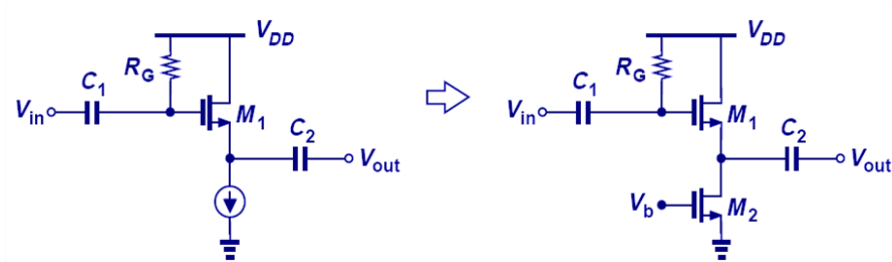
# Source Follower with Biasing

$R_G$  sets the gate voltage to  $V_{DD}$ ;  $R_S$  sets the drain current.



# Supply-Independent Biasing

If  $R_s$  is replaced by a current source, the drain current  $I_D$  becomes independent of the supply voltage  $V_{DD}$ .



# Comparison of Amplifier Topologies

## Common Source

- **Large  $A_v < 0$**   
- degraded by  $R_S$
- **Large  $R_{in}$** 
  - determined by biasing circuitry
- **$R_{out} \cong R_D$**
- **$r_o$  decreases  $A_v$  &  $R_{out}$**   
but impedance seen looking into the drain can be “boosted” by source degeneration

## Common Gate

- **Large  $A_v > 0$**   
- degraded by  $R_S$
- **Small  $R_{in}$**   
- decreased by  $R_S$
- **$R_{out} \cong R_D$**
- **$r_o$  decreases  $A_v$  &  $R_{out}$**   
but impedance seen looking into the drain can be “boosted” by source degeneration

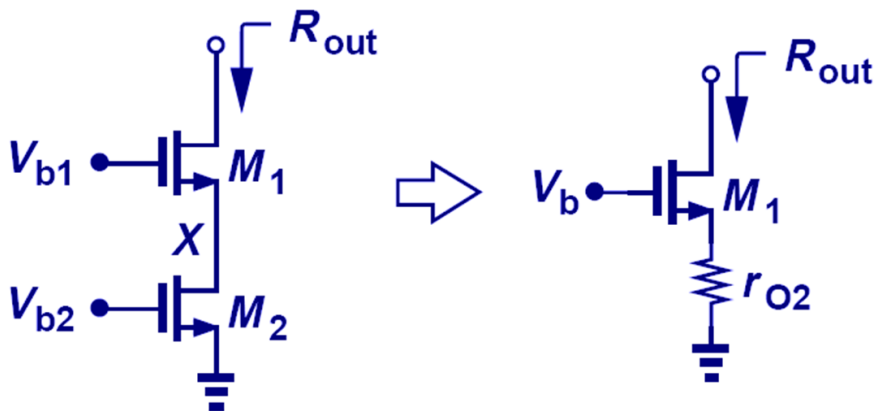
## Source Follower

- **$0 < A_v \leq 1$**
- **Large  $R_{in}$** 
  - determined by biasing circuitry
- **Small  $R_{out}$**   
- decreased by  $R_S$
- **$r_o$  decreases  $A_v$  &  $R_{out}$**



# MOS Cascode Amplifier

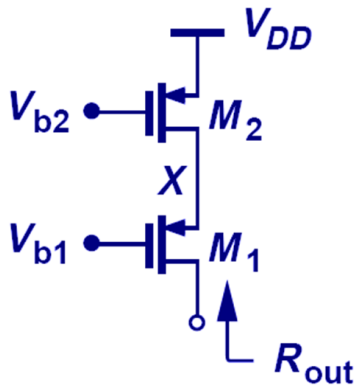
# NMOS Cascode Stage



$$R_{out} = (1 + g_{m1}r_{O1})r_{O2} + r_{O1}$$

$$R_{out} \approx g_{m1}r_{O1}r_{O2}$$

# PMOS Cascode Stage

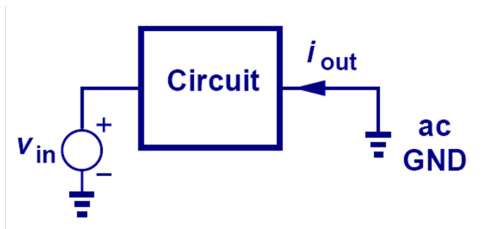


$$R_{out} = (1 + g_{m1}r_{O1})r_{O2} + r_{O1}$$

$$R_{out} \approx g_{m1}r_{O1}r_{O2}$$

# Short-Circuit Transconductance

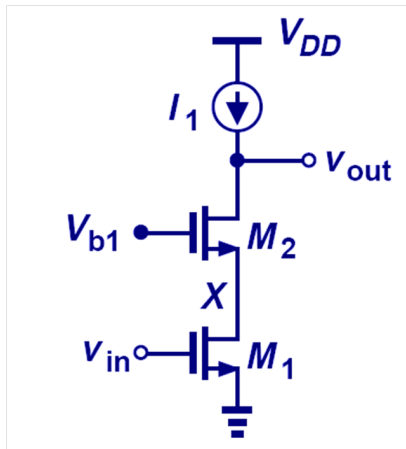
The short-circuit transconductance is a measure of the strength of a circuit in converting an input voltage signal into an output current signal:



$$G_m \equiv \left. \frac{i_{out}}{v_{in}} \right|_{v_{out}=0}$$

$$A_v = -G_m R_{out}$$

# MOS Cascode Amplifier



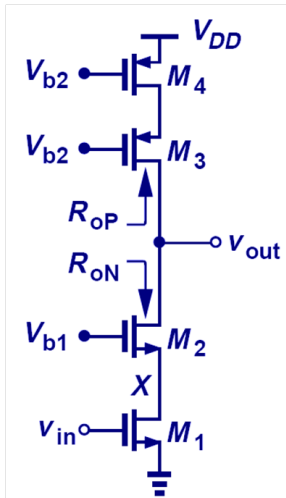
$$A_v = -G_m R_{out}$$

$$A_v \approx -g_{m1}[(1 + g_{m2}r_{O2})r_{O1} + r_{O2}]$$

$$A_v \approx -g_{m1}r_{O1}g_{m2}r_{O2}$$

# PMOS Cascode Current Source as Load

A large load impedance can be achieved by using a PMOS cascode current source.



$$R_{oN} \approx g_{m2} r_{O2} r_{O1}$$

$$R_{oP} \approx g_{m3} r_{O3} r_{O4}$$

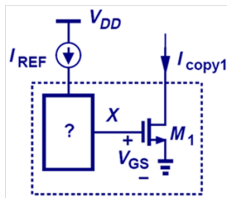
$$R_{out} = R_{oN} \parallel R_{oP}$$

# MOS Current Mirror

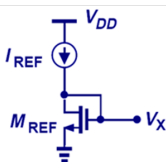
# MOS Current Mirror

The motivation behind a current mirror is to duplicate a (scaled version of the) “golden current” to other locations.

Current mirror concept



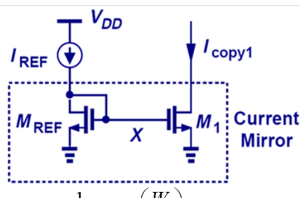
Generation of required  $V_{GS}$



$$I_{REF} = \frac{1}{2} \mu_n C_{ox} \left( \frac{W}{L} \right)_{REF} (V_X - V_{TH})^2$$

$$V_X = \sqrt{\frac{2I_{REF}}{\mu_n C_{ox} (W/L)_1}} + V_{TH1}$$

Current Mirror Circuitry



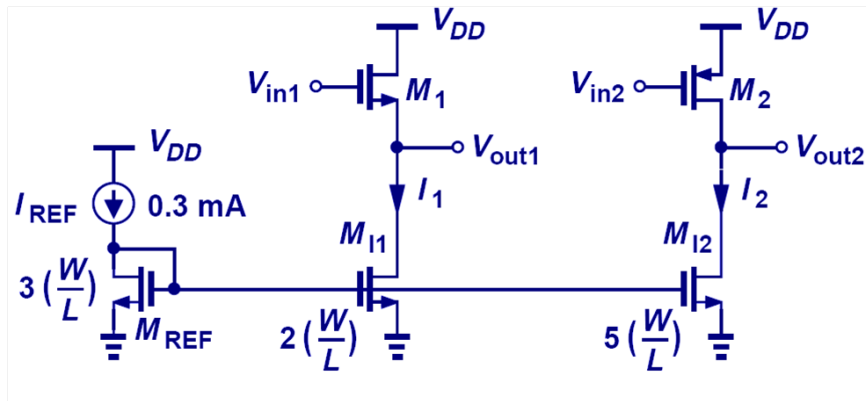
$$I_{copy1} = \frac{1}{2} \mu_n C_{ox} \left( \frac{W}{L} \right)_1 (V_X - V_{TH})^2$$

$$I_{copy1} = \frac{(W/L)_1}{(W/L)_{REF}} I_{REF}$$

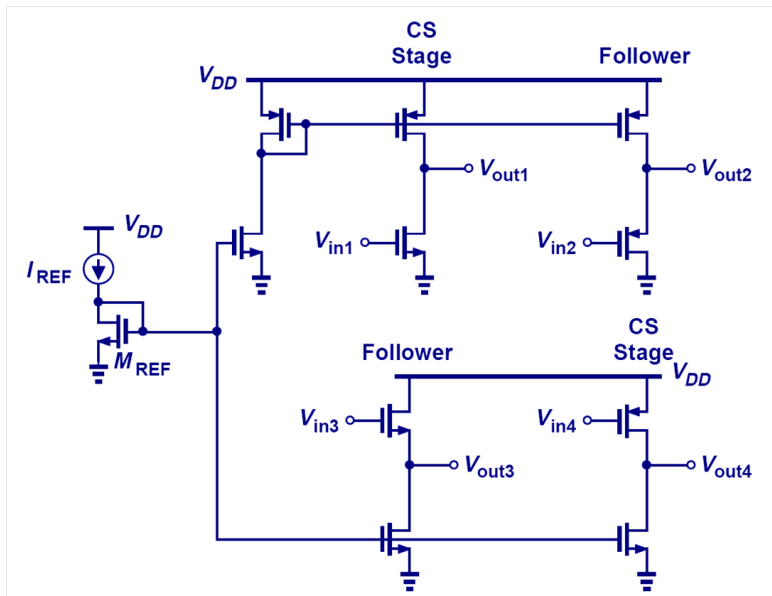


## Example: Current Scaling

MOS current mirrors can be used to scale  $I_{REF}$  up or down.



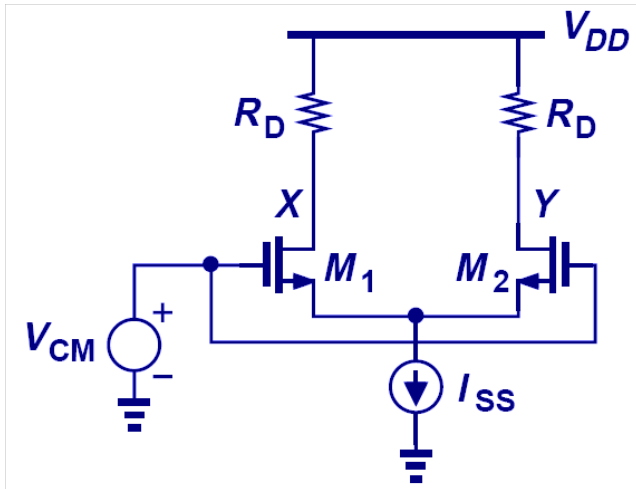
# CMOS Current Mirror



# MOSFET Differential Amplifiers

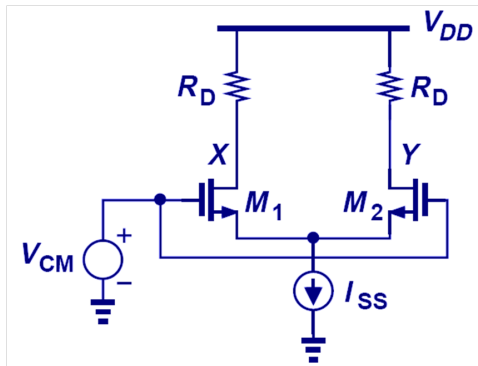
# Common-Mode (CM) Response

A MOSFET differential pair produces zero differential output as  $V_{CM}$  changes.



# Equilibrium Overdrive Voltage

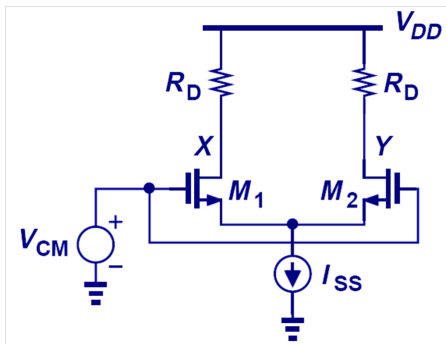
The equilibrium overdrive voltage is defined as  $V_{GS} - V_{TH}$  when  $M_1$  and  $M_2$  each carry a current of  $I_{SS}/2$ .



$$(V_{GS} - V_{TH})_{equil} = \sqrt{\frac{I_{SS}}{\mu_n C_{ox} \frac{W}{L}}}$$

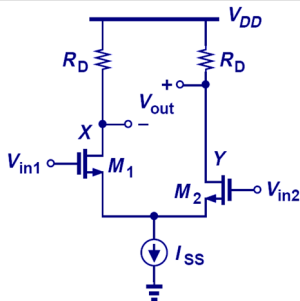
# Minimum CM Output Voltage

In order to maintain  $M_1$  and  $M_2$  in saturation, the common-mode output voltage cannot fall below  $V_{CM} - V_{TH}$ .

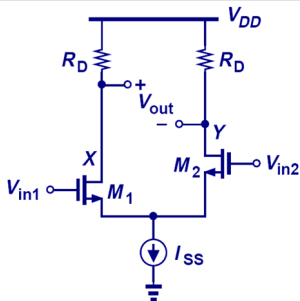


$$V_{DD} - R_D \frac{I_{SS}}{2} > V_{CM} - V_{TH}$$

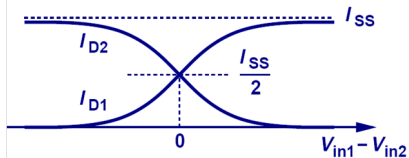
# Differential Response



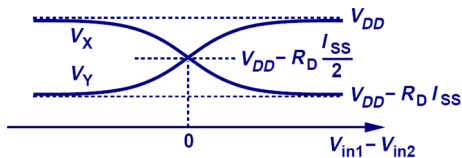
(a)



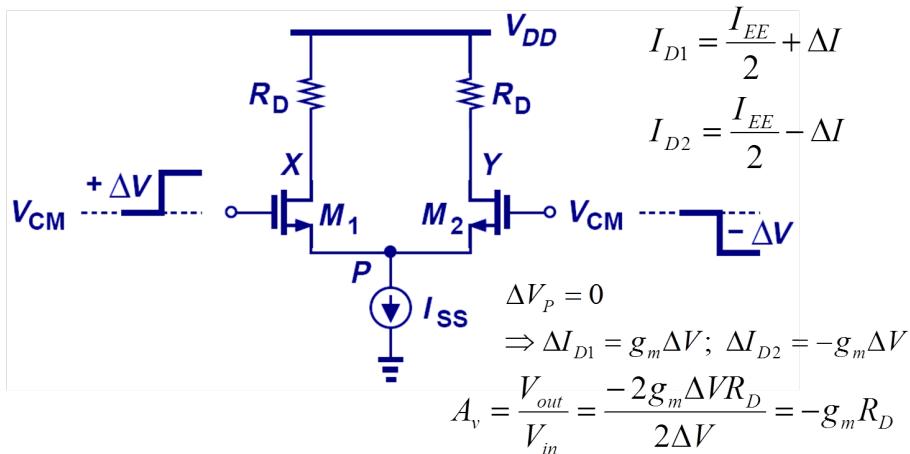
(b)



(c)



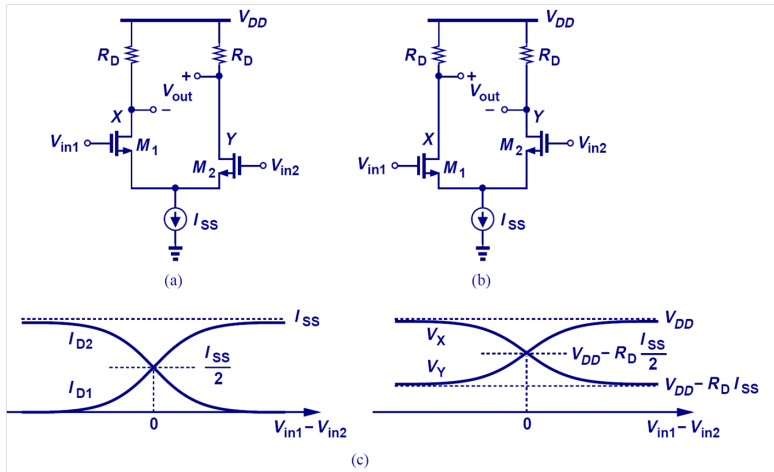
# Small-Signal Response





# Maximum Differential Input Voltage

There exists a finite differential input voltage that completely steers the tail current from one transistor to the other. This value is known as the maximum differential input voltage.



## next .... **Chapter 4: DIGITAL CMOS CIRCUITS**