```
template <class K, class V>
class BKUTree
public:
        class AVLTree;
        class SplayTree;
        class Entry
        public:
                K key;
                V value;
                Entry(K key, V value) : key(key), value(value) {}
        };
private:
        AVLTree *avl;
        SplayTree *splay;
        queue<K> keys;
        int maxNumOfKeys;
public:
        BKUTree(int maxNumOfKeys = 5)
        {
                this->avl = NULL;
                this->splay = NULL;
                this->maxNumOfKeys = maxNumOfKeys;
        ~BKUTree() { this->clear(); }
        void add(K key, V value)
                if (this->avl == NULL || this->splay == NULL)
                {
                        this->splay = new SplayTree();
                        this->avl = new AVLTree();
                this->splay->add(key, value);
                this->avl->add(key, value);
                this->splay->root->corr = this->avl->insertNode;
                this->splay->root->corr->corr = this->splay->root;
                int size = keys.size();
                if (size >= maxNumOfKeys)
                        keys.pop();
                keys.push(key);
        }
        void remove(K key)
```

```
this->avl->remove(key);
                vector<K> KEY;
                while (keys.size() != 0)
                {
                        if (keys.front() != key)
                                KEY.push_back(keys.front());
                        keys.pop();
                }
                for (auto it : KEY)
                        keys.push(it);
                KEY.clear();
                if (this->splay->root != NULL)
                        keys.push(this->splay->root->entry->key);
                int n = keys.size();
                if (n > this->maxNumOfKeys)
                        keys.pop();
        }
        V search(K key, vector<K> &traversedList)
                if (this->splay->root->entry->key == key)
                {
                        int n = keys.size();
                        if (n >= maxNumOfKeys)
                                keys.pop();
                        keys.push(key);
                        return this->splay->root->entry->value;
                }
                vector<K> KEY;
                V result;
                while (keys.size() != 0)
                {
                        KEY.push_back(keys.front());
                        keys.pop();
                }
                if (find(KEY.begin(), KEY.end(), key) != KEY.end())
                {
                        typename BKUTree<K, V>::SplayTree::Node *target =
this->splay->search(this->splay->root, key, traversedList);
                        if (target == NULL)
                                throw "Not found!";
                        this->splay->Splay(target, 1);
                        if (target->parent == NULL)
```

this->splay->remove(key);

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this->splay->root = target;
                        result = target->entry->value;
                }
                else
                {
                        typename BKUTree<K, V>::AVLTree::Node *target =
this->avl->search(this->splay->root->corr, key, traversedList);
                        if (target == NULL)
                                target = this->avl->search(this->avl->root, key,
traversedList);
                                 if (target == NULL)
                                         throw "Not found!";
                        }
                        this->splay->Splay(target->corr, 1);
                        if (target->corr->parent == NULL)
                                this->splay->root = target->corr;
                        result = target->entry->value;
                }
                for (auto i : KEY)
                        keys.push(i);
                int n = keys.size();
                if (n >= maxNumOfKeys)
                        keys.pop();
                keys.push(key);
                KEY.clear();
                return result;
        }
        void traverseNLROnAVL(void (*func)(K key, V value))
        {
                this->avl->traverseNLR(func);
        void traverseNLROnSplay(void (*func)(K key, V value))
        {
                this->splay->traverseNLR(func);
        }
        void clear()
        {
                this->avl->clear();
                this->splay->clear();
                delete avl;
                delete splay;
                avl = splay = NULL;
                while (!keys.empty())
                {
                        keys.pop();
                }
```

```
this->maxNumOfKeys = 5;
       }
       CLASS SPLAYTREE
       ///
       class SplayTree
       public:
               class Node
               {
                      Entry *entry;
                      Node *left;
                      Node *right;
                      Node *parent;
                      typename AVLTree::Node *corr;
                      friend class SplayTree;
                      friend class BKUTree<K, V>;
                      Node(Entry *entry = NULL, Node *parent = NULL, Node *left =
NULL, Node *right = NULL)
                      {
                              this->entry = entry;
                              this->left = left;
                              this->parent = parent;
                              this->right = right;
                              this->corr = NULL;
                      }
               };
       public:
               Node *root;
               SplayTree() : root(NULL){};
               ~SplayTree() { this->clear(); };
               void rotateLeft(Node *&root)
                      Node *tempPtr = root->right;
                      root->right = tempPtr->left;
                      tempPtr->left = root;
                      root = tempPtr;
                      root->parent = root->left->parent;
                      root->left->parent = root;
                      if (root->left->right != NULL)
                              root->left->right->parent = root->left;
                      if (root->parent != NULL)
                              if (root->parent->left == root->left)
                                      root->parent->left = root;
                              else
```

```
root->parent->right = root;
        }
}
void rotateRight(Node *&root)
        Node *tempPtr = root->left;
        root->left = tempPtr->right;
        tempPtr->right = root;
        root = tempPtr;
        root->parent = root->right->parent;
        root->right->parent = root;
        if (root->right->left != NULL)
                root->right->left->parent = root->right;
        if (root->parent != NULL)
        {
                if (root->parent->right == root->right)
                         root->parent->right = root;
                else
                         root->parent->left = root;
        }
}
void zigzag(Node *root)
{
        Node *ptr = root->right;
        rotateRight(ptr);
        rotateLeft(root);
}
void zagzig(Node *root)
{
        Node *ptr = root->left;
        rotateLeft(ptr);
        rotateRight(root);
void zigzig(Node *root)
        rotateRight(root);
        rotateRight(root);
void zagzag(Node *root)
        rotateLeft(root);
        rotateLeft(root);
void Splay(Node *&root, bool SplayOnce)
        if (root->parent == NULL)
        {
                return;
        Node *Parent = root->parent;
```

```
Node *grand = Parent->parent;
        if (grand == NULL)
                //ZIG
                if (root == Parent->left)
                         rotateRight(Parent);
                //ZAG
                else
                         rotateLeft(Parent);
        }
        else
        {
                if (Parent == grand->left)
                         //ZIGZIG
                         if (root == Parent->left)
                                 zigzig(grand);
                         //ZAGZIG
                         else
                                 zagzig(grand);
                }
                else
                {
                         //ZAGZAG
                         if (root == Parent->right)
                                 zagzag(grand);
                         //ZIGZIG
                         else
                                 zigzag(grand);
                }
        if (!SplayOnce)
                Splay(root, 0);
}
void add(Entry *entry)
        if (this->root == NULL)
                this->root = new Node(entry);
        else
        {
                Node *walker = this->root;
                Node *prev = walker;
                while (walker != NULL)
                         prev = walker;
                         if (walker->entry->key > entry->key)
                                 walker = walker->left;
                         else if (walker->entry->key < entry->key)
                                 walker = walker->right;
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else
                                 throw "Duplicate key";
                if (prev->entry->key > entry->key)
                         Node *node = new Node(entry, prev);
                         prev->left = node;
                         Splay(node, 0);
                         this->root = node;
                }
                else
                         Node *node = new Node(entry, prev);
                         prev->right = node;
                         Splay(node, 0);
                         this->root = node;
                }
        }
void add(K key, V value)
{
        add(new Entry(key, value));
}
Node *search(Node *root, K key, vector<K> &traversedList)
{
        if (root == NULL)
                return NULL;
        traversedList.push_back(root->entry->key);
        if (root->entry->key > key)
                return search(root->left, key, traversedList);
        else if (root->entry->key < key)</pre>
                return search(root->right, key, traversedList);
        else
        {
                traversedList.pop_back();
                return root;
        }
V search(K key)
{
        vector<K> traversedList;
        Node *target = search(root, key, traversedList);
        traversedList.clear();
        if (target == NULL)
                throw "Not found!";
        Splay(target, 0);
        this->root = target;
        return target->entry->data;
}
```

```
void remove(K key)
{
        vector<K> traversedList;
        Node *nodeDel = search(root, key, traversedList);
        traversedList.clear();
        if (nodeDel == NULL)
                throw "Not found!";
        Splay(nodeDel, 0);
        this->root = nodeDel;
        if (this->root->left == NULL)
                if (this->root->right != NULL)
                {
                         this->root->right->parent = NULL;
                         this->root = this->root->right;
                         delete nodeDel;
                }
                else
                {
                         delete this->root;
                         this->root = NULL;
                }
        }
        else
        {
                if (this->root->right == NULL)
                {
                         this->root->left->parent = NULL;
                         this->root = this->root->left;
                         delete nodeDel;
                }
                else
                {
                         this->root->left->parent = NULL;
                         Node *walker = this->root->left;
                         while (walker->right != NULL)
                                 walker = walker->right;
                         Splay(walker, 0);
                         walker->right = this->root->right;
                         this->root->right->parent = walker;
                         delete nodeDel;
                         this->root = walker;
                }
        }
}
void traverseNLR(Node *root, void (*func)(K key, V value))
{
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```
if (root == NULL)
                              return;
                      (*func)(root->entry->key, root->entry->value);
                      traverseNLR(root->left, func);
                      traverseNLR(root->right, func);
               }
              void traverseNLR(void (*func)(K key, V value))
               {
                      traverseNLR(this->root, func);
               }
              void clear(Node *root)
              {
                      if (root == NULL)
                              return;
                      clear(root->left);
                      clear(root->right);
                      delete root;
              void clear()
               {
                      clear(root);
               }
       };
       CLASS AVLTREE
       class AVLTree
       public:
              class Node
                      Entry *entry;
                      Node *left;
                      Node *right;
                      int balance;
                      typename SplayTree::Node *corr;
                      friend class AVLTree;
                      friend class BKUTree<K, V>;
                      Node(Entry *entry = NULL, Node *left = NULL, Node *right =
NULL)
                      {
                             this->entry = entry;
                             this->left = left;
                             this->right = right;
                             this->balance = 0;
                             this->corr = NULL;
                      }
               };
```

```
public:
        Node *root;
        Node *insertNode;
        AVLTree() : root(NULL), insertNode(NULL){};
        ~AVLTree() { this->clear(); };
        void rotateLeft(Node *&root)
        {
                Node *tempPtr = root->right;
                root->right = tempPtr->left;
                tempPtr->left = root;
                root = tempPtr;
        void rotateRight(Node *&root)
                Node *tempPtr = root->left;
                root->left = tempPtr->right;
                tempPtr->right = root;
                root = tempPtr;
        }
        void leftBalance(Node *&root, bool &taller)
                switch (root->left->balance)
                case 1:
                        rotateRight(root);
                        root->balance = 0;
                        root->right->balance = 0;
                        taller = 0;
                        break;
                case 2:
                        rotateLeft(root->left);
                        rotateRight(root);
                        switch (root->balance)
                        case 0:
                                 root->left->balance = 0;
                                 root->right->balance = 0;
                                 break;
                        case 1:
                                 root->left->balance = 0;
                                 root->right->balance = 2;
                                 break;
                        case 2:
                                 root->left->balance = 1;
                                 root->right->balance = 0;
                                 break;
                        }
```

```
root->balance = 0;
                break;
        }
        taller = 0;
void rightBalance(Node *&root, bool &taller)
        switch (root->right->balance)
        case 2:
                rotateLeft(root);
                root->balance = 0;
                root->left->balance = 0;
                taller = 0;
                break;
        case 1:
                rotateRight(root->right);
                rotateLeft(root);
                switch (root->balance)
                {
                case 0:
                         root->left->balance = 0;
                         root->right->balance = 0;
                         break;
                case 1:
                         root->left->balance = 0;
                         root->right->balance = 2;
                         break;
                case 2:
                         root->left->balance = 1;
                         root->right->balance = 0;
                         break;
                root->balance = 0;
                break;
        }
        taller = 0;
void insertAvlTree(Node *&root, Entry *value, bool &taller)
        if (root == NULL)
        {
                root = new Node(value);
                taller = 1;
                this->insertNode = root;
                return;
        if (value->key < root->entry->key)
        {
                insertAvlTree(root->left, value, taller);
```

```
if (taller)
                         switch (root->balance)
                         case 0:
                                 root->balance = 1;
                                 break;
                         case 1:
                                 leftBalance(root, taller);
                                 break;
                         case 2:
                                 root->balance = 0;
                                 taller = 0;
                                 break;
                         }
                }
        }
        else if (value->key > root->entry->key)
                insertAvlTree(root->right, value, taller);
                if (taller)
                 {
                         switch (root->balance)
                         {
                         case 0:
                                 root->balance = 2;
                                 break;
                         case 1:
                                 root->balance = 0;
                                 taller = 0;
                                 break;
                         case 2:
                                 rightBalance(root, taller);
                                 break;
                         }
                }
        }
        else
                throw "Duplicate key";
}
void add(Entry *entry)
        bool taller = 1;
        insertAvlTree(root, entry, taller);
void add(K key, V value)
{
        add(new Entry(key, value));
}
```

```
if (root->balance == 1)
                                 root->balance = 0;
                                 return root;
                        else if (root->balance == 0)
                                 root->balance = 2;
                                 shorter = false;
                                 return root;
                        }
                        else
                        {
                                 if (root->right->balance == 1)
                                         rotateRight(root->right);
                                         rotateLeft(root);
                                         if (root->balance == 1)
                                                 root->right->balance = 2;
                                                 root->left->balance = 0;
                                         else if (root->balance == 2)
                                                 root->right->balance = 0;
                                                 root->left->balance = 1;
                                         }
                                         else
                                         {
                                                 root->right->balance = 0;
                                                 root->left->balance = 0;
                                         }
                                         root->balance = 0;
                                 }
                                 else
                                 {
                                         rotateLeft(root);
                                         if (root->balance == 2)
                                         {
                                                 root->left->balance =
root->right->balance = 0;
                                                 root->balance = 0;
                                         }
                                         else
                                         {
                                                 root->balance = 1;
                                                 root->left->balance = 2;
```

Node *deleteRightBalance(Node *root, bool &shorter)

```
root->right->balance = 0;
                                 shorter = false;
                         }
                }
        }
        return root;
}
Node *deleteLeftBalance(Node *root, bool &shorter)
        if (root->balance == 2)
        {
                root->balance = 0;
                return root;
        else if (root->balance == 0)
        {
                root->balance = 1;
                shorter = false;
                return root;
        }
        else
        {
                if (root->left->balance == 2)
                         rotateLeft(root->left);
                         rotateRight(root);
                         if (root->balance == 2)
                         {
                                 root->left->balance = 1;
                                 root->right->balance = 0;
                         else if (root->balance == 1)
                                 root->right->balance = 2;
                                 root->left->balance = 0;
                         }
                         else
                         {
                                 root->right->balance = 0;
                                 root->left->balance = 0;
                         }
                         root->balance = 0;
                 }
                else
                 {
                         rotateRight(root);
                         if (root->balance == 1)
                         {
                                 root->right->balance =
```

```
root->balance = 0;
                                         }
                                         else
                                         {
                                                 root->balance = 2;
                                                 root->left->balance = 0;
                                                 root->right->balance = 1;
                                                  shorter = false;
                                         }
                                 }
                        return root;
                Node *AVLDelete(Node *root, K deleteKey, bool &shorter, bool
&success)
                {
                        if (root == NULL)
                         {
                                 success = shorter = 0;
                                 return root;
                         }
                        else if (deleteKey < root->entry->key)
                                 root->left = AVLDelete(root->left, deleteKey,
shorter, success);
                                 if (shorter)
                                         root = deleteRightBalance(root, shorter);
                        }
                        else if (deleteKey > root->entry->key)
                                 root->right = AVLDelete(root->right, deleteKey,
shorter, success);
                                 if (shorter)
                                         root = deleteLeftBalance(root, shorter);
                        }
                        else
                                 if (root->left == NULL)
                                 {
                                         Node *tmp = root->right;
                                         success = shorter = true;
                                         delete root;
                                         return tmp;
                                 else if (root->right == NULL)
                                 {
                                         Node *tmp = root->left;
                                         success = shorter = true;
                                         delete root;
                                         return tmp;
```

```
}
                                 else
                                 {
                                         Node *findmax = root->left;
                                         while (findmax->right != NULL)
                                         {
                                                  findmax = findmax->right;
                                         root->entry = findmax->entry;
                                         root->corr = findmax->corr;
                                         findmax->corr->corr = root;
                                         root->left = AVLDelete(root->left,
findmax->entry->key, shorter, success);
                                         if (shorter)
                                         {
                                                  root = deleteRightBalance(root,
shorter);
                                         }
                                 }
                         return root;
                }
                void remove(K key)
                         bool shorter = 0;
                         bool success = 0;
                         root = AVLDelete(root, key, shorter, success);
                }
                Node *search(Node *root, K key, vector<K> &traversedList)
                {
                         if (root == NULL)
                                 return NULL;
                         if (traversedList.size() > 0)
                                 if (root->entry->key == traversedList[0])
                                         return NULL;
                         traversedList.push_back(root->entry->key);
                         if (root->entry->key > key)
                                 return search(root->left, key, traversedList);
                         else if (root->entry->key < key)</pre>
                                 return search(root->right, key, traversedList);
                         else
                         {
                                 traversedList.pop_back();
                                 return root;
                         }
                V search(K key)
```

```
{
                        vector<K> traversedList;
                        Node *target = search(root, key, traversedList);
                        if (target != NULL)
                                 traversedList.clear();
                                 return target->entry->value;
                         }
                        else
                        {
                                 traversedList.clear();
                                 throw "Not Found";
                        }
                }
                void traverseNLR(Node *r, void (*func)(K key, V value))
                        if (r == NULL)
                                 return;
                         (*func)(r->entry->key, r->entry->value);
                        traverseNLR(r->left, func);
                        traverseNLR(r->right, func);
                void traverseNLR(void (*func)(K key, V value))
                {
                        traverseNLR(root, func);
                }
                void clear(Node *root)
                {
                        if (root == NULL)
                                 return;
                        clear(root->left);
                        clear(root->right);
                        delete root;
                void clear()
                {
                        clear(root);
                         delete (insertNode);
                         insertNode = NULL;
                }
        };
};
```