



ĐẠI HỌC TÔN ĐỨC THẮNG
Ton Duc Thang University (TDTU)

Digital Image Processing

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Image filtering

In Digital Image Processing

Image transformations

- As with any function, we can apply operators to an image



$$g(x,y) = f(x,y) + 20$$



$$g(x,y) = f(-x,y)$$

- We'll talk about a special kind of operator, *convolution* (linear filtering)

Question: Noise reduction

- Given a camera and a still scene, how can you reduce noise?



Take lots of images and average them!

What's the next best thing?

Image filtering

- Modify the pixels in an image based on some function of a local neighborhood of each pixel

| | | |
|----|---|---|
| 10 | 5 | 3 |
| 4 | 5 | 1 |
| 1 | 1 | 7 |

Local image data

Some function



| | | |
|--|---|--|
| | | |
| | 7 | |
| | | |

Modified image data

Image filtering

- **Filtering:**

- Form a new image whose pixels are a combination original pixel values

- **Goals:**

- Extract useful information from the images
 - Features (edges, corners, blobs...)
 - Modify or enhance image properties:
 - super-resolution; in-painting; de-noising

De-noising



Salt and pepper noise

Super-resolution



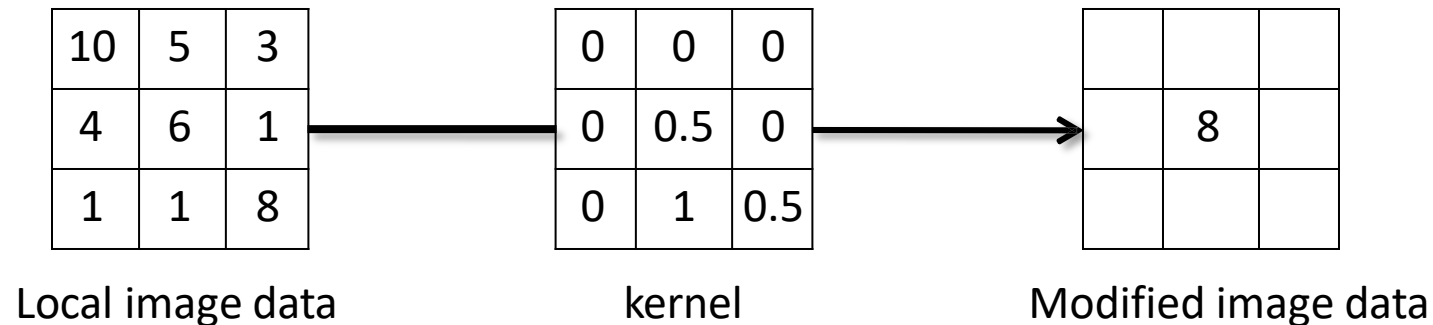
In-painting



Bertamio et al

Linear filtering

- One simple version: linear filtering (cross-correlation, convolution)
 - Replace each pixel by a linear combination of its neighbors
- The prescription for the linear combination is called the “kernel” (or “mask”, “filter”)



Convolution

- Same as cross-correlation, except that the kernel is “flipped” (horizontally and vertically)

$$G[i, j] = \sum_{u=-k}^k \sum_{v=-k}^k H[u, v] F[i - u, j - v]$$

This is called a **convolution** operation:

$$G = H * F$$

- Convolution is **commutative** and **associative**

2D Convolution

$$g(x,y) = h(x,y) * f(x,y)$$

- f, g: input/output
- h: mask/filter/kernel

1. Flip the mask (horizontally and vertically) only once
2. Slide the mask onto the image.
3. Multiply the corresponding elements and then add them
4. Repeat this procedure until all values of the image has been calculated.



| | | | | |
|-----------------|-----------------|-----------------|---|---|
| 1 _{x1} | 1 _{x0} | 1 _{x1} | 0 | 0 |
| 0 _{x0} | 1 _{x1} | 1 _{x0} | 1 | 0 |
| 0 _{x1} | 0 _{x0} | 1 _{x1} | 1 | 1 |
| 0 | 0 | 1 | 1 | 0 |
| 0 | 1 | 1 | 0 | 0 |

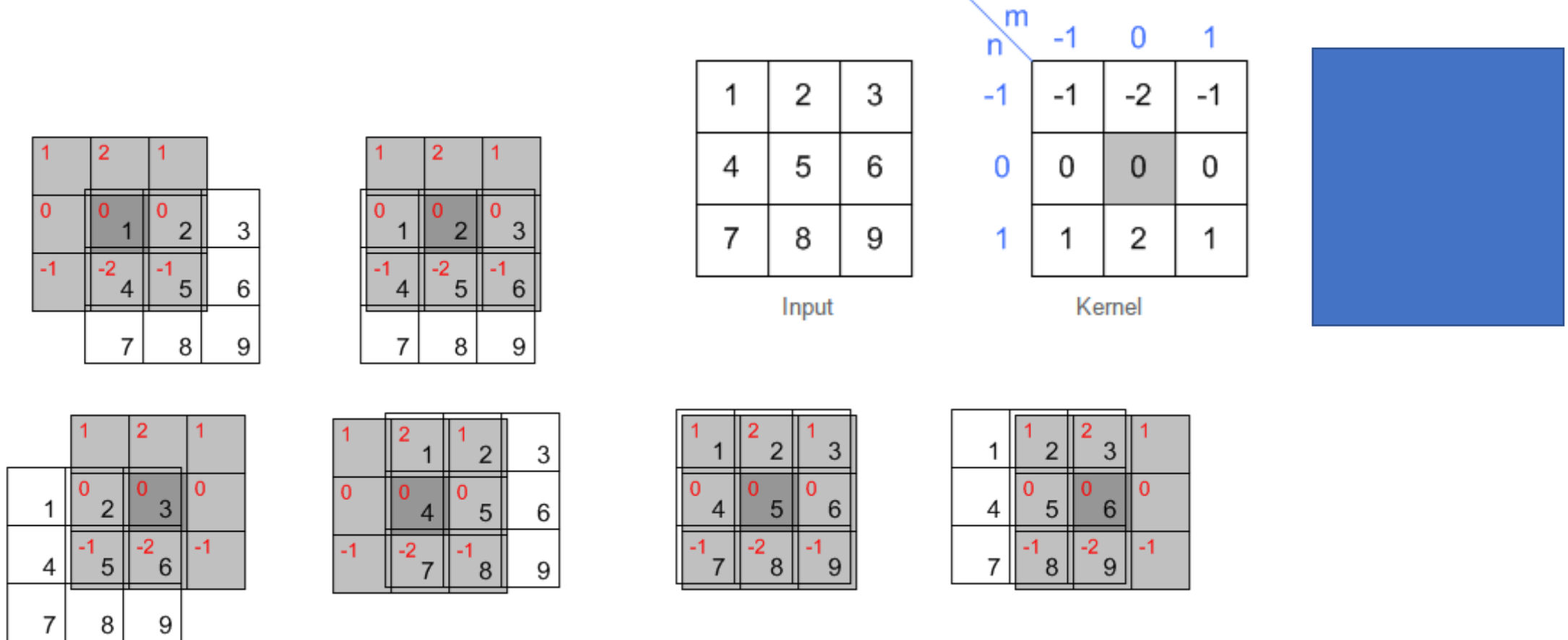
Image

| | | |
|---|--|--|
| 4 | | |
| | | |
| | | |

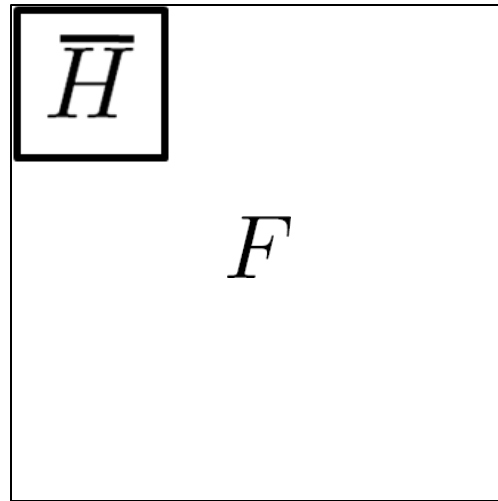
Convolved
Feature

Example

- http://www.songho.ca/dsp/convolution/convolution2d_example.html



Convolution



Cross-correlation

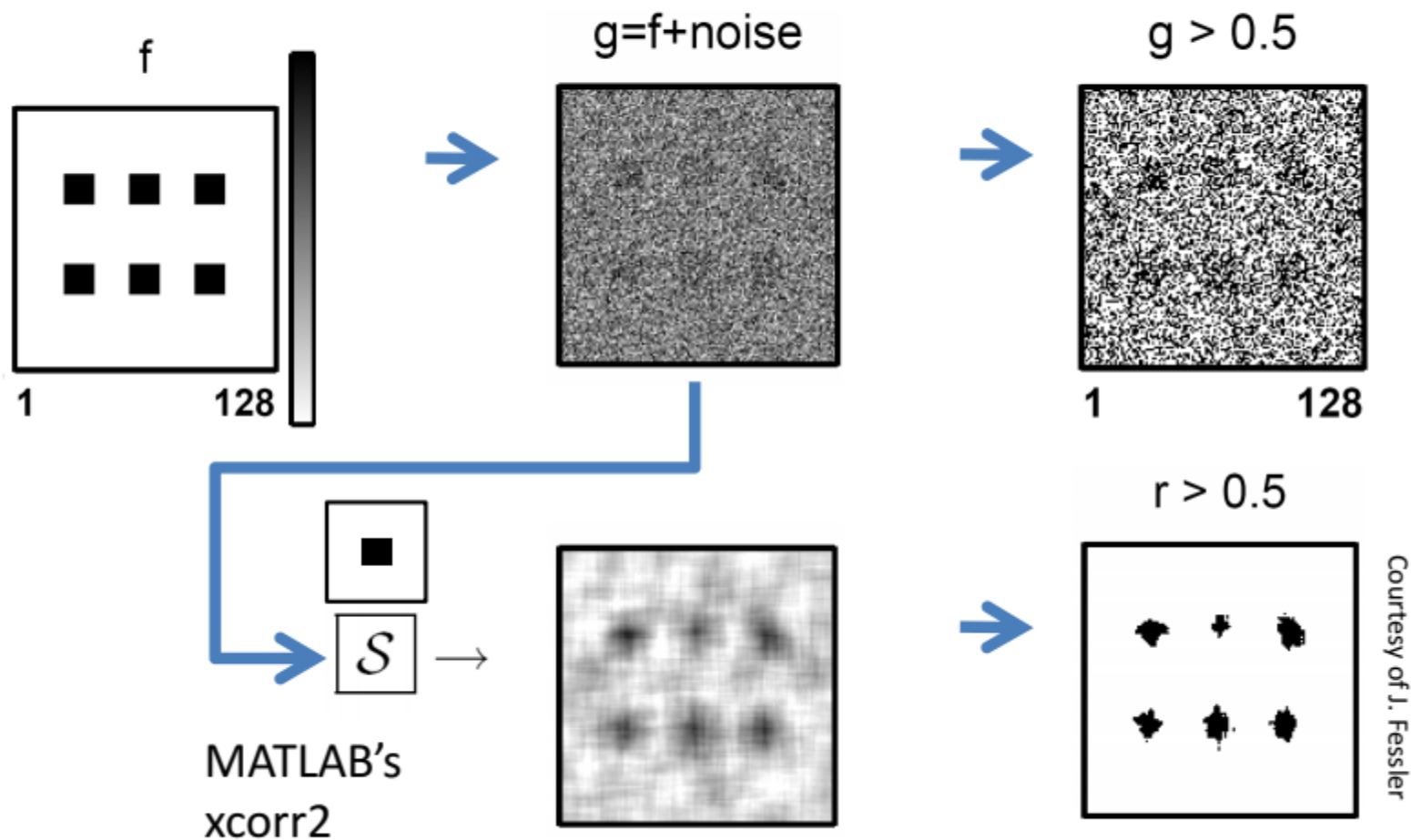
Let F be the image, H be the kernel (of size $2k+1 \times 2k+1$), and G be the output image

$$G[i, j] = \sum_{u=-k}^k \sum_{v=-k}^k H[u, v] F[i + u, j + v]$$

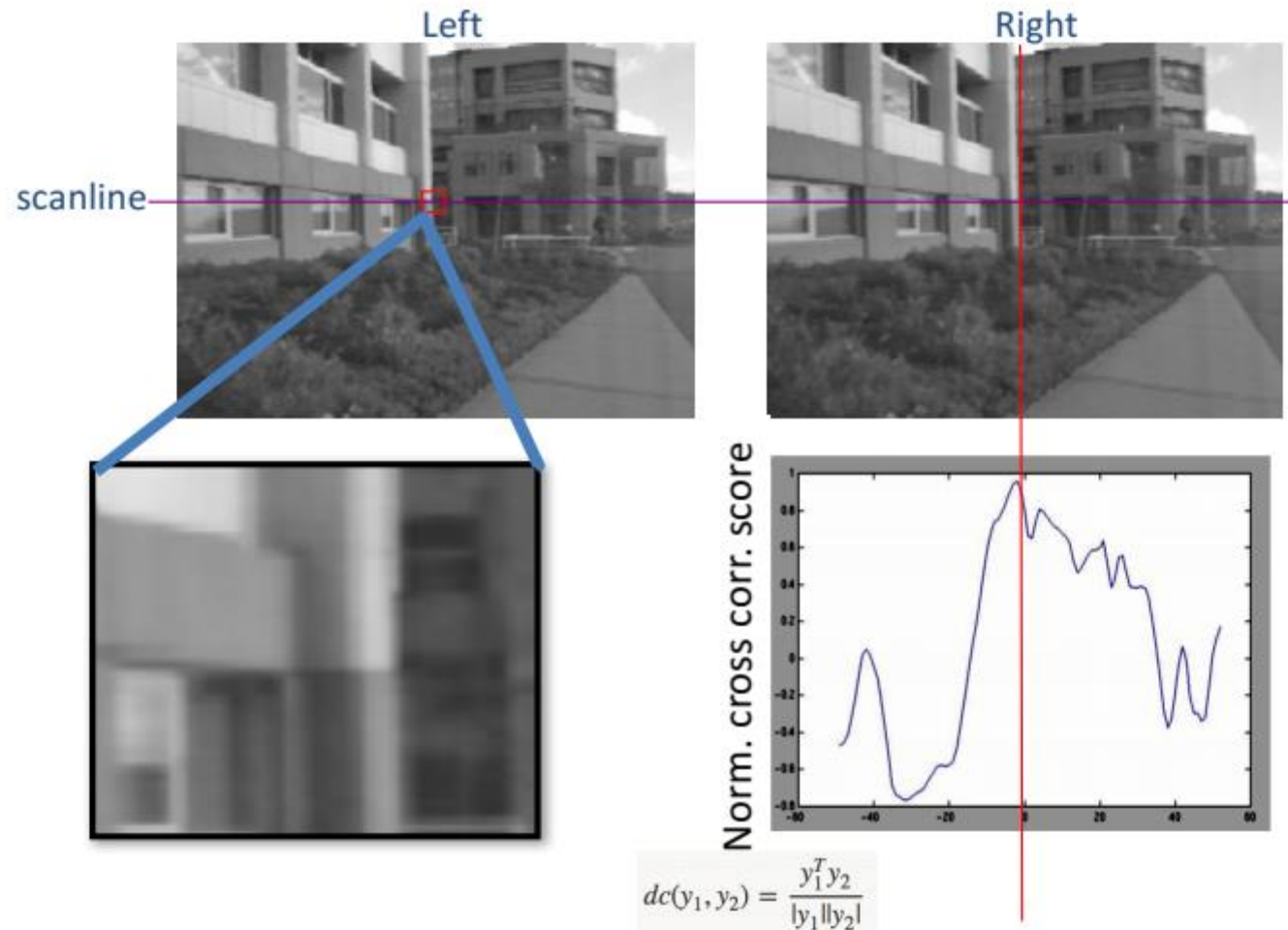
This is called a **cross-correlation** operation:

$$G = H \otimes F$$

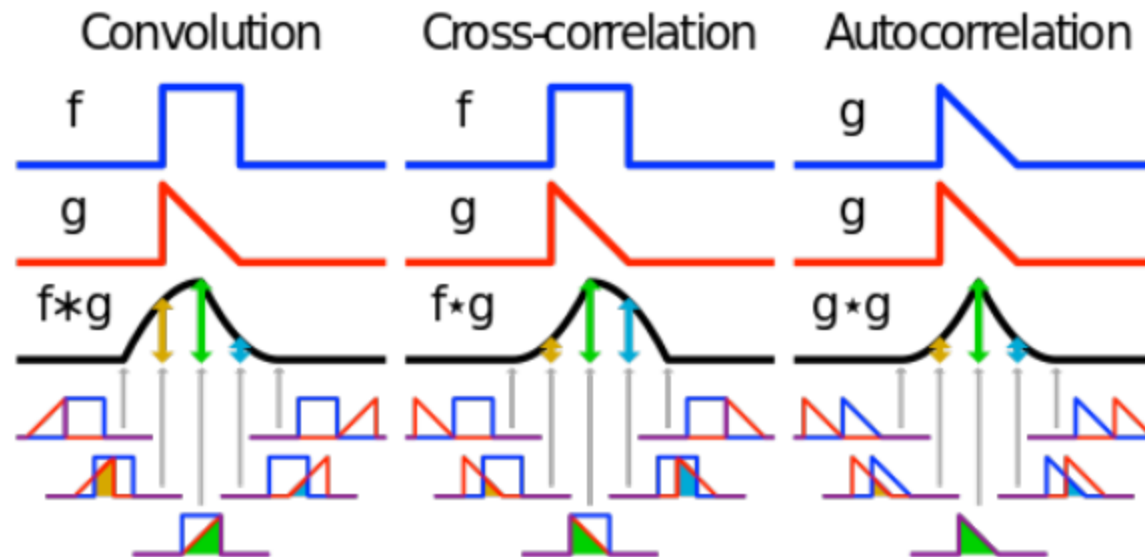
(Cross) correlation – example



(Cross) correlation – example



Convolution vs. (Cross) Correlation



Convolution vs. (Cross) Correlation

- A **convolution** is an integral that expresses the amount of overlap of one function as it is shifted over another function.
 - convolution is a filtering operation
- **Correlation** compares the *similarity of two sets of data*. Correlation computes a measure of similarity of two input signals as they are shifted by one another. The correlation result reaches a maximum at the time when the two signals match best .
 - correlation is a measure of relatedness of two signals



Cross Correlation Application: Vision system for TV remote control

- uses template matching

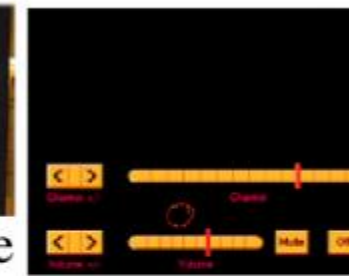
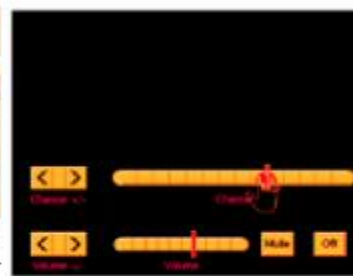
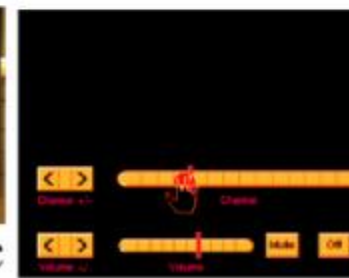
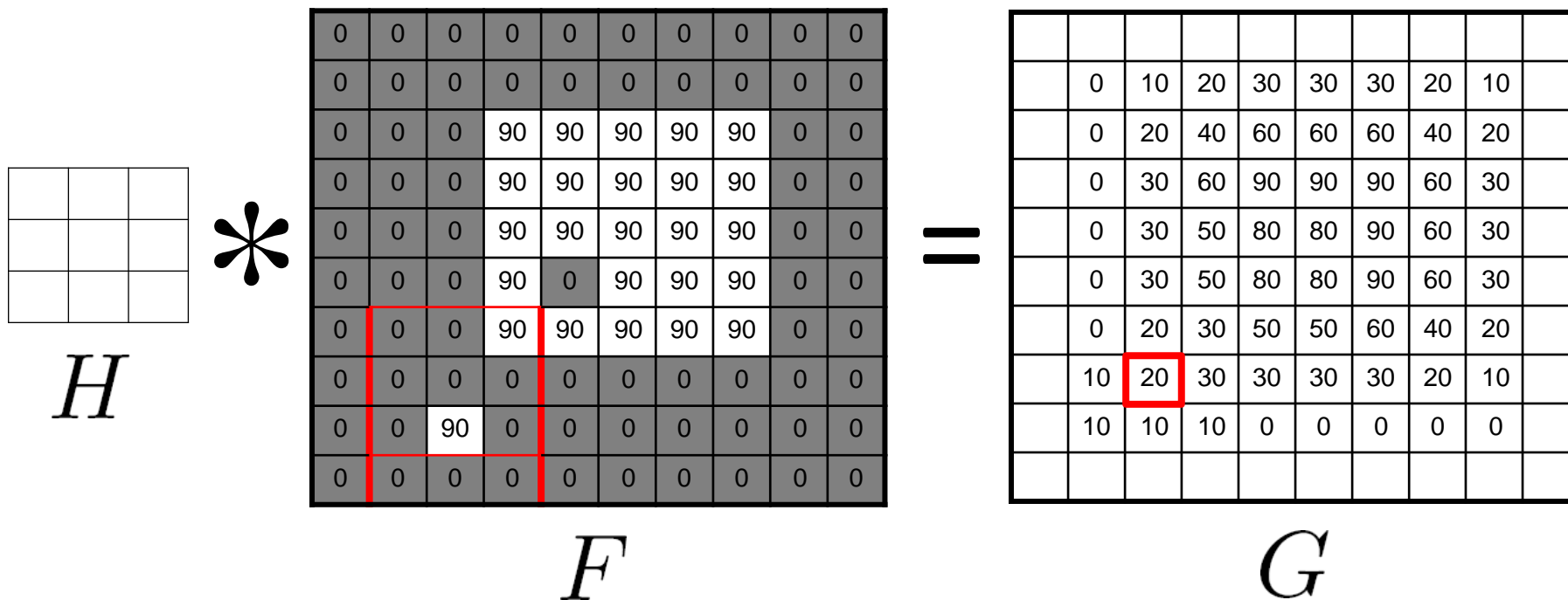


Figure from "Computer Vision for Interactive Computer Graphics," W.Freeman et al, IEEE Computer Graphics and Applications, 1998 copyright 1998, IEEE

Mean filtering



Linear filters: examples



Original



| | | |
|---|---|---|
| 0 | 0 | 0 |
| 0 | 1 | 0 |
| 0 | 0 | 0 |



Identical image

Linear filters: examples



Original



| | | |
|---|---|---|
| 0 | 0 | 0 |
| 1 | 0 | 0 |
| 0 | 0 | 0 |



Shifted left
By 1 pixel

Linear filters: examples

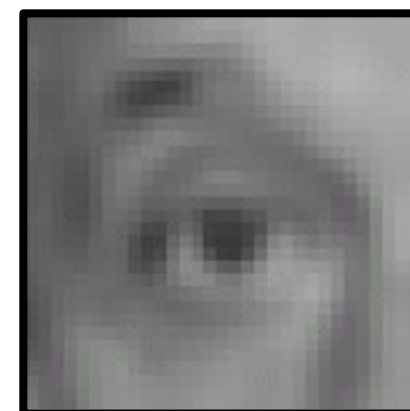


Original




$\frac{1}{9}$

| | | |
|---|---|---|
| 1 | 1 | 1 |
| 1 | 1 | 1 |
| 1 | 1 | 1 |




Blur (with a mean filter)

Linear filters: examples

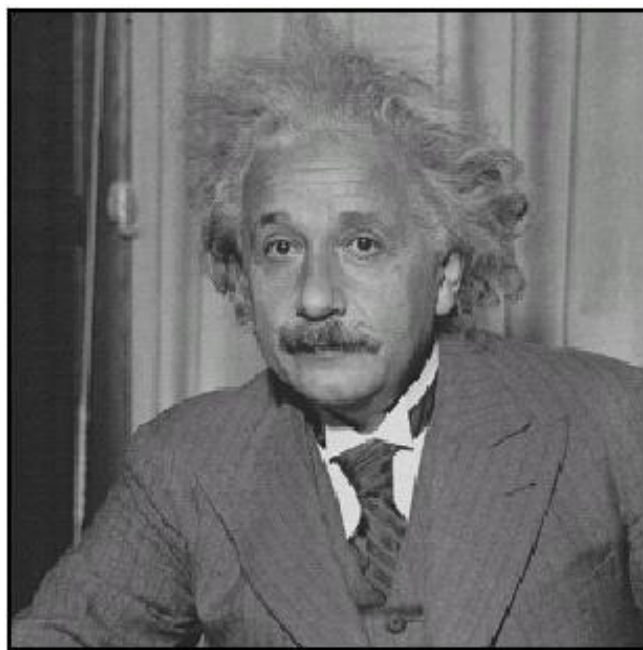


Original

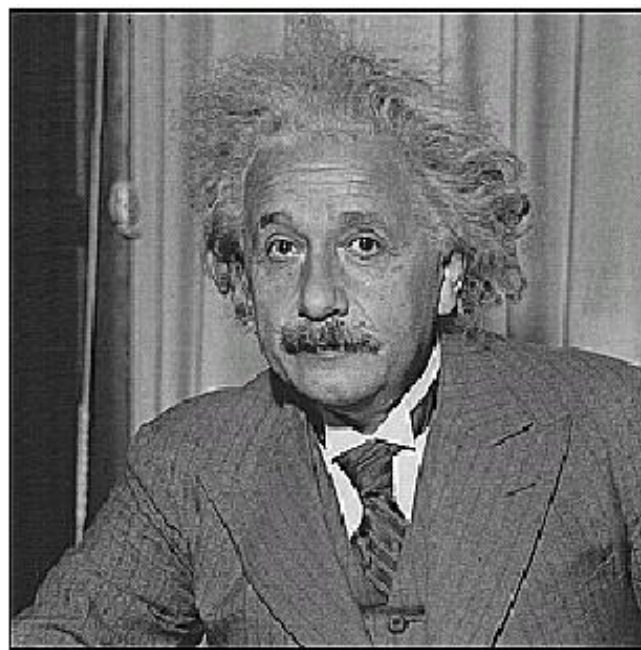
$$* \left(\begin{bmatrix} 0 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 0 \end{bmatrix} - \frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} \right) =$$


Sharpening filter
(accentuates edges)

Sharpening

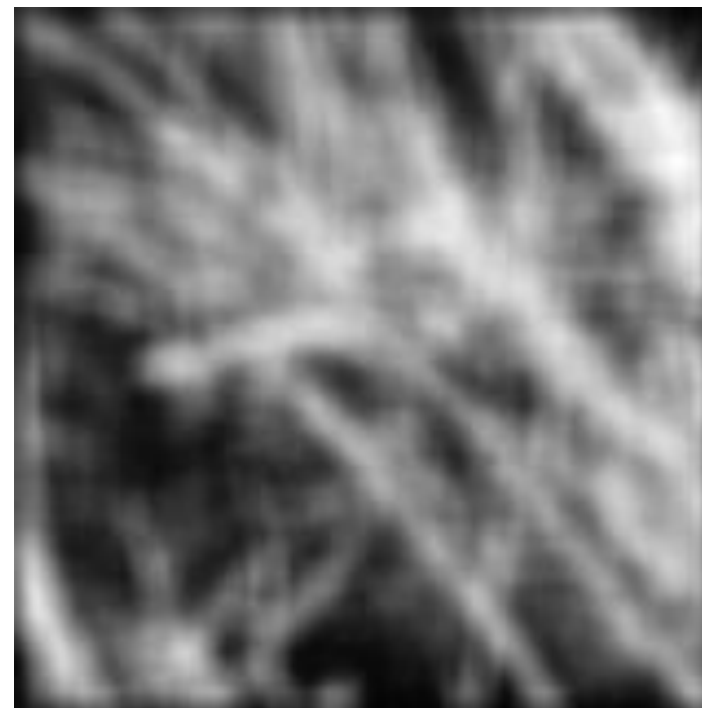
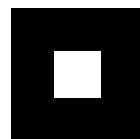


before

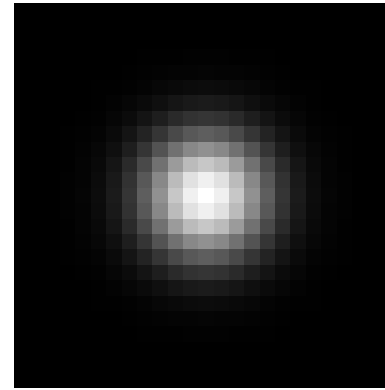
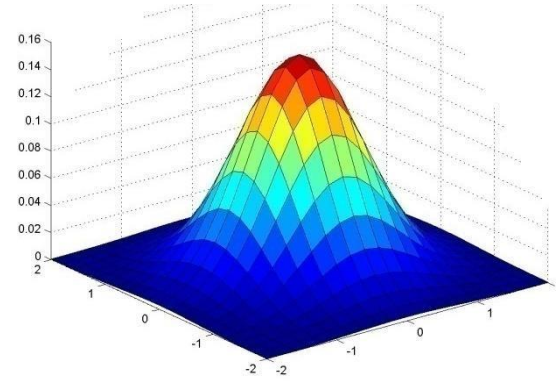


after

Smoothing with box filter revisited

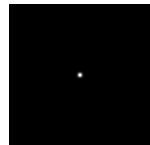
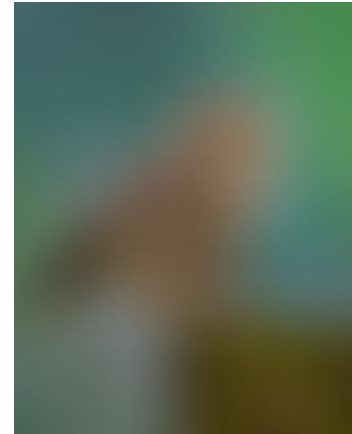
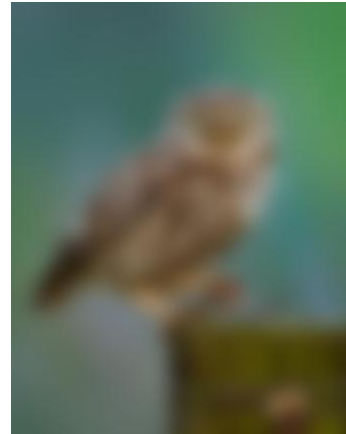


Gaussian Kernel

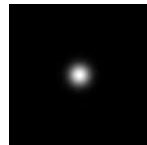


$$G_{\sigma} = \frac{1}{2\pi\sigma^2} e^{-\frac{(x^2+y^2)}{2\sigma^2}}$$

Gaussian filters



$\sigma = 1$ pixel



$\sigma = 5$ pixels



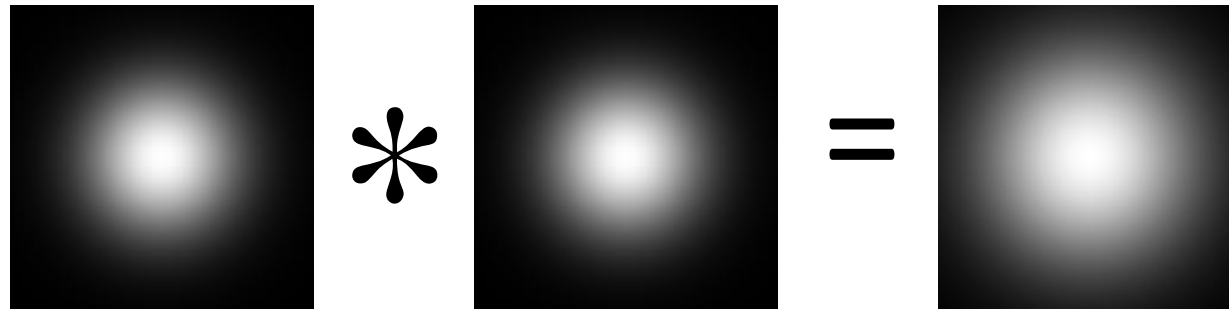
$\sigma = 10$ pixels



$\sigma = 30$ pixels

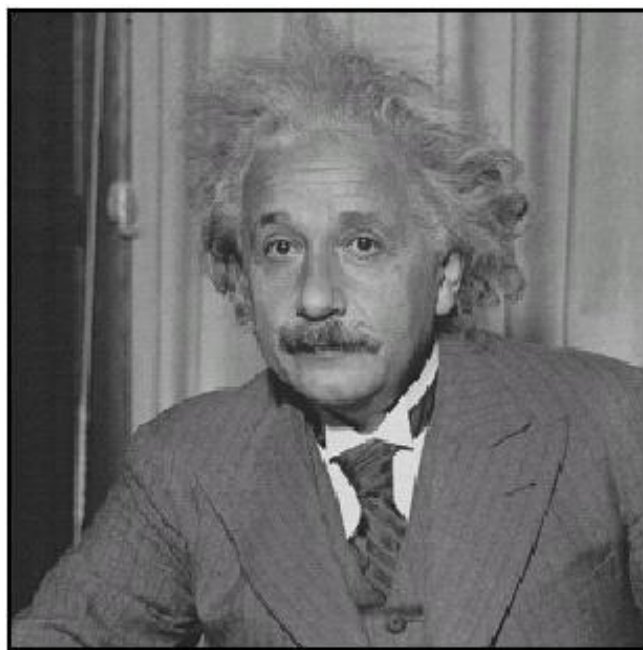
Gaussian filter

- Removes “high-frequency” components from the image (low-pass filter)
- Convolution with self is another Gaussian

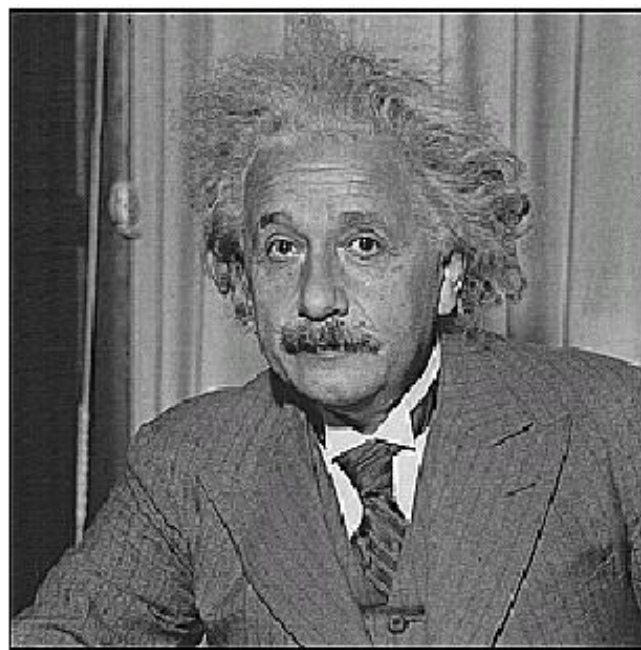


- Convolving two times with Gaussian kernel of width σ = convolving once with kernel of width $\sigma\sqrt{2}$

Sharpening



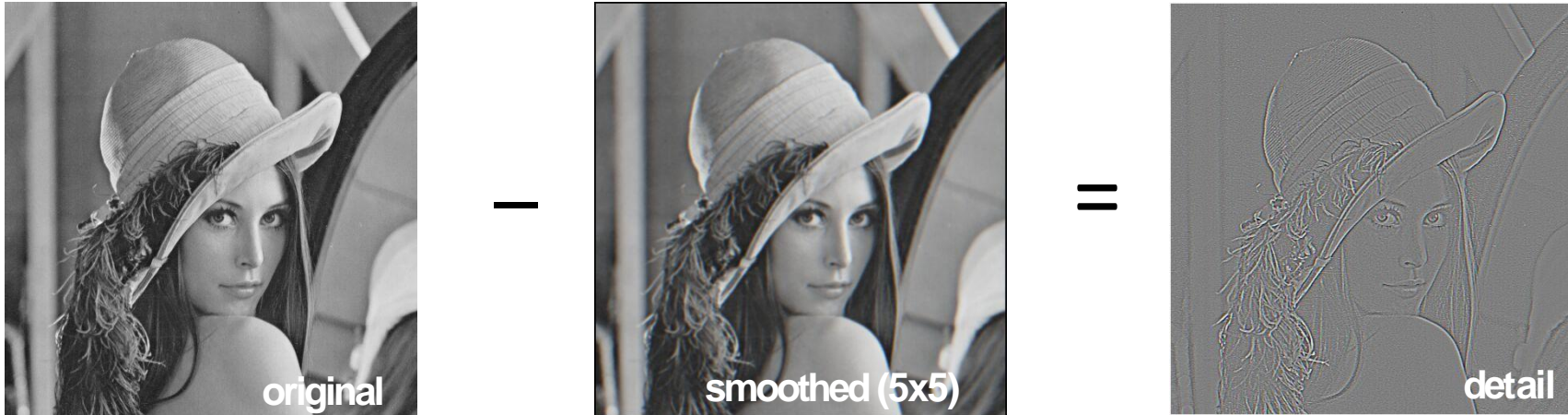
before



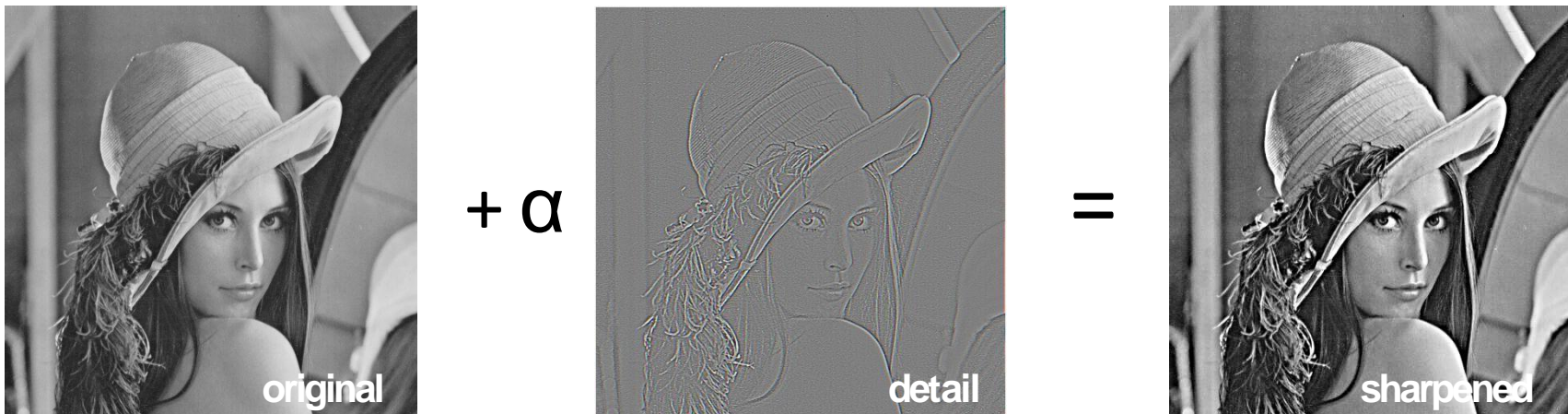
after

Sharpening revisited

- What does blurring take away?



Let's add it back:

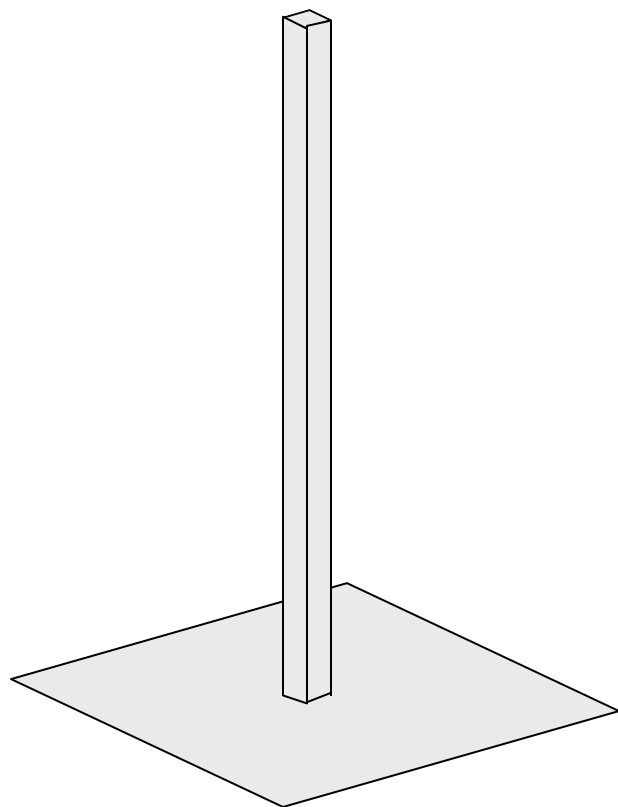


Sharpen filter

$$F + \alpha (F - \underbrace{F * H}_{\text{blurred image}})$$

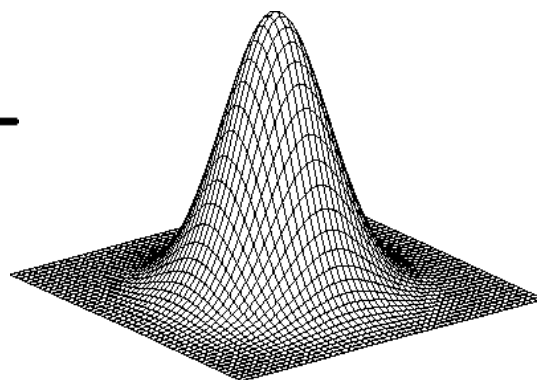
↑
image

↑
unit impulse
(identity)



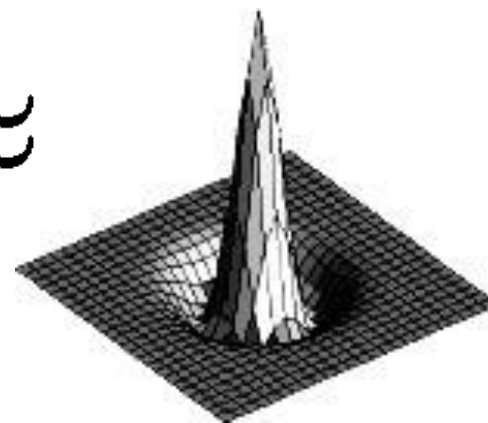
scaled impulse

—



Gaussian

≈



Laplacian of Gaussian

Sharpen filter



Convolution in the real world

Camera shake



Source: Fergus, *et al.* "Removing Camera Shake from a Single Photograph", SIGGRAPH 2006

Bokeh: Blur in out-of-focus regions of an image.



Source: <http://lullaby.homepage.dk/diy-camera/bokeh.html>

Questions?