- Quantifying error in effect size estimates in attention, executive function and implicit
- learning
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20 Abstract

Accurate quantification of effect sizes has the power to motivate theory, and reduce 21 misinvestment of scientific resources by informing power calculations during study planning. 22 However, a combination of publication bias and small sample sizes ($\sim N=25$) hampers 23 certainty in current effect size estimates. We sought to determine the extent to which sample sizes may produce error in effect size estimates for four commonly used paradigms assessing 25 attention, executive function and implicit learning (Attentional Blink (AB), Multitasking (MT), Contextual Cueing (CC), Serial Response Task (SRT)). We combined a large data-set 27 with a bootstrapping approach to simulate 1000 experiments across a range of N (13-313). Beyond quantifying the effect size and statistical power that can be anticipated for each study design, we demonstrate that experiments with lower N may double or triple information loss. We also show that basing power calculations on effect sizes from similar studies yields a problematically imprecise estimate between 40-67\% of the time, given 32 commonly used sample sizes. Last, we show that skewness of inter-subject behavioural 33 effects may serve as a predictor of an erroneous estimate. We conclude with practical 34 recommendations for researchers and demonstrate how our simulation approach can yield 35 theoretical insights that are not readily achieved by other methods; such as identifying the information gained from rejecting the null hypothesis, and quantifying the contribution of 37 individual variation to error in effect size estimates.

Introduction

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Despite the complexity involved in disentangling the processes that underpin cognition, 40 decision making regarding experimental outcomes is often made on binary (i.e. pass or fail) 41 terms, across the psychological, neuroscientific and biomedical sciences (Szucs & Ioannidis, 2017). Theoretical predictions are often specified in terms of the presence or absence of a given effect, and a yes/no decision is made about whether the null hypothesis (usually a hypothesis of null differences) can be rejected. It seems unlikely that such binary decision-making will be sufficient to disentangle the myriad functional systems that comprises the brain's processes. An alternate approach is to develop theory and models that predict the magnitude of the effect. Providing predictions in terms of effect size magnitude prompts theorists to consider the variability as well as the presence of predicted effects, and is demonstrably a useful metric when considering practical relevance (Funder & Ozer, 2019). Such magnitudes are often characterised as an effect size: a standardised measure that 51 reflects the extent to which an effect, such as a mean difference between two conditions, is expected to generalise to the population (Cohen, 1988).

A prediction of effect magnitude is easier to disprove than a binary outcome, and
therefore constitutes a more desirable prediction for theory testing (Popper, 1959). To move
towards theories that predict changes in effect size magnitude, it is helpful to gain an
understanding of how much insight is yielded from our current effect size estimates; i.e. how
well are we currently quantifying effect sizes, and should we increase sample sizes to quantify
them better? Indeed, recent work suggests that insufficiently powered studies are at
increased risk of producing effect size estimates that are either inflated in magnitude, or are
in the incorrect direction (Chen et al., 2019; Gelman & Carlin, 2014). Here we seek to
address how well we currently characterise effect sizes in the study of cognition, using some
established paradigms in the fields of attention, executive function and implicit learning;
namely the Attentional Blink (AB, Raymond, Shapiro, & Arnell, 1992), Multitasking (MT,

Schumacher et al., 2001), Serial Response Task (SRT, Nissen & Bullemer, 1987), and Contextual Cueing (CC, Chun & Jiang, 1998) paradigms.

Accurate quantification of effect sizes is also desirable for study planning, as effect sizes 67 form the foundation of a priori power calculations (Cohen 1988). Here the researcher determines the sample size (N) required to achieve sufficient power to correctly reject the null hypothesis. The importance - and difficulty - of accurately determining the anticipated effect size has been considered extensively elsewhere (Cohen, 1988; Gelman & Carlin, 2014; 71 Albers & Lakens, 2018; Cumming, 2014;, Egger, Smith, Schneider, & Minder, 1997; Guo, Logan, Glueck, & Muller, 2013; Lakens, 2013; Szucs & Ioannidis, 2017; Westfall, Kenny, & Judd, 2014). Standard approaches of determining an anticipated effect size involve consulting a meta-analysis, basing effect-size estimates on a few similar studies (incomplete sampling), or determining the smallest effect that is of theoretical relevance (e.g. Gelman & Carlin, 2014). What remains somewhat less considered is the utility of knowing how effect size estimates may vary across replications of an experiment (e.g. Cumming, 2014; Lorca-Puls et al., 2018), i.e. what are the distributional properties of the effect size, given a field that uses a comparable N across experiments?

The answer to this question can facilitate both study planning and theory development.

A paradigm that elicits a small effect that manifests with low variability across replications

may be considered a more desirable target for theory and model development than a

paradigm that produces the same mean effect size but with wider variability. With regard to

study planning, identifying the lower bound of an expected effect size facilitates computation

of the N required to achieve sufficient statistical power under the worst case scenario

(Gelman & Carlin, 2014). Understanding how effect sizes vary across replications with a

given N also allows computation of the likelihood that any single study has produced a

reasonably accurate estimate, which can inform the researcher who may be computing

anticipated effect sizes on the basis of one or a few similar studies. There is also utility in

knowing to what extent variability in effect size observations reduces when larger N are used

instead. There may be an upper bound on the accuracy with which a particular effect can be estimated, for example, when the construction of a paradigm introduces a certain level of noise or measurement error that is larger than variation at the level of the individual.

Consequently, there may be a point of diminishing returns, where the cost of recruiting extra N will outweigh the gains in accuracy of effect size estimation.

Quantifying the range of effect sizes that may be observed across experimental 97 replications is not trivial. Indeed, it has been noted that the largest challenge in 98 experimental design is the prior identification of a plausible range of effect sizes (Gelman & 99 Carlin, 2014). Meta-analytic and incomplete sampling approaches for determining an 100 expected effect size are hampered by the quality of the existing literature (Brand, Bradley, 101 Best, & Stoica, 2008; Friston, 2012; Gelman & Carlin, 2014; Lane & Dunlap, 1978; 102 Lorca-Puls et al., 2018). A recent survey of 900 effect sizes across psychology disciplines 103 showed that effects from non-pre-registered studies were much larger than pre-registered 104 studies (r = 0.36 vs 0.16, Schäfer and Schwarz (2019)) suggesting that prior to 105 pre-registration, under-powered studies were contributing inflated effect size estimates to the 106 psychology literature. Although multiple correction methods have been developed within the 107 meta-analytic framework to account for biases due to missing literature (Schmidt & Hunter, 2015), they typically involve assumptions about the sources of missing data, which can never be fully tested (McShane, Böckenholt, & Hansen, 2016; Wiernik & Dahlke, 2020). Thus even if one were to define an expected effect size using corrected meta-analyses (if available), there 111 is much to gain from corroborating meta-analytic results with alternate methods that can 112 guarantee a lack of bias in the available dataset. It is also difficult to determine, on the basis 113 of existing literature - such as when using meta-analysis - how conclusions about effect sizes 114 would differ if a given field of study was different, e.g. how much published literature is likely 115 to be missing if a larger N was used as standard? 116

Simulation studies offer the opportunity to ask how well a field is currently quantifying effect sizes, and how a field's estimate of an effect size would change with differing levels of

statistical power. Typically, simulation studies generate data under some simplifying 119 assumptions about the data generation process (e.g. Albers & Lakens, 2018; Hedges, 1982; 120 Lane & Dunlap, 1978; Troncoso Skidmore & Thompson, 2013; Westfall et al., 2014). 121 Although this work is necessary for informing how effect size estimates behave under varying 122 conditions where ground truth is known, it is challenging to anticipate all the complexities of 123 data from the repeated-measures designs used across a range of phenomena and processes, 124 such as in the study of attention, executive function and implicit learning. Such data are 125 often not normally distributed and carry varying levels of covariance between conditions. 126 Thus, there remains a question mark over the extent to which the results from simulation 127 work generalizes to real-world data. An alternative method is to simulate experimental 128 outcomes by bootstrapping smaller samples from larger, real data-sets (e.g. Lorca-Puls et al., 129 2018). This approach offers the opportunity to characterize the distributional qualities of effect sizes estimated from high-dimensional data-sets, using varying levels of N, while 131 maintaining ecological validity. 132

In the current study, we applied the latter simulation approach to characterize effect 133 size distributions yielded from the study of cognition. Participants (N = 313) completed a 134 battery of cognitive tasks (AB, MT, SRT and CC) originally assembled to test the 135 relationship between attention, executive function and implicit learning. For each paradigm, 136 we simulated 1000 bootstrapped experiments across 20 Ns ranging from 13 to 313. For each 137 paradigm and from each set of simulations, we determined the impact of N on error in effect 138 size estimates. We asked how much variability of effect size estimates changes as a function of 139 N, and sought to identify a point at which increasing N may offer lower gains for improving effect size estimates. We next determined how likely it is that a study will produce an effect size estimate with sufficiently low error, as a function of N. We also sought to determine the impact of N on the potential for missing literature for each paradigm, given the case of publication bias. Last, we identified data features that predict error in effect size estimates, 144 beyond the mean and standard deviation measures of which they are a function. Such

features may serve as a flag for whether data from a single experiment may be susceptible to
error in effect size estimates. We focused on the skew and kurtosis of inter- and intra-subject
effects, as such measures can bias mean and variance estimates when datasets violate
normality assumptions, yet remain undiscussed in simulation studies that assume normality.
The results motivate guidelines for study design and interpretation, not only for future AB,
MT, SRT and CC studies, but also more broadly for the investigation of cognition.

152 Methods

153 Participants

The current study used a data set collected for a different pre-registered project 154 examining the relationship between executive function and implicit learning. This data set 155 contains performance measures from N=313 participants. Participants were undergraduate 156 students, aged 18 to 35 years old (mean = 20.14 yrs, sd = 3.46). Of the total sample, 208 157 reported being female, and 269 reported being right handed. Participants received course 158 credits as compensation. All procedures were approved by The University of Queensland 159 Human Research Ethics Committee and adhered to the National Statement on Ethical 160 Conduct in Human Research. 161

62 Apparatus

Experimental procedures were run on an Apple Mac Minicomputer (OS X Late 2014, 2.8 GHz Intel Core i5) with custom code using the Psychophysics toolbox (v3.0.14)

(Brainard, 1997; Pelli, 1997) in Matlab v2015b. Participants completed 7 tasks; Attentional Blink (AB), Multitasking (MT), Contextual Cueing (CC), Serial Response Task (SRT),

Visual Statistical Learning (VSL), Operation Span task and a Stop Signal Inhibition task.

Only the data from the AB, MT, CC and SRT are reported here. We opted not to report

the VSL, OSPAN or Stop Signal data as their design did not lend themselves to the computation of a standardised effect size.

Procedures

Across all tasks, participants sat approximately 57 cm from the monitor. An overview of the task procedures is presented in Figure 1. Details regarding each of the task protocols are presented within each section below.

Attentional Blink (AB). The AB task taps limitations in the deployment of visual information processing over time. Participants are instructed to detect two targets from a rapidly presented series of visual items. Accuracy for the second target is poorer if it appears closer in time to the first target (at early lags, from lag 2 onwards), relative to further apart in time (Raymond et al., 1992).

The AB protocol was the same as that reported in Bender et al (2016). 180 Each trial began with a black fixation cross in the center of a gray screen [RGB: 128, 128, 181 128 for a variable interval of 200-600 ms. On each trial, letter targets and digit distractors 182 were presented centrally for 100 ms in rapid serial presentation. The eight distractors were 183 drawn without replacement from the digits 2-9. The target letters were randomly selected 184 from the English alphabet, excluding I, L, O, Q, U, V and X. The first target (T1) was 185 presented third in the series (serial position 3), and T2 was presented at either lag 2 (200 ms), 3 (300 ms), 5 (500 ms) or 7 (700 ms) relative to T1. All stimuli subtended 1.72 x 2.31° (w x h) visual angle. Participants were instructed to make an unspeeded report of the identity of both targets at the end of each trial. Participants completed 24 practice trials 189 and four test blocks of 24 trials. For the current analysis we calculated T2 accuracy, given 190 that T1 was correctly reported (T2|T1), for each lag. 191

Multitasking (MT). MT paradigms tap the performance costs incurred when individuals attempt to perform more than one task concurrently. Participants are instructed

to complete two simple sensorimotor tasks as accurately and quickly as possible under single or multitask conditions. RTs to the constituent tasks are typically slowed for multitask relative to single task conditions (see Pashler (1994), for a review).

The MT protocol was previously reported in Bender et al (2016). Each Protocol. 197 trial began with a black fixation cross presented in the center of a gray screen [RGB: 128, 198 128, 128 for a variable interval of 200-600 ms. Next either one of two coloured circles [red, 199 RGB: 237, 32, 36 or blue, RGB: 44, 71, 151] or one of two sounds (complex tones taken from 200 Dux, Ivanoff, Asplund, & Marois, (2006)), or both (circle and sound) were presented for 200 201 ms. The coloured circle subtended 1.3° visual angle. Participants were instructed to respond 202 to all tasks as quickly and accurately as possible, by using the appropriate key presses ['A' or 203 'S' for left hand responses, 'J' or 'K' for right hand responses, with the task-hand mapping 204 counterbalanced across participants. The MT protocol consisted of 4 blocks of 36 trials, 205 with each trial type (single-task [ST] visual, ST auditory or MT) randomly mixed within 206 blocks. Participants completed the MT protocols after completing two ST blocks as practice, 207 one for the visual task and one for the auditory task. We analysed mean response times 208 (RTs) to each task x modality condition. 209

Serial Response Task (SRT). The SRT paradigm taps sensorimotor sequence 210 learning; specifically the extent to which individuals speed up responses when cue stimuli 211 follow a predictable sequence, relative to when cue stimuli are presented randomly (Nissen & 212 Bullemer, 1987). As participants receive no explicit instructions or cues regarding the 213 sequence, it has been assumed that the SRT taps implicit sequence learning (Nissen & 214 Bullemer, 1987), although the extent to which performance gains reflect implicit or explicit learning mechanisms continues to be debated (Clegg, DiGirolamo, & Keele, 1998; Goschke, 1998). Participants are instructed to make a button press response to one of four spatially compatible target stimuli as quickly and accurately as possible. Unknown to the participants, 218 the presentation of the target stimuli will on occasions follow a repeating rather than a 219 random sequence. 220

The SRT was adapted from Nissen & Bullemer (1987). Four square 221 placeholders were presented across the horizontal meridian. A red circle [RGB: 255, 0, 0] 222 appeared in one of the 4 squares for 500 ms. This served as the target stimulus. Participants 223 responded by pressing the finger of their dominant hand that spatially aligned to the target 224 circle, using the relevant 'j', 'k', 'l' or ';' keys. The subsequent target stimulus appeared 500 225 ms after a correct response had been made. Participants completed 4 blocks of 100 trials. 226 For blocks 1 and 4, the location of the target stimulus for each trial was randomly selected 227 from a uniform distribution. These blocks are referred to as 'Random'. For blocks 2 and 3, a 228 repeating sequence of 10 elements was used to determine the target location. The sequence 220 was repeated 10 times. The repeating sequence was 4-2-3-1-3-2-4-2-3-1, with 1 being the 230 leftmost placeholder, and 4 being the rightmost placeholder. These blocks are referred to as 231 'Sequence' blocks. Learning in the SRT is tested by comparing mean RTs between Sequence and Repeat blocks in the latter half of the experiment (block 4 vs 3). 233

Contextual Cueing (CC). CC tasks tap how the visual system exploits statistical 234 regularities to guide visual search (Sisk, Remington and Jiang, (2019); Jiang and Sisk 235 (2020)). Participants are typically asked to report the orientation of a rotated 'T' target 236 presented among an array of distractor 'L's. Participants are not informed that a set of the displays are repeated throughout the course of the experiment, while the remaining displays 238 are novel to each trial. Typically RTs to the repeat displays become faster than novel displays throughout the course of the experiment (e.g. Chun & Jiang, 1998; Nydam, Sewell, & Dux, 2018). Participants are typically poor at recognising repeat displays in a subsequent 241 recognition test (Sisk, Remington and Jiang, (2019); Jiang and Sisk (2020)), which has prompted the conclusion that CC reflects a process of implicit learning (but see Vadillo, 243 Konstantinidis, & Shanks, 2016; Vadillo, Linssen, Orgaz, Parsons, & Shanks, 2020; Vadillo, 244 Malejka, Lee, Dienes, & Shanks, 2021). 245

Protocol. The CC protocol was the same as that reported by Nydam et al (2018)
 which is modeled on Chun and Jiang (1998). Each trial began with a white fixation cross

presented on a grey screen [RGB: 80, 80, 80]. An array of 12 L's and a single T were then 248 presented presented within an invisible 15 x 15 grid that subtended 10° x 10° of visual angle. 249 Orientation of each L was determined randomly to be rotated 0°, 90°, 180° or 270° clockwise. 250 The T was oriented to either 90° or 270°. Participants reported whether the T was oriented 251 to the left (using the 'z' key) or the right (using the 'm' key), as quickly and accurately as 252 possible. The task consisted of 12 blocks of 24 trials. For half the trials in each block, the 253 display was taken (without replacement) from 1 of 12 configurations that was uniquely 254 generated for each participant, where the location of the distractors and target (but not the 255 orientation of the target) was fixed. These trials were called 'repeats'. For the remaining 256 trials, the display was randomly generated for each trial, making them 'novel'. Displays were 257 generated with the constraint that equal items be placed in each quadrant and each 258 eccentricity. Target positions were matched between the repeat and novel displays for both quadrant and eccentricity. The exact location of the item was jittered within each cell for each presentation, to prevent perceptual learning or adaptation to the specific position of the 261 item. The order of display type (repeat vs novel), configuration (1:12) and target orientation 262 (left or right) was randomised for each block. Mean RTs to each block (1:12) and display 263 type (repeat vs novel) were taken as the dependent variable.

265 Statistical Approach

All the data and code used for the current analyses are available online. All data were analysed using R (2023) and RStudio (RStudio Team, 2020). The analysis of the data from each task followed two steps; first, to ascertain that we observed the typical findings for each of the paradigms, we applied the relevant conventional statistical model to the full dataset (N=313). Next, we implemented a simulation procedure to determine the effect sizes and p-values that would be attained over many experiments conducted at multiple levels of sample size.

Simulation procedure. For each paradigm, we simulated experiments across 20 273 different sample sizes (N), defined on a logarithmic interval between N_{13} and N_{313} (N = [13,274 15, 18, 21, 25, 30, 36, 42, 50, 59, 69, 82, 97, 115, 136, 160, 189, 224, 265, 313]). We opted for 275 a logarithmic interval given that changes in effect size variability should be greater across 276 changes of N when N is lower, relative to when Ns are higher. To simulate k=1000277 experiments at each of our chosen N, we sampled N participants from N_{max} (N₃₁₃) over k 278 iterations. The relevant analysis was applied to each of the samples. Details regarding which 279 analyses were applied to each k sample are listed below for each paradigm. Sampling with 280 replacement ensured that the samples carried the Markov property. One potential concern is 281 that any reductions in observed effect size variability may be attributable to saturation as 282 the simulated N approaches the maximum (N_{313}) , rather than a genuine reduction in 283 variance of the estimate of the effect. Specifically, it could be that as N approaches 313, the overlap of participants between samples is greater than when N equals a lower number such 285 as 13. It follows then that any decreasing variability in effect size estimates at higher Ns 286 could be due to the decrease in variability of the samples, rather than the improved estimate 287 of the population variance that should come with a larger N. We have run simulations that 288 argue against this explanation (see appendix i). 289

Effect Sizes. For each paradigm, we report the following information from the simulated effect size distributions; first we used simulations using N_{313} to provide a best estimate of the effect size distribution. We therefore report, for each paradigm, the mean (M), median (Mdn): when different to the M, standard deviation (SD), the .025 (lower bound, (LB)) and .975 (upper bound, (LB)) quantiles. These values can be used to define, (LB)) (LB) (LB) (LB)0 and .975 (upper bound, (LB)0 quantiles. These values can be used to define, (LB)1 used to inform study design.

We next determined to what extent using an N that is typical for the field impacts the effect size distribution. We report the same summary statistics as above, from the simulation using the N that is closest to the typical N for that task (N_{med}) . To identify the typical N,

we conducted a survey of the recent literature and computed the median N for each paradigm (see below). We next computed the *precision loss* incurred from using N_{med} by taking the ratio of the difference between the LB and UB quantiles for N_{med} and N_{313} :

$$qq\text{-}ratio = \frac{UB_{N_{med}} - LB_{N_{med}}}{UB_{N_{313}} - LB_{N_{313}}}$$

We refer to this measure from now as the qq-ratio. The qq-ratio indicates how under-303 or over-inflated effect size estimates may be - a qq-ratio of 2 would suggest that effect sizes 304 may be twice as low or high as the LB or UB of the best estimate. For each task, we also 305 report the largest observed qq-ratio and the N for which the qq-ratio reaches less than 306 double. Note that although we expect qq-ratios to decrease as some function of $\frac{1}{N}$ (given 307 that variance depends on this term), the exact relationship between N and precision loss will 308 be dependent on population variance and measurement error for any given paradigm. We 309 also present qq-ratios across all N's, to provide an idea of potential precision gains from 310 increasing sample size. 311

Next we computed estimates regarding the extent to which precision loss in effect size 312 estimates may lead a researcher awry during study planning. To determine how often 313 sampling one or two similar studies with N_{med} may induce biases in power calculations, we 314 computed for each task and N, the proportion of simulated observations that fell within the 315 LB and UB quantiles of the best estimate (N_{313}) . This provides the probability that 316 sampling one study will provide an accurate estimate of the true effect size. We refer to this 317 as the probability of attaining a hit, given the sample size $(p(hit|N_x))$. (As above, although 318 we expect this to change as a function of $\frac{1}{N}$, the exact relationship is dependent on measurement noise). We next estimate effect size biases that result from aggregating across 320 experiments with statistically significant results (p<.05), under the assumption that the 321 published literature is more likely to only contain significant findings. We computed the 322 difference between the mean effect size from significant results and the mean effect size from 323

all results, and refer to this value as the *inflation bias*. Effectively, this analysis is assessing
the severity of the file-drawer effect for different sizes of N. To inform understanding of
potential file-drawer effects, we also report the proportion of studies that rejected the null
hypothesis (p < .05) for N_{med} , and the N where this value reached 90% (note: this is related
to the observed effect size, but we report it here for clarity).

Last, we sought metrics that may inform whether an experiment has yielded an imprecise effect size estimate. Effect sizes are a function of the variability of the effect across individuals, as well as intra-individual variability over trials (Rouder & Haaf, 2018). If either of these stem from a non-normal distribution, mean and standard deviation estimates - and consequently effect size computations - may be impacted. We thus determined whether the skewness and kurtosis of this data could predict error in effect size estimates.

Error in effect sizes were defined for each task as the difference between the expected 335 value for N_{313} and each observed effect size from N_{med} . To attain predictors for each N_{med} 336 simulation, we calculated the key behavioural effect for each participant (in raw units) and 337 computed the Pearson's skewness and kurtosis coefficients of the resulting distribution of 338 effects. We also computed the variability, skew and kurtosis from each participant's 339 performance across trials, and took the means of these measures across participants. The resulting variables (effect skewness, effect kurtosis, mean intra-individual variance, skewness, and kurtosis) served as predictors in a multiple regression analysis, using effect size error as the criterion variable. If any of the regressors themselves showed high levels of skew then a log transformation was applied. All model residuals were checked for homoscedasticity. Note that although we present the full models below, performing stepwise regression yielded the 345 same pattern of results. 346

To protect against interpreting over-fitted models, we performed k-fold cross-validation for each multiple regression model, where k=10, and we report the mean r_{cv}^2 (and standard deviation) across folds. Next, we determined which regressors consistently predicted effect size error across the four tasks. We then sought to identify which values of such predictors suggest a problematic effect size error (defined as effect size errors that were less or more than the .025 and .975 quantiles for N_{313}). We achieved this using simple regression, as we sought to simulate how much variability may be accounted for when a researcher uses a single piece of information to estimate effect size imprecision.

Computing Effect Sizes. To compute effect sizes for the paradigms analysed using a repeated-measures ANOVA (AB, MT and CC), we computed partial epsilon squared (ϵ_p^2) , as this measure is unbiased, unlike η_p^2 (Okada, 2013). (Indeed, an earlier version of our manuscript showed that η_p^2 estimates are biased on average, even for sample sizes of N=313, 359 1). We use the formula for ϵ_p^2 as defined in (Carroll & Nordholm, 1975, eq 11):

$$\epsilon_p^2 = \frac{F - 1}{F + \frac{df_w}{df_b}} \tag{1}$$

where F is the F statistic for the effect, df_w is the degrees of freedom within groups, and df_b is the degrees of freedom between groups. The SRT paradigm instead uses a paired-samples design. For this paradigm we computed Cohen's d_z (see Lakens (2013), eq 6):

$$d_z = \frac{M_{\text{diff}}}{\sqrt{\frac{\sum (X_{\text{diff}} - M_{\text{diff}})^2}{N - 1}}}$$
 (2)

where M_{diff} is the mean difference between groups, and X_{diff} is the difference score for one subject.

To facilitate our interpretation of effect sizes as small, medium or large, we refer to Cohen (1992) for ϵ_p^2 and to Gignac & Szodorai, (2016) for d_z .

¹ See for Supplemental Figures documenting this analysis: https://github.com/kel-github/Super-Effects/tree/master/doc/supp-figs. Note: we thank a helpful reviewer for drawing our attention to this

Representative N. To attain an N that reflects what is commonly used for each paradigm, we surveyed the three most relevant Journal of Experimental Psychology journals (General, Human Perception & Performance and Learning, Memory & Cognition) for all articles mentioning use of any of the current paradigms. We searched back for a total of 60 experiments or back from today to 2005, whichever occurred first. We then computed the median sample size used across all experiments found from the survey. The results from the survey are presented in Table 1.

Analysis of Experimental Tasks.

374

Attentional Blink. As is typical for the field, and to ascertain the effectiveness of 375 the lag manipulation, T2|T1 accuracy was subject to a repeated measures ANOVA, with lag 376 (2, 3, 5, & 7) as the independent variable. This analysis was also applied to each k sample. 377 For each k sample, ϵ_p^2 and the resulting p value were taken for the main effect of lag. For this 378 task, and all remaining ANOVA tests, models were fit using the anova test() function from 379 the rstatix package. Where possible, the models were fit using type 3 sum of squares, owing 380 to the computational expediency and match to commercial statistical software packages. In 381 some cases, models were unable to be fit using type 3 sum of squares, owing to rank 382 deficiencies in the underlying design matrix (e.g. when one participant was drawn more than 383 twice within a sample). In these cases, models were fit using type 1 sum of squares. However, 384 as the experiment designs were fully balanced, each sum of squares type should yield the 385 same results. 386

Multitasking. To ascertain the effectiveness of the multitasking manipulation, the data were modelled using a 2 (task-modality: visual-manual vs auditory-manual) x 2 (task: ST vs MT) repeated-measures ANOVA. This analysis was also applied to each k sample; ϵ_p^2 and p are reported for both the main effect of task and the task-modality x task interaction.

Serial Response Task. To ascertain whether participants learned the repeating sequences, RTs in the final block of sequence trials (block 3) were compared to those in the

final block of random trials (block 4) using a paired-samples t-test. This analysis was also applied to each k sample, and we present the resulting Cohen's d_z , and p value from each test.

Contextual Cueing. To ascertain whether participants became faster for repeat relative to novel trials over the course of the experiment (i.e. whether participants learned the statistical regularities of the repeated displays), the data were subject to a block (1:12) x condition (repeat vs novel display) repeated measures ANOVA. Specifically, learning should be evidenced by a significant block x condition interaction. This analysis was applied to each k sample, and we report ϵ_p^2 and p for the block x condition interaction.

As some studies from the contextual cueing literature suggest that the effect is better characterised by a main effect of condition thereby implying rapid learning of the statistical regularities (e.g. Peterson & Kramer, 2001; Travis, Mattingley, & Dux, 2013), we also report the ϵ_p^2 and p for the main effect of condition.

406 Results

We first present the results from the standard analyses used for each task, to show that
we replicate the classic findings from each task. The key behavioural data are presented in
Figure 2.

410 Behavioural Results

Attentional Blink. The AB data are presented in Figure 2A. Accuracy for T2|T1 was lower for early relative to late lags; accuracy for T2|T1 decreased (by around p = 0.32) when T2 was presented at lag 2, relative to lag 7. A one-way ANOVA revealed that the effect of lag was statistically significant (F (2.4, 749) = 508, $\epsilon_p^2 = 0.62$, p = 1.88e-157). Post-hoc t-tests showed that accuracy at each lag differed statistically from accuracy at each

of the other lags (all p's \leq 3.68e-18). Therefore, the AB paradigm yielded the typically observed effects.

As anticipated, RTs were slowed for multitask relative to single task Multitasking. 418 conditions (see Figure 2B). Mean RTs were on average 0.31 (95\% CI[0.30, 0.33]) seconds (s) 419 slower on MT trials (F(1, 312) = 2653, $\epsilon_p^2 = 0.89$, p<.0001). There was also a significant 420 task modality (sound or visual) x task (ST vs MT) interaction (F(1, 312) = 59.4, ϵ_p^2 = 0.16, 421 p<.0001). The MT cost (MT RT - ST RT) was larger for the sound task relative to the 422 visual task by on average 0.08 s (95\% CI[0.06, 0.10]). This latter finding has been reported 423 previously (Hazeltine & Ruthruff, 2006). We continue to interrogate this effect, as it serves 424 as an example of an interaction with a small effect size. This facilitates comparisons to the 425 contextual cueing task, as reported below. 426

SRT. The results from the SRT paradigm are presented in Figure 2C. Participants learned the repeating sequence; RTs were on average 0.049 s faster (95% CI [0.046, 0.051]) for the sequence relative to the random condition (t(312) = 33.60, $d_z = 1.90$, p = 1.13e-105).

Contextual Cueing. Participants learned the repeat displays over blocks (see Figure 2D); the RT data showed a significant albeit small block x condition interaction (F (10.12, 3158.9) = 4.80, $\epsilon_p^2 = 0.01$, p = 6.01e-07). There was no statistically significant difference between RTs for repeat and novel displays for block 1: (t (312) = 0.53, p = 0.60, μ difference = 0.01 s, sd: 0.20). However, by block 12, RTs for repeat displays were on average 0.04 s faster than novel displays (sd: 0.14, t (312) = 5.33, p = 1.87e-07. There was also a significant and larger main effect of block (F(5.03, 1567.97) = 131.08, $\epsilon_p^2 = 0.29$, p = 1.07e-116). and a significant main effect of condition (F(1.00, 312.00) = 32.78, $\epsilon_p^2 = 0.09$, p = 2.42e-08).

88 Effect Sizes

Summary Statistics and Precision Loss. Across tasks, we observed a range of small to large effect sizes $(epsilon_p^2: .01 - .9)$, thus we are able to characterize the extent of

precision loss across a range of effect size scenarios. For studies run with N_{med} , the range of 441 precision losses we observed was 1.78 - 4.16, suggesting that caution is warranted when 442 basing power calculations on the outcomes of a small number of studies. The N required to 443 reduce precision loss to < 2 ranged from 36 - 82. For both the interaction effects currently 444 studied (MT and CC), the effect size distributions for N_{med} spanned from below to above 445 zero, suggesting that differing conclusions may be reached across studies. Specifically, when 446 the effect size is less than zero, the direction of the effect has the opposite sign. The observed 447 power to reject the null hypothesis ranged from p=.35 - 1, suggesting areas where there may be missing literature owing to publication bias. We next report these details for each task. 449

Attentional Blink. The AB effect was large (see Figure 3A); $N_{313} \epsilon_p^2 M = 0.62$ (SD: 0.03, LB: 0.57, UB: 0.67). The simulated effect sizes for N_{med} (N_{25}) produced the same mean effect size estimate (M: 0.62, SD: 0.06, LB: 0.48, UB: 0.74, see Figure 3B). With regard to extent of precision loss; the qq-ratio for N_{med} was 2.38. The qq-ratio for small N was ~ 3 ($N_{13} = 3.06, N_{15} = 2.98$), and reached < 2 at N_{42} ($N_{36} = 2.09, N_{42} = 1.81$). The remaining qq-ratios are presented in Figure 5.

Across all N, the probability of rejecting the null hypothesis was 1.

Multitasking.

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Main effect of task condition. For the MT paradigm, the main effect of task condition was large $(N_{313} \epsilon_p^2 M = 0.90, SD: 0.01, LB: 0.87, UB: 0.92)$, and the simulated effect sizes for N_{med} (N_{42}) produced the same mean effect size estimate (M: 0.90, SD: 0.03, LB: 0.84, UB: 0.94, see Figure 3D). With regard to precision loss, the qq-ratio for N_{med} was 1.89.

Comparable to the AB, qq-ratio for small N was ~ 3 $(N_{13} = 2.97, N_{15} = 3.03)$, and was < 2 for N_{36} $(N_{30} = 2.12, N_{36} = 1.96)$. The remaining qq-ratios are presented in Figure 5.

Across all N, the probability of rejecting the null hypothesis was 1.

Task condition by modality interaction. The task condition x modality interaction achieved a medium effect size $(N_{313} \epsilon_p^2 M = 0.17, SD: 0.06, LB: 0.06, UB: 0.30,$ see Figure

3E), and the simulated effect sizes for N_{med} produced the same mean effect size estimate (M: 0.17, Mdn: 0.16, SD: 0.12). However, the LB and UB quantiles from N_{med} crossed zero (LB: -0.02, UB: 0.43, see Figure 3F), suggesting that using N_{med} will sometimes produce differing inferences with regard to the effect size, compared to N_{313} . With regard to precision loss, the qq-ratio for N_{med} was 1.78. The qq-ratio for small N was ~2.75 ($N_{13} = 2.88$, $N_{15} = 2.72$), and reached < 2 at N_{36} ($N_{30} = 2.00$, $N_{36} = 1.87$). The remaining qq-ratios are presented in Figure 5.

The probability of rejecting the null hypothesis at N_{med} was 0.79. A sample size of N_{82} was required to achieve statistical power of > 90 % ($N_{69} p = 0.90$, $N_{82} p = 0.95$).

Serial Response Task. For the SRT, the effect of sequence vs random was large (N_{313} d_z M: 1.93, SD: 0.21, LB: 1.53, UB: 2.33, Figure 4A). Here, there was disagreement between N_{313} and N_{med} (N_{36}) regarding the means of the simulated effect size distributions (N_{med} d_z M = 2.02, SD: 0.44, LB: 1.22, UB: 2.86, see Figure 4B). With regard to precision loss, the qq-ratio for N_{med} was 2.05. The remaining qq-ratios are presented in Figure 5. The qq-ratio for small N was ~3.5 (N_{13} = 3.62, N_{15} = 3.35), and reached under 2 at N_{42} (N_{36} = 2.05, N_{42} = 1.88).

Across all sampled N, the probability of rejecting the null hypothesis was 1.

Contextual Cueing.

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Block x Condition Interaction. The block x condition interaction effect was on the boundary between very small and small $(N_{313} \epsilon_p^2 M: 0.02, SD: 0.01, LB: 0.01, UB: 0.04,$ Figure 4C). There was a minor discrepancy between the N_{313} and N_{med} (N_{25}) means, but the N_{med} Mdn agreed (M: 0.03, Mdn: 0.02, SD: 0.03). Similar to the SRT task, the effect size distribution for N_{med} included zero $(N_{med} LB: -0.02, UB: 0.11)$, thus experiments with N_{med} may sometimes motivate different conclusions to N_{313} . Specifically, when the effect size is below zero, it would be concluded that repeating displays leads to a slowing of RTs (rather than speeding RTs), relative to novel displays. There was also a greater extent of precision

loss at N_{med} than was observed for other tasks (qq-ratio: 4.16). The qq-ratio for small N was ~6 ($N_{13} = 6.41$, $N_{15} = 5.64$), and reached under 2 at N_{82} ($N_{69} = 2.08$, $N_{82} = 1.84$). The remaining qq-ratios are presented in Figure 5.

The probability of rejecting the null hypothesis at N_{med} was p=0.35. A sample size of N_{82} was required to achieve statistical power of > 90 % (N_{69} p=0.90, N_{82} p=0.95).

Main Effect of Condition. The main effect of condition was large $(N_{313} \epsilon_p^2 M: 0.31, SD: 0.03, LB: 0.25, UB: 0.37,$ see Figure 4E). There was a minor discrepancy between the mean estimates for N_{313} and N_{med} (M: 0.33, Mdn: 0.32, SD: 0.08, LB: 0.20, UB: 0.47, see Figure 4F). Precision loss was comparable to the SRT (qq-ratio: 2.19). The qq-ratio for small N was ~2.8 $(N_{13} = 2.82, N_{15} = 2.75)$, and reached under 2 at N_{36} $(N_{30} = 2.19, N_{36} = 1.97)$. The remaining qq-ratios are presented in Figure 5.

The probability of rejecting the null hypothesis at N_{med} was p=0.39. A sample size of N_{136} was required to achieve statistical power of > 90 % (N_{115} p=0.97, N_{136} p=0.99).

Impacts of imprecision and missing literature. Having characterized the effect 506 size distributions for each task, we next sought to determine the impact of effect size 507 imprecision when basing power calculations on a similar study that uses N_{med} , and the 508 extent to which effect size estimates could be inflated in cases where there may be missing 509 information owing to publication bias. For the former, we computed p(hit|N); for the AB, 510 MT and SRT paradigms, the p(hit N_{med}) was ~0.66 (AB: 0.65, MT tc: 0.67, MT tc x m: 511 0.67, SRT: 0.65). This suggests that sampling a similar study will produce a reasonable a 512 priori effect size estimate 2/3 of the time (Note: it is interesting that the AB, MT and SRT fields appear to have converged on an N_{med} that puts them on a comparable footing for hitting the best effect size. Indeed, if the MT and SRT fields used the same sample size as 515 the AB field, the p(hit N_{25}) ratios for the three effects would be ~0.57 (MT tc: 0.59, MT tc x 516 m: 0.54, SRT: 0.57)). For the CC paradigm, the p(hit| $N_{med} = \sim .48$ (b x c: 0.40, c: 0.55). 517 This suggests that basing effect size estimates on a similar CC study will result in an 518

appropriately powered study 50% of the time. The remaining p(hit| N_x) are presented in Figure 6.

Next, we estimate the *inflation bias* that is incurred by using a given N. Here we focus on the MT and CC paradigms, as they contained effects where the null was not consistently rejected at N_{med} . For the MT task, the task condition x modality inflation bias for N_{med} was 0.04 ϵ_p^2 . No inflation bias was present for the main effect of task condition (all N=0). For the CC, the block x condition interaction inflation bias at N_{med} was 0.03 ϵ_p^2 , for the main effect of condition the N_{med} inflation bias was nominal (-0.003 ϵ_p^2). These and the remaining inflation bias estimates are presented in Figure 7.

Predicting error in effect size estimates. Last, we determined which aspects of 528 the data were predictive of erroneous effect size estimates. Multiple-regression analysis 520 showed that between ~9-40\% of the variance in effect size errors were predicted by effect 530 skewness, effect kurtosis, mean intra-individual variance, mean intra-individual skewness, 531 and mean intra-individual kurtosis (M r_{cv}^2 s (SD): AB: 0.39 (0.08), MT main effect of task: 532 0.09, (0.05), MT task x modality interaction: 0.11 (0.04), SRT: 0.22 (0.09), CC main effect 533 of condition: 0.19 (0.08), all model ps < .001), apart from for the block x condition effect 534 from the CC task, where the model accounted for a negligible proportion (~1%) of effect size 535 error (F(5,994) = 2.35, p = .04). This suggests that both inter- and intra-individual 536 skewness and kurtosis predict variability in effect size errors.

The resulting regression equations (see appendix ii) are useful for researchers using the
tasks studied here, who wish to predict the extent to which their own experiment may have
yielded an imprecise effect size estimate. However, what is more widely useful is
understanding which regressors significantly predict effect size imprecision across tasks. We
therefore determined which regressors showed significant predictive power across tasks,
applying Bonferronni correction for multiple comparisons. For the AB, MT, and SRT tasks,
effect skewness and kurtosis were significant predictors of effect size error (all ps <= .005,
see appendix ii). Mean intra-individual skew was a significant predictor across all four tasks

(all ps < .008), apart from for the MT task x condition interaction (p=.08).

Having identified the regressors that suggest imprecision in effect size estimates across 547 tasks, we next sought to determine which predictors could be used as a marker of 548 imprecision when a researcher is unable to hold the influence of other predictors constant. 549 Such a finding would suggest that use of a single piece of information (e.g. effect skewness) 550 could act as a marker for whether a single experiment has yielded an imprecise effect size 551 estimate. Simple regressions between each predictor and effect size errors showed that effect 552 skewness tended to predict a higher proportion of the variance (Adjusted R^2 s: 0.04 - 0.10, all 553 ps < .001) than kurtosis (Adjusted R^2 : -0.00 - 0.01, all ps < .7), apart from for the MT 554 condition x task interaction (skewness: Adjusted R^2 : 0.0004, p<.01, kurtosis: Adjusted R^2 : 555 0.06, p<.001). Although mean within-participant skewness predicted higher amounts of error 556 variance for the AB (Adjusted R^2 : 0.18) and CC main effect of condition (Adjusted R^2 : 557 0.16), its predictive power was poor for the remaining tasks (Adjusted R^2 s: \leq .02, all ps \leq 558 .17). This suggests that effect skewness is the best potential general proxy of effect size 559 imprecision, when not controlling for other influences.

As effect skewness is the best candidate for predicting variance in effect size error across tasks, we next determined which values of effect skewness predict problematic levels of effect size error (defined as values falling outside the .025 and .075 quantiles for N_{313}).

Across tasks, moderate to large negative effect skewness (-0.70 - -1.29) predicted erroneous over-estimates of effect size, whereas large positive effect skewness (1.35 - 3.80) predicted erroneous under-estimates. Thus, if data from a single experiment shows moderate to large values of effect skewness, this is a signal that extra caution is warranted when interpreting effect size estimates.

569 Discussion

We simulated 1000 bootstrapped experiments across 20 Ns ranging from 13 to 313. 570 For each paradigm and from each set of simulations, we determined the impact of N on error 571 in effect size estimates. In doing so, we were able to quantify a range of effect sizes that 572 researchers can consider when performing power analyses, particularly when using the AB, 573 MT, SRT or CC paradigms. We determined precision loss in effect size estimates as a 574 function of N and found that decreasing N_{max} to N_{med} inflated the range of effect sizes by 575 factors ranging between 1.78-4.16. We also computed the probability of attaining an accurate 576 effect size estimate (defined as falling between the .025 and .975 quantiles of N_{max}), and 577 found that sampling a single study would result in a reasonable estimate on between 40-67% 578 of samples. Last we computed the inflation bias for effects that carried less than 90% power 579 at N_{med} . We found that inflation biases ranged from a nominal to small effect (ϵ_p^2 : -.003-.03). 580 These findings can inform study planning, study interpretation and theory development. 581

Study Planning. Our findings have practical relevance for study planning. First, we 582 have provided a range of effect sizes that researchers can use to inform power calculations for 583 their own studies. Furthermore, we have shown that in the case of smaller effects (ϵ_p^2) 584 0.01-0.3), N_{med} was consistently smaller than is required to attain 90% power to reject the 585 null hypothesis. This suggests that researchers should consider whether their research 586 question concerns an effect that may be subtle or variable across participants, and if so, 587 recruit higher Ns than is currently standard. This would promote maintenance of 588 appropriate type 2 error rates. For the small effects observed here, a minimum N of 69 participants was required. Note also that for each task, the statistical model used was one geared at ascertaining the existence of an effect (e.g. was there an AB present?). These 591 findings suggest that as soon as hypotheses become more nuanced, for example, referring to 592 factors that should modulate the strength of a known effect, effect sizes are likely to be of a 593 smaller range. 594

The current findings also reveal that sampling a few similar studies to determine a 595 suitable minimum effect size for power analysis is a questionable approach, given the 596 standard N_{med} s. For larger effects, this will lead to an inappropriately powered study ~33% 597 of the time, whereas this rate will be $\sim 50\%$ for smaller effects. Furthermore, the current 598 inflation bias data suggest that in the case of interactions, (and smaller effects), a 590 comprehensive meta-analysis is likely to yield an inflated estimate when the field uses $< N_{69}$ 600 as standard. Therefore, researchers using existing research to determine appropriate effect 601 sizes for power analyses would be well advised to adjust (decrease) anticipated minimum 602 effect sizes to ensure they avoid an underpowered study. However, given the suggested 603 currently indicated state of the field, the better approach is for researchers to use 604 theoretically motivated minimum effect size estimates, that include consideration for how 605 likely the effect is to vary across individuals, when conducting power calculations.

These findings complement the insights offered by previous simulation studies into the 607 factors influencing effect size estimates. Previous simulation work has highlighted conditions 608 that cause bias in effect size estimates (Gelman & Carlin, 2014; e.g. Lane & Dunlap, 1978; 609 Okada, 2013; Troncoso Skidmore & Thompson, 2013) and the consequences for power 610 calculations (Albers & Lakens, 2018; Anderson, Kelley, & Maxwell, 2017), by generating 611 data-sets under simplifying conditions such as using between subjects designs or using lower 612 and fewer samples of N. Collectively, these studies have determined which effect size 613 measures provide unbiased estimates (e.g. ϵ_p^2 vs η_p^2), that effect size estimates are likely to be 614 inflated due to publication bias and low statistical power, and that the process of study 615 design should account for uncertainty in the magnitude and direction of anticipated effect sizes. However, it can be challenging to determine the uncertainty around effect size estimates and the impact of differing N on that uncertainty without quantifications of the 618 expected effect size, and the variability around that effect size, for a given field of study. By 619 taking the current step away from simplifying data generating conditions, and instead 620 simulating experiments based on data from specific paradigms with more complex designs, 621

we provide insight into the uncertainty regarding effect size estimates for ecologically valid data taken from the AB, MT, SRT and CC paradigms.

We also show that for the larger effect sizes studied here (ϵ_p^2 : 0.6-0.9, $d \sim 1.9$), effect 624 skewness, which is driven by inter-participant variability, shows a predictive relationship 625 with imprecision in effect size estimates. This was not the case for the smallest effects under 626 study (ϵ_p^2 : 0.02-0.31), where intra-individual skewness and kurtosis of the data were the 627 significant predictors of imprecision. Thus, researchers wishing to determine the likelihood of 628 an erroneous estimate in their own data should examine different features of the data (inter-629 vs intra-individual skewness) according to the expected effect size. This finding also carries 630 potential consequences for the trade-off between N and repeated measures (number of trials) 631 that must be decided for any given study. Specifically, when an effect size is small across 632 participants, intra-individual variability is the limiting factor for precisely quantifying an 633 effect. This accords with previous observations concerning the reduction of type 2 errors 634 (Rouder & Haaf, 2018). What the current findings suggest is that decision processes 635 regarding the trade-off between N and repeated measures should also consider the number of 636 each required to attain a relatively normal distribution of effects, for either inter- or 637 intra-individual data, depending on whether the anticipated effect size is large or small respectively. Future work should use simulation approaches to verify the causal link between skewness and error in effect size estimates. 640

Study Interpretation. Our findings also offer insight into the interpretation of
existing studies using the AB, MT, SRT and CC paradigms. Researchers evaluating existing
studies can use the current findings to estimate the potential imprecision of a given effect
size, and can accordingly weight their belief in consequent theoretical assertions. The current
findings also enable (largely positive) evaluations of the broader literature for each paradigm.
Statistical power was largely very strong, apart from for interactions, which involved small or
medium effects. This suggests that the published literature will likely cumulatively reflect a
reasonable effect size estimate, across all N, when the effect under study is a main effect.

However, for interaction effects (for which we only saw very small to medium effect sizes $[\epsilon_p^2]$ 649 .02-.17), we consistently found that ~82 participants were required to achieve > 90\% power, 650 which was far above the N_{med} for each paradigm. It follows that interactions would be 651 relatively under-powered since data is being divided into more bins, and this accords with 652 other observations that current practices result in low statistical power for interaction effects 653 (e.g. Lakens & Caldwell, 2021). However, our survey of the field suggests that investigation 654 of interaction effects with low N remains common practice when measuring attention. 655 executive function and implicit learning. The current findings demonstrate that cumulative 656 approaches would be hampered by current practices in characterizing interaction effects (at 657 least in the case of MT and CC). 658

We believe these findings offer new insights when considering what constitutes a well 659 powered study for investigations into attention, executive function and implicit learning. The 660 current findings show that achieving statistical power to reject the null hypothesis is either 661 trivially easy, or, in the case of very small effects (as we observed for CC b x c), is inevitable 662 with sufficient N. Therefore, demonstrating rejection of the null hypothesis has relatively 663 little to offer if the goal is to develop theory and leverage insights from cumulative science 664 (Chen et al., 2019; Cumming, 2014; Gelman & Carlin, 2014; Lorca-Puls et al., 2018). Here 665 we show that if a given field can pool data, or collectively provide the appropriate simulation parameters, then it is possible to plan research studies with the aim of producing an effect 667 size estimate that has an acceptable level of precision. Here we defined an acceptable level of 668 precision as falling within the .025 and .975 quantiles of the distribution of the best estimate(N_{313}). The usefulness of our definition could potentially be limited to the current sample and task materials. It would be useful to conduct multiple large N studies aimed at characterising effect size distributions across multiple cognitive phenomena. This would not 672 only inform tolerable precision levels, but could also help with theory development. For 673 example, we would better understand the effect magnitude that candidate models should 674 emulate. Further, there would exist more baseline effect magnitudes that could serve as a 675

reference, or upper limit, when hypothesising factors that modulate the effect.

Just as knowing about the distributional properties of effect sizes observed across many 677 replications provides information about study design and interpretation, so too can 678 considering the distributional qualities of observed p-values. The p-value is itself a random 679 variable that will vary from experiment to experiment (e.g. Chen et al., 2019), yet this 680 variation is rarely considered when researchers report a single p-value for each reported effect. 681 Understanding exactly how a p-value may vary across replications can help identify where 682 there may be missing literature owing to publication bias, or uncertainty regarding the 683 rejection of the null hypothesis (e.g. Nolan, Vromen, Cheung, & Baumann, 2018). Moreover, although it is known that p-values are inversely related to effect size, the relationship is both 685 non-linear and non-trivial to compute as it depends on other factors such as the sample size, the underlying data type (e.g. independent vs dependent) and the statistical test (Faul, Erdfelder, Lang, & Buchner, 2007). The current simulation approach could also be employed to better map the relationship between N and p-values, for varying effects. This can yield 689 insights into uncertainty over p-values and assist with interpretation of research findings. We 690 provide the p-value data from the current simulations as Supplemental figures ² to help with 691 this endeavour. 692

Theory Development. The current simulation approach can also inform theory 693 development. In the case of implicit learning, our results showed that for the CC paradigm, 694 the block x condition interaction effect was very small (ϵ_p^2 : .01-.04). This may be because the 695 effect is very small across all variations of the paradigm, or that the current design 696 parameters may not effectively measure the effect. The current paradigm was modeled on 697 the seminal demonstration (Chun & Jiang, 1998). Nonetheless, there may be critical design 698 parameters that with modification, elicit a larger (and more positive) range of interaction 699 effects. Applying the current simulation approach to data collected across varying 700

² See https://github.com/kel-github/Super-Effects/tree/master/doc/supp-figs

implementations of the CC paradigm can yield insights into what produces the effect, and consequently can help refine theory regarding the causes of the effect.

The current approach of using a large data-set also offers insight into the impact of 703 increasing individual variation while holding measurement error relatively constant, for each 704 paradigm under study here. Hopefully, at N_{313} the contribution of individual variation is 705 relatively low compared to the measurement error. Given this, the currently observed 706 comparable rates of change for the qq-ratio and p(hit|N) values across paradigms may be 707 unsurprising. This consistency may be of some value when quantifying the impact of 708 individual variation on predicted effect magnitudes. Furthermore, the range of effect sizes 709 observed for experiments at N_{313} provides an estimate of measurement error that could be 710 built into quantitative predictions for the AB, MT, SRT and CC effects. 711

Limitations. It remains an open question whether the current findings generalize 712 beyond the paradigms and participant pool used here. There are some suggestions of 713 generalizability of the current observations across tasks that should be investigated in future 714 research. Across all the ϵ_p^2 findings, the standard deviations at N_{313} were small (SDs: 715 .01-.03), and each SD doubled or tripled as a function of moving from N_{313} to N_{med} . 716 Therefore, it is possible that effect sizes such as ϵ_p^2 will show a comparable reduction in 717 variability as N increases to the hundreds, across all paradigms. If this were found to be 718 true, then researchers could apply the rates of change observed here to effect size estimates 719 from their own field of study in order to determine the N required to achieve a tolerable level 720 of precision. Moreover, changes in p(hit N) and qq-ratio rates were comparable across N for 721 all effects, regardless of size, suggesting invariance to the measurement differences across paradigms. Future research should determine the extent to which these rates were dependent 723 upon the current sample of N_{313} , which was arguably homogeneous with regard to 724 population characteristics. Indeed, it is pertinent to determine the extent to which our 725 results would hold with more heterogeneous samples. For example, estimates of effect sizes 726 may be more variable under less constrained conditions, such as when community samples 727

complete online studies. Future work should determine the extent to which study design choices may hamper precise effect size estimates in such groups.

A further limitation is that the p(hit|N) and qq-ratio values were dependent on the range of effect sizes observed at N_{313} . The results may be different if we had sampled N_{1000} (for example). Thus interpretation of the current findings is dependent on how willing the researcher is to assume that several hundred participants is a sufficient representation of 'as good as it gets'. Given the small ranges of effect sizes observed for N_{313} , we certainly think this is a reasonable place to start.

736 Conclusions

By simulating experiments across varying N for popular paradigms from the study of 737 attention, executive function and implicit learning, we are able to provide insights into the 738 precision of effect size estimates that are unknowable from simulation approaches that make 739 simplifying assumptions regarding the data. Using the current approach, we can identify the 740 mean effect size and the variability of that effect size, under the best case scenario. This 741 allows us to quantify the change in precision of effect size estimates with varying N. We 742 identify that using a typical N can double imprecision of effect size estimates, and 743 characterize to what extent this reduces the chances that a single study will provide a 744 reasonable effect size estimate. In the case of the small effect sizes observed here, inflation 745 bias can amount to the equivalent of a small effect size. Amassing large data-sets to allow characterisation of error in effect size estimates is a useful exercise when seeking to plan 747 studies that facilitate cumulative science.

References

- Albers, C., & Lakens, D. (2018). When power analyses based on pilot data are biased:
- Inaccurate effect size estimators and follow-up bias. Journal of Experimental Social
- Psychology, 74, 187–195. https://doi.org/10.1016/j.jesp.2017.09.004
- Anderson, S. F., Kelley, K., & Maxwell, S. E. (2017). Sample-Size Planning for More
- Accurate Statistical Power: A Method Adjusting Sample Effect Sizes for Publication Bias
- and Uncertainty. Psychological Science, 28(11), 1547–1562.
- https://doi.org/10.1177/0956797617723724
- ⁷⁵⁷ Bender, A. D., Filmer, H. L., Garner, K. G., Naughtin, C. K., & Dux, P. E. (2016). On the
- relationship between response selection and response inhibition: An individual differences
- approach. Attention, Perception & Psychophysics, 78(8), 2420–2432.
- 760 https://doi.org/10.3758/s13414-016-1158-8
- Brainard, D. H. (1997). The Psychophysics Toolbox. Spatial Vision, 10(4), 433–436.
- https://doi.org/10.1163/156856897X00357
- Brand, A., Bradley, M. T., Best, L. A., & Stoica, G. (2008). Accuracy of Effect Size
- Estimates from Published Psychological Research. Perceptual and Motor Skills, 106(2),
- 765 645-649. https://doi.org/10.2466/pms.106.2.645-649
- Carroll, R. M., & Nordholm, L. A. (1975). Sampling Characteristics of Kelley's ϵ and Hays'
- ω . Educational and Psychological Measurement, 35(3), 541–554.
- 768 https://doi.org/10.1177/001316447503500304
- Chen, G., Xiao, Y., Taylor, P. A., Rajendra, J. K., Riggins, T., Geng, F., ... Cox, R. W.
- 770 (2019). Handling Multiplicity in Neuroimaging through Bayesian Lenses with Multilevel
- Modeling. Neuroinformatics, 17(4), 515–545. https://doi.org/10.1007/s12021-018-9409-6
- Chun, M. M., & Jiang, Y. (1998). Contextual cueing: Implicit learning and memory of
- visual context guides spatial attention. Cognitive Psychology, 36(1), 28–71.
- https://doi.org/10.1006/cogp.1998.0681
- Clegg, B. A., DiGirolamo, G. J., & Keele, S. W. (1998). Sequence learning. Trends in

- 776 Cognitive Sciences, 2(8), 275–281. https://doi.org/10.1016/S1364-6613(98)01202-9
- Cohen, J. (1988). Statistical power analysis for the behavioral sciences. Hillsdale, NJ:
- Lawrence Erlbaum.
- Cohen, Jacob. (1992). A power primer. Psychological Bulletin, 112, 155–159.
- 780 https://doi.org/10.1037/0033-2909.112.1.155
- Cumming, G. (2014). The New Statistics: Why and How. Psychological Science, 25(1), 7–29.
- https://doi.org/10.1177/0956797613504966
- Dux, P. E., Ivanoff, J., Asplund, C. L., & Marois, R. (2006). Isolation of a Central
- Bottleneck of Information Processing with Time-Resolved fMRI. Neuron, 52(6),
- 785 1109–1120. https://doi.org/10.1016/j.neuron.2006.11.009
- Egger, M., Smith, G. D., Schneider, M., & Minder, C. (1997). Bias in meta-analysis detected
- by a simple, graphical test. *BMJ*, 315(7109), 629–634.
- https://doi.org/10.1136/bmj.315.7109.629
- Faul, F., Erdfelder, E., Lang, A.-G., & Buchner, A. (2007). G*Power 3: A flexible statistical
- power analysis program for the social, behavioral, and biomedical sciences. Behavior
- 791 Research Methods, 39(2), 175–191. https://doi.org/10.3758/BF03193146
- Friston, K. (2012). Ten ironic rules for non-statistical reviewers. NeuroImage, 61(4),
- ⁷⁹³ 1300–1310. https://doi.org/10.1016/j.neuroimage.2012.04.018
- Funder, D. C., & Ozer, D. J. (2019). Evaluating Effect Size in Psychological Research: Sense
- and Nonsense. Advances in Methods and Practices in Psychological Science, 2(2),
- 796 156–168. https://doi.org/10.1177/2515245919847202
- Garner, K., & Nolan, C. (2023). Quantifying error in effect size estimates in executive
- function and implicit learning. https://doi.org/10.48610/b63ecc2
- Garner, K., Nolan, C., & Nott, Z. (2023). Quantifying error in effect size estimates: Code
- base. https://github.com/kel-github/Super-Effects.
- https://doi.org/https://github.com/kel-github/Super-Effects
- 602 Gelman, A., & Carlin, J. (2014). Beyond Power Calculations: Assessing Type S (Sign) and

- Type M (Magnitude) Errors. Perspectives on Psychological Science: A Journal of the
- Association for Psychological Science, 9(6), 641-651.
- https://doi.org/10.1177/1745691614551642
- 806 Gignac, G. E., & Szodorai, E. T. (2016). Effect size guidelines for individual differences
- researchers. Personality and Individual Differences, 102, 74–78.
- https://doi.org/10.1016/j.paid.2016.06.069
- Goschke, T. (1998). Implicit learning of perceptual and motor sequences: Evidence for
- independent learning systems. In Handbook of implicit learning (pp. 401–444). Thousand
- Oaks, CA, US: Sage Publications, Inc.
- Guo, Y., Logan, H. L., Glueck, D. H., & Muller, K. E. (2013). Selecting a sample size for
- studies with repeated measures. BMC Medical Research Methodology, 13(1), 100.
- https://doi.org/10.1186/1471-2288-13-100
- Hazeltine, E., & Ruthruff, E. (2006). Modality pairing effects and the response selection
- bottleneck. Psychological Research, 70(6), 504–513.
- https://doi.org/10.1007/s00426-005-0017-3
- Hedges, L. V. (1982). Estimation of effect size from a series of independent experiments.
- Psychological Bulletin, 92, 490–499. https://doi.org/10.1037/0033-2909.92.2.490
- Jiang, Y., & Sisk, C. (2020). Contextual cueing. In Neuromethods (Vol. 151). Humana Press
- 821 Inc.
- Lakens, D. (2013). Calculating and reporting effect sizes to facilitate cumulative science: A
- practical primer for t-tests and ANOVAs. Frontiers in Psychology, 4.
- https://doi.org/10.3389/fpsyg.2013.00863
- Lakens, D., & Caldwell, A. R. (2021). Simulation-Based Power Analysis for Factorial
- Analysis of Variance Designs. Advances in Methods and Practices in Psychological
- Science, 4(1), 2515245920951503. https://doi.org/10.1177/2515245920951503
- Lane, D. M., & Dunlap, W. P. (1978). Estimating effect size: Bias resulting from the
- significance criterion in editorial decisions. British Journal of Mathematical and

- Statistical Psychology, 31(2), 107–112.
- https://doi.org/10.1111/j.2044-8317.1978.tb00578.x
- Lorca-Puls, D. L., Gajardo-Vidal, A., White, J., Seghier, M. L., Leff, A. P., Green, D. W., ...
- Price, C. J. (2018). The impact of sample size on the reproducibility of voxel-based
- lesion-deficit mappings. Neuropsychologia, 115, 101–111.
- https://doi.org/10.1016/j.neuropsychologia.2018.03.014
- McShane, B. B., Böckenholt, U., & Hansen, K. T. (2016). Adjusting for Publication Bias in
- Meta-Analysis: An Evaluation of Selection Methods and Some Cautionary Notes.
- Perspectives on Psychological Science, 11(5), 730–749.
- https://doi.org/10.1177/1745691616662243
- Nissen, M. J., & Bullemer, P. (1987). Attentional requirements of learning: Evidence from
- performance measures. Cognitive Psychology, 19(1), 1–32.
- https://doi.org/10.1016/0010-0285(87)90002-8
- Nolan, C. R., Vromen, J. M. G., Cheung, A., & Baumann, O. (2018). Evidence against the
- Detectability of a Hippocampal Place Code Using Functional Magnetic Resonance
- Imaging. eNeuro, 5(4). https://doi.org/10.1523/ENEURO.0177-18.2018
- Nydam, A. S., Sewell, D. K., & Dux, P. E. (2018). Cathodal electrical stimulation of
- frontoparietal cortex disrupts statistical learning of visual configural information. *Cortex*,
- 99, 187-199. https://doi.org/ 10.1016/j.cortex. 2017.11.008
- Okada, K. (2013). Is Omega Squared Less Biased? A Comparison of Three Major Effect Size
- Indices in One-Way Anova. Behaviormetrika, 40(2), 129–147.
- https://doi.org/10.2333/bhmk.40.129
- Pashler, H. (1994). Dual-task interference in simple tasks: Data and theory. Psychological
- Bulletin, 116(2), 220–244. https://doi.org/10.1037/0033-2909.116.2.220
- Pelli, D. G. (1997). The VideoToolbox software for visual psychophysics: Transforming
- numbers into movies. Spatial Vision, 10(4), 437-442.
- https://doi.org/10.1163/156856897X00366

- Peterson, M. S., & Kramer, A. F. (2001). Attentional guidance of the eyes by contextual
- information and abrupt onsets. Perception & Psychophysics, 63(7), 1239-1249.
- https://doi.org/10.3758/BF03194537
- Popper, K. (1959). The Logic of Scientific Discovery. Routledge.
- R Core Team. (2023). R: A language and environment for statistical computing [Manual].
- Vienna, Austria: R Foundation for Statistical Computing.
- Raymond, J., Shapiro, K., & Arnell, K. (1992). Temporary Suppression of Visual Processing
- in an RSVP Task: An Attentional Blink? Journal of Experimental Psychology. Human
- Perception and Performance, 18(3), 849-860.
- Rouder, J. N., & Haaf, J. M. (2018). Power, Dominance, and Constraint: A Note on the
- Appeal of Different Design Traditions. Advances in Methods and Practices in
- Psychological Science, 1(1), 19–26. https://doi.org/10.1177/2515245917745058
- RStudio Team. (2020). RStudio: Integrated development environment for r [Manual].
- Boston, MA: RStudio, PBC.
- Schäfer, T., & Schwarz, M. A. (2019). The Meaningfulness of Effect Sizes in Psychological
- Research: Differences Between Sub-Disciplines and the Impact of Potential Biases.
- Frontiers in Psychology, 10, 813. https://doi.org/10.3389/fpsyg.2019.00813
- Schmidt, F. L., & Hunter, J. E. (2015). Methods of Meta-Analysis: Correcting Error and
- Bias in Research Findings. SAGE Publications, Ltd.
- https://doi.org/10.4135/9781483398105
- Schumacher, E. H., Seymour, T. L., Glass, J. M., Fencsik, D. E., Lauber, E. J., Kieras, D. E.,
- & Meyer, D. E. (2001). Virtually perfect time sharing in dual-task performance:
- Uncorking the central cognitive bottleneck. Psychological Science, 12(2), 101–108.
- https://doi.org/10.1111/1467-9280.00318
- Sisk, C. A., Remington, R. W., & Jiang, Y. V. (2019). Mechanisms of contextual cueing: A
- tutorial review. Attention, Perception, & Psychophysics, 81(8), 2571–2589.
- https://doi.org/10.3758/s13414-019-01832-2

- 884 Szucs, D., & Ioannidis, J. P. A. (2017). When Null Hypothesis Significance Testing Is
- Unsuitable for Research: A Reassessment. Frontiers in Human Neuroscience, 11, 390.
- https://doi.org/10.3389/fnhum.2017.00390
- Travis, S. L., Mattingley, J. B., & Dux, P. E. (2013). On the role of working memory in
- spatial contextual cueing. Journal of Experimental Psychology: Learning, Memory, and
- 889 Cognition, 39(1), 208–219. https://doi.org/http://dx.doi.org/10.1037/a0028644
- Troncoso Skidmore, S., & Thompson, B. (2013). Bias and precision of some classical
- ANOVA effect sizes when assumptions are violated. Behavior Research Methods, 45(2),
- 536–546. https://doi.org/10.3758/s13428-012-0257-2
- Vadillo, M. A., Konstantinidis, E., & Shanks, D. R. (2016). Underpowered samples, false
- negatives, and unconscious learning. Psychonomic Bulletin & Review, 23(1), 87–102.
- https://doi.org/10.3758/s13423-015-0892-6
- Vadillo, M. A., Linssen, D., Orgaz, C., Parsons, S., & Shanks, D. R. (2020). Unconscious or
- underpowered? Probabilistic cuing of visual attention. Journal of Experimental
- 898 Psychology. General, 149(1), 160–181. https://doi.org/10.1037/xge0000632
- 899 Vadillo, M. A., Malejka, S., Lee, D. Y. H., Dienes, Z., & Shanks, D. R. (2021). Raising
- awareness about measurement error in research on unconscious mental processes.
- Psychonomic Bulletin & Review. https://doi.org/10.3758/s13423-021-01923-y
- 902 Westfall, J., Kenny, D. A., & Judd, C. M. (2014). Statistical power and optimal design in
- experiments in which samples of participants respond to samples of stimuli. Journal of
- Experimental Psychology. General, 143(5), 2020–2045.
- 905 https://doi.org/10.1037/xge0000014
- 906 Wiernik, B. M., & Dahlke, J. A. (2020). Obtaining Unbiased Results in Meta-Analysis: The
- Importance of Correcting for Statistical Artifacts. Advances in Methods and Practices in
- 908 Psychological Science, 3(1), 94–123. https://doi.org/10.1177/2515245919885611

Table 1 Typical N found from literature survey. n exp = number or experiments, med N = median N

task	n exp	med N
AB	60	24
MT	60	40
CC	49	24
SRT	60	34

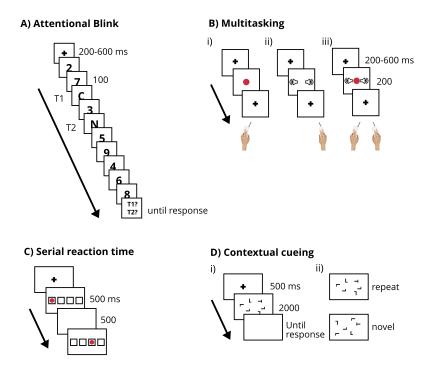


Figure 1. Task battery. A) Attentional Blink Paradigm (AB). Participants report the two letter targets from the rapid serial visual presentation of numbers and letters. B) Multitasking Paradigm (MT). Participants discriminate the colour of a disc, a complex tone, or both. C) Serial reaction time task (SRT). Participants respond to one of four stimuli, each mapped to a spatially-compatible button press. Unknown to participants, for half of the experimental blocks, the stimulus follows a repeating sequence. D) Contextual Cueing Paradigm (CC). i) Participants perform an inefficient visual search task where they search for a rotated T among L distractors. ii) Unknown to participants, half of the search arrays are repeated throughout the course of the experiment.

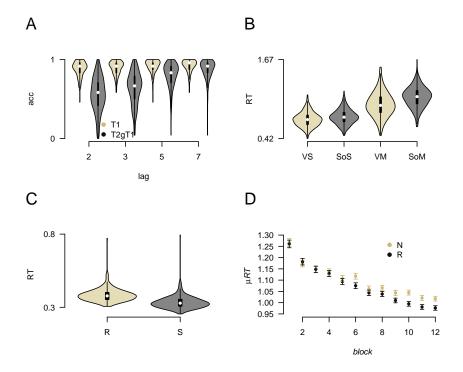


Figure 2. Behavioural Results. A) Attentional Blink Paradigm (AB). Accuracy (acc) for T2|T1 was lower at early lags, relative to later lags. Note that T1 accuracy is also plotted. B) Multitasking Paradigm (MT). RTs were slowed for multitask (M) conditions, relative to single-tasks (S). This difference was larger for sound tasks (So) than for visual (V) tasks. C) Serial Response Task (SRT). In the second half of the experiment, RTs were faster in the sequence (S) relative to the random (R) condition. D) Contextual Cueing (CC). RTs were faster for the repeat (R) than for the novel (N) displays, and this difference became larger throughout the course of the experiment.

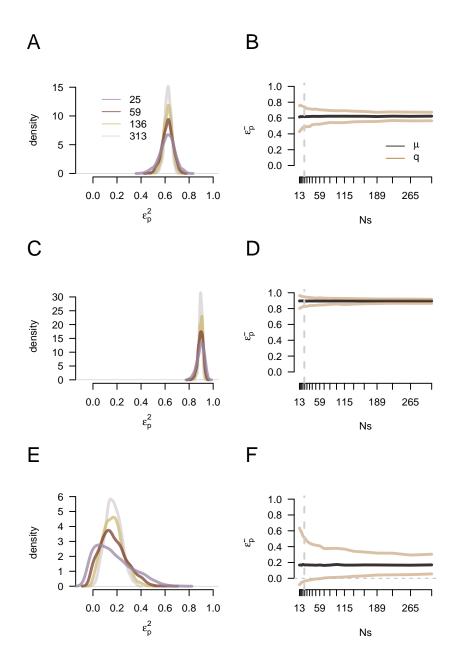


Figure 3. Effect size distributions for the AB and MT paradigms. A) AB: Partial epsilon sq distributions for selected N for the main effect of lag. B) Showing the mean partial epsilon squared, and the UB and LB quantiles [.025, .975], for the main effect of lag, across N (AB). C) MT: Same as in A, but for the main effect of task condition (MT). D) Same as in B, for the main effect of task condition (MT), E) As in C, but for the task x modality interaction (MT), E) As D, but for the MT task x modality interaction

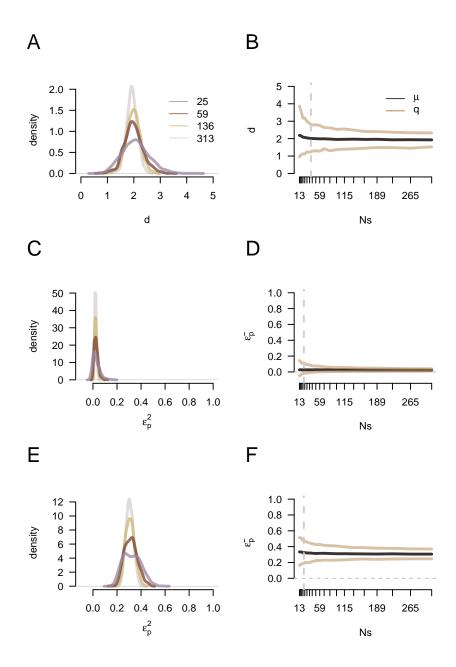


Figure 4. Effect size distributions observed for the SRT and CC paradigms. A) SRT: Cohens dz for the effect of sequence learning, for selected N. B) Showing the mean dz, and the UB and LB quantiles [.025, .975], for the effect of sequence, across N (SRT). C) CC: Same as in A, but for the block x condition interaction. D) Same as in B, for the block x condition interaction (CC), E) As in C, but for the main effect of condition (CC), E) As D, but for the main effect of condition (CC)

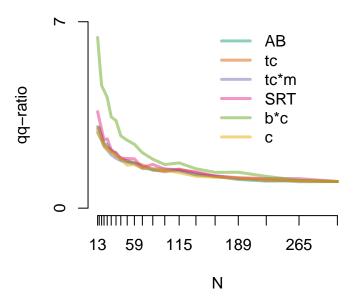


Figure 5. QQ-ratios plotted by N for each task effect. AB: Attentional Blink, tc: main effct of task condition from the MT paradigm, tc*m: trial condition x modality interaction, SRT: Serial Response Task, b*c: block x condition interaction from the CC task, c: main effect of condition from the CC task.

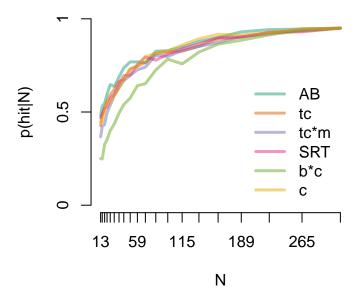


Figure 6. probability of a single study producing an effect size estimates that are within the LB and UB for the best estimate (p(hit|N)), plotted by N for each task effect. AB: Attentional Blink, tc: main effect of task condition from the MT paradigm, tc*m: trial condition x modality interaction, SRT: Serial Response Task, b*c: block x condition interaction from the CC task, c: main effect of condition from the CC task.

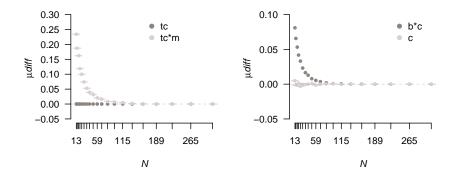


Figure 7. Inflation bias scores plotted by N for the A) the task condition and task condition x modality interactions for the MT paradigm, and B) the block x condition interaction and main effect of condition from the CC paradigm. IB: Implicit Bias, tc: task condition, tc*m: task condition x modality, b*c: block x condition interaction, c: main effect of condition. Error bars reflect pooled standard error of the difference.