

Decomposing time  
series into trends,  
seasonality, residuals

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# Classical timeseries decomposition (ca. 1920's)

## Assumptions

Additive:  $Y = T + S + R$

Multiplicative:  $Y = TSR$

Either way,  $Y = "f(t) + e(t)"$

## Basic building blocks

Trends,  $T$

Seasonality,  $S$

Residuals,  $R$

The image shows five glass jars with white stoppers, each containing a different type of dried herb or pill. From left to right: the first jar contains dark red, dried, almond-shaped seeds; the second jar contains bright yellow, dried flower heads; the third jar contains light brown, dried, irregularly shaped pieces of root or bark; the fourth jar contains numerous small, white, circular pills with embossed markings; and the fifth jar contains dark green, dried, leafy herbs. The jars are arranged in a row on a light blue surface.

Additive and Multiplicative

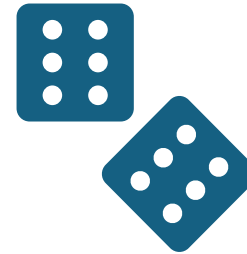
# We use *statsmodels.tsa.seasonal*

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## **Function:**

*seasonal\_decompose*



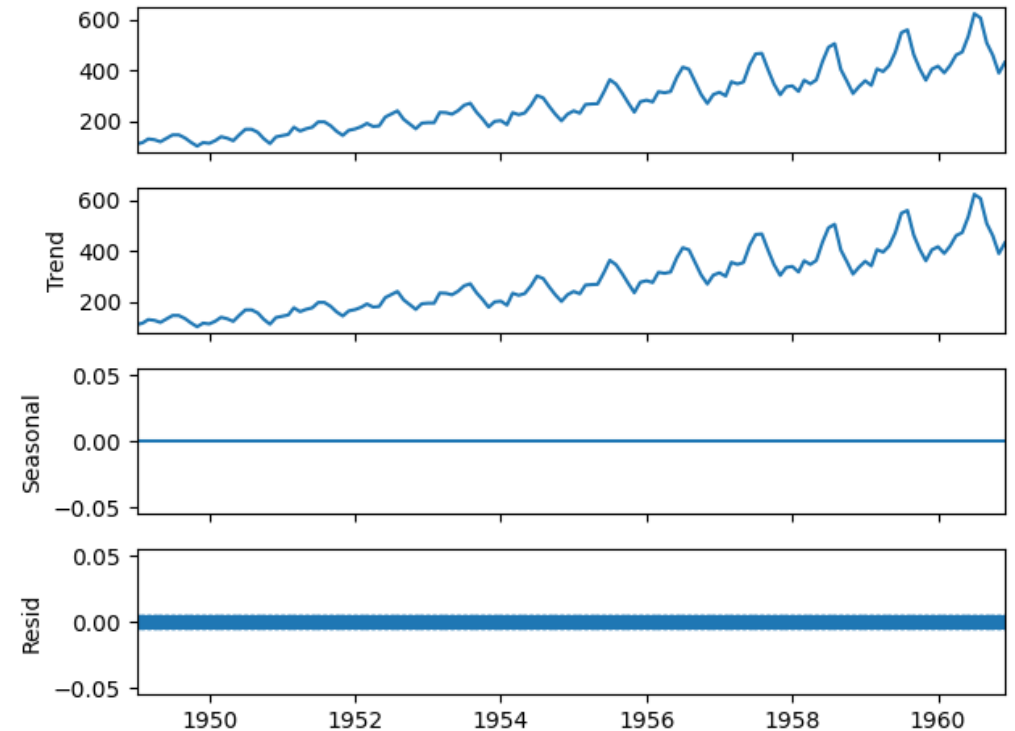
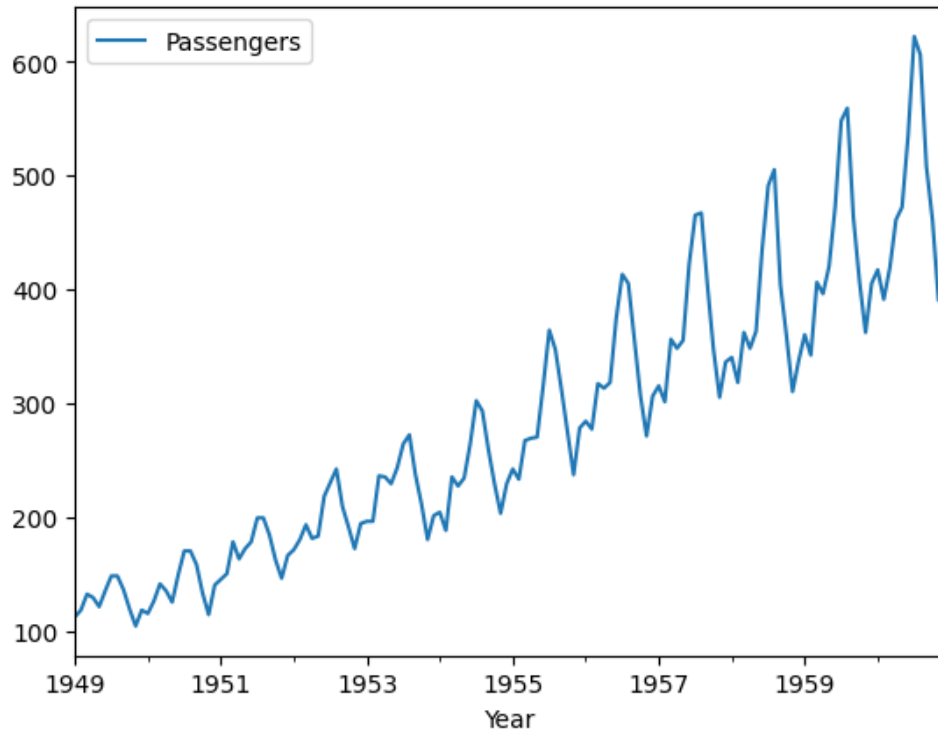
## **Hyperparameters**

Model (additive/multiplicative/++)

Period (how many datapoints in each season)

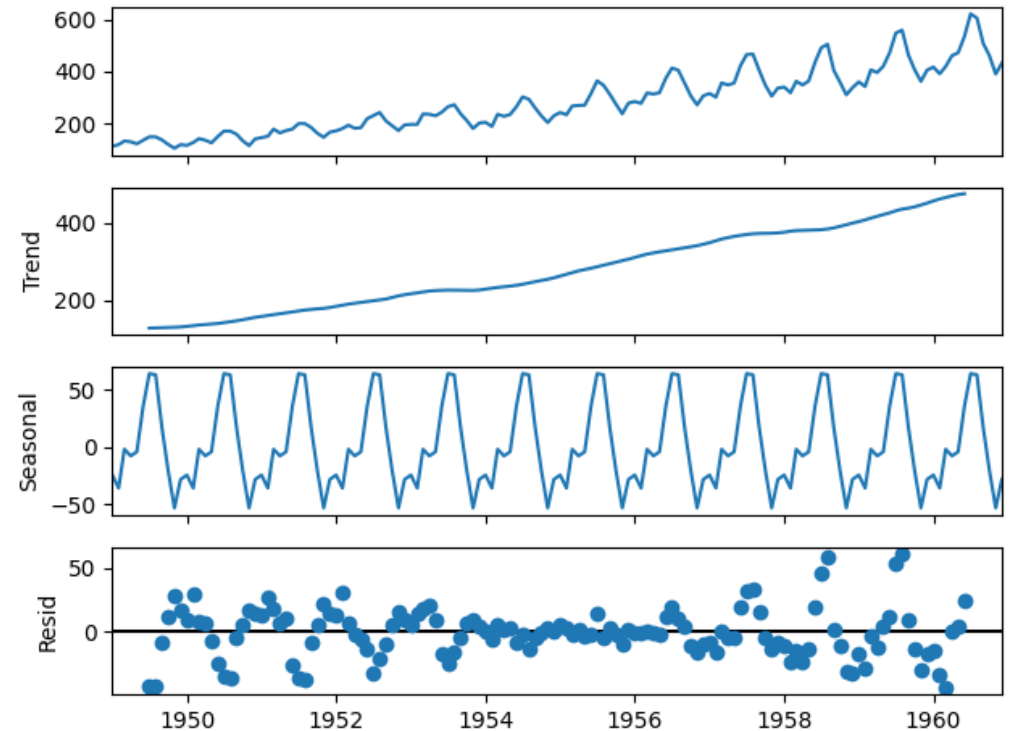
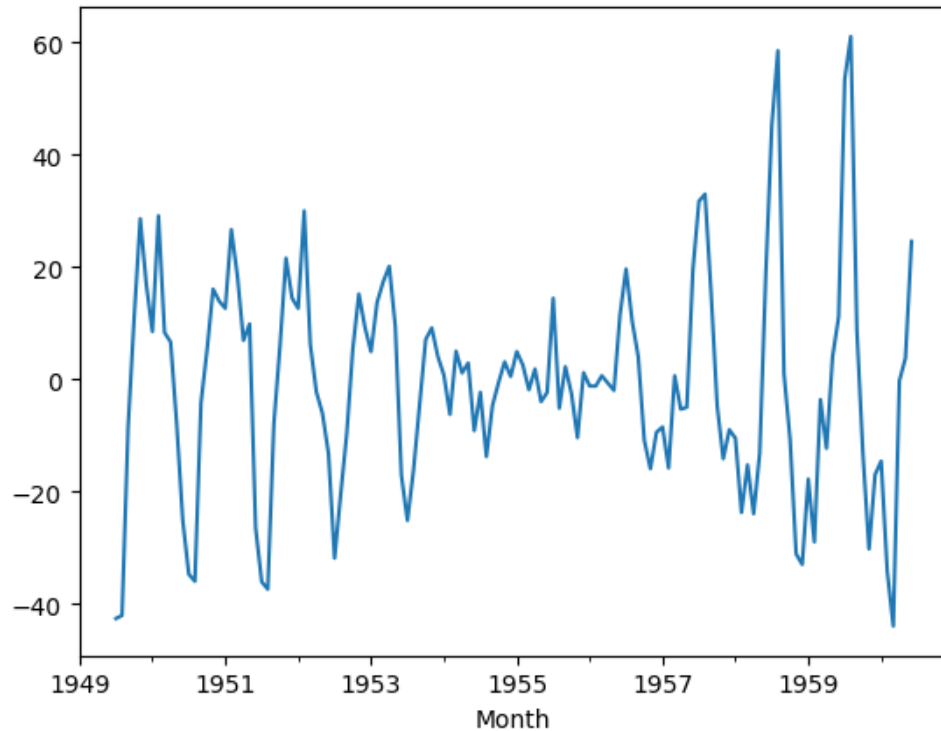
# Method 1: Additive

Period = 1



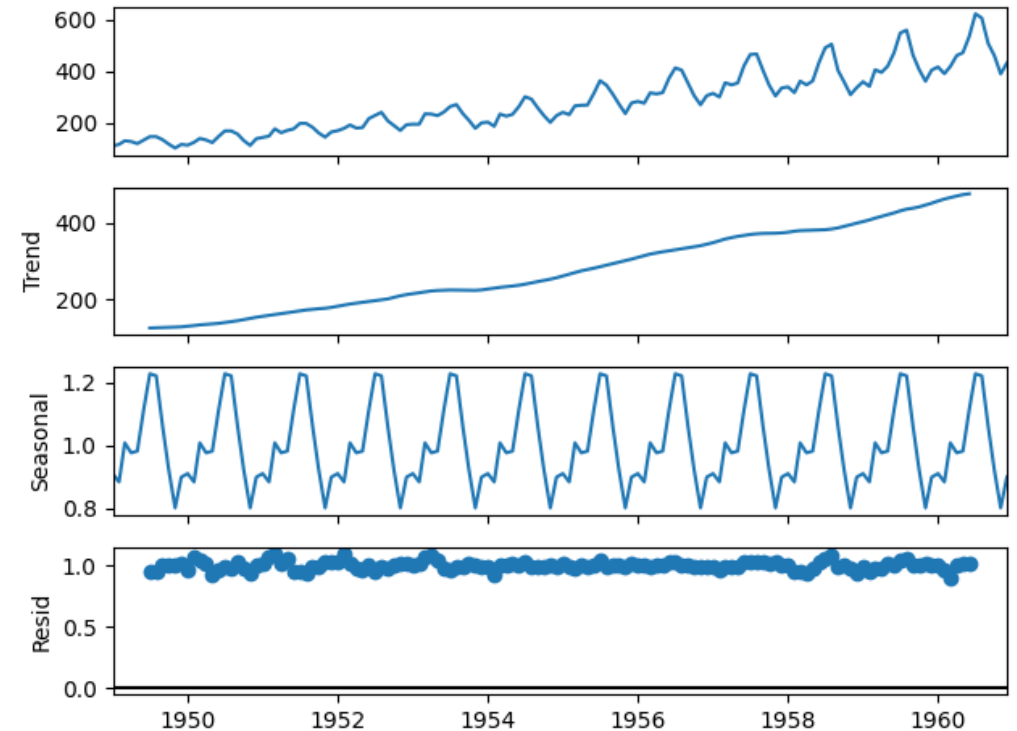
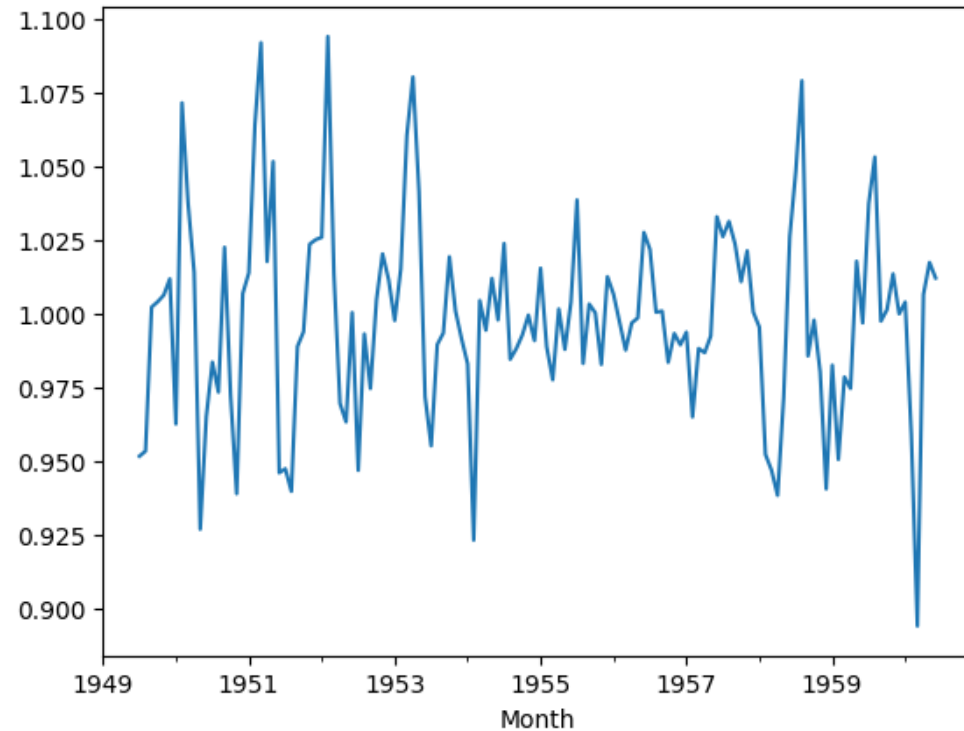
# Method 1: Additive

Period = 12



# Method 2: Multiplicative

Period = 12





# Quick tips

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Trends should be "smooth" and aperiodic

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Seasons should definitely be periodic

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Irregularities should "not have patterns"

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And noise "should look random"



If a trend has periods:  
decompose it further



If a season looks to trend (or have  
an envelope): decompose it  
further



If the noise looks to have  
patterns: keep changing your  
model and decomposing further

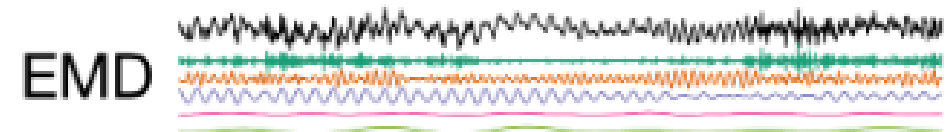
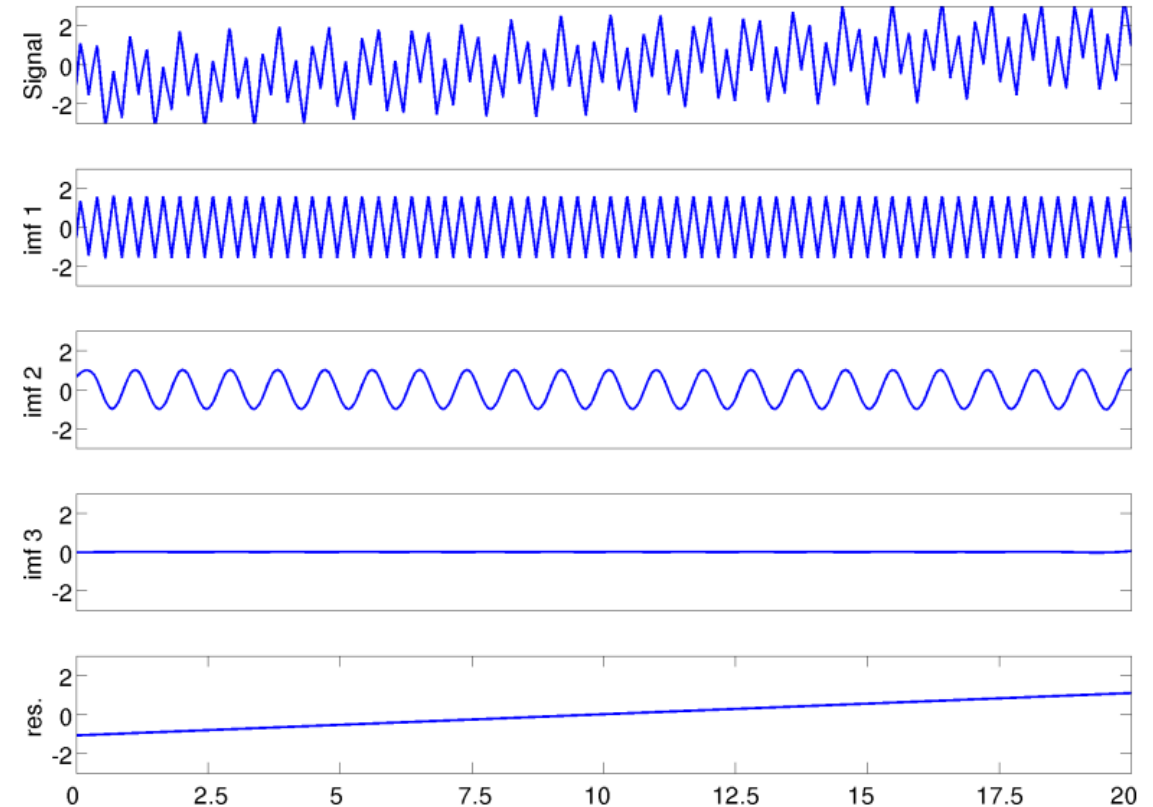


# Empirical Mode Decomposition

## EMD

# EMD Overview

- Decomposes a signal into oscillatory components
- Components known as Intrinsic mode Functions (IMF) + residual components.
- Data-Driven method, operating on nonlinear and nonstationary signals
- Assumes additive timeseries\*
- Requires no prior knowledge about the data
- Depends on ***Sifting*** to compute the IMF



# Sifting Process

(EMD cont')

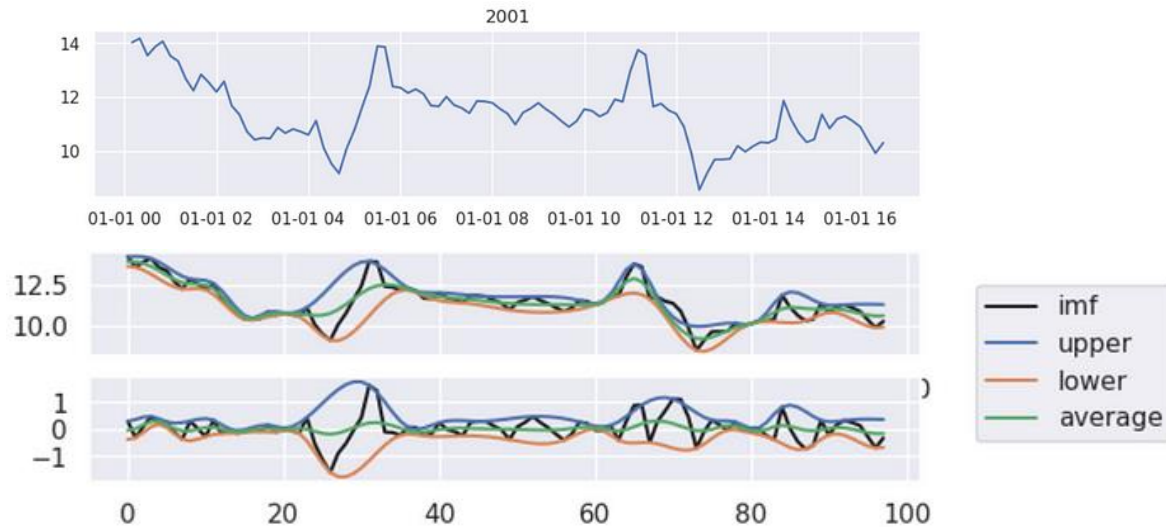


Figure source: [AlMavercik](#)

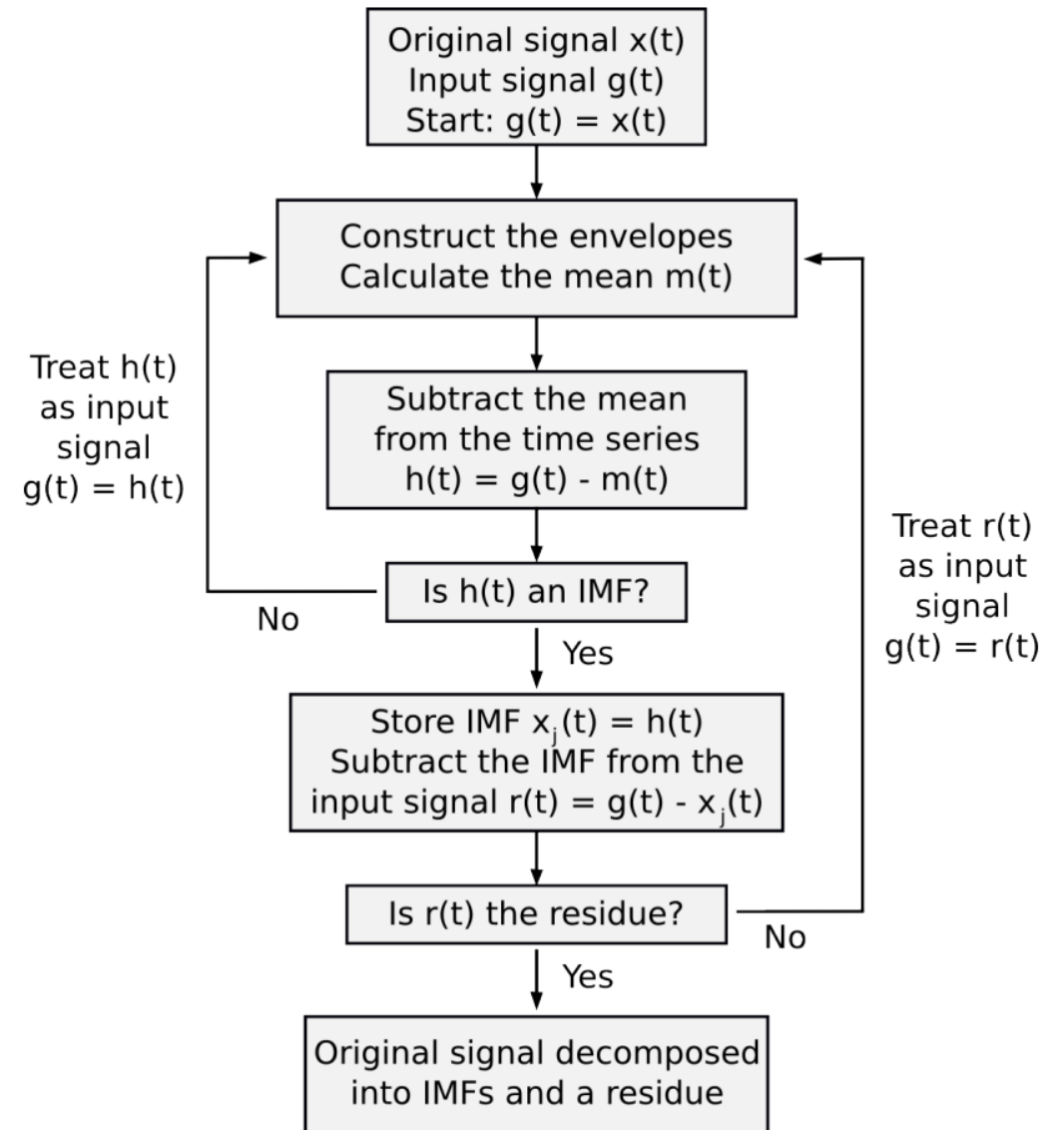
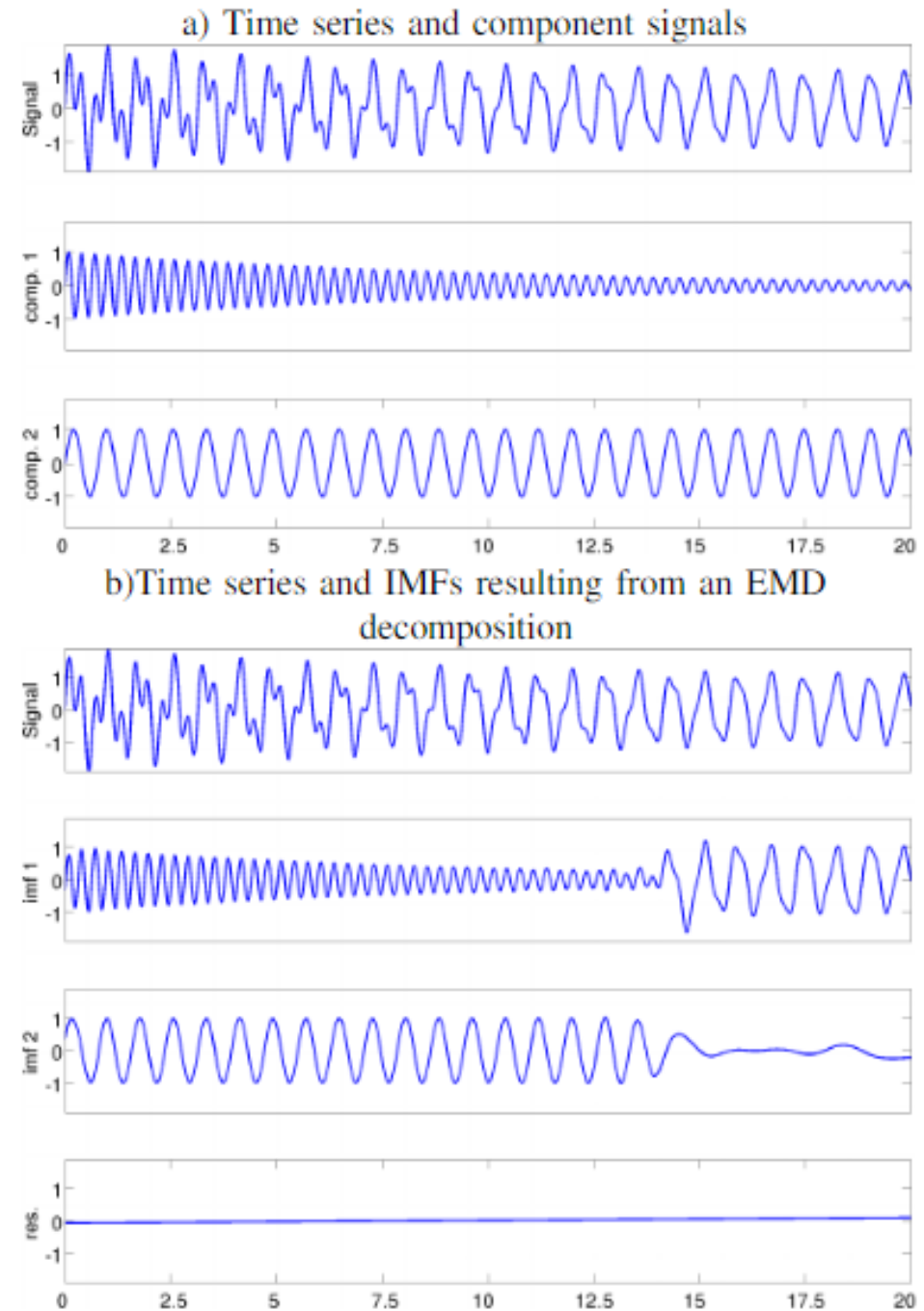


figure: Zeiler et al. (2010). [Empirical Mode Decomposition - an introduction.](#)

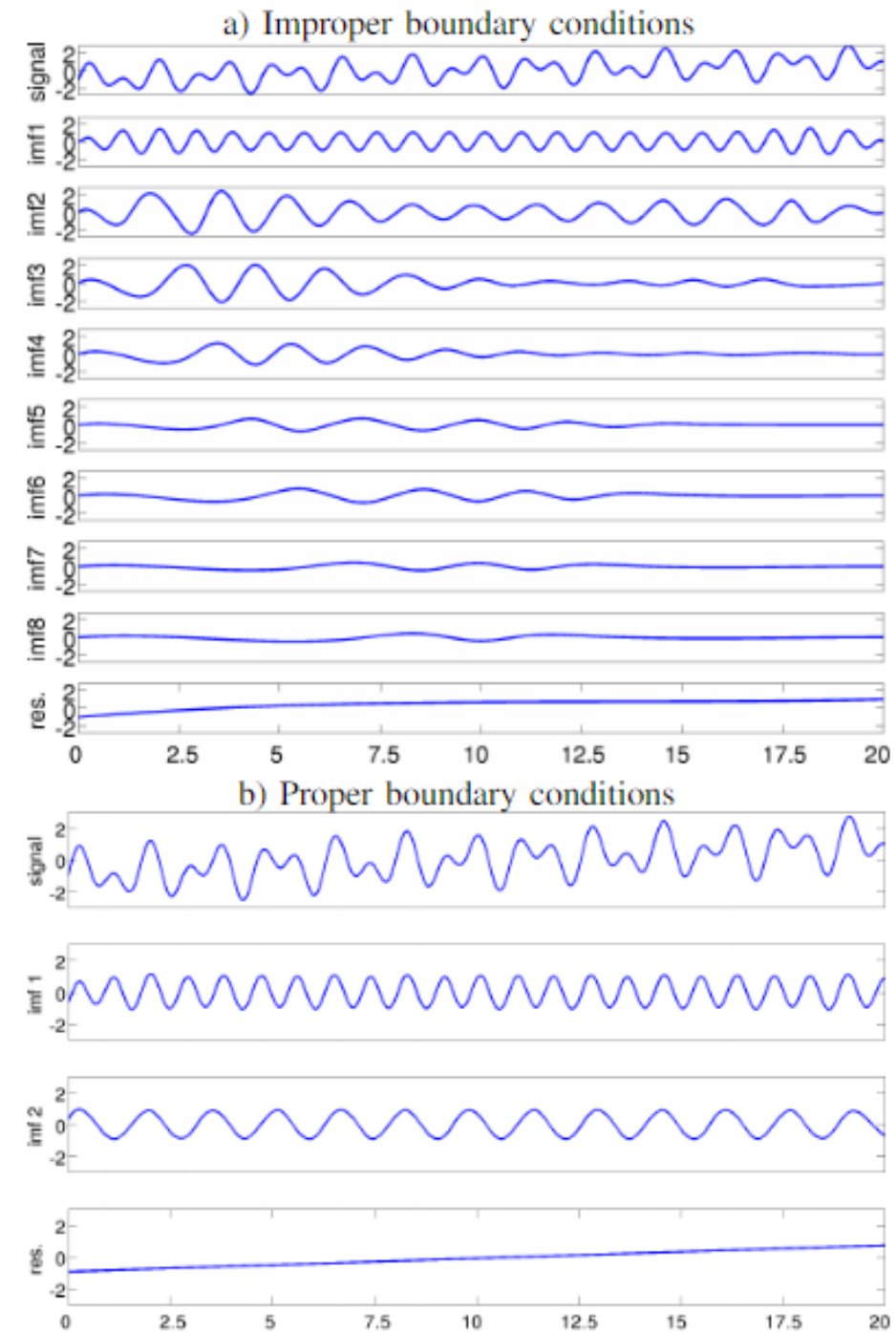
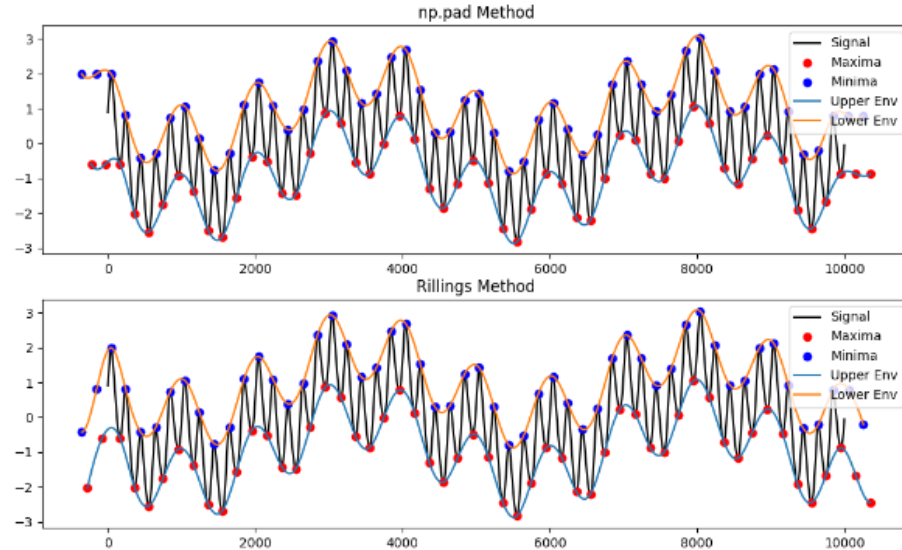
# Limitations

- Mode mixing
- Limited to additive models \*



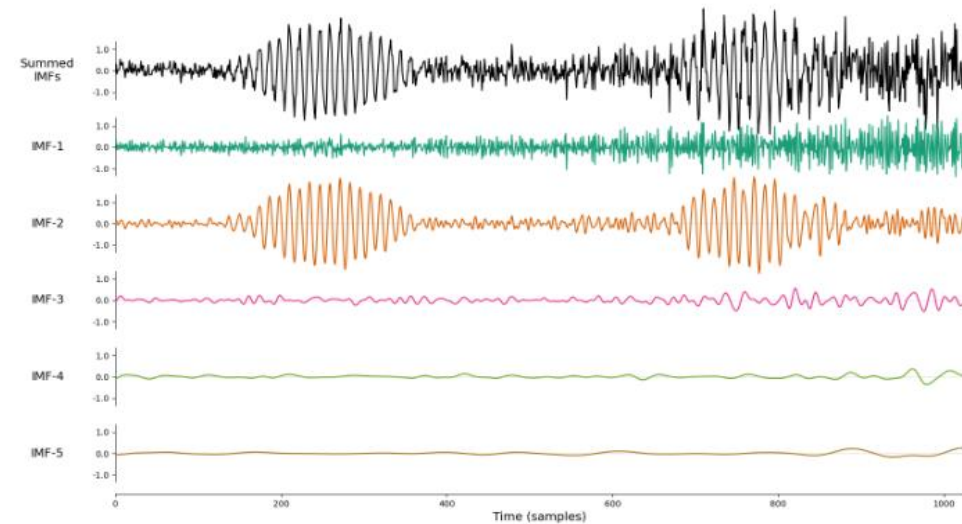
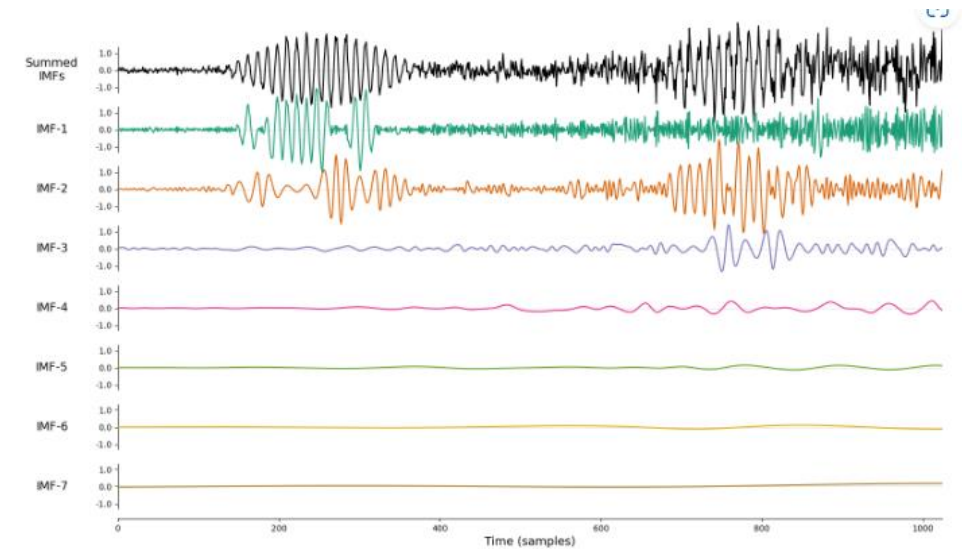
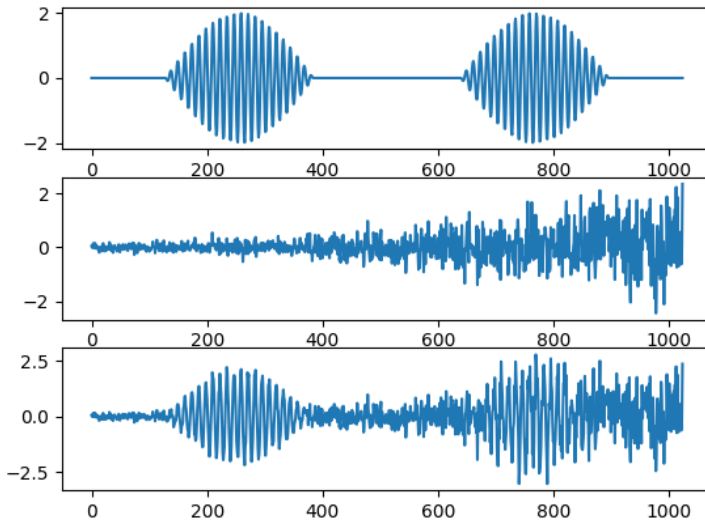
# Limitations

- Sensitive to boundary condition



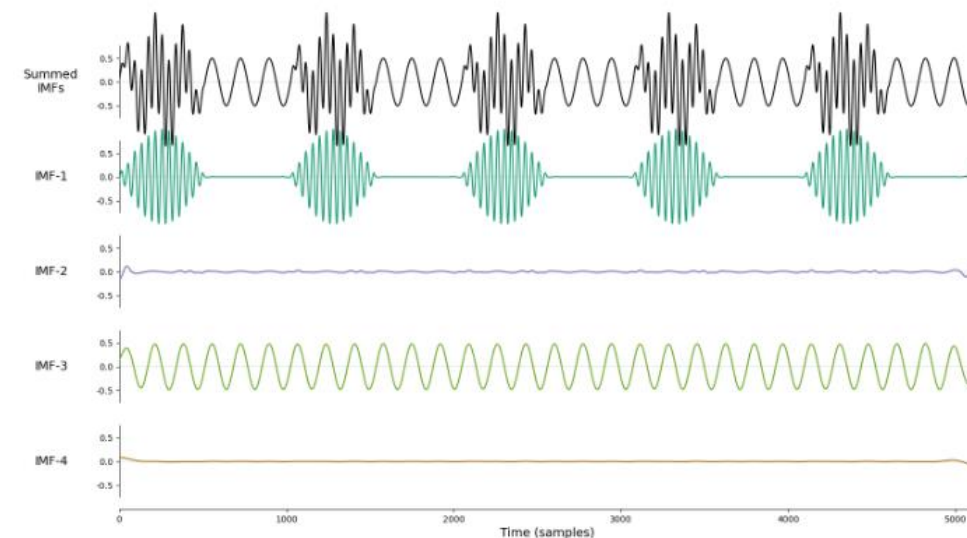
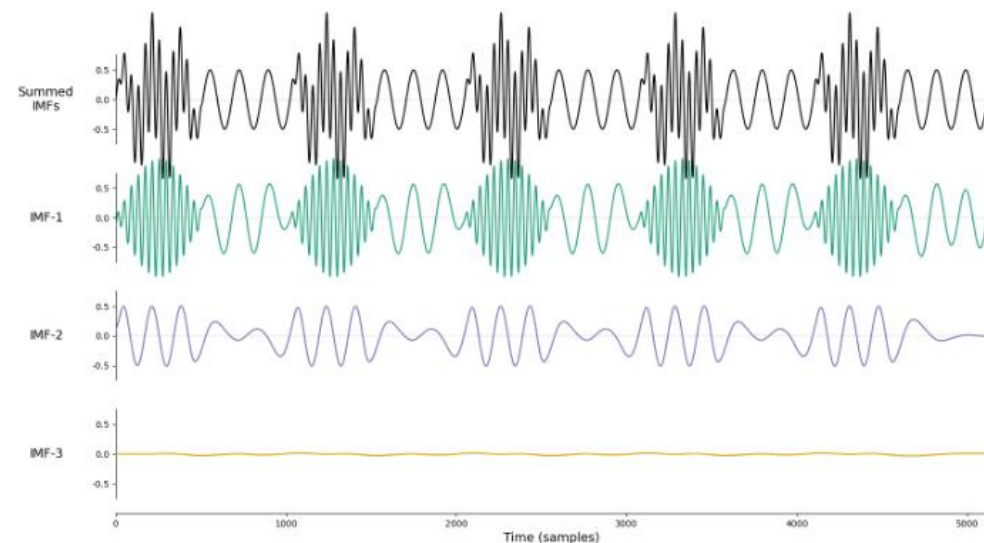
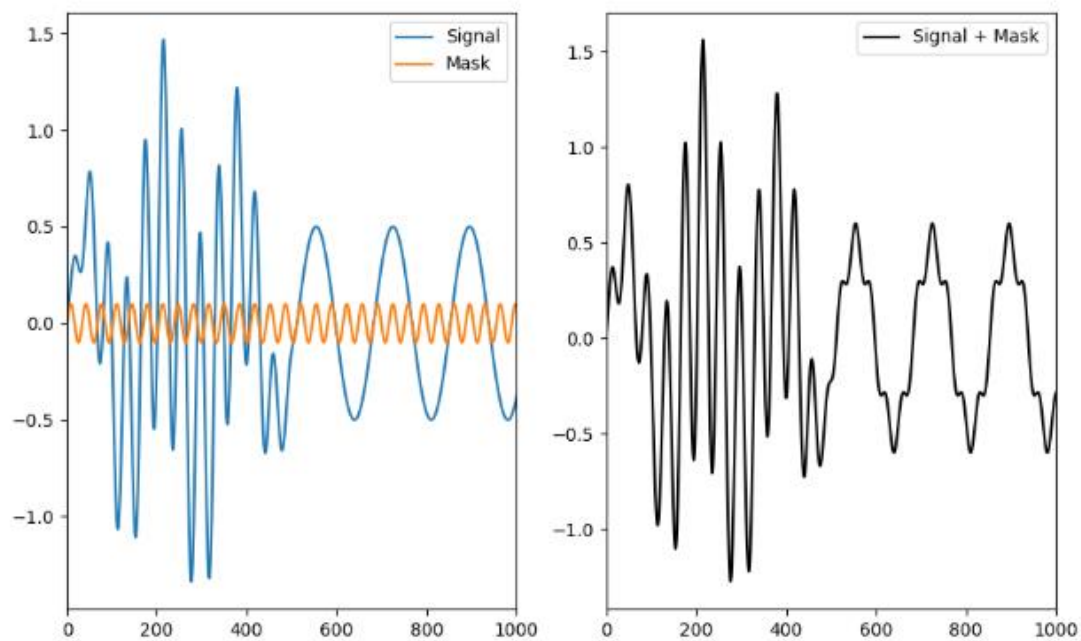
# Other Sifting Variations

- Noise Assisted sifting (ensemble EMD)



# Other Sifting Variations

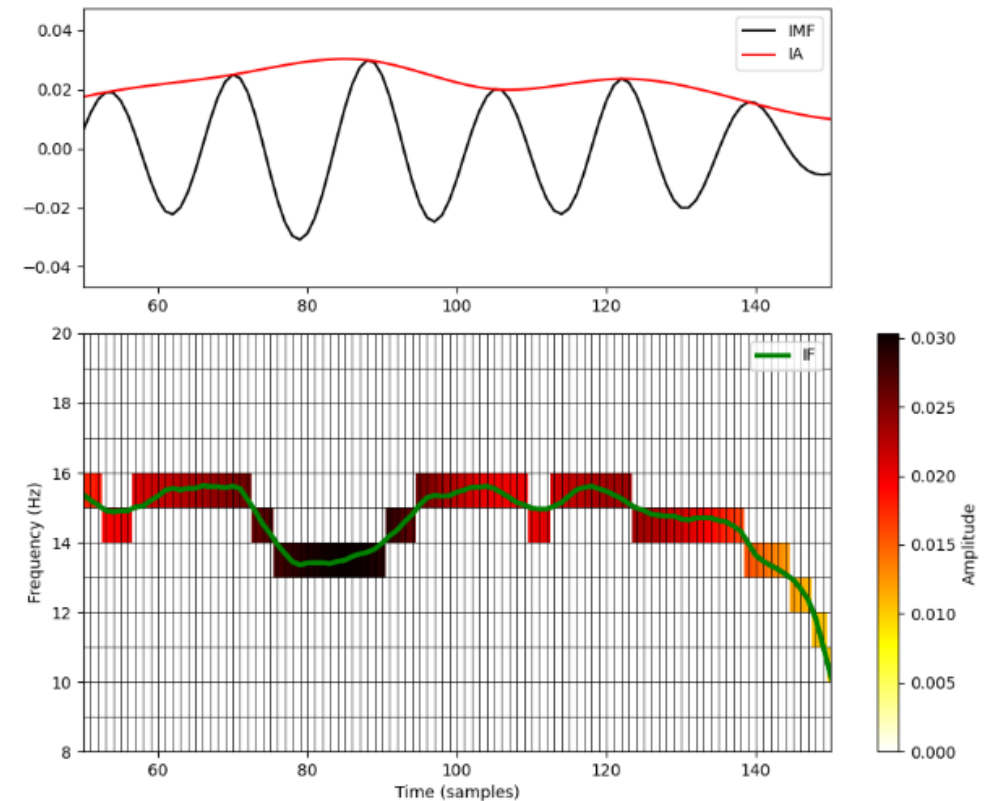
- Masked Sifting





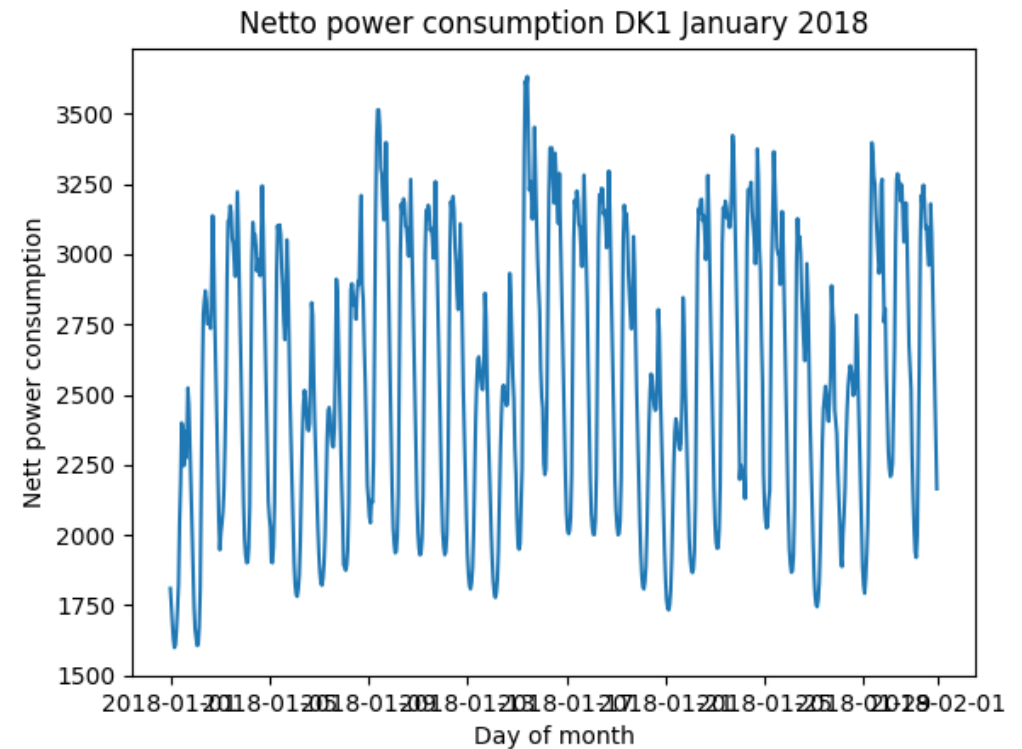
# The Hilbert-Huang Transform (HHT)

- Provides a description of how the energy or power within a signal is distributed across frequency.
- The distributions are based on the **instantaneous frequency** and **amplitude** of a signal.

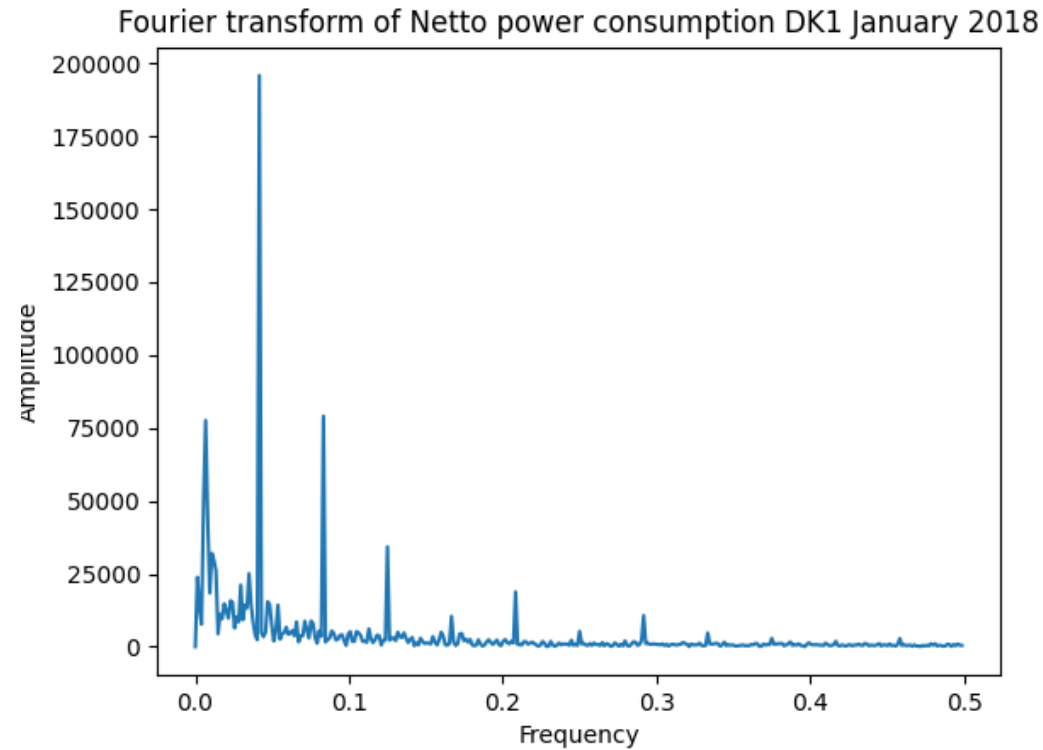


# Frequency based methods

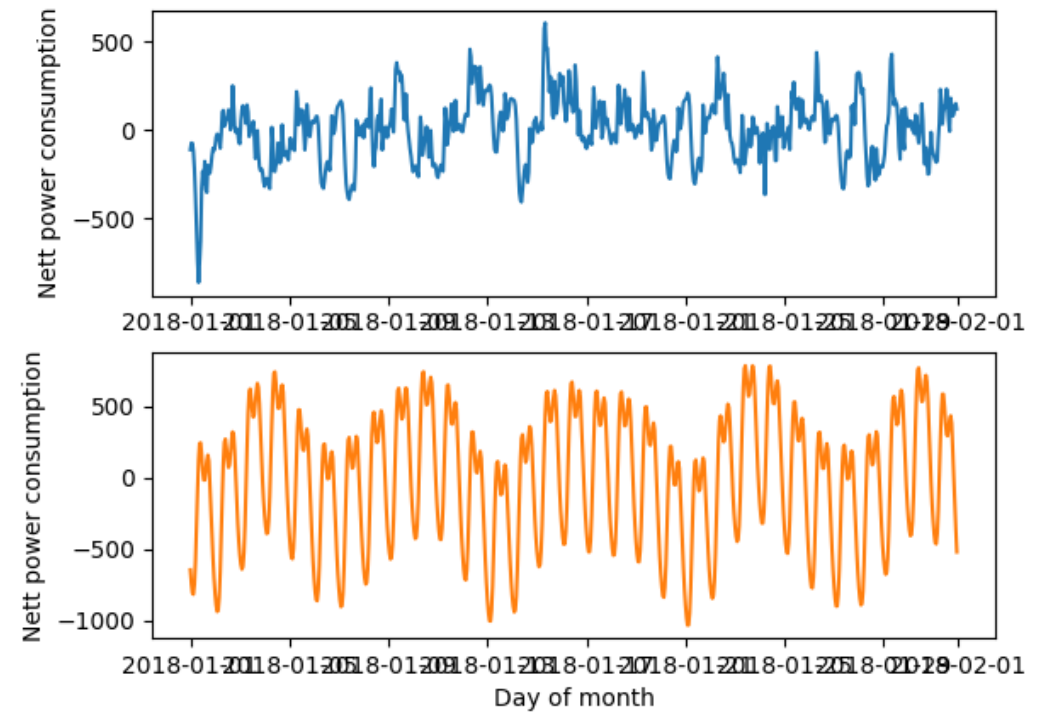
- How to handle periodic signals
- Same seasonal trends over whole signal, wide sense stationarity
- Remember to remove median



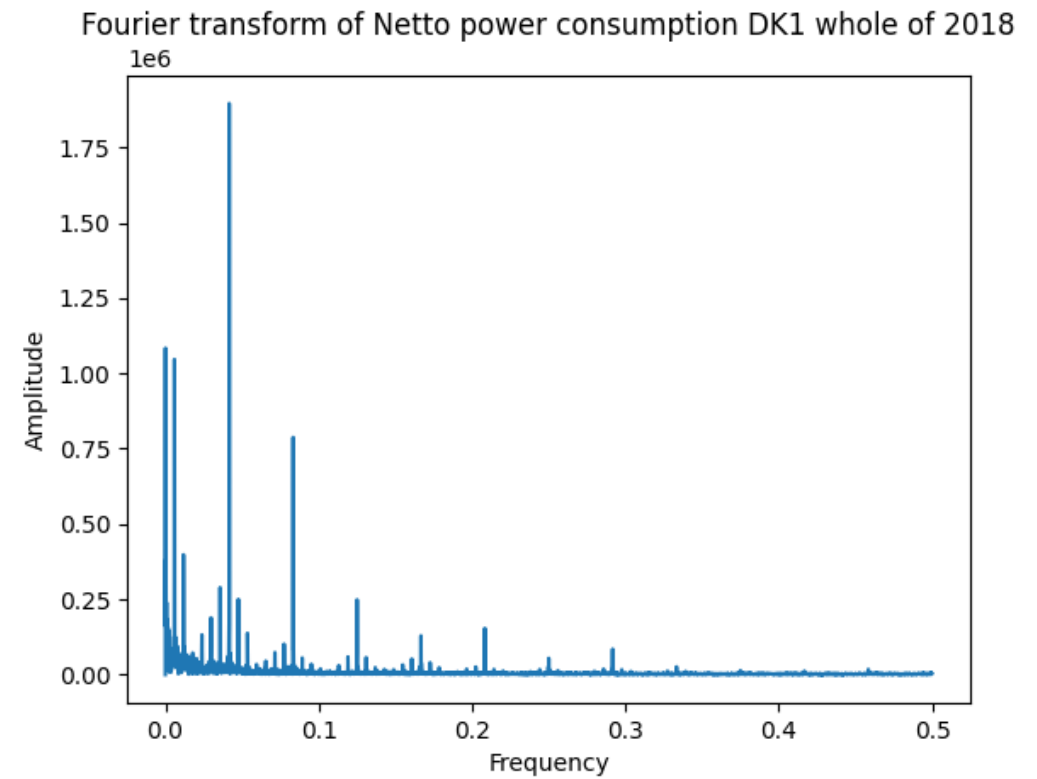
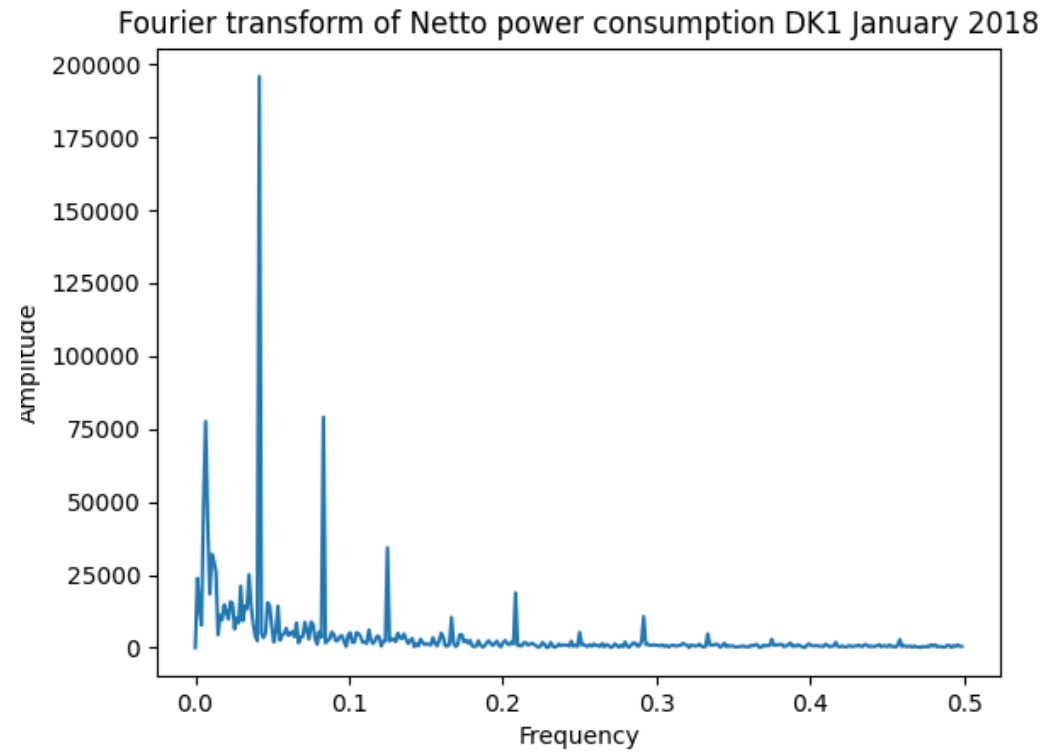
# Filtering in Fourier domain



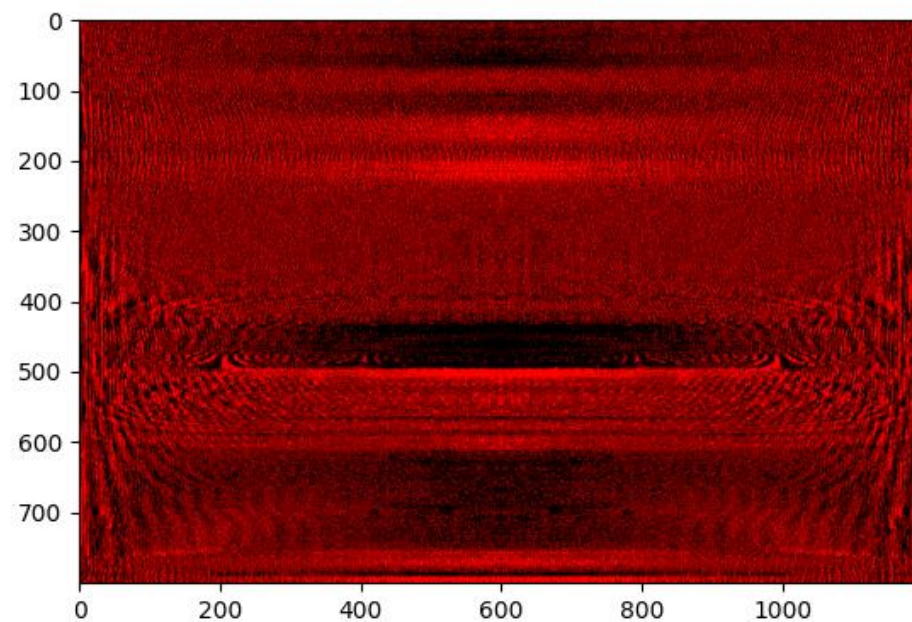
verse Fourier transform of filtered Netto power consumption DK1 January 2018:



# Longer data -> better spectra

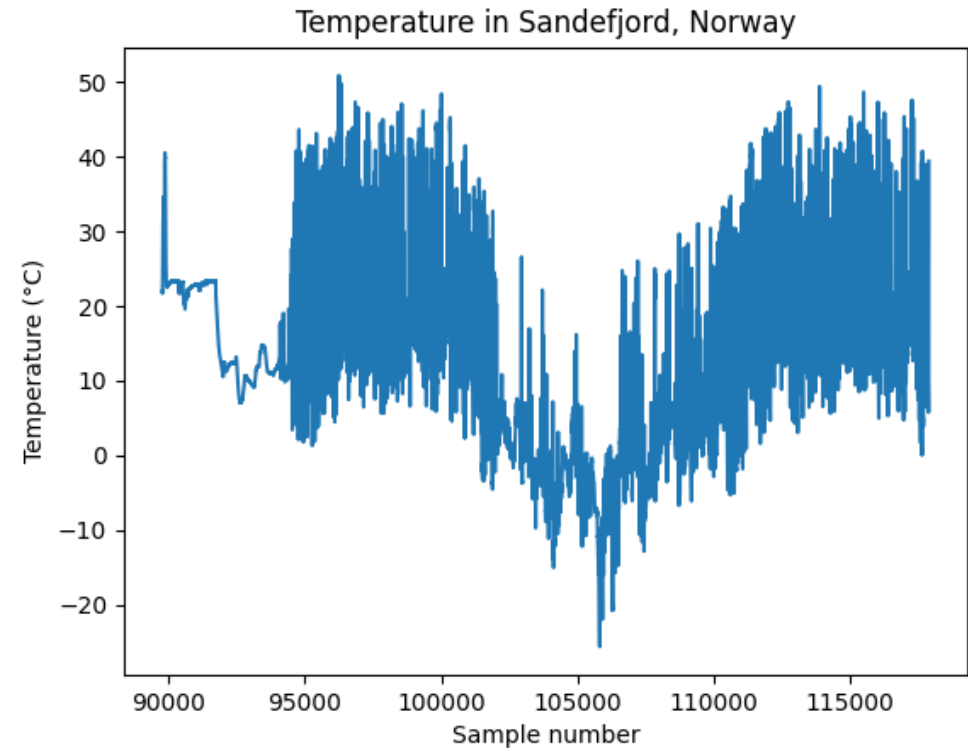


# Works in all dimensions

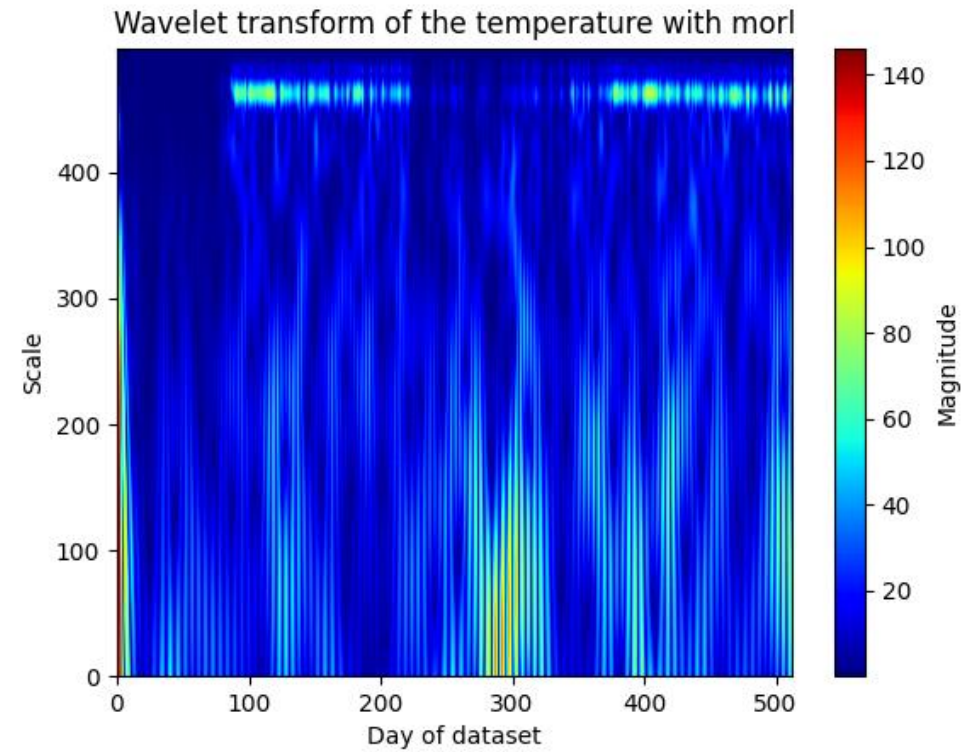
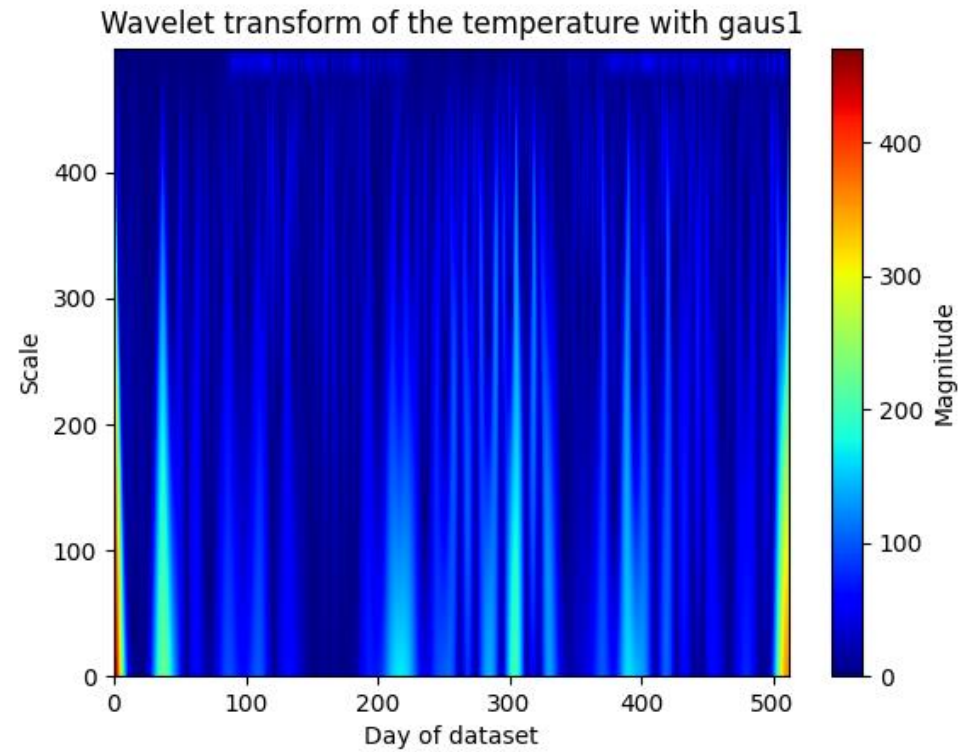


# Non-stationary signals

- Some time variation
- Fourier transform doesn't show time
- Wavelet transform fixes this

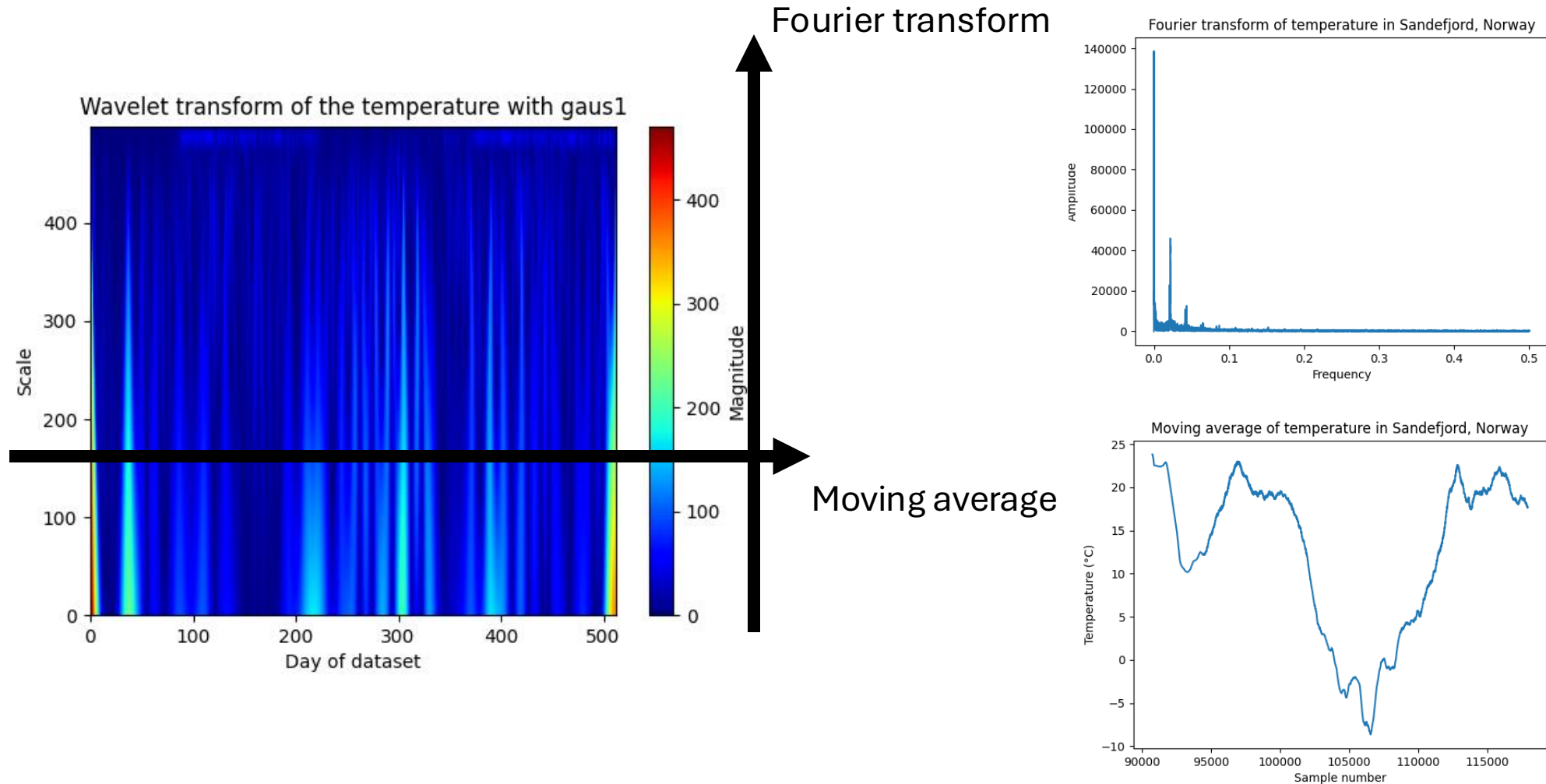


# Wavelet transform





# Connection with other methods



# In conclusion

- Infinite decomposition algorithms exists
- Prior and domain knowledge is key
- It is worth trying multiple methods