How to compose point-free functions

utashih

Warm-up: eta-reduction

 The following two functions are equivalent under eta-conversion:

```
\x -> f x
and
f
```

Warm-up: eta-reduction

 Haskell's partially applying functionality enables us to remove the last (rightmost) parameter of curried functions

```
sum xs = foldr (+) 0 xs
By applying eta-reduction
sum = foldr (+) 0
```

Point-free style

- also called tacit programming
- (from Wikipedia) Function definitions do not identify the arguments (points) on which they operate; they merely compose other functions
- considered unnecessarily obscure
- ...and we're going into this obscurity!

Examples from H-99

```
last = foldr1 (const id)
reverse = foldl (flip (:)) []

elementAt :: [a] -> Int -> a
elementAt = (last .) . flip take

isPalindrome :: (Eq a) => [a] -> Bool
isPalindrome = (==) <*> reverse
```

Composition of functions

- (.) :: (b -> c) -> (a -> b) -> (a -> c)
 (f . g) x = f (g x)
- will be used ubiquitously

WelrD StRiNg CaSe

```
toWeirdCase :: String -> String
toWeirdCase =
    unwords . map (zipWith ($) weird) . words
    where weird = cycle [toUpper, toLower]
```

Digression: functor

• types that can be mapped over (with restrictions)

```
class Functor f where
  fmap :: (a -> b) ~> f a -> f b
```

Hom functor

- For each type r, the (covariant) hom functor Hom(r, -) maps
 - each type a to type $r \rightarrow a$
 - each function of type $a \rightarrow b$ to a function of type $(r \rightarrow a) \rightarrow (r \rightarrow b)$

fmap ::
$$(a \rightarrow b) \sim (r \rightarrow a) \rightarrow (r \rightarrow b)$$

Hom functor

• a more familiar name would be the Reader functor

```
instance Functor ((->) r) where
fmap = (.)
```

```
concatMap :: (a -> [b]) -> [a] -> [b]
concatMap = (concat .) . map
```

Or equivalently

```
concatMap f xs = concat (map f xs)
```

To validate the equivalence

```
concatMap f xs = concat (map f xs)
concatMap f xs = concat $ map f xs
concatMap f xs = concat . map f $ xs
concatMap f = concat . map f
concatMap f = (.) concat (map f)
concatMap f = (.) concat $ map f
concatMap f = (.) concat . map $ f
              = (.) concat . map
concatMap
          = (concat .) . map
concatMap
```

 The key idea is to find the rightmost parameter by changing (nested) function applications into single composed function applied to single argument

```
concatMap f xs = concat (map f xs)
concatMap f xs = concat $ map f xs
concatMap f xs = concat . map f $ xs
concatMap f = concat . map f
```

Note that it is incorrect to take the second step like

```
concatMap f xs = concat $ map f xs
concatMap f xs = concat . map $ f xs
```

- The latter formula corresponds to concat (map (f xs))
- Function application associates to the left while (\$) associates to the right; thus the outermost application is (map f) xs instead of map (f xs)

Example: elementAt

```
elementAt :: [a] -> Int -> a
elementAt = (last .) . flip take

(last .) :: (r -> [a]) -> (r -> a)
flip take :: [a] -> (Int -> [a])
```

...so we have more dots!

Composing function with 2 arguments

```
(.:) :: (c -> d) -> (a -> b -> c) -> a -> b -> d
(.:) = (.) . (.)
f .: g = \x y -> f (g x y)
```

Thus we have

```
concatMap = concat .: map
```

This operator is defined in Data. Composition in the composition package

Back to the hom functor

- Of course, it is an applicative functor/monad as well
- Some more definitions:

```
instance Applicative ((->) r) where
   pure = const
   f <*> g = \r -> f r (g r)

instance Monad ((->) r) where
   f >>= g = \r -> g (f r) r
```

Example from H-99

Equal Sides of An Array

```
findEvenIndex :: [Int] -> Int
findEvenIndex = fromMaybe (-1) . elmIndex True .
  (zipWith (==) <$> scanl1 (+) <*> scanr1 (+))
```

• Note that fmap, (<\$>) and (.) serve the same purpose

Sort the Odd

```
sortArray :: [Int] -> [Int]
sortArray = replaceOdd <$> id <*> sort .
    filter odd

replaceOdd :: [Int] -> [Int] -> [Int]
```

Are they the "same"

```
comp :: [Integer] -> [Integer] -> Bool
comp = (. sort) . (==) . sort . map (^2)
comp xs ys = sort (map (^2) xs) == sort ys
```

Example: map filter

```
mp :: (b -> Bool) -> (a -> b) -> [a] -> [b]
mp p f xs = filter p (map f xs)
mp p f = filter p . map f
mp = (. map) . (.) . filter
```

Partial applying to (.)

Putting it off

```
f :: (a -> b)
(f .) :: (r -> a) -> (r -> b)
```

Bringing it forward

```
g :: (a -> b)
(. g) :: (b -> s) -> (a -> s)
```

In all: understanding (.)

- Composition of functions
- Functor map of hom functor
- Continuation-like

"Boilerplate" pattern

```
func x y = f (g x y)
func = (f .) . g
func x = f(g x)(h x)
func = f 
      = f \cdot g \iff h
func x y = f (g x) (h y)
func = (. h) . f . g
```

Try it out

```
agreeLen :: (Eq a) => [a] -> [a] -> Int
agreeLen x y = length $
   takeWhile (\(a, b) -> a == b) (zip x y)
```

Check your answer at http://pointfree.io/

Typical misuse

Q&A