

3a)

$$\Delta P_t = m_t - m_{t-1} + c(q_t - q_{t-1}) \quad \text{where } m_t - m_{t-1} = u_t \sim N(0,1)$$

$$\text{so, } \Delta P_t = u_t + c(q_t - q_{t-1})$$

$$\gamma_2 = \text{cov}(\Delta P_{t-2}, \Delta P_t)$$

$$= E[\Delta P_{t-2} \Delta P_t]$$

$$= E[(u_{t-2} + c(q_{t-2} - q_{t-3})) \cdot (u_t + c(q_t - q_{t-1}))]$$

$$u_{t-2} + c q_{t-2} - c q_{t-3}$$

$$u_t + c q_t - c q_{t-1}$$

$$= E[u_t \cdot u_{t-2} + c^2(q_{t-2} \cdot q_t - q_{t-2} q_{t-1} - q_{t-3} \cdot q_t + q_{t-3} q_{t-1}) + c(u_{t-2} q_t - u_{t-2} q_{t-1} + u_t q_{t-2} - u_t q_{t-3})]$$

$$= E[\cancel{u_t u_{t-2}}] + c(E[\cancel{u_{t-2} q_t}] - E[\cancel{u_{t-2} q_{t-1}}] + E[\cancel{u_t q_{t-2}}] - E[\cancel{u_t q_{t-3}}]) + c^2(E[\cancel{q_{t-2} q_t}] - E[\cancel{q_{t-2} q_{t-1}}] - E[\cancel{q_{t-3} q_t}] + E[\cancel{q_{t-3} q_{t-1}}])$$

$$= 0 + c(0) + c^2(0)$$

$$\boxed{\gamma_2 = 0}$$

When  $l \geq 2$ , you will never have a  $q$  from the same period again (ex: will never have  $q_{t-l} \cdot q_{t-l}$  when  $l \geq 2$ )

Therefore, the expected values will always evaluate to 0.

$$\boxed{\text{Thus, } \gamma_l = 0 \text{ for all } l \geq 2}$$