# Accelerating Joins with Filters

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### **Abstract**

In query optimization on star schemas, lookahead information passing (LIP) is a strategy exploiting the efficiency of probing succinct filters to eliminate practically all facts that do not appear in the final join results before performing the actual join. Assuming data independency across all columns in the fact table, LIP achieves efficient and robust query optimization. We present LIP-k, a variant of LIP that only remembers the hit/miss statistics for the previous k batches, achieving empirically efficient query execution on fact table with correlated and even adversarial data columns. We implemented LIP and LIP-k on a skeleton database on top of Apache Arrow and analyze the performance of each variant of LIP using the notion of competitive ratio in online algorithms.

### 1 Introduction

Performing join operations in database management systems using Star Schemas is a fundamental and prevalent task in the modern data industry. Continuous efforts have been spent on building a reliable query optimizer over the last few decades. However, the current optimizers may still produce disastrously inefficient query plans which involves processing unnecessarily gigantic intermediate tables [1, 4]. The *lookahead Information Passing (LIP)* strategy aggressively uses Bloom Filters to filter the fact tables to effectively reduce the sizes of the intermediate tables, provably as efficient and robust as computing the join using the optimal query plan [5]. The key idea behind LIP is to estimate the filter selectivity of each dimension table and adaptively reorder the sequence of applying the filters to the fact table.

The filtering process can be modeled as the LIP problem in an online setting: Suppose we fix n filters, and the tuples in the fact table arrives in an online fashion. Upon arrival of each tuple, one has to decide a sequence of filters to probe the tuple, with an objective of minimizing the number of probes needed to decide whether to accept the tuple and forward it to the hash join phase, or to eliminate it. A mechanism deciding the sequence of applying the filters is thus crucial to the success of LIP. If a tuple passes all filters, *all* mechanisms have to probe the tuple to all filters to confirm its passage; and if a tuple is eliminated by the filters, the *optimal* mechanism would apply any filter that rejects the tuple in the first place, using only one probe. Thus given any fact table F, the number of probes that an optimal mechanism requires to process all tuples in the fact table can be readily computed:

$$OPT(F) = n|F_{pass}| + |F_{reject}|,$$

where  $|F_{pass}|$  and  $|F_{reject}|$  are the number of tuples in F that pass all filters and are rejected in F respectively. For any mechanism  $\mathcal{M}$ , denoted by  $ALG_{\mathcal{M}}(F)$  the number of probes that  $\mathcal{M}$  performed to process all tuples in the fact table. The performance of any mechanism  $\mathcal{M}$  can thus be measured by

$$\max_{F} \frac{ALG_{\mathcal{M}}(F)}{OPT(F)},$$

called the *competitive ratio* of  $\mathfrak{M}$ . The competitive ratio is always at least 1 by definition, and in this problem the competitive ratio is at most  $\mathfrak{n}$ , the number of filters, since one mechanism can probe each tuple to at most  $\mathfrak{n}$  filters.

This project aims at designing efficient LIP mechanisms and measure their performance in terms of their overall running time and competitive ratio. We will build a skeleton database system on top of Apache Arrow supporting LIP and hash-joins to conduct our experiments and test the performance of our variant LIP mechanisms against the hash-join and the original LIP. We also present a theoretical result showing that no deterministic mechanism can have a competitive ratio better than n, and discuss possible extensions of LIP to use randomness to design a better mechanism.

## 2 Lookahead Information Passing (LIP)

In this section, we first present the LIP strategy in [5], and then discuss our variant LIP-k, designed to respond to local skewness more quickly than LIP. Finally, we discuss the competitive ratios of all deterministic mechanisms and provide proof on its lower bound. Some possible extensions of LIP using randomness is also discussed.

### 2.1 LIP

The LIP strategy has three stages: (1) Building a hash table and a filter for each dimension table, (2) probe each fact tuple on the filters, producing a set of fact tuples with false positives, and (3) probe the hash table of each dimension table to eliminate the false positives. In what follows we mainly discuss stage (2) since stages (1) and (3) are readily implemented by either the database engine or the filter constructors.

Let F be the fact table and  $D_i$  the dimension tables for  $1 \le i \le n$ . We denote the number of facts in F and each  $D_i$  as |F| and  $|D_i|$ . A LIP filter on  $D_i$  is implemented using a Bloom filter, with false positive rate  $\epsilon$ . The true selectivity  $\sigma_i$  of  $D_i$  on fact table F is given by  $\sigma_i = |D_i \bowtie_{pk_i = fk_i} F|/|F|$ , where  $pk_i$  is the primary key of  $D_i$  and  $fk_i$  is the foreign key of  $D_i$  in F. The LIP-join algorithm, depicted in Figure 1, computes the indices of tuples in F that pass the filtering of each Bloom filter of  $D_i$ . Note that there is an innate false positive rate  $\epsilon$  associated with each Bloom Filter, and thus the set of indices is a superset of the true set of indices of tuples appearing in the final join result.

The partition in [5] satisfies that  $|F_{t+1}| = 2|F_t|$  at line 5, and the algorithm approximates the true selectiveness  $\sigma_i$  of each dimension  $D_i$  using pass[i]/count[i], the aggregated selectiveness since the beginning.

### **2.2** LIP-k

LIP strategy in Figure 1 estimates the selectivity of each filter using statistics from the beginning batch, which is inefficient for certain distribution or physical layout of data. Consider some filter f that is very selective for the first  $t_0$  iterations at line 6 and not selective for the remaining iterations. (For example, a filter f filtering for year  $\geq 2017$  and the Date table is sorted in year.) In this case, LIP would obtain a good estimate of the selectivity of f during the first  $t_0$  iterations, and thus tend to apply f early in the remaining iterations. However, it is more efficient to postpone applying f in the remaining iterations, despite f has good selectivity in the first  $t_0$  iterations. One remedy to this is to only "remember" the hit/miss statistics of each filter over the previous k batches.

Empirical data shows that for the original SSB dataset and certain queries, LIP-k is as fast as LIP, and for certain datasets and queries LIP-k is faster than LIP. Detailed empirical data are presented and analyzed in Section 4.

```
PROCEDURE: LIP-join
Input: a fact table F and a set of n Bloom filters f_i for each D_i with 1 \leqslant i \leqslant n
OUTPUT: Indices of tuples in F that pass the filtering
1. Initialize I = \emptyset
2. foreach filter f do
         count[f] \leftarrow 0
3.
         pass[f] \leftarrow 0
4.
5. Partition F = \bigcup_{1 \le t \le T} F_t.
6. foreach fact block Ft do
7.
         foreach filter f in order do
             foreach index j \in F_t do
8.
9.
                  count[f] \leftarrow count[f] + 1
                  if f contains F<sub>t</sub>[j]
10.
                      I \leftarrow I \cup \{i\}
11.
                      pass[f] \leftarrow pass[f] + 1
12.
         sort filters f in nondesending order of pass[f]/count[f]
13.
14. return I
```

Figure 1: The LIP algorithm for computing the joins.

### 2.3 Competitive Ratio Analysis

The LIP strategy and its variant LIP-k depicted in Figure 1 and 2 are *deterministic*, i.e. multiple executions over the same fact table would produce the same result. Experimental results show that LIP performs almost optimally compared to the performance of hash join in the optimal sequence [5] on the benchmark dataset, in which the keys are distributed almost uniformly. However, it can be shown that deterministic mechanism in the worst case can never achieve a competitive ratio less than n, when played against an adversary producing an adversarial dataset.

**Theorem 2.1.** Let n be the number of filters in the LIP problem. There is no deterministic mechanism  $\mathfrak{M}$  achieving a competitive ratio less than n for the LIP problem.

*Proof.* We present an adversary to the mechanism  $\mathfrak{M}$  such that  $\mathfrak{M}$  only achieves a competitive ratio of  $\mathfrak{n}$  in the worst case. Let the  $\mathfrak{n}$  filters be  $f_1, f_2, \ldots, f_n$  and consider  $\mathfrak{n}$  tuples  $t_1, t_2, \ldots, t_n$ , where  $t_i \notin f_i$  but  $t_i \in f_j$  for any  $i \neq j$ .

The adversary proceeds as follows: It first observes the sequence of filters  $\sigma_t$  at any step t set by the mechanism  $\mathcal{M}$ , and produce the input  $f_{\sigma_t(n)}$  to the mechanism  $\mathcal{M}$ . Thus the mechanism  $\mathcal{M}$  would require n filter probes to eliminate  $f_{\sigma_t(n)}$  at each step t, whereas the optimal sequence is to apply  $\sigma_t(n)$  at the first place. Thus it yields a competitive ratio of n.

It might be possible to design a randomized mechanism  $\mathfrak{M}_{\sqrt{}}$  that can achieve a better competitive ratio than n. The randomized mechanism would, at the end of each batch, select a sequence of applying the filters from a distribution of all filter permutations, based on the estimated selectivities. However, we have not obtained any algorithmic upper bound on the competitive ratio.

```
PROCEDURE: LIP-k
INPUT: a fact table F and a set of n Bloom filters f_i for each D_i with 1 \le i \le n
OUTPUT: Indices of tuples in F that pass the filtering
1. Initialize I = \emptyset
   foreach filter f do
3.
        Initialize count[f] \leftarrow 0, pass[f] \leftarrow 0
4.
        Initialize count_queue[f] with k zeros and pass_queue[f] with k zeros.
5. Partition F = \bigcup_{1 \le t \le T} F_t.
    foreach fact block Ft do
        foreach filter f in order do
7.
            foreach index j \in F_t do
8.
9.
                 count[f] \leftarrow count[f] + 1
10.
                 if f contains F<sub>t</sub>[j]
11.
                     I \leftarrow I \cup \{i\}
12.
                     pass[f] \leftarrow pass[f] + 1
13.
            count_queue(f).dequeue() and pass_queue(f).dequeue()
14.
            count_queue[f].enqueue(count[f]) and pass_queue[f].enqueue(pass[f])
15.
            Reset count[f] \leftarrow 0, pass[f] \leftarrow 0
        sort filters f in nondesending order of sum(pass_queue[f])/sum(count_queue[f])
16.
17. return I
```

Figure 2: The LIP algorithm for computing the joins.

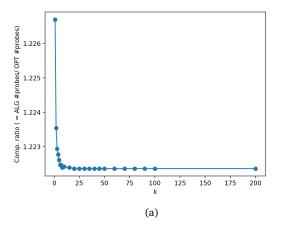
In the practical perspective however, one wishes to minimize the total running time of the mechanism  $\mathfrak{M}$ , which is effectively the sum of the running time of the mechanism and the running time of building the filters and performing the probes. A trade-off between having a near optimal mechanism that consumes much time and allowing many failed probes to eliminate each non-participating tuple is therefore of much interest.

# 3 Database Implementation

We have developed a prototype database system supporting basic join/select operations on star schemas sufficient to benchmark the performance of LIP and its variants on top of Apache Arrow. We assume that the fact table schema contains foreignkeys to all dimension tables, and each dimension table is single-key. Given a star schema fact table F and dimension tables  $D_i$  for  $1 \le i \le n$ , a join query in our system specifies selectors  $\sigma_F$  for F and  $\sigma_i$  for each  $D_i$ , and executing that query will return  $\sigma_F(F) \bowtie \sigma_1(D_1) \bowtie \ldots \bowtie \sigma_n(D_n)$ , projected on the schema of F.

The supported premitive selectors are comparison with integer/string values (=,  $\leq$ ,  $\geq$ , <, >) and between, where the semantic of BETWEEN ( $\ell$ , h) is to select all x with  $\ell \leq x \leq h$ . The selectors for each dimension can be either a premitive selector, or a composition (logical AND and OR) of multiple primitive/composite selectors. This is implemented using the Composite design pattern.

The hash join algorithm first produces a hash table  $T_i$  for each  $\sigma_i(D_i)$ , projected on the  $k_i$ , and then probe each tuple in the fact table against all  $T_i$ . We used Sparseepp (accessible at https://github.com/greg7mdp/sparsepp)



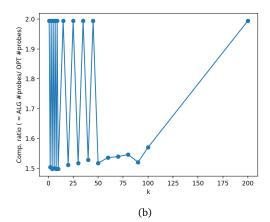


Figure 3: The competitive ratios of LIP-k against different k values. We ran LIP-k on uniform data and skewed (and adversarial) dataset to produce (a) and (b) respectively. The data point at k = 200 represents LIP (which is essentially LIP- $\infty$ ).

as our implementation of the hash table, in which the sparsehash by Google (accessible at https://github.com/sparsehash/sparsehash) is used as the underlying hash function. All primary keys are regarded as 64-bit integers.

The succinct filter structure we choose is the Bloom filters. The default false-positive rate is set to 0.001 and the default number of inserts to the filter is set to 50,000. The hash function for the Bloom Filter is Knuth's Multiplicative hash function, extended to accept a 64-bit integer as a seed.

Our code is available at https://github.com/NicholasCorrado/CS764.

# 4 Empirical Results

In this section we present the empirical results obtained from running Hash-join, LIP and LIP-k on several datasets. In Section 4.1, we present the dataset we used and how we manually apply skewness to generate skewed and adversarial datasets; in Section 4.2 we present the running time of multiple strategies and discuss their performance; and in Section 4.3 we discuss how k affects the competitive ratio of LIP-k empirically on our dataset.

#### 4.1 Skewed and Adversarial Datasets

The dataset for testing is obtained from the Star Schema Benchmark [3]. We will hard-code each queries in [3] to measure the join processing time.

### 4.2 Execution Time

### 4.3 Competitive Ratio

We ran LIP-k on each skewed dataset we produced and compute the competitive ratio of each LIP-k by taking the maximum of the competitive ratios achieved across all queries in all datasets. The results are depicted in Figure 3.

When the keys in the fact table columns are distributed uniformly, the filters need not to react to the local changes. Hence for LIP with higher k, it remembers more batches in the uniform data, therefore may produce relatively more accurate estimate of the selectivities than the LIP with lower k. Hence the competitive ratio would decrease (slightly) when k increases, as depicted in Figure 3.

Figure 3 (b) displays how an adversarial dataset can make LIP-k and LIP perform inefficiently. In fact, each LIP-k with even k achieves an approximation ratio less than 2; LIP and LIP-k with odd k achieve an approximation ratio of almost 2 precisely at Query 3.2 in dataset date-part-adversary. Query 3.2 has two joins, and thus the performance of LIP-k with even k matches the worst case competitive ratio. By construction of date-part-adversary, the first batch has  $\sigma_1^1 = 2/5$  and  $\sigma_2^1 = 3/5$ , and each batch  $\sigma_2^2 = 1$ ; and each batch  $\sigma_2^2 = 1$  and  $\sigma_2^2 = 1$  and  $\sigma_2^2 = 1$  and  $\sigma_2^2 = 1$ .

For LIP-k with odd k, it always contains one more odd (or even) batch than the other, and thus the estimated selectivity and the filtering sequence are in favor of the majority batch type, resulting in a false prediction in the next batch, yielding a competitive ratio of 2. For LIP-k with even k, at even sized batches, the estimated selectivities remain the same (1/2 by construction) throughout the execution, and thus the sequence of applying filter is never changed, once determined after the first batch. Thus for half batches it is optimal, and for the other half it is worse, resulting a competitive ratio of

$$\frac{1 \times 1/2 + 2 \times 1/2}{1} = 1.5,$$

as depicted in Figure 3. For LIP, since it remembers the statistics from the beginning, by construction it would also make the same decision as LIP-k with odd k, losing at every batch. <sup>1</sup>

### 5 Future Works

# 6 Concluding Remarks

The contributions of this project come in two-folds: We implemented Hash-join and LIP on top of Apache Arrow and thus provided an interface for future integration of Hustle on Apache Arrow; and we proposed LIP-k, a variant of LIP, which opens up an area for improving the performance LIP. It would also be interesting to study the problem of LIP in the online algorithmic setting to design an efficient mechanism utilizing randomness with better worst case guarantees.

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<sup>&</sup>lt;sup>1</sup>Does this mean  $\infty$  is odd?

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