



Figure 1. Labeled Plot of Problem 1's Orbit Transfer

```
% This is the code for HW2 - Problem 1
% By Nicholas Luis (PSU ID 930841391)
```

```
clear; clc; close all;
```

```
% Constants
MU = 398600; %  $\text{km}^3 / \text{s}^2$ 
PI = 3.141592654;
```

```
% Departure Orbit
a1 = 8000; % km
e1 = 0.01;
```

```

f1 = 30; % degrees
r1 = getRadius(a1, e1, f1);
v1 = getVelo(r1, a1); % velocity at point 1 (on departure orbit)

% Arrival Orbit
a2 = 27000; % km
e2 = 0.6;
f2 = 210; % degrees
r2 = getRadius(a2, e2, f2);
v2 = getVelo(r2, a2); % velocity at point 2 (on arrival orbit)

% Transfer Orbit
delta_f = f2-f1;
a_T = get_aMin(r1, r2, delta_f);
p_T = getPT(a_T, r1, r2, delta_f);
e_T = (p_T / r1) -1;
v1T = getVelo(r1, a_T); % velocity at point 1 (on transfer orbit)
v2T = getVelo(r2, a_T); % velocity at point 2 (on transfer orbit)
t = PI * sqrt((a_T^3) / MU); % Transfer time

% Delta V
dV1 = abs(v1T - v1);
dV2 = abs(v2T - v2);

%% Plotting Values
fvec = 0:0.1:360; % Creates a list of true anomaly values to iterate through (in degrees)

% X Y values. Note that (0,0) will be located on the Earth
r1vec = (a1*(1-e1^2)) ./ (1+e1*cosd(fvec)); % List of the radii of the departure orbit
xvec1 = r1vec.*cosd(fvec); % List of the x coordinates of the departure orbit
yvec1 = r1vec.*sind(fvec); % List of the y coordinates of the departure orbit

rTvec = (a_T*(1-e_T^2)) ./ (1+e_T*cosd(fvec)); % List of the radii of the transfer orbit
xvecT = rTvec.*cosd(fvec); % List of the x coordinates of the transfer orbit
yvecT = rTvec.*sind(fvec); % List of the y coordinates of the transfer orbit

r2vec = (a2*(1-e2^2)) ./ (1+e2*cosd(fvec)); % List of the radii of the arrival orbit
xvec2 = r2vec.*cosd(fvec-30); % List of the x coordinates of the arrival orbit
yvec2 = r2vec.*sind(fvec-30); % List of the y coordinates of the arrival orbit

```

```

figure(1)
hold on
plot(xvec1, yvec1, LineWidth=2)
plot(xvec2, yvec2, LineWidth=2)
plot(xvecT(1:1801), yvecT(1:1801), ':', LineWidth=2) % Only plotting half of the transfer
orbit
title('Two-Impulse Minimum Energy Orbit Transfer')
xlabel("x (km)")
ylabel("y (km)")
legend('Departure Orbit', 'Arrival Orbit', 'Transfer Orbit')
hold off

```

```

exportgraphics(gca,"HW2_Problem1_Figure.jpg");
%% Functions
function radius = getRadius(a_input, e_input, f_input)
    p = a_input * (1 - (e_input^2));
    radius = p / (1+e_input*cosd(f_input));
end

```

```

function aMinT = get_aMin(r1_in, r2_in, df)
    % This function gets the semimajor axis of minimum energy transfer
    % orbit given r1, r2, and the change in f
    sqrtTerm = sqrt( r1_in^2 + r2_in^2 - 2*r1_in*r2_in*cosd(df) ) ;
    aMinT = 0.25 * (r1_in + r2_in + sqrtTerm);
end

```

```

function P_output = getPT(amin, r1_in, r2_in, df)
    % This function gets the semilatus rectum of a transfer orbit given r1,
    % r2, and the change in f
    k = r1_in*r2_in*(1-cosd(df));
    m = r1_in*r2_in*(1+cosd(df));
    l = r1_in + r2_in;

    P_output = (k*m - 2*amin*k*l) / (4*amin*m - 2*amin*l);

end

```

```

function velo = getVelo(r_input, a_input)
    % This function gets the velocity using energy given MU, r, and a
    MU = 398600; % km^3 / s^2

```

```
    velo = sqrt(2 * MU * ( 1/r_input) - (1 / (2*a_input)) );  
end
```