

FPGA Development for the LHCb Vertex Locator Upgrade

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Abstract

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1 Introduction

1.1 The Standard Model of Particle Physics

Central to the modern age of particle physics in the standard model,

$$\begin{aligned}
L_{GWL} = & \sum_f (\bar{\Psi}_f (i\gamma^\mu \partial_\mu - m_f) \Psi_f - e Q_f \bar{\Psi}_f \gamma^\mu \Psi_f A_\mu) + \frac{g}{\sqrt{2}} \sum_i (\bar{a}_L^i \gamma^\mu b_L^i W_\mu^+ + \bar{b}_L^i \gamma^\mu a_L^i W_\mu^-) \\
& + \frac{g}{2x_w} \sum_f \bar{\Psi}_f \gamma^\mu (I_f^3 - 2s_w^2 Q_f - I_6 e_f \gamma_5) \Psi_f Z_\mu - \frac{1}{4} |\partial_\mu A_v - \partial_v A_\mu - ie(W_\mu^- W_v^+ - W_\mu^+ W_v^-)|^2 \\
& - \frac{1}{2} |\partial_\mu W_v^+ - \partial_v W_\mu^+ - ie(W_\mu^+ A_v - W_v^+ A_\mu) + ig' c_w (W_\mu^+ Z_v - W_v^+ Z_\mu)|^2 \\
& - \frac{1}{4} |\partial_\mu Z_v - \partial_v Z_\mu + ig' c_w (W_\mu^- W_v^+ - W_\mu^+ W_v^-)|^2 - \frac{1}{2} M_\eta^2 \eta^2 - \frac{g M_\eta^2}{8 M_W} \eta^3 - \frac{g'^2 M_\eta^2}{32 M_W} \eta^4 \\
& + |M_W W_\mu^+ + \frac{g}{2} \eta W_\mu^+|^2 + \frac{1}{2} |\partial_\mu \eta + i M_Z Z_\mu + \frac{ig}{2c_w} \eta Z_\mu|^2 - \sum_f \frac{gm_f}{2M_W} \bar{\Psi}_f \Psi_f \eta. \quad (1)
\end{aligned}$$

The standard model, shown in equation 1, is a quantum field theory that describes the fundamental particles and how they interact. While this essay does require, or attempt, to understand the intricate detail of the standard model; the aim of many particle physics experiments is to Test, measure and verify the model. Despite being the current best theory to explain particle interactions, the model is not complete. There are many undescribed phenomena, such as the matter domination in the universe, that require physics beyond the standard model. To that end, major international efforts, namely in the form of the Large Hadron Collider, aim to further knowledge and understanding of the underlying physics of the universe. [1]

1.2 The LHCb Experiment

One such Experiment and the Large Hadron Collider is Large Hadron Collider beauty (LHCb). Located at intersection point

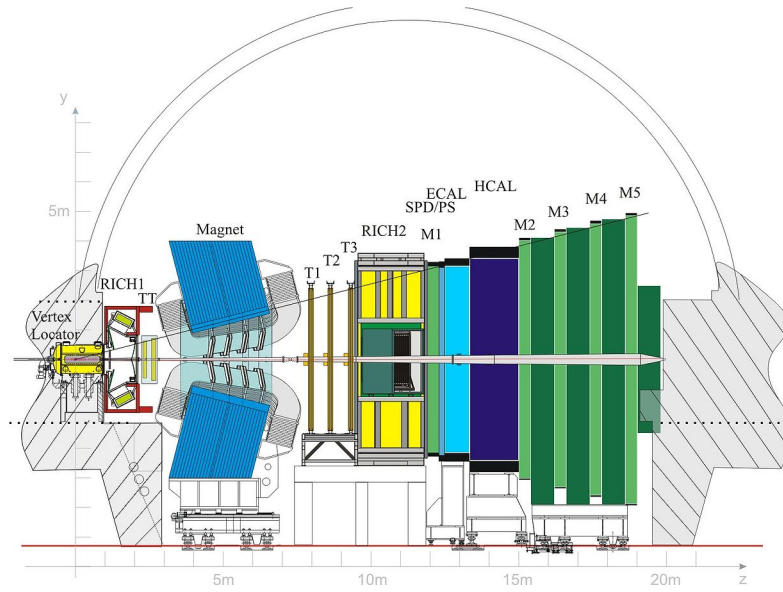


Figure 1: The LHCb Detector along the bending plane.

1.2.1 The Detector

1.2.2 Physics Studied at LHCb

1.2.3 VELO Upgrade

1.3 FPGAs in Particle Detectors

1.3.1 Field Programable Gate Arrays

1.3.2 The Role of FPGA's in the VELO Upgrade

2 Scrambling Algorithms

Due to radiation levels inside the detector chamber, the main data processing takes place in a concrete bunker away from the detector, minimising radiation damage to the hardware. To facilitate this, optical links, 20 per modular, are used to transfer the data from the front end VELO to the Data Acquisition FPGA (DAQ). When communicating data digitally, the transferring modular (TX) and the receiving modular (RX) must have synchronised clocks. When achieving this, there are three main approaches:

- I. Synchronise both the TX and RX from a single central clock.
- II. Transmit the TX clock to the RX modular.
- III. Use bit-changes in the data to continuously synchronise the RX clock.

The two former of these options, although the most convenient, are not appropriate for the VELO as they are susceptible to unforeseen delays that could cause desynchronisation. The latter, while less susceptible to delays, requires data with a high density of transitions to reduce the likelihood of a desynchronisation event. Because delays in the data are possible, the latter option has been selected.

2.1 The Role of Scrambling Data in the VELO

For the reasons described in Section 2, it is necessary to ensure that the data has large density of transitions before being transmitted from the front-end detector to the DAQ modular. However, as the majority of SP hitmaps are empty, the data has a large bias towards 0s. This reduces the frequency of transitions in the data - increasing the probability of a desynchronisation event. It is therefore necessary to scramble the data prior to transmission and descramble the data in the DAQ FPGA.

Scrambling and later descrambling the data is not a trivial exercise. The scrambling (TX) modular and descrambling (RX) modular must use a synchronised 'key', derived from the previous states of the data. There are two options when generating this 'key':

Additive The 'key' is generated by evolving the previous 'key' at each iteration of data using the incoming frame.

Multiplicative The 'key' is generated from the previous n frames. (Here n is a variable specific to the algorithm).

2.2 Scrambler Options

Three scrambling algorithms have been considered:

Additive Scrambler

This algorithm is simple and easy to use, however has the drawback of time dependence. If a desynchronisation event occurs, all subsequent data is rendered unrecoverable until such time as a global reset signal is sent. Further adding to the drawbacks, if a data packet is not sent from the TX during any clock cycle the RX descrambler will still evolve its descramble key - the TX scrambler, however, will not. This will ofcourse desynchronise the ‘keys’, and as before all subsequent data is lost.

Intermediate Scrambler

Deriving its name from being the second algorithm under consideration, the Intermediate Scrambler is a **multiplicative** algorithm. The ‘key’ is generated from the current incoming frame and the previous frame. Therefore, in the event of desynchronisation, only two frames are lost before the ‘key’ is automatically recovered. This is a significant improvement over the Additive Scrambler.

VeloPix Scrambler

Named as, at the time of the start of the project (*September 2015*), this algorithm is the current preferred option by the VeloPix team; this too is a **multiplicative** algorithm. The ‘key’ is, again like the Intermediate Scrambler, generated from the current and previous data frame. The VeloPix Scrambler differs from the Intermediate scrambler as it aims to more efficiently scramble the data.

2.3 Algorithm Analysis

Intuitively, one can assume that fully scrambled data will be indistinguishable from randomly generated data. For this reason, the three algorithms are not only tested against each other and the pre-scrambled data but also randomly generated binary. The randomly generated data was created using the Python ‘random’ library, selecting a ‘0’ or ‘1’ with probability 1/2 each. While the Python ‘random’ library is only pseudo-random, on the scale of this example (i.e. $> 100,000$ frames), this is by far sufficient.

More mathematically rigorous, however, is to evaluate the system abstractly in the framework of statistical physics. In this abstraction, the ensemble is the 120 bit frame (with the header and parity removed); microstates are the particular form of the frames; and macroscopic quantities can be calculated by averaging a large number of frames (i.e. the desync data). For the analysis outlined in section 2.3.1, predictions will be made using these principles and outlined in section 2.3.2.

In the context of the statistical model, it is reasonable to consider the degree of ‘*scrambled-ness*’ as entropy. Therefor a scrambled system can be assumed to one of maximum entropy; and from Boltzmans law,

$$S \sim \ln(\Omega) \quad (2)$$

where Ω is the number of microstates associated with the macrostate, we learn that this state of maximum entropy is a macrostate with the maximum number of associated microstates.

2.3.1 Measurements of the Algorithms

To compare the effecincy of the three algorithms in section 2.2, the algorithms where run over the same unput data and compared for the following measures:

Number of Transitions Per Frame

This measure counts the total number of bit transitions (i.e. $bit(n) \neq bit(n-1)$) in a 120 bit frame. The header and parity information was not included as they are not scrambled. This is an important test as one of the roles of the scrambler is to maximise the number of transitions.

Common Bit Chain Length

One of the downfalls of the ‘Number of Transitions Per Frame’ analysis is that the two 20 bit frames,

a) 10101010101111111111

b) 10011001100110011001

both with 10 transitions, will be considered equal. However, (b) is clearly a more suitable output for data transfer as (a) has a large probability of desynchronised due to the long chains of ‘1’s. It is therefore also nessecary to evaluate the length of common bit chains within the scrambled data.

Total Bit Frequancy

Pre-scramble, the data had a large bais towards ‘0’s due to the majority of the hitmaps being empty. Scrambled data, via entropic arguments, *should* show zero bias eitherway. Therefor, by investigating how the number of ‘1’s - ‘0’s evolves over many frames, any bias in the scrambler can be found.

166 2.3.2 Statistical Predictions

Number of Transitions Per Frame

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Consider a particle in a symmetric, discrete time-dependent, two state system,

$$p_0(t) = p_1(t) = 0.5 \quad : \quad \forall t \in \mathbb{N} \quad (3)$$

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At each time iteration,

$$p_{i \rightarrow j}(t) = p_{i \rightarrow i}(t) = 0.5 \quad : \quad i, j = [0 \ 1], \quad \forall t \in \mathbb{N} \quad (4)$$

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However, as $p_{1 \rightarrow 0}(t)$ is equal in both probability and importance to $p_{0 \rightarrow 1}(t)$, the probability of a bit change shall herefore be referred to as $p_t(t)$.

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Over a n step process, analogous to a n bit frame, the probability distribution of the number of transitions N_t is given by Binomial statistics,

$$f(N_t) = \frac{n!}{N_t!(n - N_t)!} p^{N_t} (1 - p)^{n - N_t} \quad (5)$$

Simplified for the special case $p = p_t = 0.5$,

$$f_t(N_t) = \frac{n!}{N_t!(n - N_t)!} (p_t)^n \quad (6)$$

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For $n = 120$, we can calculate,

$$\langle N_t \rangle^{Binomial} = \sum_{N_t=0}^{n-1} N_t f(N_t) = n p_t = 60 \quad (7)$$

$$\sigma_{N_t}^{Binomial} = \sqrt{n p_t^2} = 5.48 \quad (8)$$

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Furthermore, when considering the entropic argument in section 2.2 equation 2, the number of microstates corresponding to each macrostate N_t can be related to equation 6,

$$\Omega_t \sim \frac{n!}{N_t!(n - N_t)!} \quad (9)$$

$$\langle N_t \rangle^{Entropic} = MAX[S_t] = MAX[\Omega_t] \quad (10)$$

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This can be numerically solved,

$$\langle N_t \rangle^{Entropic} = 60 \quad (11)$$

Common Bit Chain Length

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The probability of a chain of length n is,

$$p_n = (1 - p_t)^n \quad (12)$$

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As $p_t = 0.5$,

$$p_n = (p_t)^n \quad (13)$$

Therefore, the proportion of chains of length

$$\text{addsomeeqnhere} \quad \text{whataboutthis?} \quad (14)$$

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Total Bit Frequency

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2.3.3 Results of Analysis

2.4 Conclusion

190 **3 Event Isolation Flagging**

3.1 Motivation

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5 Conclusion

200 6 Acknowledgments

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References

- ²⁰⁴ [1] Cern. *The Standard Model*. 2015. URL: <http://home.cern/about/physics/standard-model>.