

# FPGA Development for the LHCb Vertex Locator Upgrade

Nicholas Mead  
8064141  
School of Physics and Astronomy  
University of Manchester

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## Abstract

This document discusses two areas of FPGA development for the LHCb VELO upgrade scheduled to coincide with LHC Long Shutdown 2 in 2019.

The analysis for three scrambling algorithms, required for data transfer from the front end electronics to the Data Acquisition FPGA, was compared against the theoretical form of scrambled data. This was found that the currently implemented VeloPix scrambler is the optimum of the choices but also that an alternative multiplicative scrambler was suitable for computer simulations.

Current development of an Event Isolations Flaging system is discussed. This system is intended to identify and flag the easier to re-construct events in order to reduce event pill-up in the computer network. While a bug is identified in the simulated data, the VHDL development has continued and is ongoing.



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# 1 Introduction

## 1.1 The Standard Model of Particle Physics

Central to the modern study of particle physics is the standard model,

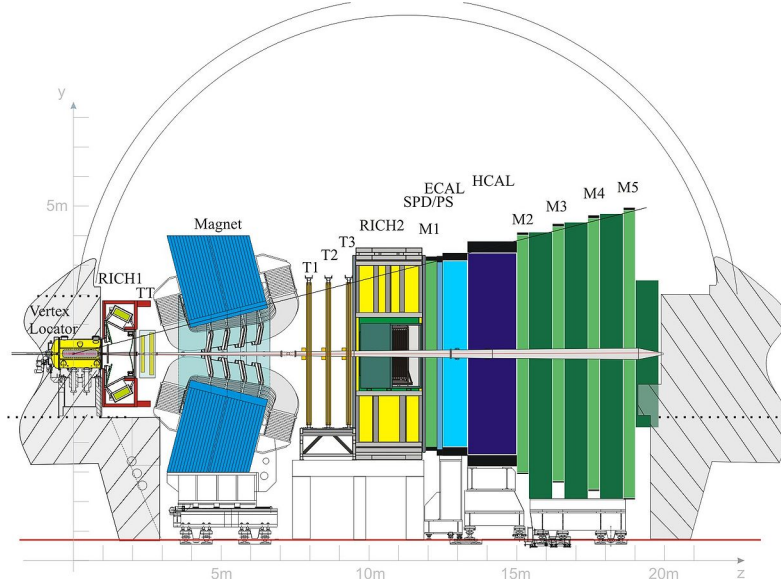
$$\begin{aligned}
L_{GWL} = & \sum_f (\bar{\Psi}_f (i\gamma^\mu \partial_\mu - m_f) \Psi_f - e Q_f \bar{\Psi}_f \gamma^\mu \Psi_f A_\mu) + \frac{g}{\sqrt{2}} \sum_i (\bar{a}_L^i \gamma^\mu b_L^i W_\mu^+ + \bar{b}_L^i \gamma^\mu a_L^i W_\mu^-) \\
& + \frac{g}{2x_w} \sum_f \bar{\Psi}_f \gamma^\mu (I_f^3 - 2s_w^2 Q_f - I_6 e_f \gamma_5) \Psi_f Z_\mu - \frac{1}{4} |\partial_\mu A_\nu - \partial_\nu A_\mu - ie(W_\mu^- W_\nu^+ - W_\mu^+ W_\nu^-)|^2 \\
& - \frac{1}{2} |\partial_\mu W_\nu^+ - \partial_\nu W_\mu^+ - ie(W_\mu^+ A_\nu - W_\nu^+ A_\mu) + ig' c_w (W_\mu^+ Z_\nu - W_\nu^+ Z_\mu)|^2 \\
& - \frac{1}{4} |\partial_\mu Z_\nu - \partial_\nu Z_\mu + ig' c_w (W_\mu^- W_\nu^+ - W_\mu^+ W_\nu^-)|^2 - \frac{1}{2} M_\eta^2 \eta^2 - \frac{g M_\eta^2}{8 M_W} \eta^3 - \frac{g'^2 M_\eta^2}{32 M_W} \eta^4 \\
& + |M_W W_\mu^+ + \frac{g}{2} \eta W_\mu^+|^2 + \frac{1}{2} |\partial_\mu \eta + i M_Z Z_\mu + \frac{ig}{2c_w} \eta Z_\mu|^2 - \sum_f \frac{gm_f}{2M_W} \bar{\Psi}_f \Psi_f \eta. \quad (1.1)
\end{aligned}$$

The standard model, shown in equation 1.1, is a quantum field theory that describes the fundamental particles and how they interact. While this report does not require, or attempt, a detailed understanding the intricate detail of the standard model; the aim of many particle physics experiments is to verify, measure and expand the model. Despite being the current best theory to explain particle interactions, the model is not complete. There are many undescribed phenomena, such as the matter domination in the universe, that require physics beyond the standard model in order to be described. To that end, major international efforts, namely in the form of the Large Hadron Collider, aim to gain further knowledge and understanding of the underlying physics of the universe. [1]

## 1.2 The LHCb Experiment

One experiment at the Large Hadron Collider is Large Hadron Collider beauty (LHCb). Located at intersection point 8, LHCb is designed to study rare particle physics phenomena, such as lepton flavour violation and CP violation. The decays studied in the LHCb are via exotic hadronic decays of Bottom or Charm quarks that form short lived hadrons. These hadrons, commonly B mesons, travel in the order of mm's in the detector before decaying. As such, B meson decays can be identified by decay products that propagate via a secondary vertex.

As B mesons are light (in comparison to other particles studied in the LHC), the decay products are produced at a shallow angle relative to the beam pipe; this is the driving factor in the design of the experiment. LHCb is a single arm forward spectrometer. Surrounding the point of collision is the Vertex Locator (VELO), this high precision detector uses silicon strips to detect ionising particles as they propagate from a collision



**Figure 1.1:** The LHCb Detector along the bending plane.

and provides the coordinates of the particle in terms of  $R^1$  and  $\phi^2$ . By reconstructing the paths of particles back to the intersection point, it can be identified whether or not the particular decay products are a product of the primary vertex<sup>3</sup>, or a secondary vertex<sup>4</sup>.

The Rich detector, comprised of two subdetectors either side of the magnet, uses Cherenkov radiation to deduce the velocity of the particle. The silicon trackers, labeled TT and T1-3 in Figure 1.1, calculate the angle deflection by the magnet. By combining the velocity and angle of deflection, the mass, momentum and energy of the particles can be deduced from simple relativistic kinematics.

The muon detectors, labeled M1-5 in Figure 1.1, are important to detect muons. This is of particular importance on LHCb as muons can be easily misidentified as charged pions, due to their similar mass and pions are a common decay product of the interactions studied.

HCAL and ECAL, shown in Figure 1.1, are hadronic and electric calorimeters respectively. Both measure the total energy of incoming particles. As the calorimeters are absorbing the particles they detect, any leptonic particle reaching the M2-5 muon detectors can be assumed to be a muon. Electrons and Photons are absorbed by the ECAL and any Tauons would have decayed long before reaching the far muon detectors.

<sup>1</sup>Radial distance from the beam pipe.

<sup>2</sup>Asumthal angle.

<sup>3</sup>The position at which the protons collided.

<sup>4</sup>The decay point of a short lived particle. i.e. B Meson.

## 1.3 LHCb Upgrade

With the advancements in accelerator technology, the detectors must also advance in order to make best use of the accelerators. The LHC is scheduled to increase its luminosity during Long Shutdown 2 (LS2), and as such LHCb will have to cope with this greater luminosity. The front end electronics of LHCb implement a hardware trigger and this is limited to a 1MHz maximum readout speed. Post LS2, LHCb will have to cope with a luminosity of  $\mathcal{L} = 2.10^{33} \text{cm}^{-2} \text{s}^{-1}$ , this is significantly greater than the current  $\mathcal{L} = 4.10^{32} \text{cm}^{-2} \text{s}^{-1}$ . A simple luminosity increase will not significantly increase that statistics for some statistical error dominated channels. To achieve this, greater resolution of the VELO and fully software triggers are required. Detailed in the ‘*LHCb VELO Upgrade Technical Design Report*’ [2] the main goals of the 2019 upgrade are as follows:

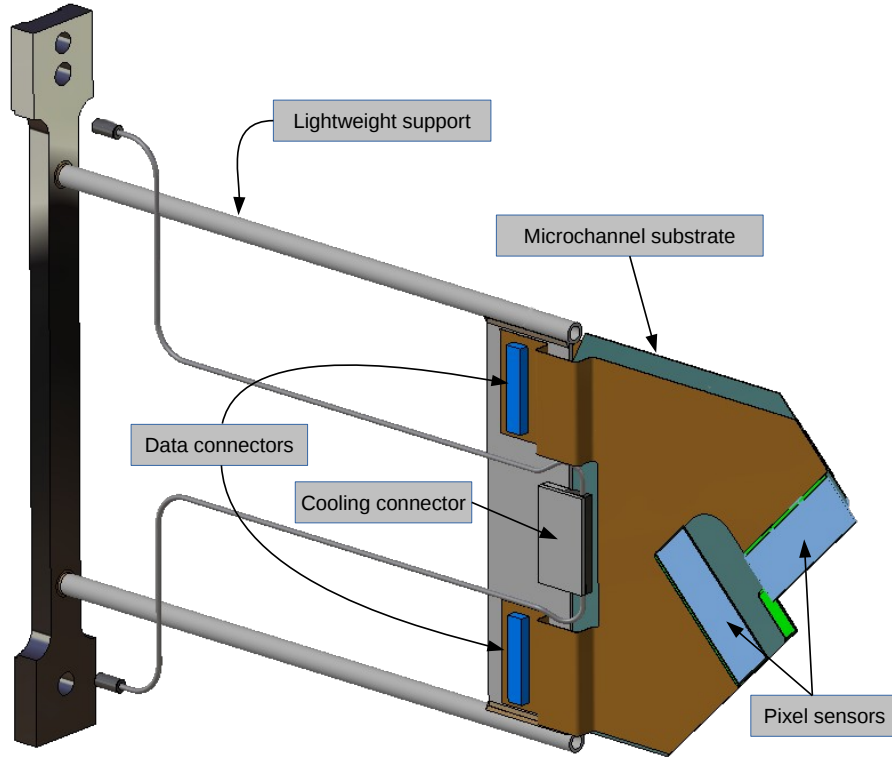
- Increase the luminosity to  $\mathcal{L} = 2.10^{33} \text{cm}^{-2} \text{s}^{-1}$ .
- Read data from the detector at the bunch crossing frequency, 40 Mhz.
- Convert to a fully software based trigger.

### 1.3.1 VELO Upgrade

Common with its predecessor, the upgraded VELO uses thin, retractable modules. The advantage of this approach is that during collisions, the modules can sit closer than otherwise possible to the beam line. The modules retract for the beam fill, avoiding the radiation damage from the wider fill beams. In order to gain greater resolution of secondary vertices, the upgraded VELO will sit at 5.1 mm from the beam at the closest pixel [2]. The current VELO achieves 8 mm [3].

As previously mentioned, the current VELO uses silicon strips to detect particles. The upgraded VELO, however, will use silicon pixels. These pixels,  $55\mu\text{m} \times 55\mu\text{m}$  in size and  $200\mu\text{m}$  thick [2], are arranged in a 256 wide square matrix on a ASIC chip. The pixels are arranged into groups of 8 to form a Super Pixel (SP). The ASIC chips are arranged in a straight configuration of 3 and bonded to a sensor. Each module has 4 sensors, 2 a side, as shown in Figure 1.2. The module is cooled by bi-phase  $\text{CO}_2$  in micro-channels etched into the microchannel substrate.

The VELO modules will operate in the LHC secondary vacuum. It is separated from the primary vacuum by RF foil that is 3.5mm from the beamline, at the closest point [2]. The foil is made of  $250\mu\text{m}$  thick aluminum, it is required to be of this thickness to reduce the interaction with the collision decay products.



**Figure 1.2:** The current module design. Two sensors are shown, the remaining two are mounted to the rear face of the module to for two horizontal rows - covering the right most area of the module (as viewed in the figure).

### 1.3.2 Data Flow and Low Level Interface

Field Programmable Gate Arrays (FPGAs) are extensively used in new technology due to their fast data transfer rates and reconfigurability [4]. FPGAs are used in the Data Acquisition (DAQ) modules for speed and parallel processing capabilities. The DAQ, in its simplest form, is a series of optical links, a data processing FPGA and a PCIe port for data transfer to the VELO computer system.

The data from each SP is packaged in a 30 bit Super Pixel Packet (SPP). The SPP is comprised of a (from most to least significant bits) 9 bit Bunch Cross ID (BCID); 13 bit SPP location information (horizontal and vertical coordinates); 8 bit SP hitmap.

A GWT serialiser forms a 128 bit 'frame' comprising of a header (1010), four single bit parity flags and four SPPs. The parity flags indicate the parity of the four SPPs as a validation check for downstream processes. The data then is transmitted via an electrical to optical converter through optical fibers to the DAQ.

In the DAQ is the Low Level Interface (LLI). The LLI is responsible for sorting the incoming data into time order and packaging the data in the correct form for computer systems to optimise output bandwidth. Other processes included in the LLI are, descrambling and event isolation tagging. These processes will be discussed in more detail later in this document.

## 2 Scrambler

Due to radiation levels inside the detector chamber, the main data processing takes place in a concrete bunker away from the detector. To facilitate this, 20 optical links (per modual) are used to transfer the data from the front end VELO to the DAQ FPGA. When communicating data digitaly, the transferring modual (TX) and the recieving modual (RX) must have syncrinised clocks. In these case, the GWT serialiser is the TX, and the DAQ is the RX. When achieving synchronised clock, there are two main approuches:

- Transmit the TX clock with the data to the RX modual - used in I<sup>2</sup>C and SPI communication.
- Use bit-changes in the data to continuously synchronise the RX clock.

The former of these options, although widely used in convertional electronics, requires a finely tuned clock accounting for all possible delays. The latter, while negating cons of the former, requires data with a high density of tranitions to reduce the likelihood of a desynchronisation event. Becuase delays in the data are possible, the latter option has been selected.

As mentioned, it is nessesary to ensure that the data has large density of transitions before being transmitted from the front-end detector to the DAQ modual. However, as the majority of super pixel hitmaps are empty, the data has a bais towards '0's. This reduces the frequency of transitions in the data - increasing the probability of a desynchronisation event. It is therefor nessecary to scramble the data prior to transmittion and descramble the data in the LLI of the DAQ FPGA.

Scrambling and later descrambling the data is not a trivial exercise. The scrambling (TX) modual and descrambling (RX) modual must use a sycronised 'key', that is used in both the scrambling and descrambling processes. In the FPGA, the 'key' is derived from the previous states of the data. There are two methods when generating this 'key':

**Additive** The 'key' is generated by evolving the previous 'key' at each itteration of data using the incoming frame.

**Multiplicative** The 'key' is generated from the previos  $n$  frames. (Here  $n$  is a variable specific to the algorithm).

### 2.1 Scrambler Options

Three scrambling algorithums have been concidered:

#### Additive Scrambler

This scrambler is was origionally impremented and used two sets of two-input XOR



logic gates. As the name implies, this scrambler used additive key generation which is dependent all previous input frames since the last reset signal.

### Intermediate Scrambler

Created by Karol Hennessy, and deriving its name arbitrarily from the order of consideration, this multiplicative scrambler combines the current and previous frames to generate the *'key'*. Therefor, in the event of desynchronisation, only two frames are lost before the *'key'* is automatically recovered. This feature alone is a significant improvement over the Additive Scrambler.

### VeloPix Scrambler

This is the current implemented scramble algorithm in the DAQ and VeloPix code. Like the Intermediate Scrambler, it uses multiplicative *'key'* generation. However, the VeloPix scrambler is compatible with further constraints enforced by the ASIC, including the number of combinational logic operations. The Intermediate Scrambler was design purely for simulation purposes and as such does not meet these constraints.

## 2.2 Cross Checks

The main priority when scrambling data, is ensuring that the data is recoverable. For all three scramblers, the algorithm was synthesised in Quartus [5] and simulated in Modelsim [6]. The aim of synthesising and simulating the scramblers in these programs was to ensure that the design was both physical in term of on-board logic gates, and to check that the scrambled data was recoverable, respectively.

Furthermore, a C++ simulation was created for the three scramblers. This simulation had two main purposes: firstly to cross check the output of the C++ against the Modelsim simulations; secondly to simulate the scrambler over a much larger sample of data as Modelsim simulations are less time effecient. In attition to the cross checks, the C++ code allowed for the injection of a descnronisation event, in which the *'key'* is lost. As expected, the Additive Scarmbler was unable to recover any data post descnronisation, however the intermediate and VeloPix scarmblers both recovered the *'key'* after two frames and contiinoud to recover data.

## 2.3 Algorithm Analysis

For analytical purposes, it is assumed that fully scrambled data is indistinguishable from randomly generated data. For this reason, the three algorithm are not only tested against eachother and the pre-scrambled QWT data but also randomly generated binary. The randomly generated data was created using the Python *'random'* library, selecting a *'0'* or *'1'* with equal probubility. While the Python *'random'* library is only sudo-random, on the scale of this example (i.e.  $\gg 100,000$  frames), it is by far sufficient.

A more mathematically rigorous aprouch, however, is to evaluate the system abstractly

in the framework of statistical physics. In this abstraction, the 120 bit frame (with the header and parity removed) is considered an ensemble; microstates are the particular form of the frames; and macroscopic quantities can be calculated by averaging a large number of frames. For the analysis outlined in section 2.3.1, predictions will be made using these principles and outlined in section 2.3.2.

In the context of the statistical model, it is reasonable to consider the degree of ‘*scrambled-ness*’ analogous to entropy. This analogy is not dissimilar to the common interpretation of entropy as a measure of disorder. From Boltzmann’s equation for entropy,

$$S \sim \ln(\Omega) \quad (2.1)$$

where  $\Omega$  is the number of microstates associated with the macrostate, we learn that this state of maximum entropy is a macrostate with the maximum number of associated microstates.

The entropic argument of Equation 2.1 is not only mathematically founded. For a scramble algorithm to hold for all possible data sets, it must also be capable of outputting all possible permutations. As such, assuming all possible outputs are equally likely, the count of each macroscopic output will be proportional to the number of microstates associated.

### 2.3.1 Measurements of the Algorithms

To compare the efficiency of the three algorithms in section 2.1, the algorithms were run over the same input data and compared for the following measures:

#### Number of Transitions Per Frame

This measure counts the total number of bit transitions (i.e.  $bit(n) \neq bit(n-1)$ ) in a 120 bit frame. The header and parity information was not included as they are not scrambled. This is an important test as one of the roles of the scrambler is to maximise the number of transitions.

#### Common Bit Chain Length

One of the downsides of the ‘Number of Transitions Per Frame’ analysis is that the two hypothetical 20 bit frames,

a) 10101010101111111111,

b) 10011001100110011001,

both with 10 transitions, are considered equal. However, (b) is clearly a more suitable output for data transfer as (a) has a large probability of desynchronisation due to the long chains of ‘1’s in the right most bits. It is therefore also necessary to evaluate the length of common bit chains within the scrambled data as shorter chains are more suitable for data transfer.

## Bit Asymetry

Pre-scramble, the data had a large bias towards '0's due to the majority of the hitmaps being empty. Scrambled data, via entropic arguments, *should* show zero bias eitherway. Therefor, by investigating how the number of '1's - '0's evolves over many frames, any bias in the scrambler can be found.

### 2.3.2 Statistical Predictions

#### Number of Transitions Per Frame

Consider a particle in a symmetric, discrete time-dependent, two state system,

$$p_0(t) = p_1(t) = 0.5 \quad : \quad \forall t \in \mathbb{N}, \quad (2.2)$$

At each time iteration,

$$p_{i \rightarrow j}(t) = 0.5 \quad : \quad i, j = [0 \ 1], \quad \forall t \in \mathbb{N}. \quad (2.3)$$

However, assuming zero bias and detailed balance, as  $p_{1 \rightarrow 0}(t)$  is equal in both probability and importance to  $p_{0 \rightarrow 1}(t)$ , the probability of a bit change shall herefore be referred to as  $p_\tau(t)$ .

Over a  $n$  step process, analogous to a  $n$  bit frame, the probability distribution of the number of transitions  $N_\tau$  is given by Binomial statistics,

$$f(N_\tau) = \frac{n!}{N_\tau!(n - N_\tau)!} p^{N_\tau} (1 - p)^{n - N_\tau} \quad (2.4)$$

Simplified for the special case  $p = p_\tau = 0.5$ ,

$$f_\tau(N_\tau) = \frac{n!}{N_\tau!(n - N_\tau)!} (p_\tau)^n \quad (2.5)$$

For  $n = 120$ , we can calculate,

$$\langle N_\tau \rangle^{Binomial} = \sum_{N_\tau=0}^{n-1} N_\tau f(N_\tau) = n p_\tau = 60 \quad (2.6)$$

$$\sigma_{N_\tau}^{Binomial} = \sqrt{n p_\tau^2} = 5.48 \quad (2.7)$$

Furthermore, when considering the entropic argument of equation 2.1, the number of microstates corresponding to each macrostate  $N_\tau$  can be related to equation 2.5,

$$\Omega_\tau \sim \frac{n!}{N_\tau!(n - N_\tau)!} \quad (2.8)$$

$$< N_\tau >^{Entropic} = MAX[S_\tau] = MAX[\Omega_\tau] \quad (2.9)$$

256 This can be numerically solved,

$$< N_\tau >^{Entropic} = 60 \quad (2.10)$$

258 While the result of equation 2.10 does not contribute anything new, it is important as a ‘*sanity check*’. Because the system can be described as in section 2.3, it would indicated a problem in the theoretical framework if the result did not match.

## 260 Common Bit Chain Length

262 The probability of a chain of length  $n$  is,

$$p_n = p_1(1 - p_\tau)^{n-1}, \quad : \quad n \in \mathbb{N}, \quad n > 1 \quad (2.11)$$

264 where  $p_1$  is the number of chains of length 1. As  $p_1 = N_0(1 - p_\tau)$ , where  $N_0$  is the total number of chains,

$$\frac{N_n}{N_0} = (1 - p_\tau)^n, \quad : \quad n \in \mathbb{N}, \quad n > 1 \quad (2.12)$$

where  $N_n$  is the number of chains of length  $n$ . Taking the log of both sides,

$$\begin{aligned} \log\left(\frac{N_n}{N_0}\right) &= n \log(1 - p_\tau), \\ \log(N_n) &= n \log(1 - p_\tau) + \log(N_0). \end{aligned} \quad (2.13)$$

266 Therefor, for a graph of  $\log(N_n)$  against  $n$  for a large sample of data, the gradient would be  $\log(1 - p_\tau)$ . In this case, as  $p_\tau = 0.5$ ,

$$\log(1 - p_\tau) = -0.30. \quad (2.14)$$

## 268 Bit Asymetry

270  $A_{1,0}$ , the assymetry of ‘1’s and ‘0’s is defined as,

$$A_{1,0} = N_1 - N_0, \quad (2.15)$$

272 where  $N_1$  and  $N_0$  are the number of ‘1’s and ‘0’s respectively. We can consider the evolution of  $A_{1,0}$  with frame  $t$  of size  $n$  as a stockastic iterative map with zero deterministic growth [7],

$$A_{1,0}(nt + n \Delta t) = A_{1,0}(nt) + \mathcal{N}(nt) \quad (2.16)$$

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Where  $\mathcal{N}$  is an independant random variable picked from a gaussian distribution. While  $A_{1,0}(t) \in \mathbb{Z}$ , in the limit of large  $nt$  we can approximate that  $A_{1,0}$  is continious.

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If we consider the moments of  $A_{1,0}$ ,

$$\langle A_{1,0}(nt = M n \Delta t) \rangle = \sum_{m=0}^{M-1} \mathcal{N}(m n \Delta t), \quad (2.17)$$

$$\begin{aligned} \langle A_{1,0}(nt = M n \Delta t)^2 \rangle &= \sum_{m=0}^{M-1} \sum_{m'=0}^{M-1} \mathcal{N}(m n \Delta t) \mathcal{N}(m' n \Delta t) \delta_{mm'} \\ &= \sum_{m=0}^{M-1} \langle \mathcal{N}(m n \Delta t)^2 \rangle. \end{aligned} \quad (2.18)$$

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Clearly, in Equation 2.17,  $\langle A_{1,0} \rangle = 0$ . In Equation 2.18, we assume the variance is of form  $(n \Delta t)^\alpha$  [7]. Then,

$$\langle A_{1,0}(nt = M n \Delta t)^2 \rangle = M(n \Delta t)^\alpha. \quad (2.19)$$

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Running the analysis over the frames  $t = 0$  to  $t_f$ , the number of bits sampled is  $M = t_f/n \Delta t$ . Substituting this into Equation 2.19,

$$\langle A_{1,0}(nt = M n \Delta t)^2 \rangle = t_f (n \Delta t)^{\alpha-1}. \quad (2.20)$$

Concidering the three cases of  $\alpha$  in the approximation of continious  $n\Delta t$ :

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- $\alpha > 1$ : Here  $A_{1,0} \rightarrow 0$  as  $\Delta t \rightarrow 0$ .

- $\alpha < 1$ : Here  $A_{1,0} \rightarrow \infty$  as  $\Delta t \rightarrow 0$ .

284

- $\alpha = 1$ : This is the only sensible choice.

With  $\alpha = 1$ ,

$$\langle A_{1,0}(nt = M n \Delta t)^2 \rangle = M(n \Delta t). \quad (2.21)$$

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And thus,

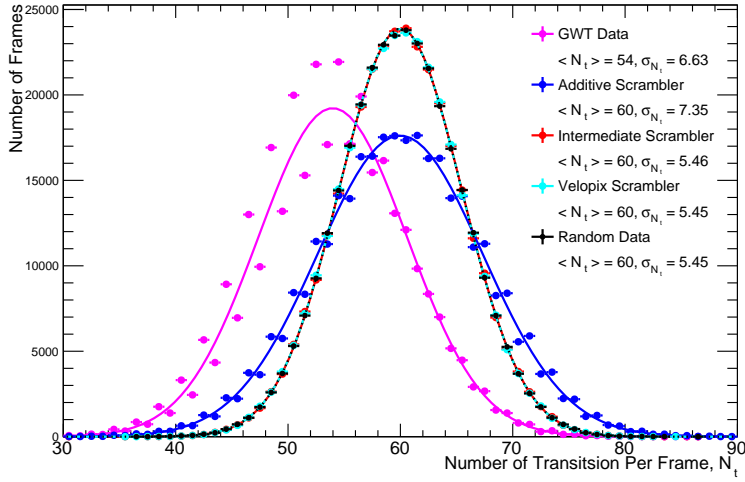
$$\sigma_{A_{1,0}} = \sqrt{\langle A_{1,0}^2 \rangle - \langle A_{1,0} \rangle^2} = \sqrt{\langle A_{1,0}^2 \rangle} = \sqrt{n \Delta t}. \quad (2.22)$$

### 2.3.3 Results of Analysis

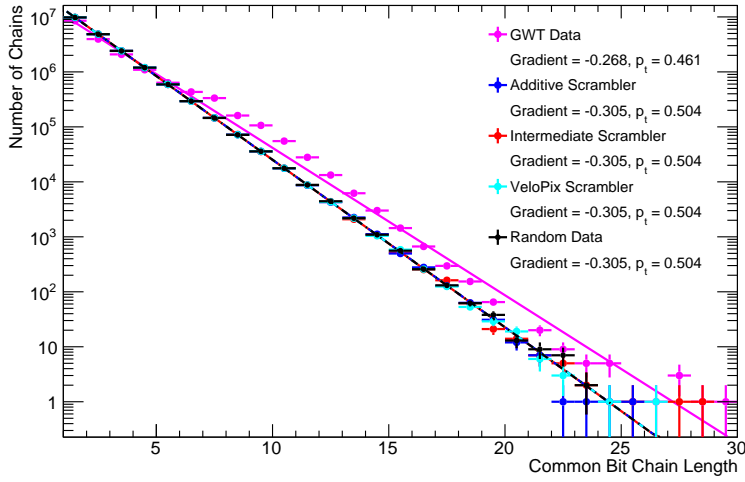
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The results from the ‘*Number of Transitions Per Frame*’ analysis, shown in Figure 2.1, show a strong similarity between the Intermediate and VeloPix Scramblers with the randomly generated data. These results are withing 1% agreement with the theoretical

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**Figure 2.1:** Results of the ‘Number of Transitions Per Frame’ analysis. The results for the Random Data, Intermediate Scrambler and VeloPix Scrambler overlap for the ‘Number of Transitions Per Frame’ analysis.

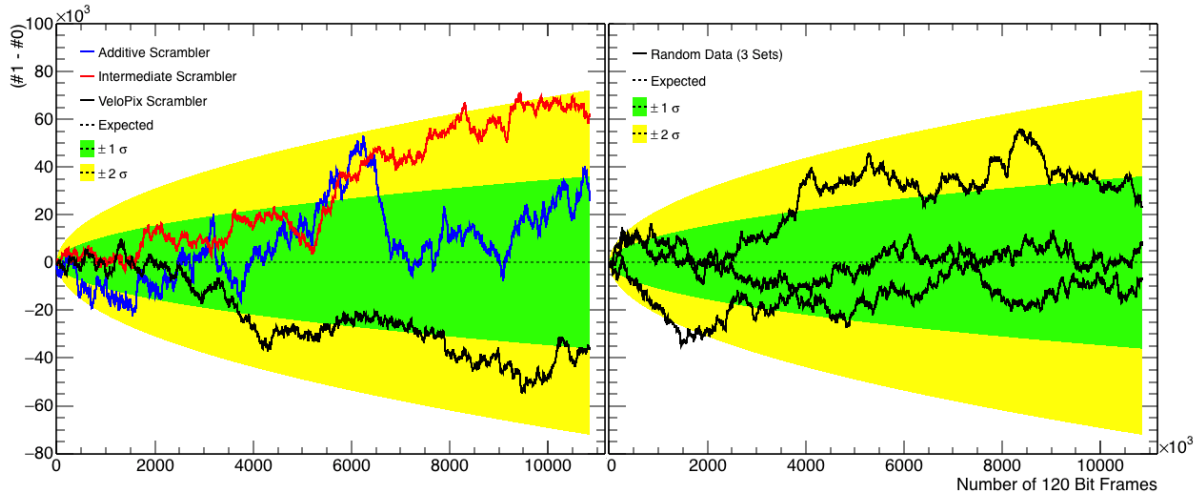


**Figure 2.2:** Results of the ‘Common Bit Chain Length’ analysis. The results for the Random Data, Additive Scrambler, Intermediate Scrambler and VeloPix Scrambler approximately overlap for the ‘Common Bit Chain Length’ analysis.

predictions for  $\langle N_\tau \rangle = 60$  and  $\sigma_{N_\tau} = 5.48$ , made in Section 2.3.2. The remarkable consistency between the theoretical predictions and the randomly generated data provides confidence in both the theory, and the scrambled nature of the Intermediate and VeloPix scrambler outputs.

All three scramblers, the random data, and the theoretical predictions are consistent within 1%. Comparing the two results for the Additive Scrambler, however, it is shown that while the frequency of longer chains is consistent with random data - the variance of transitions is larger than predicted, and thus the long and short trains are more locally clustered.

The ‘Bit Asymmetry’ of each scrambler, shown in Figure 2.3, is consistent with the theoretical prediction. The deviation of  $A_{1,0}$  for the predicted mean of 0 is fully consistent with stochastic noise. The random data also shows consistency. This gives confidence in the assumptions made in Section 2.3.2.



**Figure 2.3:** The results of the ‘*Bit Asymmetry*’ analysis.

## 2.4 Conclusion

	$\langle N_\tau \rangle$	$\sigma_{N_\tau}$	Gradient	$p_\tau$
GQT data	54	6.63	-0.268	0.460
Additive Scrambler	60	7.35	-0.305	0.504
Intermediate Scrambler	60	5.45	-0.305	0.504
VeloPix Scrambler	60	5.46	-0.305	0.504
Random Data	60	5.45	-0.305	0.504
Theoretical Prediction	60	5.48	-0.3	0.5

**Table 2.1:** The combined results of the algorithm analysis.

The consistency of random data and the theoretical predictions justifies the assumptions and approximations made in Section 2.3 and Section 2.3.2. Furthermore, the conformation of the statistical model allows for accurate comparisons to be made from predicted values and their measured counterparts.

The Additive Scrambler, while consistent with the ‘*Chain Length*’ and ‘*Bit Asymmetry*’ analysis, has a variance in the transition frequency that leads to the conclusion that long and short chains are locally clustered. This is not ideal for data transfer. Many sequential long chains increase the probability of TX-RX clock desynchronisation. Furthermore, the additive scrambler will not recover from this loss of synchronisation, as the ‘*key*’ will never be recovered without a common reset signal.

The Intermediate Scrambler produced an output consistent with random data. This makes the algorithm suitable for data transfer. As already mentioned, however, the scram-

bler is designed for computer simulated. As such, it is not suitable for implementation  
as it does not meet the additional requirements of the ASIC.

The VeloPix Scrambler, like the Intermediate Scrambler, produces a statistically scrambled output. Furthermore, the algorithm is inline with the additional requirements of the ASIC. As such, it is ideal for implementation, and hence is currently the choice algorithm for use in the 2019 VELO upgrade.

steam

### 3 Event Isolation Flagging

One challenge of increasing the readout speed of the detector is processing the data produced. Because of this, any pre-computer data processing possible reduces the load and processing time of the computer system. One area where the DAQ's FPGA will be used for this purpose is in Event Isolation Flagging (EIF).

Particles traversing the VELO have a probability that they will pass through the boundary of two or more Super Pixels. This will cause multiple SPPs for the same particle. As such, the reconstruction of the particles path is a more complicated process than a particle path that only intersects with one SP.

The aim of EIF is to identify the SPPs that completely describe the particles interaction with the module and flag then event as isolated. These flagged events will allow the computer systems to prioritise these easier to re-construct paths. This reduces event pile up the computer network.

#### 3.1 Time Sorting Data

Frames arriving the DAQ from the GWT are not time ordered. When fully implemented, the LLI will have time sorted the data before the EIF. However, the provided simulated data of the VELO not time ordered.

In order to test any EIF development, it is necessary to time order the simulation data. This was done using a python script that sorted the SPPs into lists according to BCID. The script has three main phases:

- Read in SPP and retrieve BCID.
- Add SPP to correct list according to BCID.
- Print list of opposite BCID (i.e. input SPP's BCID + 124 accounting for BCID 256 rolling over to 0) to file.



As not all BCID's are present, measures were put in place to ensure all BCID lists were outputted in time order, preventing lists containing two or more bunch crosses. The time order of the data was tested and confirmed as correct.

One advantage of this process is that, regardless of the number of isolated events, the data no longer needs to be sorted by the computer network. This further reduced the computational load on the computers.

### 3.2 Bubble Sorting

The first step in EIF is to sort all the SPP's that correspond to the same bunch crossing (Hereafter referred to as a 'data train') by their row.

Bubble sorting, when implemented in series processing, is a relatively slow sorting algorithm. At worst case, Bubble sorting requires  $n^2$  iterations to complete the sort. However, as FPGAs can easily parallel process. By making  $\frac{n}{2}$  comparisons simultaneously (even-odd or odd-even), FPGA Bubble Sorting in the worst case scenario only requires  $n$  iterations. This is made clear in Figure 3.1.

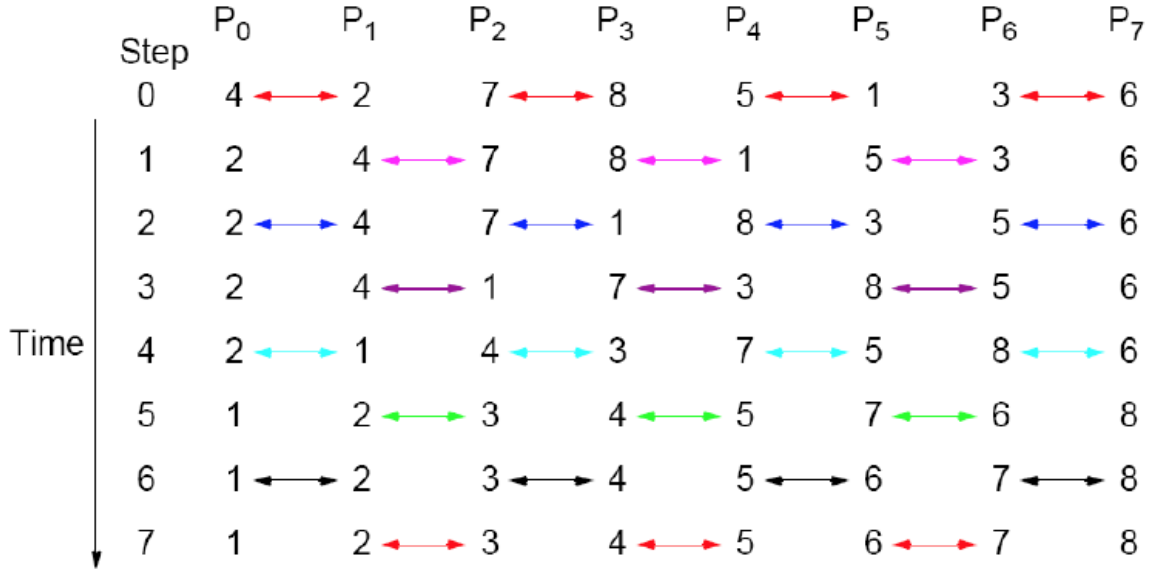


Figure 3.1: A diagram showing Bubble Sorting in an FPGA.

### 3.3 Isolation Checking

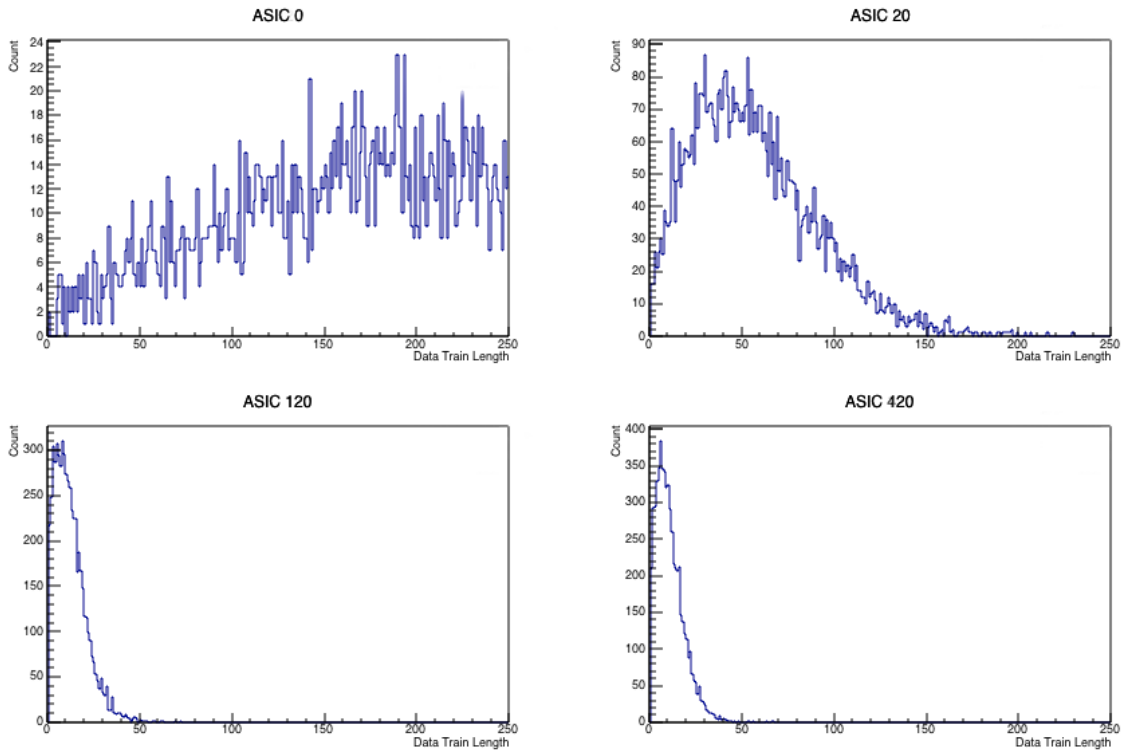
Once the data train is sorted by row, each SPP in the train can be compared against its adjacent SPP's. If the SPP is separated by  $> 1$  row to both adjacent SPP's, the event is isolated. The SPP is then stored as a 31 bit SPP, with the new bit added as the

least significant bit (shifting the original SPP 1 bit in significance), with the new bit signaling 1 for isolation and 0 for non-isolated.

### 3.4 Data Train Overflow

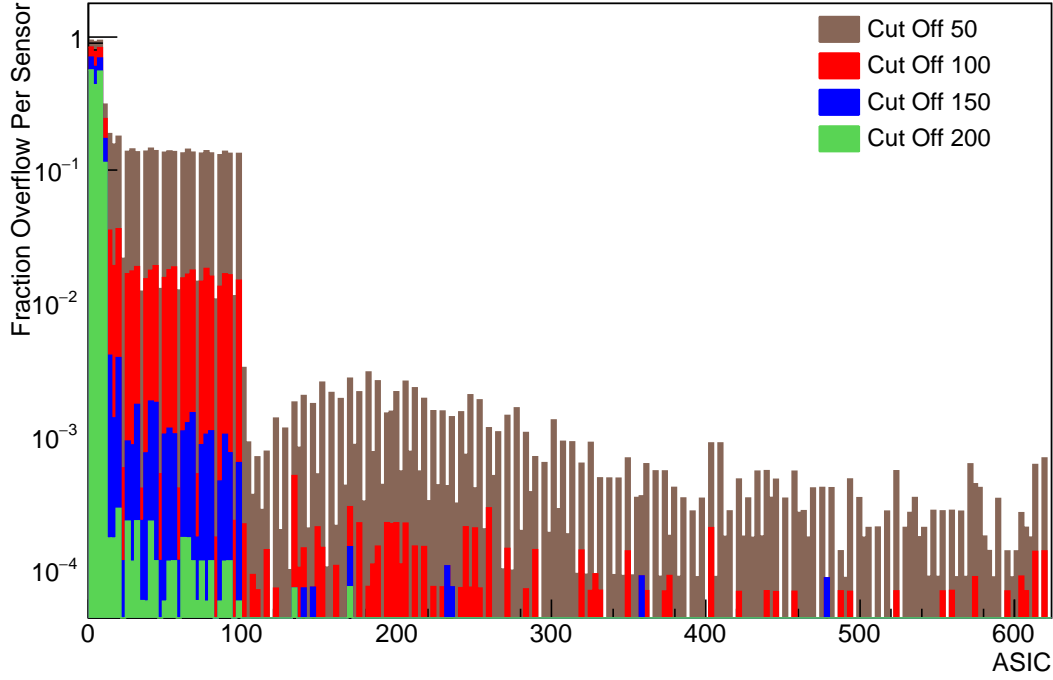
One limitation of EIF in an FPGA is the limitation on resources. The logic systems are static in design and as such there is a natural need for a cap on the size of data train that the EIF system can accept - specifically for the bubble sorting. Because of this limitation, the EIF system is required to implement an overflow system that will reject data trains above a pre-determined limit, and move them to the next step of the LLI without processing them. This system is also required to bypass data if a data train arrives at the EIF system before the previous train has been processed - preventing a pipeline up.

In order to investigate the limit needed for the overflow, the distribution of data train sizes was investigated. For each ASIC, a graph similar to those in Figure 3.2 can be created.



**Figure 3.2:** The data train length distribution of 4 ASIC chips.

More important, however, is the fraction of data trains over the bypass limit. For four theoretical limits, the fraction of overflow data trains was calculated from the VELO simulated data, and it is shown in Figure 3.3. This analysis, however, raises questions beyond that of the overflow limit. The ASICs below 100 show no similarity to those above 100.



**Figure 3.3:** fraction of overflow data trains for four overflow limits.

Further investigations as the to structure of the simulated data is shown in Appendix A. From this we learn the large variance in the data (ASIC number  $\geq 100$ ) is due to the ASIC's position on the modual this is expected. This structure is not consistant across the ACIS's pre and post 100. It can be conculed that the simulated data contains a 'bug' and it now beinging reviewed by the creators of the simulation. No further analysis can be continued on this front until this 'bug' has been properly investigated.

### 3.5 Current Stage of Development

The EIF system is still currently in active VHDL development. The current developmently code is still in a stand alone format and not intergrated with the master LLI code. Currently created, and ready for stand alone testing, is a bubble sorting module with data in and out systems. The module consistence of a top level control entity and a comparison/swap sorting entity. The control entity forms a feedback loop passing the ouput of the sorting entity back into its input at each step. At each step, the parity of comparison is changed (i.e. odd-even to even-odd).

This process continues intill the input and output of the sorting module is identical for two subsequent steps. At this point the data is sorted and passed to the output. The data flow is more simply demonsttraited in Figure 3.4.

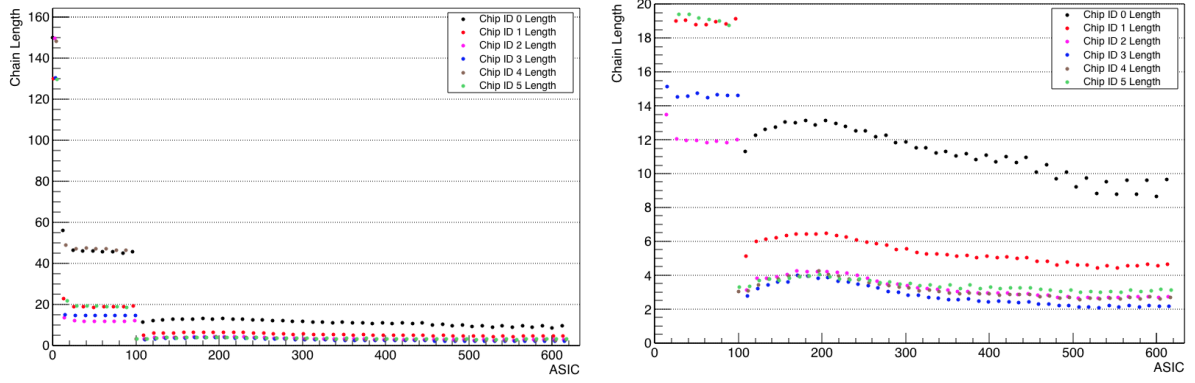
**Figure 3.4:** Data from for the developmental bubble sorting module.

402 Once testing a bug fixing is complete, the EIF will be expanded to include Isolation  
Flagging and an overflow as discussed. Once the stand alone system is complete, it will  
404 be intergrated into the LLI master code and modified to comply with theh LLI data  
managment systems.

## References

- [1] Cern. *The Standard Model*. 2015. URL: <http://home.cern/about/physics/standard-model> (visited on 12/2015).
- [2] LHCb Collaboration. *LHCb VELO Upgrade Technical Design Report*. Tech. rep. CERN-LHCC-2013-021. LHCb-TDR-013. Geneva: CERN, Nov. 2013. URL: <https://cds.cern.ch/record/1624070>.
- [3] CERN. *LHCb VELO Project*. 2015. URL: <http://lhcb-vd.web.cern.ch/lhcb-vd/html/project.htm>.
- [4] “Toward FPGA-Enabled Scientific Computing”. In: *Design Test of Computers, IEEE* 28.4 (July 2011), pp. 4–4. ISSN: 0740-7475. DOI: 10.1109/MDT.2011.91.
- [5] Altera. *Quartus Prime Software*. 2015. URL: <https://www.altera.com/products/design-software/fpga-design/quartus-prime/overview.html> (visited on 12/2015).
- [6] Mentor Graphics. *ModelSim - Leading Simulation and Debugging*. 2015. URL: <https://www.mentor.com/products/fpga/model/> (visited on 12/2015).
- [7] Kurt Jacobs. *Stochastic Processes for Physicists - Understanding Noisy Systems*. Cambridge University Press, 2010. ISBN: 9780521765428.

# A Event Isolation Flagging Appendix



**Figure A.1:** The mean data train length for each ASIC, coloured by the chip number.