


## Lumerical Mode Simulation

I kept the SiO<sub>2</sub> material to be the same size with the settings from the videos on MODE.

 Edit rectangle ✕

You are in ANALYSIS mode. Switch to LAYOUT mode to make changes: Switch To Layout Mode

name

Geometry

Material

Rotations

Graphical rendering

x (μm)

x span (μm)

x min (μm)

x max (μm)

y (μm)

y span (μm)

y min (μm)

y max (μm)

z (μm)

z span (μm)


z min (μm)

z max (μm)

☒ use relative coordinates

Cancel

Because our project deals with a 350 nm waveguide rather than a 500nm waveguide, I changed the Si geometry to have a 350nm x span. I kept the y span the same as we are not changing the waveguide thickness, just its width.

 Edit rectangle ×

You are in ANALYSIS mode. Switch to LAYOUT mode to make changes: Switch To Layout Mode

name

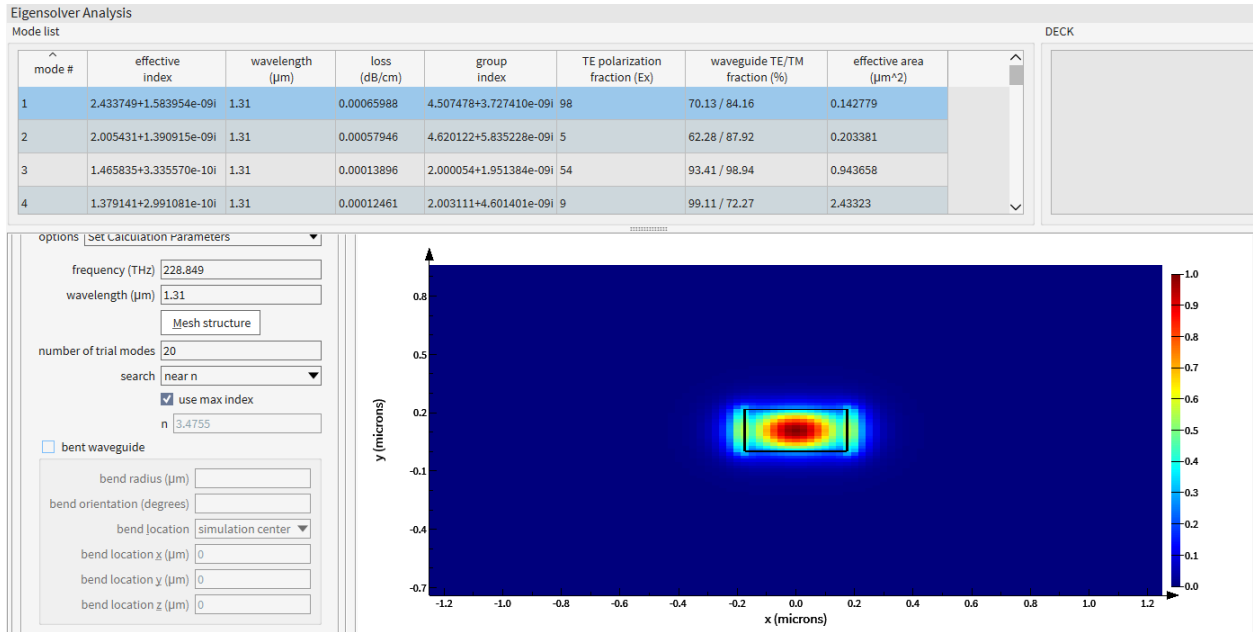
**Geometry** | Material | Rotations | Graphical rendering

x ( $\mu\text{m}$ )	<input type="text" value="0"/>	x min ( $\mu\text{m}$ )	<input type="text" value="-0.175"/>
x span ( $\mu\text{m}$ )	<input type="text" value="0.35"/>	x max ( $\mu\text{m}$ )	<input type="text" value="0.175"/>
<hr/>			
y ( $\mu\text{m}$ )	<input type="text" value="0.11"/>	y min ( $\mu\text{m}$ )	<input type="text" value="0"/>
y span ( $\mu\text{m}$ )	<input type="text" value="0.22"/>	y max ( $\mu\text{m}$ )	<input type="text" value="0.22"/>
<hr/>			
z ( $\mu\text{m}$ )	<input type="text" value="0"/>	z min ( $\mu\text{m}$ )	<input type="text" value="-0.3"/>
z span ( $\mu\text{m}$ )	<input type="text" value="0.6"/>	z max ( $\mu\text{m}$ )	<input type="text" value="0.3"/>

☒ use relative coordinates

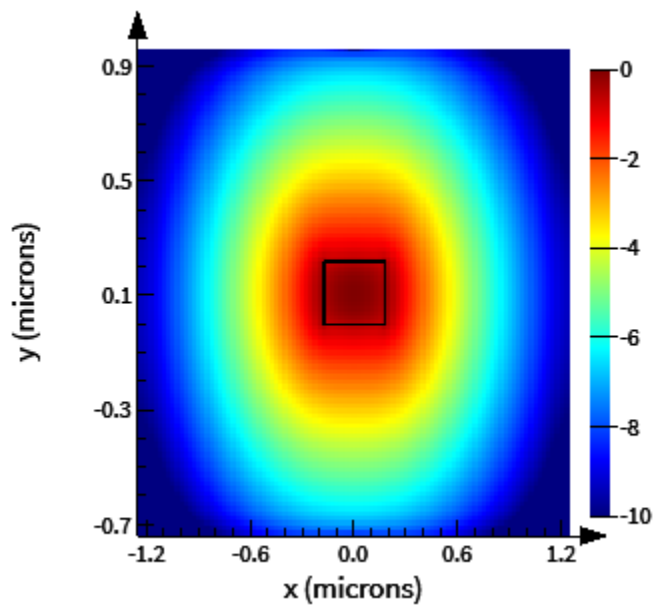
Cancel

When simulating with the 1310 nm wavelength, we need to change the wavelength parameter in the modal analysis tab.

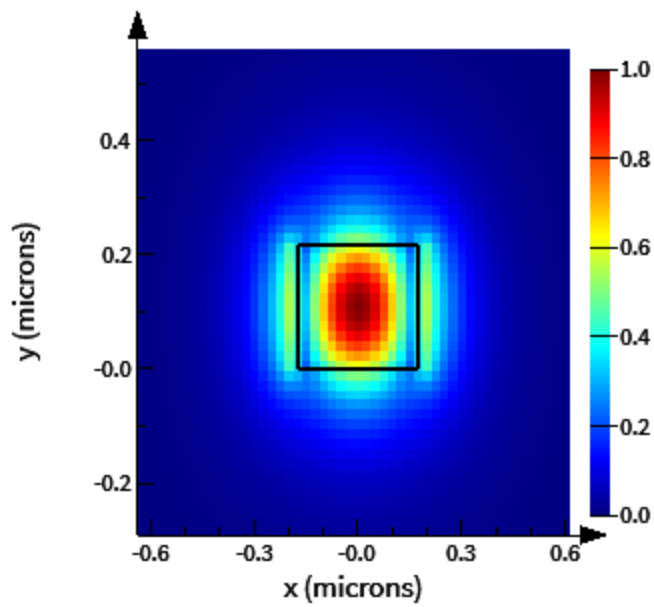


The effective Index after simulation is 2.434. With a group index of 4.507.

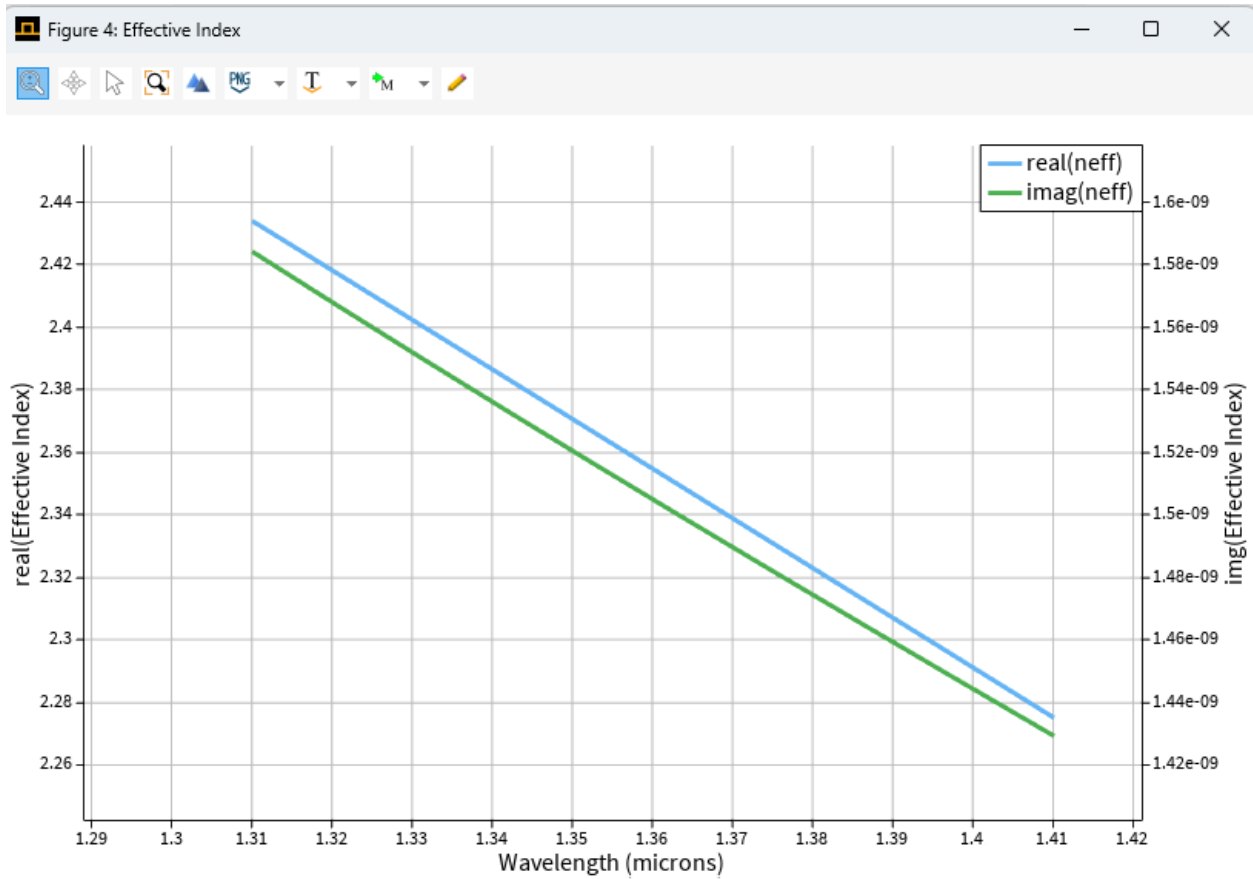
Here is the electric field intensity plotted on the log scale.



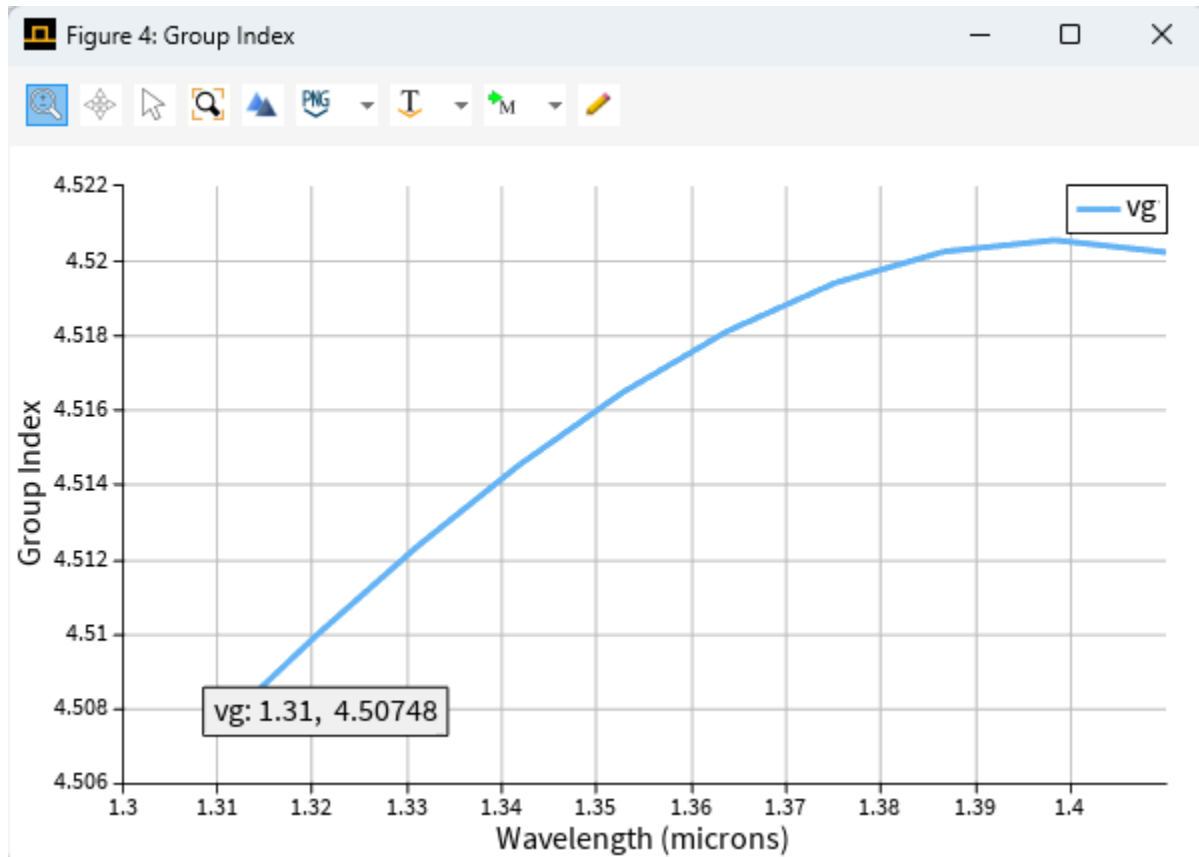
And here is the X component of the electric field.



## Frequency Analysis (Wavelength Sweep)

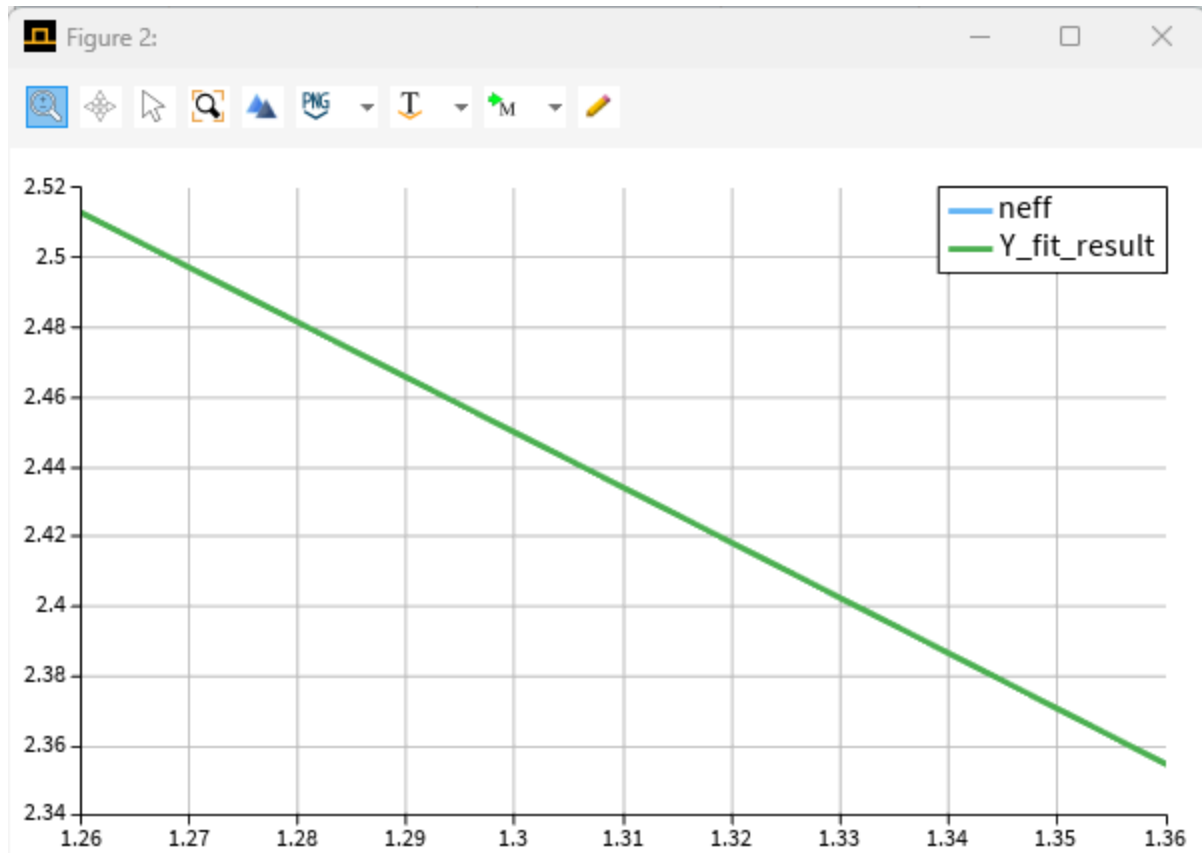


The effective index at 1310 nm for this waveguide is about 2.434, and the group index increases with wavelength and is approximately 4.50.

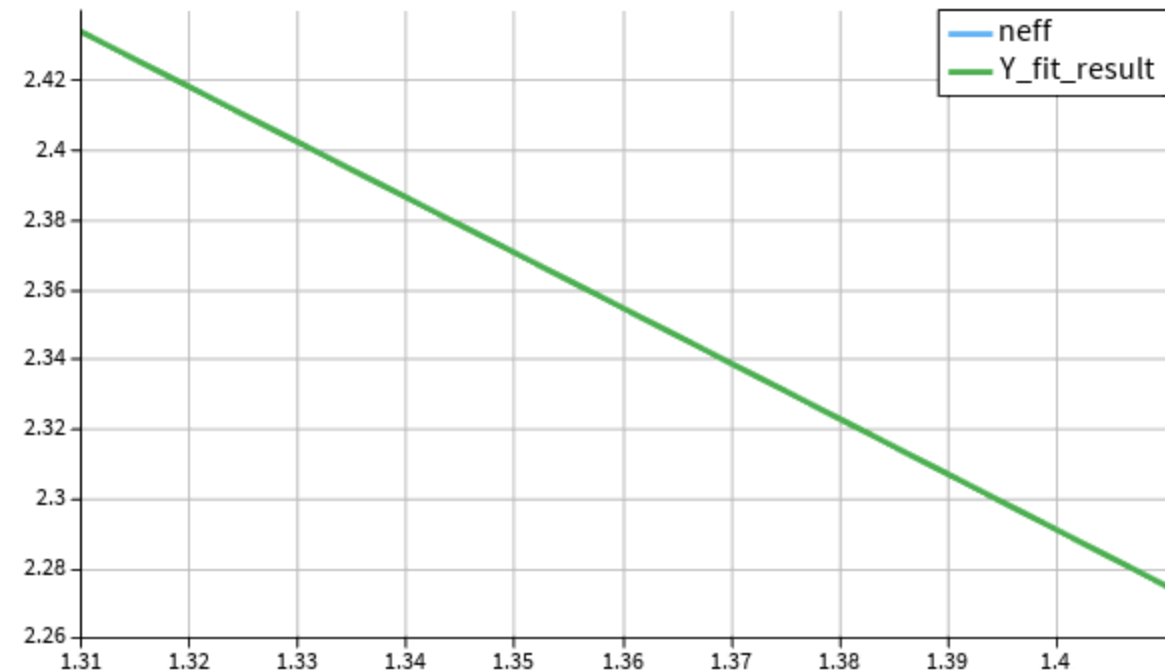
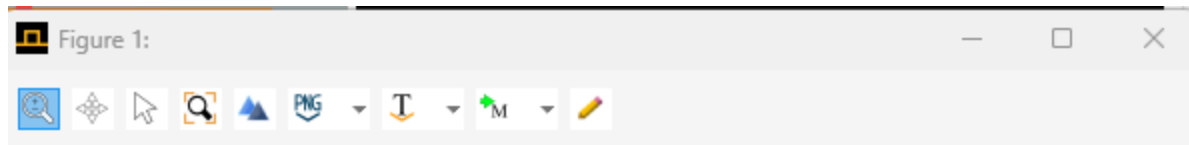


After running the script to model the wave guide's effective index, I got the following equation.

```
plot (lambda, neff, Y_fit_result); # plot the result;
result:
2.0505
-1.60896
-0.0501316
```

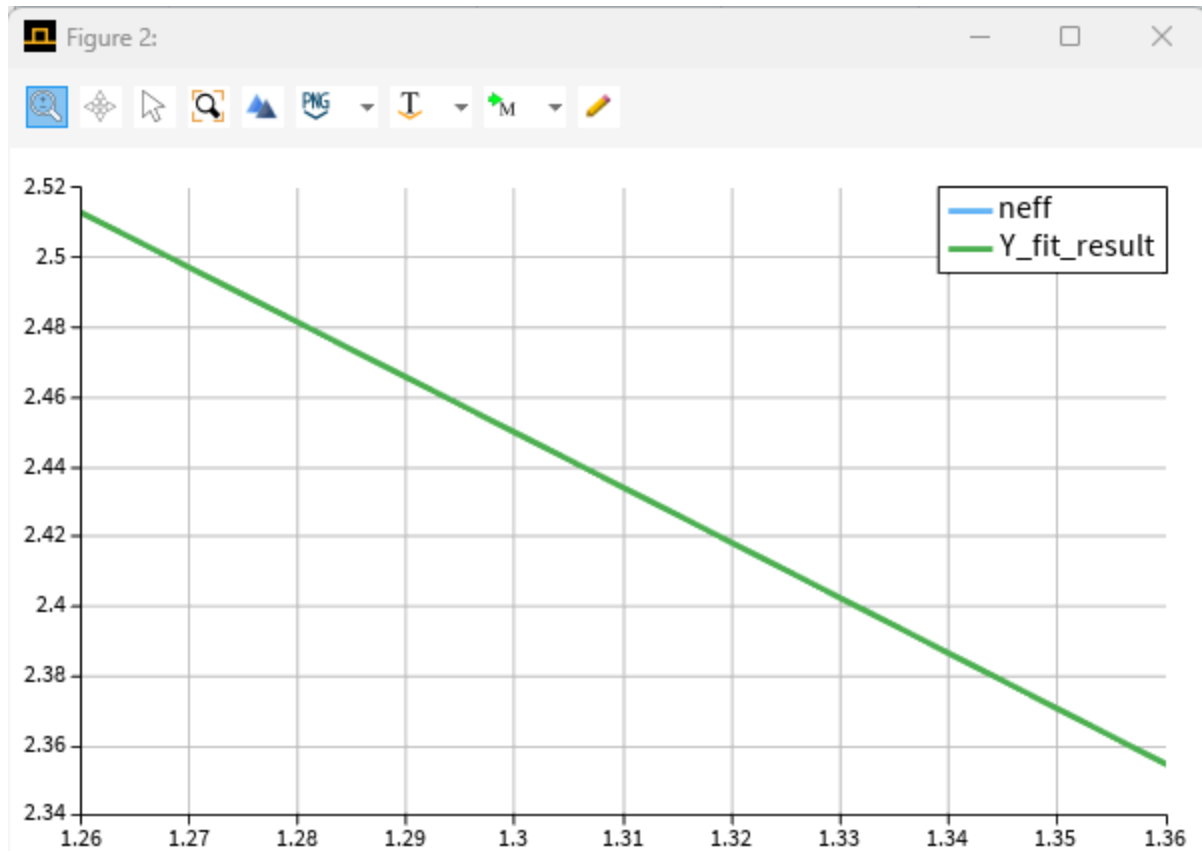


When using this method, the effective index is 2.04861, which varies quite substantially from the direct situation at 1310 nm.



Since we are operating at 1310 nm, I am also going to do a test from a 1260-1360 nm in order to double check the effective index.

```
plot (lambda, neff, Y_fit_result); # plot the result;
result:
2.04861
-1.62683
-0.0920119
>
```



The effective index is around 2.04861 at the wavelength of 1.31nm.

Given a group index of 4.507, we can calculate the path length difference from the FSR, using the equation:

$$\Delta L = c / (n_g \cdot \text{FSR})$$

$c = 299792458$

×

-10

2.997925 × 10<sup>8</sup>

×

---

$n_g = 4.507$

×

-10

10

×

---

$F_{SR} = 25 \cdot 10^6$

×

= 25 000 000

×

---

$L = \frac{c}{n_g \cdot F_{SR}}$

×

= 2.66068300865

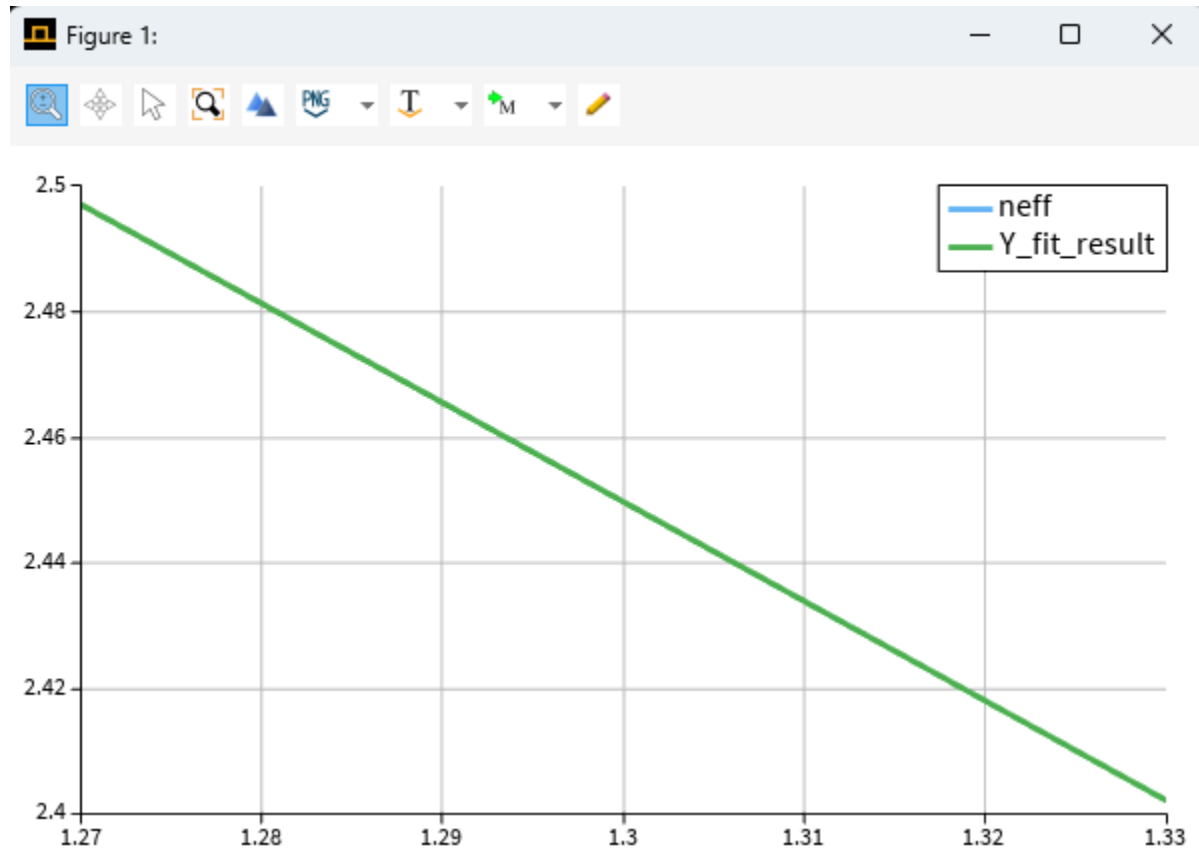
×



I calculate that the path length difference of the interferometer needs to be 2.66 mm. Now I will make this in KLayout.

I also did a frequency sweep from 1270-1330 nm, as this aligns with the range that we are testing in, and

The effective index sweep looked like this:



And the equation for effective index was:

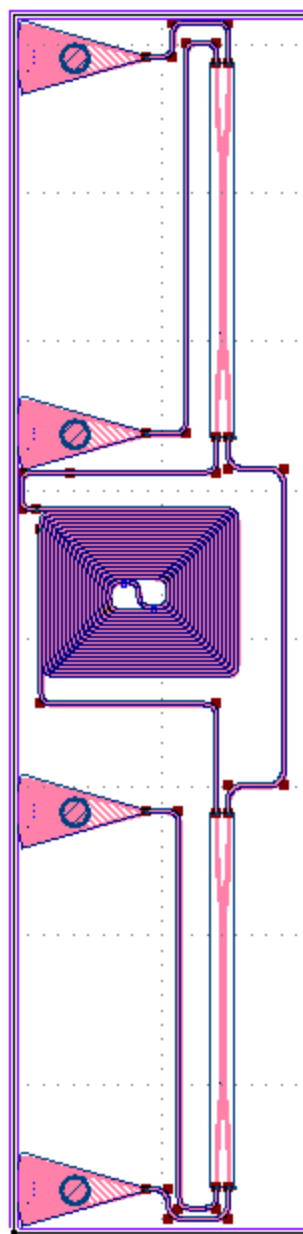
```
plot (lambda, neff, Y_fit_result); # plot the result;
result:
2.04818
-1.63017
-0.0984098
>
```

And at 1.27nm, the group index was 4.49.

So using a group index of 4.5 in my calculations is good and I will aim for a path difference of 2.66mm.

I made this design in KLayout.

$L_1 = 155.254$ -10 <input type="range"/> 155.254	✕
$L_2 = 90.285$ -10 <input type="range"/> 90.285	✕
$L_{SPIRAL} = 2578.429$ -10 <input type="range"/> 2578.429	✕
$L_3 = 151.971$ -10 <input type="range"/> 151.971	✕
$L_{Total} = L_2 + L_3 + L_{SPIRAL}$ <div>= 2820.685</div>	✕
$D = L_{Total} - L_1$ <div>= 2665.431</div>	✕

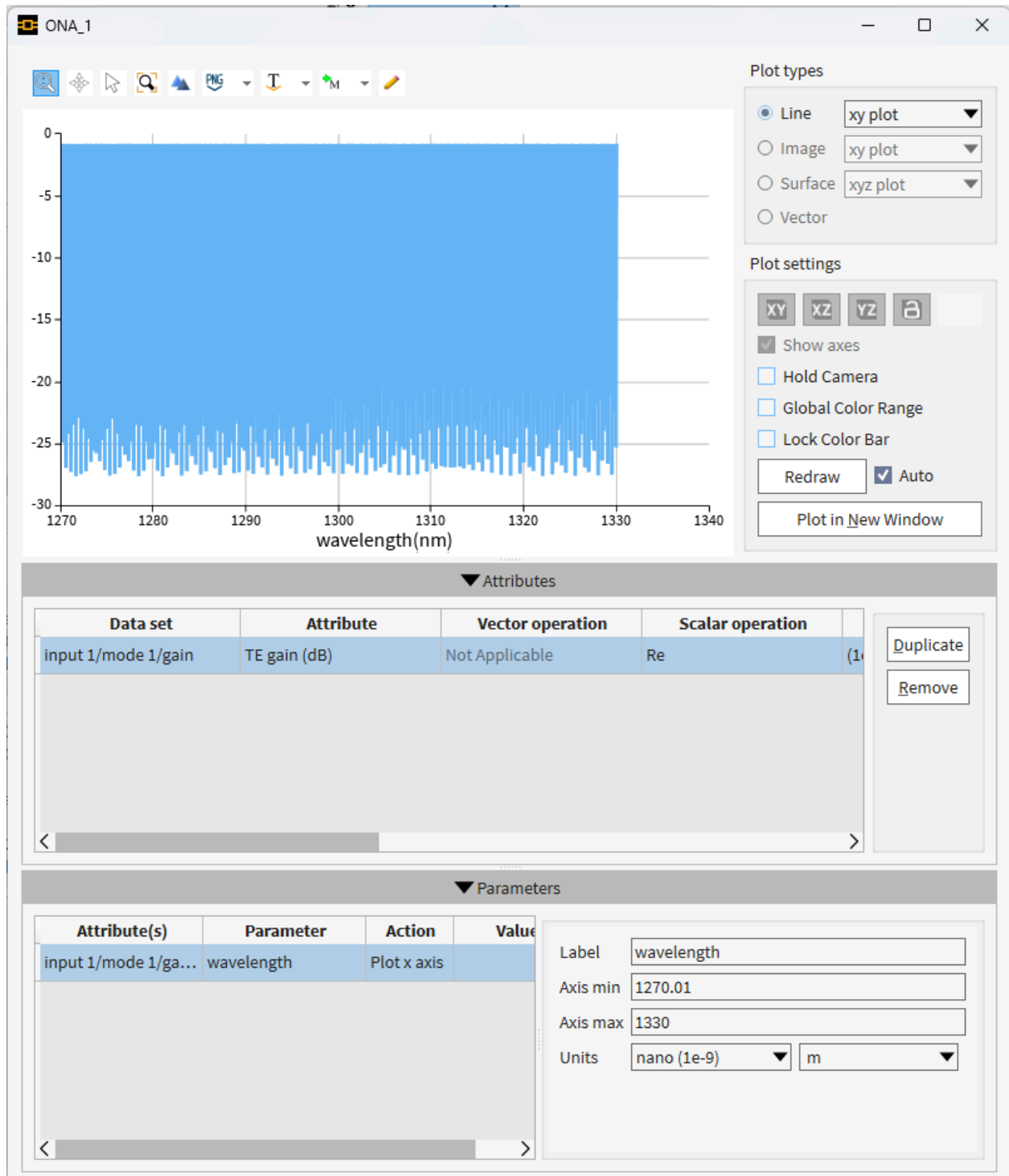


I am running the network analyzer from 1270nm to 1330nm

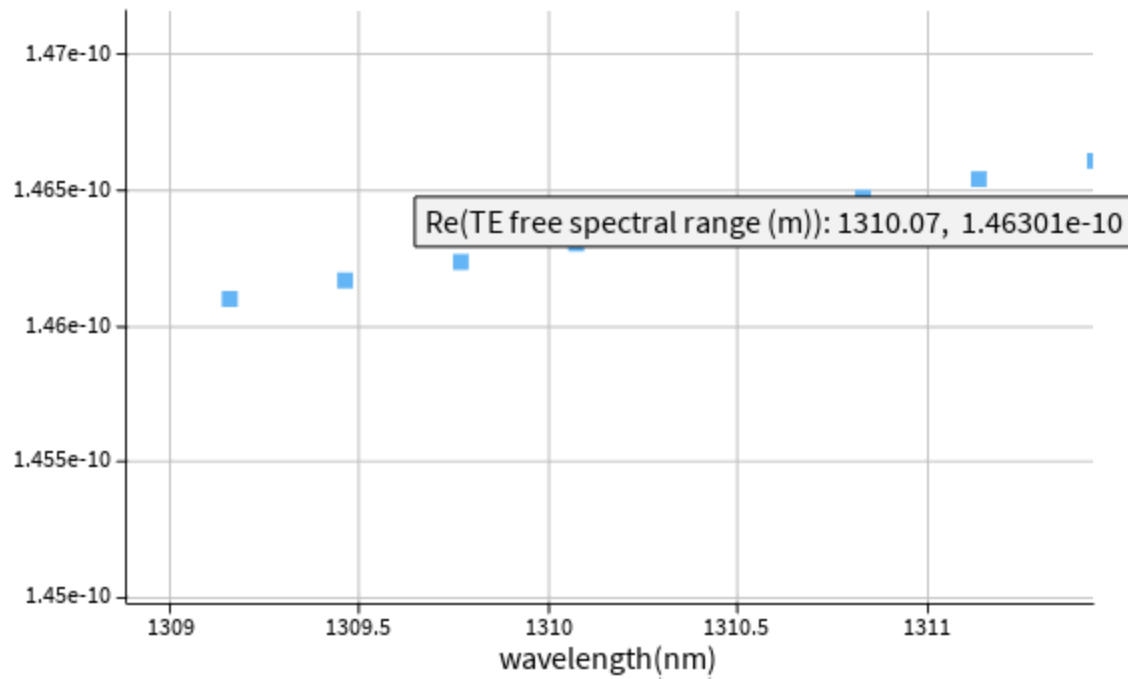
Property View - ONA_1			
Name	Value	Unit	Expre <sup>^</sup>
▶ General			
▼ Standard			
<input type="checkbox"/> number of input ...	1		
<input type="checkbox"/> power	0	dBm	
<input type="checkbox"/> excitation	0	W	
<input type="checkbox"/> input parameter	start and stop		
<input type="checkbox"/> center frequency	230.73245835...	THz	
<input type="checkbox"/> frequency range	10649.190385...	GHz	
<input type="checkbox"/> start frequency	1330	nm	
<input type="checkbox"/> stop frequency	1270	nm	
<input type="checkbox"/> number of points	5000		
<input type="checkbox"/> plot kind	wavelength		
<input type="checkbox"/> angle unit	rad		
<input checked="" type="checkbox"/> relative to center	false		
<input type="checkbox"/> delay	0	s	
<input checked="" type="checkbox"/> limit time range	false		
<input type="checkbox"/> start time	1	s	
<input type="checkbox"/> stop time	1	s	
▶ Waveguide			



Above is the plot of the free spectral range.



This was the plot for the output of the interferometer.

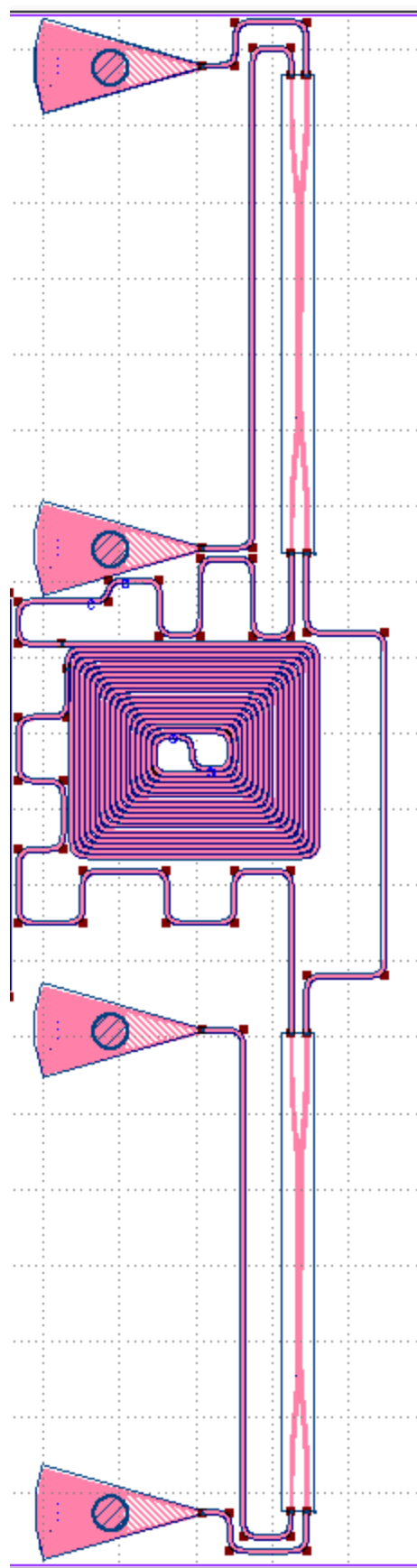


Here the FSR is 0.14nm, which is what it should be, as this is a 25 GHz FSR. To convert from

$$\Delta\nu \approx -\frac{c\Delta\lambda}{\lambda^2} = \frac{c}{\Delta L n_g}$$

nm to hertz of the FSR you use the equation:

I was able to simulate these expected output frequencies for different path lengths as well, and I made a chip design with a 23GHz spacing.



```

c = 299792458 # m/s
ng = 4.507478

FSR_GHz = 25.0e9 # GHz

wavelength = 1310e-9 # nm

FSR_wavelength_spacing = FSR_GHz * wavelength**2 / c
# Print spacing to 2 decimal places
print("Wavelength Spacing = {:.2f}".format(FSR_wavelength_spacing * 1e9), "nm")

```

✓ 0.0s

Wavelength Spacing = 0.14 nm

```

path_length_difference_1 = c / (FSR_GHz * ng)
# Print path length difference to 2 decimal places
print("Path Length Difference = {:.2f}".format(path_length_difference_1*1e3), "mm")

```

✓ 0.0s

Path Length Difference = 2.66 mm

```

def calc_path_diff_from_spacing(desired_spacing):
    L = wavelength**2 / (desired_spacing*1e-9 * ng)
    return L

lambda_diff = 0.8 # nm
for lambda_diff in [0.08, 0.10, 0.12, 0.14, 0.16]:
    print(f"Path Length Difference for {lambda_diff}nm = " + "{:.2f}".format(calc_path_diff_from_spacing(lambda_diff) * 1e6), "um")
    print(f"Resulting FSR = "+"{:.2f}".format(c / (calc_path_diff_from_spacing(lambda_diff) * ng) * 1e-9), "GHz")

```

✓ 0.0s

```

Path Length Difference for 0.08nm = 4759.04 um
Resulting FSR = 13.98 GHz
Path Length Difference for 0.1nm = 3807.23 um
Resulting FSR = 17.47 GHz
Path Length Difference for 0.12nm = 3172.69 um
Resulting FSR = 20.96 GHz
Path Length Difference for 0.14nm = 2719.45 um
Resulting FSR = 24.46 GHz
Path Length Difference for 0.16nm = 2379.52 um
Resulting FSR = 27.95 GHz

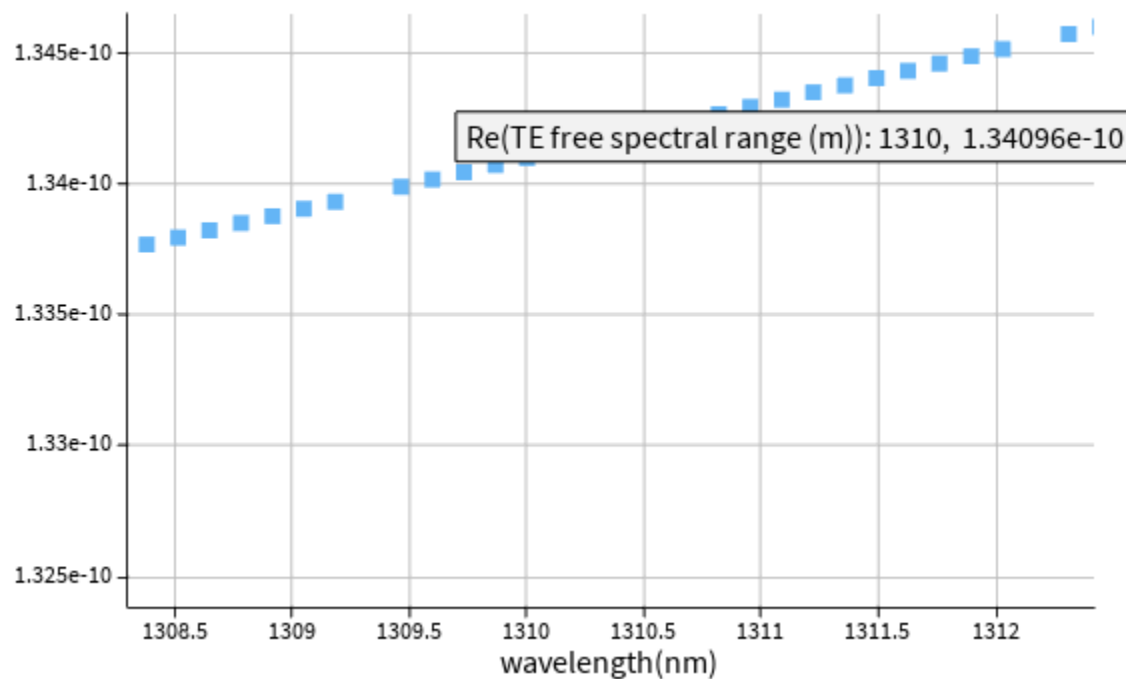
```



```
def calc_FSR_from_path_diff(path_diff):  
    return c / (path_diff * ng)  
  
L1 = 160.693e-6  
L2 = 237.315e-6  
L_Spiral = 2578.429e-6  
R1 = 161.323e-6  
  
L_Total = L1 + L2 + L_Spiral  
R_Total = R1  
  
L_Diff = L_Total - R_Total  
FSR = calc_FSR_from_path_diff(L_Diff)  
print("FSR_GHz = ", FSR * 1e-9, "GHz")  
print("FSR_nm = ", FSR * wavelength**2 / c * 1e9, "nm")  
✓ 0.0s  
  
FSR_GHz = 23.626049014977255 GHz  
FSR_nm = 0.1352424373351062 nm
```

The function above calculated the expected FSR in GHz for the path length difference that I had in the second circuit.

This matches the INTERCONNECT simulation.



- Consider fabrication variations (width +/- 10 nm, thickness +/- 10 nm, process bias  $\Delta w$ , range of propagation loss values) and how they will impact the filter performance. Start with identifying the process corners, simulating the waveguide for each corner, then simulating the circuit for each corner.

Corners:

Design #	Waveguide Size	Group Index	Path Difference	File_name
1	350 x 220	4.507478	2660.40	350x220_wg.ldf
2	360 x 230	4.469343	2683.10	360x230_wg.ldf
3	360 x 210	4.466558	2684.77	360x210_wg.ldf
4	340 x 230	4.525866	2649.59	340x230_wg.ldf
5	340 x 210	4.518220	2654.08	340x210_wg.ldf

```
def calc_necessary_path_diff(ng):
    FSR = 25e9 # GHz
    return c / (FSR * ng)

print("Path Length Difference for ng = 4.5: ", calc_necessary_path_diff(4.5) * 1e6, "um")
```

✓ 0.0s Python

Path Length Difference for ng = 4.5: 2664.821848888889 um

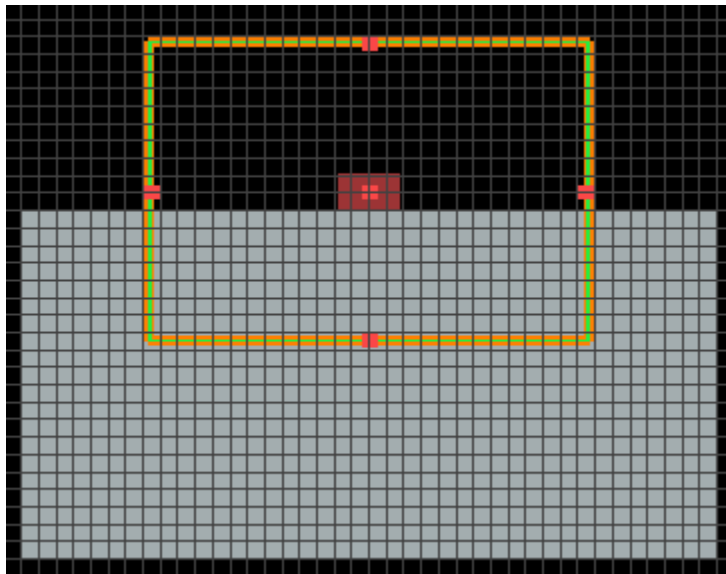
Now I am going to simulate different sized waveguides in lumerical mode to get a variation in group indexes, and then try to make a variety of designs with those size variations.

```
Path Length Difference for ng = 4.507478: " + "{:.2f}".format(calc_necessary_path_diff(4.507478) * 1e6), "um")
Path Length Difference for ng = 4.469343: " + "{:.2f}".format(calc_necessary_path_diff(4.469343) * 1e6), "um")
Path Length Difference for ng = 4.466558: " + "{:.2f}".format(calc_necessary_path_diff(4.466558) * 1e6), "um")
Path Length Difference for ng = 4.525866: " + "{:.2f}".format(calc_necessary_path_diff(4.525866) * 1e6), "um")
Path Length Difference for ng = 4.518220: " + "{:.2f}".format(calc_necessary_path_diff(4.518220) * 1e6), "um")
```

✓ 0.0s Python

Path Length Difference for ng = 4.507478: 2660.40 um  
 Path Length Difference for ng = 4.469343: 2683.10 um  
 Path Length Difference for ng = 4.466558: 2684.77 um  
 Path Length Difference for ng = 4.525866: 2649.59 um  
 Path Length Difference for ng = 4.518220: 2654.08 um

For Chip 2 I began by simulating the waveguide.



**Edit rectangle** X

You are in ANALYSIS mode. Switch to LAYOUT mode to make changes: [Switch To Layout Mode](#)

name

**Geometry** Material Rotations Graphical rendering

x (μm)	<input type="text" value="0"/>	x min (μm)	<input type="text" value="-0.175"/>
x span (μm)	<input type="text" value="0.35"/>	x max (μm)	<input type="text" value="0.175"/>

y (μm)	<input type="text" value="0.11"/>	y min (μm)	<input type="text" value="0"/>
y span (μm)	<input type="text" value="0.22"/>	y max (μm)	<input type="text" value="0.22"/>

z (μm)	<input type="text" value="0"/>	z min (μm)	<input type="text" value="-0.3"/>
z span (μm)	<input type="text" value="0.6"/>	z max (μm)	<input type="text" value="0.3"/>

☒ use relative coordinates

[Cancel](#)

**Edit rectangle** X

You are in ANALYSIS mode. Switch to LAYOUT mode to make changes: [Switch To Layout Mode](#)

name

**Geometry** Material Rotations Graphical rendering

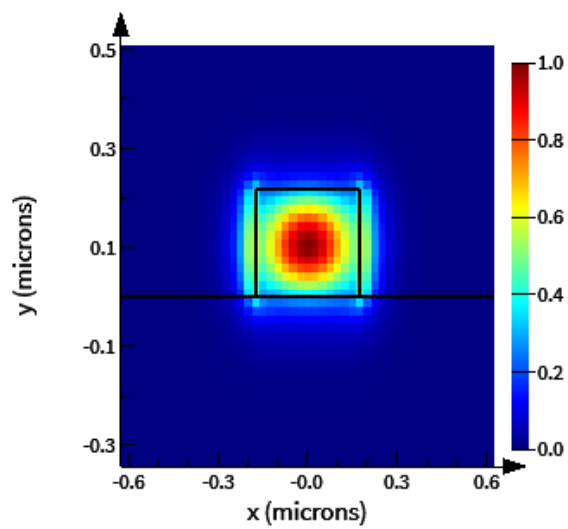
x (μm)	<input type="text" value="0"/>	x min (μm)	<input type="text" value="-2"/>
x span (μm)	<input type="text" value="4"/>	x max (μm)	<input type="text" value="2"/>

y (μm)	<input type="text" value="-1"/>	y min (μm)	<input type="text" value="-2"/>
y span (μm)	<input type="text" value="2"/>	y max (μm)	<input type="text" value="0"/>

z (μm)	<input type="text" value="0"/>	z min (μm)	<input type="text" value="-0.3"/>
z span (μm)	<input type="text" value="0.6"/>	z max (μm)	<input type="text" value="0.3"/>

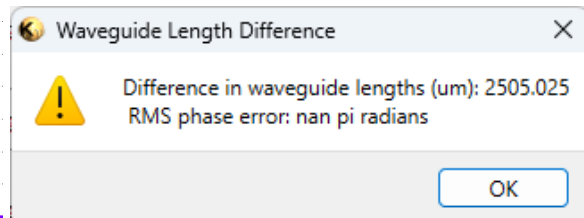
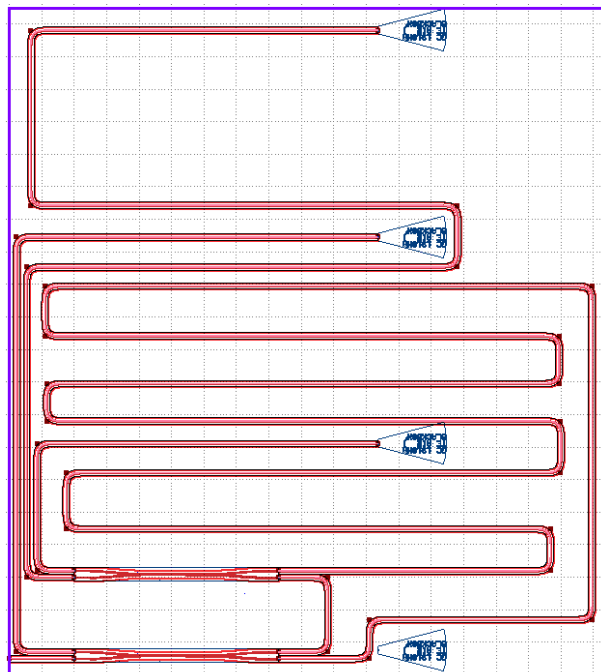
☒ use relative coordinates

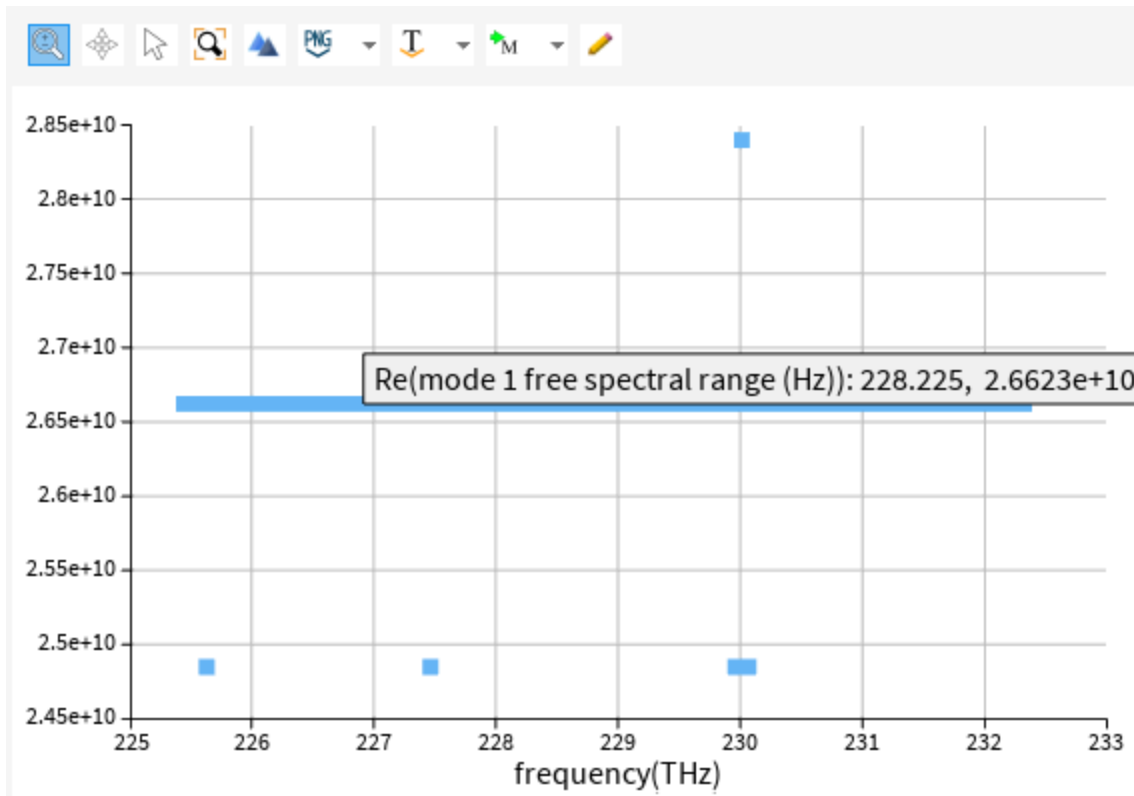
[Cancel](#)



Eigensolver Analysis							
Mode list							
mode #	effective index	wavelength (μm)	loss (dB/cm)	group index	TE polarization fraction (Ex)	waveguide TE/TM fraction (%)	effective area (μm <sup>2</sup> )
1	2.355116+1.723409e-09i	1.31	0.00071798	4.786668+3.484210e-09i	97	65.47 / 84.16	0.140897
2	1.845431+1.543339e-09i	1.31	0.00064296	5.028435+7.395737e-09i	6	59.66 / 87.37	0.200235

The group index is 4.786668, and from my python calculations, this means there is a required path length difference of 2505.22 μm.





Based on my simulation of chip 2, the FSR was about 26 GHz. This is slightly larger than I wanted, however I am confident in my path length difference calculation and so will keep the same pathlength.

**Having the correct path difference is resulting in the wrong FSR.**

## Chip 2 Design

```
print("Path Length Difference for ng = 4.78668: ", calc_necessary_path_diff(4.78668) * 1e6, "um")
ng = 4.78668
L2 = 100.219e-6
L1 = 2605.244e-6

LTotal = L1
R_Total = L2
print("Path 1", LTotal * 1e6, "um")
print("Path 2", R_Total * 1e6, "um")

L_Diff = LTotal - R_Total
print("Path Length Difference = {:.2f}".format(L_Diff*1e6), "um")
FSR = calc_FSR_from_path_diff(L_Diff, ng)
print("FSR_GHz = ", FSR * 1e-9, "GHz")
print("FSR_nm = ", FSR * wavelength**2 / c * 1e9, "nm")
```

```
Path Length Difference for ng = 4.78668: 2505.222475703411 um
Path 1 2605.244 um
Path 2 100.219 um
Path Length Difference = 2505.03 um
FSR_GHz = 25.001970795734678 GHz
FSR_nm = 0.14311861735547823 nm
```