Computing R and ϕ (0)

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ln[1]:= JU[U_] = 1 + U (Log[U] - 1)
 Out[1]= 1 + U (-1 + Log[U])
  In[2]:= D[JU[U], U]
 Out[2]= Log [ U ]
  In[3]:= Simplify[D[JU[U], U] == Log[U]]
 Out[3]= True
  ln[4]:= Wbar [\eta_{-}]=0.595+\eta/3.7+\eta^{4.55}
 Out[4]= 0.595 + 0.27027 \eta + \eta^{4.55}
  ln[5] = D[Wbar[\eta], \eta]
 Out[5]= 0.27027 + 4.55 \eta^{3.55}
  ln[6]:= Simplify D[Wbar[\eta], \eta] == 1/3.7 + 4.55 \eta^{3.55}
 Out[6]= True
  In[7]:= q[Wbar_] = (2 Wbar - 1) / (1 - Wbar)
  In[8]:= Simplify[D[q[Wbar], Wbar]]
  ln[9] = Simplify[D[q[Wbar], Wbar] == (Wbar - 1)^{-2}]
 Out[9]= True
 \ln[10] = \frac{GU[U_{q}, q]}{1 - (1 - 1 / U^{1+q}) / (1+q)} / (2+q) Ju[U]
\text{Out[10]=} \  \  \frac{-\,1\,+\,U\,-\,\frac{1-U^{-1-q}}{1+q}}{\left(\,2\,+\,q\,\right)\,\,Ju\,[\,U\,]}
 In[11]:= Simplify[Expand[GU[U, q]]]
\text{Out[11]=} \  \, - \, \frac{2 \, + \, q \, - \, U \, - \, q \, \, U \, - \, U^{-1-q}}{\left(\, 2 \, + \, 3 \, \, q \, + \, q^2 \, \right) \, \, Ju \, [\, U \, ]}
ln[12]:= Simplify \Big[GU[U, q] == \frac{U(1+q) - (2+q) + U^{-1-q}}{(1+q)(2+q) Ju[U]}\Big]
Out[12]= True
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$$\text{Out[13]=} \quad \frac{1 + \frac{\left(-1 - q\right) \; U^{-2 - q}}{1 + q}}{\left(2 + q\right) \; Ju\left[U\right]} \; - \; \frac{\left(-1 + U - \frac{1 - U^{-1 - q}}{1 + q}\right) \; Ju'\left[U\right]}{\left(2 + q\right) \; Ju\left[U\right]^2}$$

$$\ln[14] = \frac{\left(-1 + U - \frac{1 - U^{-1 - q}}{1 + q}\right) Ju'[U]}{(2 + q) Ju[U]^2} / GU[U, q]$$

$$\text{Out[14]=} \quad \frac{\text{Ju'}\left[\,\text{U}\,\right]}{\text{Ju}\left[\,\text{U}\,\right]}$$

$$I_{D[15]} = Simplify \left[D[GU[U, q], U] = \frac{1 - U^{-2-q}}{(2+q) Ju[U]} - \left(\frac{Ju'[U]}{Ju[U]} \right) GU[U, q] \right]$$

Out[15]= True

$$In[16]:= D[GU[U, q], q]$$

$$\text{Out[16]=} \ \, -\frac{-\,1\,+\,U\,-\,\frac{1\,-\,U^{-\,1\,-\,q}}{1\,+\,q}}{\left(\,2\,+\,q\,\right)^{\,2}\,Ju\,[\,U\,]} \,\,+\,\, \frac{\frac{1\,-\,U^{-\,1\,-\,q}}{\left(\,1\,+\,q\,\right)^{\,2}}\,-\,\frac{U^{-\,1\,-\,q}\,Log\,[\,U\,]}{1\,+\,q}}{\left(\,2\,+\,q\,\right)\,\,Ju\,[\,U\,]}$$

$$ln[17] = \frac{-1 + U - \frac{1 - U^{-1 - q}}{1 + q}}{(2 + q)^2 Ju[U]} / GU[U, q]$$

Out[17]=
$$\frac{1}{2+a}$$

$$ln[18] = Simplify \left[\frac{1 - U^{-1-q}}{(1+q)^2} - \frac{U^{-1-q} Log[U]}{1+q} \right]$$

Out[18]=
$$\frac{U^{-1-q} \left(-1 + U^{1+q} - (1+q) Log[U]\right)}{(1+q)^{2}}$$

$$In[19]:= Simplify \left[D[GU[U, q], q] = \left(\frac{\left(U^{1+q} - 1 \right) - (1+q) Log[U]}{Ju[U] U^{1+q} (1+q)^{2}} - GU[U, q] \right) / (2+q) \right]$$

Out[19]= True

$$ln[20] := CForm \left[\left(\frac{\frac{1-U^{-1-q}}{(1+q)^2} - \frac{U^{-1-q} Log[U]}{1+q}}{Ju[U]} - GU[U, q] \right) \right/ (2+q) \right]$$

$$ln[21] = etaBar[Zbarb_] = 1.75 \times 10^{-3} Zbarb + 0.37 (1 - Exp[-0.015 Zbarb^{1.3}])$$

$$\text{Out[21]=} \hspace{0.2cm} \textbf{0.37} \hspace{0.2cm} \left(\textbf{1} - \textbf{@}^{-\textbf{0.015} \hspace{0.1cm} Zbarb^{\textbf{1.3}}} \right) \hspace{0.1cm} + \textbf{0.00175} \hspace{0.1cm} Zbarb \right.$$

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In[22]:= Plot[etaBar[z], {z, 1, 100}]
      0.5
      0.4
      0.3
Out[22]=
      0.2
      0.1
                                                          80
                                                                      100
In[23]:= D[etaBar[Zbarb], Zbarb]
Out[23]= 0.00175 + 0.007215 e^{-0.015 \, Zbarb^{1.3}} \, Zbarb^{0.3}
log[24] = Simplify[D[etaBar[Zbarb], Zbarb] == 0.00175 + 0.007215 Exp[-0.015 Zbarb^{1.3}] Zbarb^{0.3}]
Out[24]= True
In[25]:= R[Zbarb_, E0_] = 1 - etaBarZ[Zbarb] WbarZ[Zbarb] (1 - G[E0, Zbarb])
Out[25]= 1 - etaBarZ[Zbarb] (1 - G[E0, Zbarb]) WbarZ[Zbarb]
In[26]:= D[R[Zbarb, E0], Zbarb]
Out[26]= - (1 - G[E0, Zbarb]) WbarZ[Zbarb] etaBarZ'[Zbarb] -
        etaBarZ[Zbarb] (1 - G[E0, Zbarb]) WbarZ'[Zbarb] +
        etaBarZ[Zbarb] WbarZ[Zbarb] G<sup>(0,1)</sup> [E0, Zbarb]
In[27]:= Simplify[D[R[Zbarb, E0], Zbarb] ==
         etaBarZ[Zbarb] (WbarZ[Zbarb] G^{(0,1)} [E0, Zbarb] - (1 - G[E0, Zbarb]) WbarZ' [Zbarb]) -
           (1 - G[E0, Zbarb]) WbarZ[Zbarb] etaBarZ'[Zbarb]]
Out[27]= True
In[28]:= D[R[Zbarb, E0], E0]
Out[28]= etaBarZ[Zbarb] WbarZ[Zbarb] G<sup>(1,0)</sup> [E0, Zbarb]
In[29]:= Simplify[D[R[Zbarb, E0], E0] == etaBarZ[Zbarb] WbarZ[Zbarb] G<sup>(1,0)</sup> [E0, Zbarb]]
Out[29]= True
ln[30]: Phi0[etaBar_, U0_] = 1 + 33 / 10 (1 - 1 / U0<sup>2-23/10 etaBar</sup>) etaBar<sup>6/5</sup>
Out[30]= 1 + \frac{33}{10} etaBar<sup>6/5</sup> \left(1 - U0^{-2 + \frac{23 \text{ etaBar}}{10}}\right)
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In[31]:= Simplify[D[Phi0[etaBar, U0], etaBar]]

Out[31]:= - \frac{33 \text{ etaBar}^{1/5} \left( 12 \left( -U0^2 + U0^{23} \text{ etaBar}/10 \right) + 23 \text{ etaBar} \text{ U0}^{23} \text{ etaBar}/10 \text{ Log}[U0] \right)}{100 \text{ U0}^2}

In[32]:= Simplify[D[Phi0[etaBar, U0], etaBar] == \text{ etaBar}^{1/5} \left( 396 / 100 \left( 1 - U0^{23/10} \text{ etaBar}-2 \right) - 759 / 100 \text{ etaBar} \text{ U0}^{23/10} \text{ etaBar}-2 \text{ Log}[U0] \right) \right]

Out[32]:= True

In[33]:= D[Phi0[etaBar, U0], U0]

Out[33]:= \frac{33}{10} \text{ etaBar}^{6/5} \left( -2 + \frac{23 \text{ etaBar}}{10} \right) \text{ U0}^{-3 + \frac{23 \text{ etaBar}}{10}}

In[36]:= Simplify[D[Phi0[etaBar, U0], U0] == -33 / 10 \text{ etaBar}^{6/5} \left( -2 + 23 / 10 \text{ etaBar} \right) \text{ U0}^{23/10 \text{ etaBar}-3} \right]

Out[36]:= True

In[35]:= 3 \times 0.869565

Out[35]:= 2.6087
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