

F/Rbar and Rbar

$$\text{In}[*]:= \text{X}[\text{zbarb_}] = 1 + 1.3 \text{Log}[\text{zbarb}]$$

$$\text{Out}[*]:= 1 + 1.3 \text{Log}[\text{zbarb}]$$

$$\text{In}[*]:= \text{D}[\text{X}[\text{zbarb}], \text{zbarb}]$$

$$\text{Out}[*]:= \frac{1.3}{\text{zbarb}}$$

$$\text{In}[*]:= \text{Y}[\text{zbarb_}] = 0.2 + 0.005 \text{zbarb}$$

$$\text{Out}[*]:= 0.2 + 0.005 \text{zbarb}$$

$$\text{In}[*]:= \text{D}[\text{Y}[\text{zbarb}], \text{zbarb}]$$

$$\text{Out}[*]:= 0.005$$

$$\text{In}[*]:= \text{FoRbar}[\text{zbarb_}, \text{U0_}] = 1 + \frac{\text{Xx}[\text{zbarb}] \text{Log}[1 + \text{Yy}[\text{zbarb}] (1 - \text{U0}^{-0.42})]}{\text{Log}[1 + \text{Yy}[\text{zbarb}]]}$$

$$\text{Out}[*]:= 1 + \frac{\text{Log}\left[1 + \left(1 - \frac{1}{\text{U0}^{0.42}}\right) \text{Yy}[\text{zbarb}]\right] \text{Xx}[\text{zbarb}]}{\text{Log}[1 + \text{Yy}[\text{zbarb}]]}$$

$$\text{In}[*]:= \text{D}[\text{FoRbar}[\text{zbarb}, \text{U0}], \text{zbarb}]$$

$$\text{Out}[*]:= \frac{\text{Log}\left[1 + \left(1 - \frac{1}{\text{U0}^{0.42}}\right) \text{Yy}[\text{zbarb}]\right] \text{Xx}'[\text{zbarb}]}{\text{Log}[1 + \text{Yy}[\text{zbarb}]]} - \frac{\text{Log}\left[1 + \left(1 - \frac{1}{\text{U0}^{0.42}}\right) \text{Yy}[\text{zbarb}]\right] \text{Xx}[\text{zbarb}] \text{Yy}'[\text{zbarb}]}{\text{Log}[1 + \text{Yy}[\text{zbarb}]]^2 (1 + \text{Yy}[\text{zbarb}])} + \frac{\left(1 - \frac{1}{\text{U0}^{0.42}}\right) \text{Xx}[\text{zbarb}] \text{Yy}'[\text{zbarb}]}{\text{Log}[1 + \text{Yy}[\text{zbarb}]] \left(1 + \left(1 - \frac{1}{\text{U0}^{0.42}}\right) \text{Yy}[\text{zbarb}]\right)}$$

$$\text{In}[*]:= \text{Simplify}[$$

$$\text{D}[\text{FoRbar}[\text{zbarb}, \text{U0}], \text{zbarb}] == \text{D}[\text{FoRbar}[\text{zbarb}, \text{U0}], \text{Xx}[\text{zbarb}]] \text{D}[\text{Xx}[\text{zbarb}], \text{zbarb}] + \text{D}[\text{FoRbar}[\text{zbarb}, \text{U0}], \text{Yy}[\text{zbarb}]] \text{D}[\text{Yy}[\text{zbarb}], \text{zbarb}]$$

$$\text{Out}[*]:= \text{True}$$

$$\text{In}[*]:= \text{Simplify}[\text{D}[\text{FoRbar}[\text{zbarb}, \text{U0}], \text{Xx}[\text{zbarb}]]]$$

$$\text{Out}[*]:= \frac{\text{Log}\left[1 + \text{Yy}[\text{zbarb}] - \frac{\text{Yy}[\text{zbarb}]}{\text{U0}^{0.42}}\right]}{\text{Log}[1 + \text{Yy}[\text{zbarb}]]}$$

$$\text{In}[*]:= \text{Simplify}[\text{D}[\text{FoRbar}[\text{zbarb}, \text{U0}], \text{Yy}[\text{zbarb}]]]$$

$$\text{Out}[*]:= \frac{\text{Xx}[\text{zbarb}] \left(-\frac{\text{Log}\left[1 + \text{Yy}[\text{zbarb}] - \frac{\text{Yy}[\text{zbarb}]}{\text{U0}^{0.42}}\right]}{1 + \text{Yy}[\text{zbarb}]} + \frac{(-1 + \text{U0}^{0.42}) \text{Log}[1 + \text{Yy}[\text{zbarb}]]}{\text{U0}^{0.42} + (-1 + \text{U0}^{0.42}) \text{Yy}[\text{zbarb}]} \right)}{\text{Log}[1 + \text{Yy}[\text{zbarb}]]^2}$$

In[*]:= D[FoRbar[zbarb, U0], U0]

$$\text{Out[*]} = \frac{0.42 \text{Xx[zbarb]} \text{Yy[zbarb]}}{U0^{1.42} \text{Log}[1 + \text{Yy[zbarb]}] \left(1 + \left(1 - \frac{1}{U0^{0.42}}\right) \text{Yy[zbarb]}\right)}$$

$$\text{In[*]} := \text{D[FoRbar[zbarb, U0], U0]} = \frac{0.42 \text{Xx[zbarb]} \text{Yy[zbarb]}}{U0 U0^{0.42} \text{Log}[1 + \text{Yy[zbarb]}] \left(1 + \left(1 - \frac{1}{U0^{0.42}}\right) \text{Yy[zbarb]}\right)}$$

Out[*]= True

In[*]:= F[R_, OoS_, Q1a_] = R OoS / Q1a

$$\text{Out[*]} = \frac{\text{OoS R}}{\text{Q1a}}$$

In[*]:= D[F[R, OoS, Q1a], R]

$$\text{Out[*]} = \frac{\text{OoS}}{\text{Q1a}}$$

In[*]:= D[F[R, OoS, Q1a], OoS]

$$\text{Out[*]} = \frac{\text{R}}{\text{Q1a}}$$

In[*]:= D[F[R, OoS, Q1a], Q1a]

$$\text{Out[*]} = -\frac{\text{OoS R}}{\text{Q1a}^2}$$

In[*]:= Rbar[zbarb_, U0_] = F / FoRbar

$$\text{Out[*]} = \frac{\text{F}}{\text{FoRbar}}$$

In[*]:= D[Rbar[zbarb, U0], FoRbar]

$$\text{Out[*]} = -\frac{\text{F}}{\text{FoRbar}^2}$$