

In[25]:= **B[b\_, f\_, eps\_, p\_, phi0\_] = Simplify[(b^2 f (1 + eps) - p - phi0 b (2 + eps)) / eps]**

Out[25]= 
$$-\frac{-b^2 (1 + \text{eps}) f + p + b (2 + \text{eps}) \text{phi0}}{\text{eps}}$$

In[26]:= **D[B[b, f, eps, p, phi0], b]**

Out[26]= 
$$-\frac{-2 b (1 + \text{eps}) f + (2 + \text{eps}) \text{phi0}}{\text{eps}}$$

In[29]:= **Simplify[D[B[b, f, eps, p, phi0], b] == (2 b (1 + eps) f - (2 + eps) phi0) / eps]**

Out[29]= True

In[30]:= **D[B[b, f, eps, p, phi0], f]**

Out[30]= 
$$\frac{b^2 (1 + \text{eps})}{\text{eps}}$$

In[31]:= **Simplify[D[B[b, f, eps, p, phi0], f] == b^2 (1 + eps) / eps]**

In[33]:= **Simplify[D[B[b, f, eps, p, phi0], eps]]**

Out[33]= 
$$\frac{-b^2 f + p + 2 b \text{phi0}}{\text{eps}^2}$$

**Simplify[D[B[b, f, eps, p, phi0], eps] == (p + 2 b phi0 - b^2 f) / eps^2]**

Out[34]= True

In[35]:= **Simplify[D[B[b, f, eps, p, phi0], p]]**

Out[35]= 
$$-\frac{1}{\text{eps}}$$

In[36]:= **Simplify[D[B[b, f, eps, p, phi0], p] == -1 / eps]**

Out[36]= True

In[37]:= **Simplify[D[B[b, f, eps, p, phi0], phi0]]**

Out[37]= 
$$-\frac{b (2 + \text{eps})}{\text{eps}}$$

In[38]:= **Simplify[D[B[b, f, eps, p, phi0], phi0] == -b (2 + eps) / eps]**

Out[38]= True

In[27]:= **A[B\_, b\_, phi0\_, b\_, f\_, eps\_] = (B / b + phi0 - b f) (1 + eps) / eps**

Out[27]= 
$$\frac{(1 + \text{eps}) \left( \frac{B}{b} - b f + \text{phi0} \right)}{\text{eps}}$$

In[41]:= Simplify[D[A[Bb[b, f, eps, p, phi0], b, phi0, b, f, eps], b]]

$$\text{Out[41]} = - \frac{(1 + \text{eps}) \left( \text{Bb}[b, f, \text{eps}, p, \text{phi0}] + b \left( b f - \text{Bb}^{(1,0,0,0,0)}[b, f, \text{eps}, p, \text{phi0}] \right) \right)}{b^2 \text{eps}}$$

In[42]:= Simplify[D[A[Bb[b, f, eps, p, phi0], b, phi0, b, f, eps], b] ==

$$- \frac{(1 + \text{eps}) \left( \text{Bb}[b, f, \text{eps}, p, \text{phi0}] + b \left( b f - D[\text{Bb}[b, f, \text{eps}, p, \text{phi0}], b] \right) \right)}{b^2 \text{eps}} \Big]$$

Out[42]= True

In[43]:= Simplify[D[A[Bb[b, f, eps, p, phi0], b, phi0, b, f, eps], phi0]]

$$\text{Out[43]} = \frac{(1 + \text{eps}) \left( b + \text{Bb}^{(0,0,0,0,1)}[b, f, \text{eps}, p, \text{phi0}] \right)}{b \text{eps}}$$

In[44]:= Simplify[D[A[Bb[b, f, eps, p, phi0], b, phi0, b, f, eps], phi0] ==

$$\frac{(1 + \text{eps}) \left( b + D[\text{Bb}[b, f, \text{eps}, p, \text{phi0}], \text{phi0}] \right)}{b \text{eps}} \Big]$$

Out[44]= True

In[45]:= Simplify[D[A[Bb[b, f, eps, p, phi0], b, phi0, b, f, eps], b]]

$$\text{Out[45]} = - \frac{(1 + \text{eps}) \left( \text{Bb}[b, f, \text{eps}, p, \text{phi0}] + b \left( b f - \text{Bb}^{(1,0,0,0,0)}[b, f, \text{eps}, p, \text{phi0}] \right) \right)}{b^2 \text{eps}}$$

In[46]:= Simplify[D[A[Bb[b, f, eps, p, phi0], b, phi0, b, f, eps], b] ==

$$- \frac{(1 + \text{eps}) \left( \text{Bb}[b, f, \text{eps}, p, \text{phi0}] + b \left( b f - D[\text{Bb}[b, f, \text{eps}, p, \text{phi0}], b] \right) \right)}{b^2 \text{eps}} \Big]$$

Out[46]= True

In[47]:= Simplify[D[A[Bb[b, f, eps, p, phi0], b, phi0, b, f, eps], f]]

$$\text{Out[47]} = \frac{(1 + \text{eps}) \left( -b + \frac{\text{Bb}^{(0,1,0,0,0)}[b, f, \text{eps}, p, \text{phi0}]}{b} \right)}{\text{eps}}$$

In[51]:= Simplify[D[A[Bb[b, f, eps, p, phi0], b, phi0, b, f, eps], f] ==

$$(1 + \text{eps}) \left( D[\text{Bb}[b, f, \text{eps}, p, \text{phi0}], f] - b^2 \right) / (b \text{eps}) \Big]$$

Out[51]= True

In[52]:= Simplify[D[A[Bb[b, f, eps, p, phi0], b, phi0, b, f, eps], eps]]

$$\text{Out[52]} = \frac{1}{b \text{eps}^2} \left( b \left( b f - \text{phi0} \right) - \text{Bb}[b, f, \text{eps}, p, \text{phi0}] + \text{eps} (1 + \text{eps}) \text{Bb}^{(0,0,1,0,0)}[b, f, \text{eps}, p, \text{phi0}] \right)$$

```
In[54]:= Simplify[D[A[Bb[b, f, eps, p, phi0], b, phi0, b, f, eps], eps] ==
      (b (b f - phi0) - Bb[b, f, eps, p, phi0] + eps (1 + eps) D[Bb[b, f, eps, p, phi0], eps]) /
      (b eps^2)]
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Out[54]= True
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In[55]:= Simplify[D[A[Bb[b, f, eps, p, phi0], b, phi0, b, f, eps], p]]
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Out[55]= 
$$\frac{(1 + \text{eps}) \text{Bb}^{(0,0,0,1,0)}[b, f, \text{eps}, p, \text{phi0}]}{b \text{eps}}$$

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In[56]:= Simplify[
      D[A[Bb[b, f, eps, p, phi0], b, phi0, b, f, eps], p] == 
$$\frac{(1 + \text{eps}) D[Bb[b, f, \text{eps}, p, \text{phi0}], p]}{b \text{eps}}$$
]
```

```
Out[56]= True
```