

In[53]:= **B[b_, f_, eps_, p_, phi0_] = Simplify[(b² f (1 + eps) - p - phi0 b (2 + eps)) / eps]**

Out[53]=
$$-\frac{b^2 (1 + \text{eps}) f + p + b (2 + \text{eps}) \text{phi0}}{\text{eps}}$$

In[54]:= **D[B[b, f, eps, p, phi0], b]**

Out[54]=
$$-\frac{2 b (1 + \text{eps}) f + (2 + \text{eps}) \text{phi0}}{\text{eps}}$$

In[55]:= **Simplify[D[B[b, f, eps, p, phi0], b] == (2 b (1 + eps) f - (2 + eps) phi0) / eps]**

Out[55]= True

In[56]:= **D[B[b, f, eps, p, phi0], f]**

Out[56]=
$$\frac{b^2 (1 + \text{eps})}{\text{eps}}$$

In[57]:= **Simplify[D[B[b, f, eps, p, phi0], f] == b² (1 + eps) / eps]**

Out[57]= True

In[58]:= **Simplify[D[B[b, f, eps, p, phi0], eps]]**

Out[58]=
$$\frac{-b^2 f + p + 2 b \text{phi0}}{\text{eps}^2}$$

In[59]:= **Simplify[D[B[b, f, eps, p, phi0], eps] == (p + 2 b phi0 - b² f) / eps²]**

Out[59]= True

In[60]:= **Simplify[D[B[b, f, eps, p, phi0], p]]**

Out[60]=
$$-\frac{1}{\text{eps}}$$

In[61]:= **Simplify[D[B[b, f, eps, p, phi0], p] == -1 / eps]**

Out[61]= True

In[62]:= **Simplify[D[B[b, f, eps, p, phi0], phi0]]**

Out[62]=
$$-\frac{b (2 + \text{eps})}{\text{eps}}$$

In[63]:= **Simplify[D[B[b, f, eps, p, phi0], phi0] == -b (2 + eps) / eps]**

Out[63]= True

In[98]:= **A[B_, b_, phi0_, f_, eps_] = (B / b + phi0 - b f) (1 + eps) / eps**

Out[98]=
$$\frac{(1 + \text{eps}) \left(\frac{B}{b} - b f + \text{phi0} \right)}{\text{eps}}$$

In[99]:= **Simplify**[D[A[Bb[b, f, eps, p, phi0], b, phi0, f, eps], b]]

$$\text{Out[99]} = - \frac{(1 + \text{eps}) \left(\text{Bb}[b, f, \text{eps}, p, \text{phi0}] + b \left(b f - \text{Bb}^{(1,0,0,0,0)}[b, f, \text{eps}, p, \text{phi0}] \right) \right)}{b^2 \text{eps}}$$

In[101]:= **Simplify**[D[A[Bb[b, f, eps, p, phi0], b, phi0, f, eps], phi0]]

$$\text{Out[101]} = \frac{(1 + \text{eps}) \left(b + \text{Bb}^{(0,0,0,0,1)}[b, f, \text{eps}, p, \text{phi0}] \right)}{b \text{eps}}$$

In[116]:= **Simplify**[D[A[Bb[b, f, eps, p, phi0], b, phi0, f, eps], phi0] ==

$$\frac{(1 + \text{eps})}{\text{eps}} \left(\frac{b + D[\text{Bb}[b, f, \text{eps}, p, \text{phi0}], \text{phi0}]}{b} \right)]$$

Out[116]= True

In[103]:= **Simplify**[D[A[Bb[b, f, eps, p, phi0], b, phi0, f, eps], b]]

$$\text{Out[103]} = - \frac{(1 + \text{eps}) \left(\text{Bb}[b, f, \text{eps}, p, \text{phi0}] + b \left(b f - \text{Bb}^{(1,0,0,0,0)}[b, f, \text{eps}, p, \text{phi0}] \right) \right)}{b^2 \text{eps}}$$

In[115]:= **Simplify**[D[A[Bb[b, f, eps, p, phi0], b, phi0, f, eps], b] ==

$$\frac{(1 + \text{eps})}{\text{eps}} \left(\frac{D[\text{Bb}[b, f, \text{eps}, p, \text{phi0}], b]}{b} - \left(\frac{\text{Bb}[b, f, \text{eps}, p, \text{phi0}]}{b^2} + f \right) \right)]$$

Out[115]= True

In[105]:= **Simplify**[D[A[Bb[b, f, eps, p, phi0], b, phi0, f, eps], f]]

$$\text{Out[105]} = \frac{(1 + \text{eps}) \left(-b + \frac{\text{Bb}^{(0,1,0,0,0)}[b, f, \text{eps}, p, \text{phi0}]}{b} \right)}{\text{eps}}$$

In[117]:= **Simplify**[D[A[Bb[b, f, eps, p, phi0], b, phi0, f, eps], f] ==

$$\frac{(1 + \text{eps})}{\text{eps}} \left(D[\text{Bb}[b, f, \text{eps}, p, \text{phi0}], f] - b^2 \right) / b]$$

Out[117]= True

In[118]:= D[A[Bb[b, f, eps, p, phi0], b, phi0, f, eps], p]

$$\text{Out[118]} = \frac{(1 + \text{eps}) \text{Bb}^{(0,0,0,1,0)}[b, f, \text{eps}, p, \text{phi0}]}{b \text{eps}}$$

In[119]:= **Simplify**[

$$D[A[Bb[b, f, \text{eps}, p, \text{phi0}], b, phi0, f, \text{eps}], p] = \frac{1}{b} D[\text{Bb}[b, f, \text{eps}, p, \text{phi0}], p] \frac{(1 + \text{eps})}{\text{eps}}]$$

Out[119]= True