

In[2]:= **a[phi0_, p_, rbar_, f_, b_] = (p + b (2 phi0 - b f)) / (b f (2 - b rbar) - phi0)**

Out[2]=
$$\frac{p + b (-b f + 2 \text{phi0})}{-\text{phi0} + b f (2 - b \text{rbar})}$$

In[3]:= **D[a[phi0, p, rbar, f, b], phi0]**

Out[3]=
$$\frac{p + b (-b f + 2 \text{phi0})}{(-\text{phi0} + b f (2 - b \text{rbar}))^2} + \frac{2 b}{-\text{phi0} + b f (2 - b \text{rbar})}$$

In[6]:= **Simplify[D[a[phi0, p, rbar, f, b], phi0] == $\frac{3 b^2 f + p - 2 b^3 f \text{rbar}}{(-2 b f + \text{phi0} + b^2 f \text{rbar})^2}$]**

Out[6]= True

In[6]:= **Simplify[D[a[phi0, p, rbar, f, b], p] == 1 / (b f (2 - b rbar) - phi0)]**

Out[6]= True

In[13]:= **Simplify[
D[a[phi0, p, rbar, f, b], rbar] == $\frac{b^2 f (-b^2 f + p + 2 b \text{phi0})}{(-2 b f + \text{phi0} + b^2 f \text{rbar})^2}$]**

Out[13]= True

In[14]:= **Simplify[D[a[phi0, p, rbar, f, b], f] == b $\frac{(p (-2 + b \text{rbar}) + b \text{phi0} (-3 + 2 b \text{rbar}))}{(-2 b f + \text{phi0} + b^2 f \text{rbar})^2}$]**

Out[14]= True

In[15]:= **Simplify[
D[a[phi0, p, rbar, f, b], b] == -2 $\frac{(f p + \text{phi0}^2 - b f (\text{phi0} + p \text{rbar}) + b^2 f (f - \text{phi0} \text{rbar}))}{(-2 b f + \text{phi0} + b^2 f \text{rbar})^2}$]**

Out[15]= True