**FUNDAMENTAL CONCEPTS OF CRYPTOGRAPHY**

**ASSIGNMENT TWO**

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**Question 1**

2) GCD (2543, 1672) is 1 with s = 215 and t = -327

3) Prove this statement:

Say equation 1: then,

Say equation 2: then c could be established as 3:

This would mean if then this would mean   
And if then this would mean

So any common divisor of *a* and *b*  would be a common divisor of , using equation 3 we could say that a and as such we also say which together we say therefore and by expansion

Next, since any common divisor of *b* and *c* would be a common divisor of , using equation 2 we could then say that and as such could also say which together is and by expansion

Since both and we can follow that

**Question 2**

**Original Text:**

For example as pointed out by researcher. For each set of fuzzy terms, $A \subseteq M$, $\prod\_{m\in

A}m$ represents a conjunction of the fuzzy terms in $A$. For

instance,

let $A=\{m\_{1,2},m\_{2,1},m\_{4,2}\}\subseteq M$, a new

fuzzy concept ``$m\_{1,2}$ and $m\_{2,1}$ and $m\_{4,2}$" with the linguist

interpretation ``\emph{short sepal and wide sepal and narrow petal}"

can be represented as $\prodfh

NOTE: This is shorter as I made it so the ciphertext for this would fit on one page

**Cecrypted text with p=10007, q=52121, e=25537**

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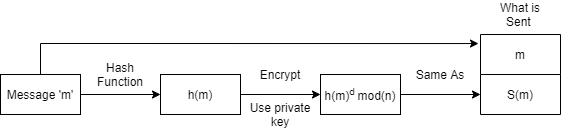
**Cipher text with p=10007, q=52121, e=25537**

396718713,243165040,124159753,501745882,45510371,123270073,394376890,449406297,374093100,81958626,45510371,501745882,394376890,412917588,501745882,374093100,243165040,352919765,40263658,119753139,45510371,129395635,501745882,243165040,195782056,119753139,501745882,326063704,482857730,501745882,124159753,45510371,412917588,45510371,394376890,124159753,434587804,267577422,45510371,124159753,25230260,501745882,396718713,243165040,124159753,501745882,45510371,394376890,434587804,267577422,501745882,412917588,45510371,119753139,501745882,243165040,272681844,501745882,272681844,195782056,264862402,264862402,482857730,501745882,119753139,45510371,124159753,449406297,412917588,280895377,501745882,417516626,297787375,501745882,505546589,412917588,195782056,326063704,412917588,45510371,119753139,45510371,198076322,501745882,52497663,417516626,280895377,501745882,417516626,505546589,374093100,124159753,243165040,129395635,255302601,206155709,449406297,505546589,352919765,40263658,371896273,297787375,453064844,449406297,417516626,501745882,124159753,45510371,374093100,124159753,45510371,412917588,45510371,40263658,119753139,412917588,501745882,394376890,501745882,434587804,243165040,40263658,476540999,195782056,40263658,434587804,119753139,352919765,243165040,40263658,501745882,243165040,272681844,501745882,119753139,267577422,45510371,501745882,272681844,195782056,264862402,264862402,482857730,501745882,119753139,45510371,124159753,449406297,412917588,501745882,352919765,40263658,501745882,417516626,297787375,417516626,25230260,501745882,396718713,243165040,124159753,371896273,352919765,40263658,412917588,119753139,394376890,40263658,434587804,45510371,280895377,371896273,501745882,81958626,45510371,119753139,501745882,417516626,297787375,373047187,505546589,206155709,449406297,255302601,206155709,335271736,280895377,332565621,453064844,280895377,449406297,255302601,206155709,332565621,280895377,335271736,453064844,280895377,449406297,255302601,206155709,338453863,280895377,332565621,453064844,505546589,453064844,505546589,412917588,195782056,326063704,412917588,45510371,119753139,45510371,198076322,501745882,52497663,417516626,280895377,501745882,394376890,501745882,40263658,45510371,458320916,371896273,272681844,195782056,264862402,264862402,482857730,501745882,434587804,243165040,40263658,434587804,45510371,374093100,119753139,501745882,424060151,424060151,417516626,449406297,255302601,206155709,335271736,280895377,332565621,453064844,417516626,501745882,394376890,40263658,129395635,501745882,417516626,449406297,255302601,206155709,332565621,280895377,335271736,453064844,417516626,501745882,394376890,40263658,129395635,501745882,417516626,449406297,255302601,206155709,338453863,280895377,332565621,453064844,417516626,303436972,501745882,458320916,352919765,119753139,267577422,501745882,119753139,267577422,45510371,501745882,81958626,352919765,40263658,289282609,195782056,352919765,412917588,119753139,371896273,352919765,40263658,119753139,45510371,124159753,374093100,124159753,45510371,119753139,394376890,119753139,352919765,243165040,40263658,501745882,424060151,424060151,505546589,45510371,449406297,374093100,267577422,206155709,412917588,267577422,243165040,124159753,119753139,501745882,412917588,45510371,374093100,394376890,81958626,501745882,394376890,40263658,129395635,501745882,458320916,352919765,129395635,45510371,501745882,412917588,45510371,374093100,394376890,81958626,501745882,394376890,40263658,129395635,501745882,40263658,394376890,124159753,124159753,243165040,458320916,501745882,374093100,45510371,119753139,394376890,81958626,453064844,303436972,371896273,434587804,394376890,40263658,501745882,326063704,45510371,501745882,124159753,45510371,374093100,124159753,45510371,412917588,45510371,40263658,119753139,45510371,129395635,501745882,394376890,412917588,501745882,417516626,505546589,374093100,124159753,243165040,129395635

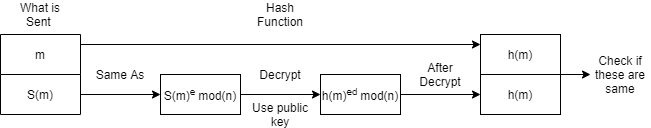
**Question 3**

The RSA signature structure depends on having a keyholder who can encrypt a message with a private key while everyone who is sent decrypts this message with their public key

Sender’s Signature:



Sender Authentication:



As part of the RSA signature scheme, the sender will have a message that they will hash to make it a certain length. Then, this hashed message is encrypted using the sender’s private key which makes up the sender’s signature. The sender will send this signature and the message to the recipient.

The recipient receives the signature which it then decrypts using its public key, the two keys will multiply and mod by n to produce just the hashed version of m. The recipient then, also takes the message sent and hashes that as well. It will compare both hashed messages, if these are the same then the authentication of the sender is achieved.

The hash function is created to have very low collision so that there are rarely collisions. But in this case Bob has two messages (*m* and *m*’) that hash to the same value but aren’t equal. In this way Bob already has Alice’s encrypted version of h(m) which is her certificate. Bob could send this encrypted version of Alice’s original h(m) along with m’. The recipient of bob’s message would decrypt Alice’s encrypted h(m) and end up with h(m) and would then hash the *m’* to get h(*m’*) . We know that h(m) and h(*m’*) are the same so therefore this recipient would think that Bob is Alice. Thus successfully forging her signature.

**Question 5**

Based on the lecture slides, the probability of at least one match is:

In this question there is a group of 24 people that can be chosen, allowing for this many combinations of two people.

So there are a total of 276 combination of 2 people in a group of 24 people

With k = 276, and n=365 we get this:

This results in a probability of 0.531