

## Low-Level Design

## Design

- ▶ High Level Design
  - public classes (used by clients/users)
  - public methods
  - public attributes
  - exceptions
- ▶ Low Level Design
  - high level design info **plus**
  - private classes, private methods, private attributes
  - data structures
  - algorithms

## Low Level Design Document

- ▶ provide the interface for all classes
  - public and private methods, including parameters, return values and exceptions thrown
  - types defined
- ▶ describe and justify your choice of data structures
  - describe the major alternatives that you considered and why you made the choice that you did
- ▶ describe all interesting algorithms
  - describe any alternatives that you considered and justify the choice that you made
- ▶ provide the inheritance relationships for your classes

## Low Level Design Presentation

- ▶ too much detail to present the full design
- ▶ what to present?
  - Review HLD
  - select representative aspects of the LLD
    - after seeing these should understand how similar parts of the design are done
  - select the most interesting aspects of the design
    - often the most controversial
    - demonstrates that you have thought about the issues

## How to do Low Level Design

- ▶ must consider alternatives
- ▶ make well-reasoned choices among alternatives
- ▶ when choice is not clear, pursue multiple solutions until
  - a choice becomes clear
  - it is too costly to pursue multiple solutions
    - make your best guess
    - plan for change
    - Try to keep the same interface so that the implementation is isolated

## Data structure and algorithm design

- ▶ still an art
- ▶ consider how the data structure will be used
  - types of operations
  - frequency of operations
- ▶ select a structure that will be
  - efficient for the proposed uses
  - easy to implement
  - easy to maintain
- ▶ usually see the finished product, not the alternatives that were explored and rejected

## Goals

- ▶ Figure out how to implement API defined during HLD:
  - What classes to create
  - How to relate those classes
  - What methods you will need
- ▶ Start to make some design decisions:
  - Data structures
  - Algorithms
  - Policies

## Goals (continue)

- ▶ Explore using existing software
  - What does it do?
  - How to extend it to do what you need?
  - How to fit it into API?
- ▶ Add/Keep Flexibility
  - Isolate low-level decisions in even lower-level structure
  - Try to make it easy to make changes

## An Incremental Approach

- ▶ Make some decisions
- ▶ Assess the consequences
  - Do other parts need to be changed now?
  - Will it be easy enough to implement?
  - Are all requirements met?
- ▶ Change these decisions or earlier ones
- ▶ Repeat

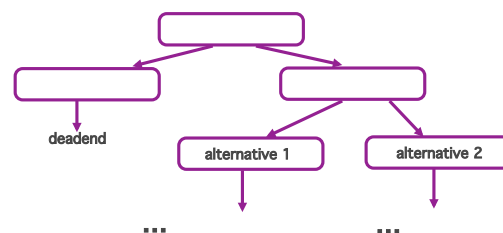
## Stepwise Refinement

- ▶ a well-known problem solving technique
- ▶ divide and conquer approach
- ▶ used in many disciplines
  - mathematics--lemmas and corollaries
  - house design--floor plans, wiring, etc.
- ▶ also called top down design, incremental development

## Guidelines for Stepwise Refinement

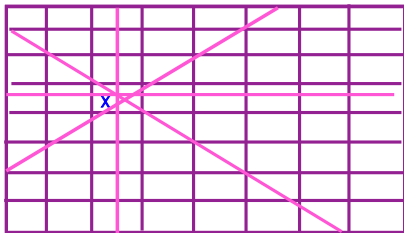
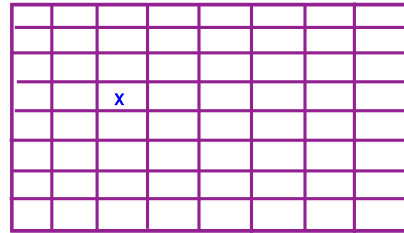
- ▶ decompose decisions
- ▶ untangle interdependencies
- ▶ defer representations and detailed algorithm decisions as long as possible
  - wait until there is information to help make these decision
- ▶ be prepared to undo previous steps and restart

## Decision Tree



## Example: 8 Queens problem

- Given an 8x8 chess board and 8 queens, find a safe position for each queen
  - i.e., every row, column, and diagonal contains at most one queen



## First Solution

$x$  an element of the set of configurations  
 $\text{safe}(x)$  is true if  $x$  satisfies the problem

```

solution := false
initialize configuration
repeat
  x := next configuration
until safe (x) or no more configurations
if safe(x) then
  solution := true
  print (" solution", x)
else print ( "no solution" )
endif
  
```

## First alternative

consider every possible board configuration

$$\begin{aligned}
 & \binom{64}{8} \\
 & \frac{64!}{(64-8)! 8!} \\
 & = \frac{64 \times 63 \times \dots \times 57}{8!} \sim 2^{32} \\
 & = 4,426,165,368
 \end{aligned}$$

## First alternative

- Could refine this solution but know it is expensive
  - Need to consider alternative solutions
- Considering efficiency at the algorithm level and data structure level

## Second alternative

- ▶ 1 queen in every column
  - $8^8 = 2^{24} = 16,777,216$
- ▶ previous algorithm is still adequate
- ▶ set of configurations is now restricted to configurations with 1 queen per column

## Second alternative elaborated

x an element of the set of configurations, where a configuration can only have one queen in each column  
safe(x) is true if x satisfies the problem

```

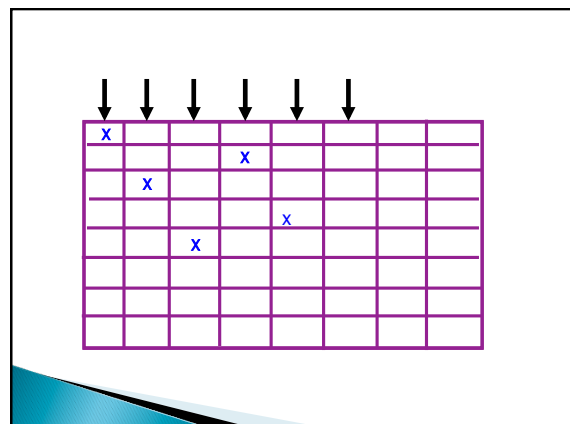
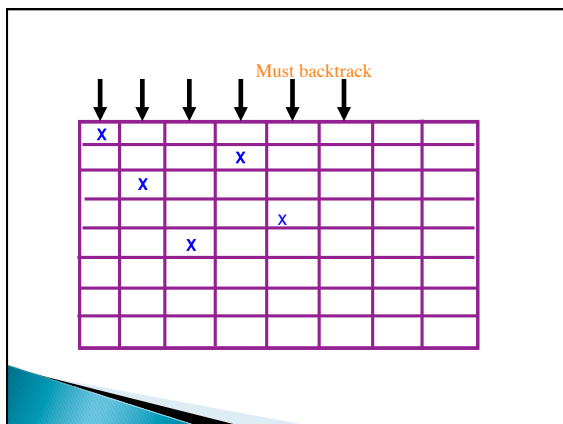
solution := false
initialize configuration
repeat
  x := next configuration
until safe (x) or no more configurations
if safe(x) then
  solution := true
  print (" solution", x)
else print ( "no solution" )
endif
  
```

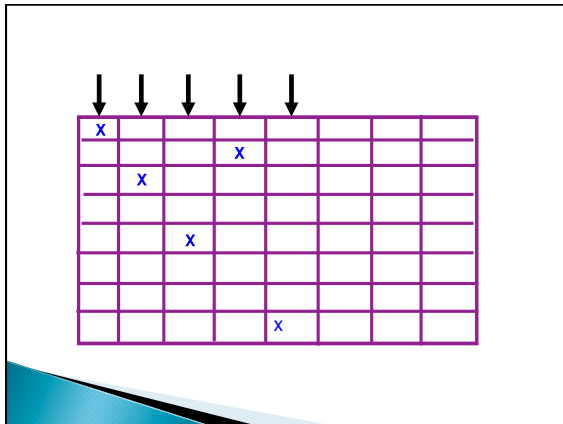
## Third alternative

- ▶ While forming next configuration, could be checking that it is safe
- ▶ safe (for a partial configuration)
  - $1 \leq i \leq 8$
  - x1
  - x1, x2
  - x1, x2, x3
- ▶ backtrack one column if there is no safe configuration for the next column

## Third Alternative

- ▶ similar to a counter
  - each solution can only increment the counter
  - must find a solution for first J columns before going to J+1





### Third alternative

```

initialize to first column
repeat
  try column
  if successful then
    set queen
    increment to next column
  else backtrack
endif
until last column done or backtracking done

```

### Third Alternative Elaborated

```

//Initialize to first column
column := 1
row:= 0
repeat
  //try column
  row:= row + 1
  if row > 8
    then
      successful := false
    else
      successful := safe (row, column)
    endif
  //If successful then
  update partial configuration
  //inc to next column
  column := column + 1
  else backtrack
endif
until last column done or
backtracking done

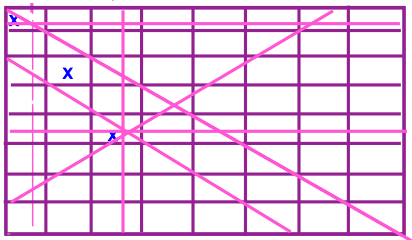
```

### must now make decisions about data structures

- ▶ alternative 1
  - board [row, column]
  - 8x8 Boolean matrix
  - set and remove queen are easy
  - safe requires checking all squares in column, row and diagonals
  - safe done frequently

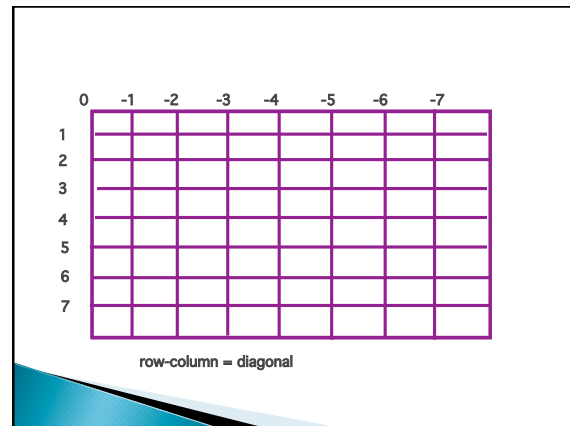
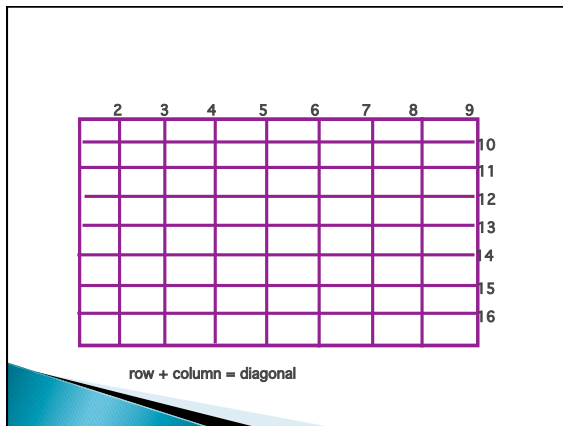
### alternative 2

- ▶ when setting a queen, mark all unusable squares
- ▶ safe is easy
- ▶ hard to remove a queen



### alternative 3

- ▶ integer columnselected [1:8]
  - columnselected( i ) is row selected for column i
- ▶ boolean rowempty[1:8]
  - rowempty( i ) = T if there is no queen in row i
- ▶ boolean uptothe right[2:16]
  - uptotheright( i ) = T if there is no queen in the ith right diagonal
  - row + column = diagonal
- ▶ boolean uptothe left[-7:7]
  - uptotheleft( i ) = T if there is no queen in the ith left diagonal
  - row - column = diagonal



### Third alternative solution with refinements

<pre>//Initialize to first column column := 1 row := 0 Repeat   //try column   row := row + 1   If row &gt; 8     then       successful := false     else       successful := safe(row, column)   endif</pre>	<pre>If successful then   update configuration   //Increment to next column   column := column + 1 else backtrack endif until last column done or backtracking done</pre>
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### Refinements

<pre>//safe(row, column) safe := rowempty(row) and uptothe right(row + column) and uptothe left(row-column)  //update configuration columnselected(column) := row rowempty(row) := false uptothe right(row + column) :=   false uptothe left(row-column) :=   false</pre>	<pre>//backtrack //remove queen column := column-1 If column &gt;= 0 then   row := columnselected(column)   columnselected(column) := 0   rowempty(row) := true   uptothe right(row + column) :=     true   uptothe left(row-column) := true endif</pre>
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### Problems with the proposed solution

- ▶ could be more general
  - what if the board size changes
- ▶ could be better decomposed
  - could provide methods to set configuration and to backtrack

### Third alternative solution with improvements

<pre>//Initialize to first column column := 1 row := 0 max := 8 Repeat   //try column   row := row + 1   If row &gt; max     then       successful := false     else       successful := safe(row, column)   endif</pre>	<pre>If successful then   update configuration   //Increment to next column   column := column + 1 else backtrack(column, row,   no solution) endif until column &gt; max or no solution</pre>
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## Refinements

```

backtrack (column, row, no solution)
//remove queen
column := column - 1
no solution := false
If column > 0 then
    row := columnselected (column)
    columnselected (column) := 0
    rowempty (row) := true
    uptothe right (row + column) := true
    uptothe left (row-column) := true
else no solution := true
endif

```

## Low Level Design Summary

- ▶ requires an exploration of the implementation alternatives
  - stepwise refinement is a general problem solving approach
- ▶ investigate each alternative until
  - the best approach becomes clear or
  - resources demand that you make your best guess
    - plan for future change if this choice must be revisited
- ▶ document your decisions for future developers
- ▶ consider data structures and algorithms together
  - consider kinds and frequency of operations
  - consider efficiency at the algorithm and data structure level

## Optimization

- ▶ Very hard to predict where the bottlenecks will be ahead of time
- ▶ Proposed strategy
  - Create a clean decomposition of the system
    - Easier to develop and maintain
    - If performance is a problem, evaluate for optimizations **later**
  - For each low-level component, can select an appropriate data structure
    - Easy to optimize later

## Optimizations

- ▶ Based on changes to low level structures are relatively easy to implement
- ▶ Based on high level decomposition are usually much more costly and can reduce future extensibility