

MAT – 112: Calculus I and Modeling

EFY 9

Instructor: Thomas R. Cameron

Due: April 13, 2018

Instructions

Please complete each of the following problems. You should work in groups of three, or at most four, and hand in only one submission per group. Be sure that your arguments are well justified and presented clearly.

Problem 1. State the integration by parts formula and prove this formula holds true using the following steps.

1. Let $h(x) = u(x)v(x)$ and apply the product rule to compute $h'(x)$.
2. Find an antiderivative of both sides of the equation relating $h'(x)$ to $u(x)$, $v(x)$, and their derivatives.
3. Rearrange to obtain the desired equation of integration by parts.

Problem 2. Consider computing the integral

$$\int x \arctan x dx$$

using integration by parts.

- (a) Apply the integration parts formula with $u(x) = \arctan x$ and $v(x) = \frac{x^2}{2} + c$, where c is some constant.
- (b) Find a c value that will simplify the integration by parts formula as much as possible, then proceed to finish computing the integral.