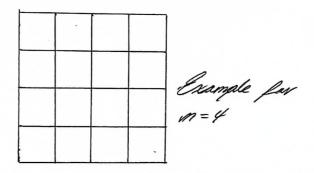
Cumelnical Sances Provy by example. (Rt. 1)

Cansider the panablem of exunting the datal number of Squares of any size that can be seen unlide a higger Square mith subdivisions at m subsquares par sude, zprzepically:



Haw can we east easily the Solicited quantity, species-My for bigger amounts of Subdivision ?

Albile analysing the problem, my first approach, Mas do manually launt them all far $n \in \{1, ..., 5\}$, and this data mas galhered:

17	J (X)
1	1
2	5
3	14
K	30
5	55

Recorded Juis Ruay by esample. (Rt 1.)

Mhere fix denate how we are supposely looking far a fundian.

If we were to make a feather plat, me would molice from the function is notably a par function, Mhere sow reales son the found, Maybe a nalve between two and otherse for the premer of the pat questing is not the way.

Mikile minually launting, you resculd metice from, for Squares of live on-1, the quantity in exactly 4.

That gives hints usual the may to go, the place suchere the patterns can be.

May we return to the example with n=1, and count the unaunt of Squares of Sizes Lower 1x1 through nxn. For nxn, the amount is cleanly 1, dre higger Square, And for Ix 1, 12. Let's See for all other Sines, what chappears.

M	2	Farmula
2	*	$(n-2)^2$
5	4	(n-1)2.

Guametnical Senies freast by example (pct. 1)

Man rue ean see the absolute partienn, there are perfect squares. There is a natable characteristics about to be exercised man:

Me een natue an inversion in the from I knows in perause there are it Sussquares If Size n, I squares as size M-1, ..., and it Secures of Size 1.

In general, as lagic ello tells, the smaller the size of the Julidinenan, the higher the quantity, County this quartity laterlated as the Square of the Size of the subdinisans as if we were daeleulating the areas in a meind may.

Its an adjustment the this invention and agreeing The our new approach, the ear yet this farmula:

fa)=(n-(x+1)]; 1=x=n

This way for X= I,..., in and far in king the selvady knam perstant, f(a) describes the amount of Jouanes of fise and inside a square with Suddinisians of size n.

Genmetrical Serviss pexay by example. At L)

Mith this your paparach, the uniquest salutions me were luaning Don, as samding the statul of Squares of any size, tenns into a sem of the certifier reduces of the punction:

 $\int_{1}^{1} (f(c)) = m^{2} + (n-1)^{2} + \cdots + d^{2}$

Du to cannotatively of addition, son we natice the equivalence of the Sum above with populiment . Distution ?

$$\sum_{i=0}^{M} \left(i^{\frac{1}{2}}\right)$$

Which, is advally, fauthatien's farmula, namely:

 $M(n+1)(2n+1): n\in \mathbb{Z}$