

Ejercicio 5. Para las siguientes especificaciones:

- Poner nombre al problema que resuelven
- Escribir un programa S sencillo en SmallLang, sin ciclos, que lo resuelva
- Dar la precondición más débil del programa escrito con respecto a la postcondición de su especificación

a) proc problema1 (in $s: seq(\mathbb{Z})$, in $i: \mathbb{Z}$, inout $a: \mathbb{Z}$)

requiere $\{0 \leq i < |s| \wedge_L a = \sum_{j=0}^{i-1} s[j]\}$

asegura $\{a = \sum_{j=0}^i s[j]\}$

b) proc problema2 (in $s: seq(\mathbb{Z})$, in $i: \mathbb{Z}$) : Bool

requiere $\{0 \leq i < |s| \wedge_L (\forall j : \mathbb{Z})(0 \leq j < i \rightarrow_L s[j] \geq 0)\}$

asegura $\{res = true \leftrightarrow (\forall j : \mathbb{Z})(0 \leq j \leq i \rightarrow_L s[j] \geq 0)\}$

c) proc problema3 (inout $s: seq(\mathbb{Z})$, in $i: \mathbb{Z}$)

requiere $\{(0 \leq i < |s|) \wedge_L (\forall j : \mathbb{Z})(0 \leq j < i \rightarrow s[j] = fibonacci(j))\}$

asegura $\{(\forall j : \mathbb{Z})(0 \leq j \leq i \rightarrow s[j] = fibonacci(j))\}$

Ejercicio 6. Dado el siguiente código y postcondición

```
if (i mod 3 = 0)
    s[i] := s[i] + 6
else
    s[i] := i
endif
```

$$Q \equiv \{(\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L s[j] \bmod 2 = 0)\}$$

Mostrar que las siguientes WPs son incorrectas, dando un contraejemplo de ser posible

- $P \equiv \{0 \leq i \leq |s| \wedge_L i \bmod 3 = 0 \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L s[j] \bmod 2 = 0)\}$
- $P \equiv \{0 \leq i < |s| \wedge_L i \bmod 3 \neq 0 \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L s[j] \bmod 2 = 0)\}$
- $P \equiv \{0 \leq i < |s| \wedge_L (i \bmod 3 = 0 \vee i \bmod 2 = 0) \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L s[j] \bmod 2 = 0)\}$ (*)
- $P \equiv \{i \bmod 3 = 0 \wedge_L (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L s[j] \bmod 2 = 0)\}$
- $P \equiv \{0 \leq i < |s|/2 \wedge_L i \bmod 3 = 0 \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L s[j] \bmod 2 = 0)\}$

(*) Para este inciso no se puede dar un contraejemplo, aunque es una WP incorrecta. Explicar por qué.

Precondición más débil en SmallLang

Ejercicio 1. Calcular las siguientes expresiones, donde a, b son variables reales, i una variable entera y A es una secuencia de reales.

- | | |
|-------------------------------|---|
| a) $\text{def}(a + 1)$. | d) $\text{def}(A[i] + 1)$. |
| b) $\text{def}(a/b)$. | e) $\text{def}(A[i + 2])$. |
| c) $\text{def}(\sqrt{a/b})$. | f) $\text{def}(0 \leq i \leq A \wedge_L A[i] \geq 0)$. |

$$a) \text{def}(a+1) \equiv \text{def}(a) \wedge \text{def}(1) = \text{True}$$

$$b) \text{def}(a/b) \equiv (b \neq 0)$$

$$c) \text{def}(\sqrt{a/b}) \equiv (\frac{a}{b} > 0 \wedge b \neq 0) \equiv (a > 0 \wedge b \neq 0)$$

$$d) \text{def}(A[i] + 1) \equiv (0 \leq i < |A|)$$

$$e) \text{def}(A[i+2]) \equiv 0 \leq i+2 < |A| \equiv (-2 \leq i < |A|-2)$$

$$f) \text{def}(0 \leq i \leq |A| \wedge A[i] \geq 0) \equiv \text{def}(0 \leq i \leq |A|) \wedge \text{def}(A[i] \geq 0)$$

$$\begin{aligned} & 0 \leq i \leq |A| \wedge 0 \leq i < |A| \\ & 0 \leq i < |A| \end{aligned}$$

Ejercicio 2. Calcular las siguientes precondiciones más débiles, donde a, b son variables reales, i una variable entera y A es una secuencia de reales.

$$wp := (E, P) = \text{def}(E) \wedge P_E^b$$

$$a) wp(a := a+1; b := a/2, b \geq 0).$$

$$b) wp(a := A[i] + 1; b := a*a, b \neq 2).$$

$$a) wp(a := a+1; b := \frac{a}{2}, b \geq 0)$$

$$wp(a := a+1; wp(b := \frac{a}{2}, b \geq 0))$$

$$wp(a := a+1, a \geq 0)$$

$$\begin{aligned} & e. \text{Aux} \\ & wp(b := \frac{a}{2}, b \geq 0) \\ & \text{def}(\frac{a}{2}) \wedge \frac{a}{2} \geq 0 \\ & \text{True} \wedge a \geq 0 \\ & a \geq 0 \end{aligned}$$

$$\text{def}(a+1) \wedge (a+1 \geq 0)$$

$$\text{True} \wedge a \geq -1 \equiv (a \geq -1)$$

$$b) wp(a := A[i] + 1; b := a*a, b \neq 2)$$

$$wp(a := A[i] + 1; wp(b := a*a, b \neq 2))$$

$$wp(a := A[i] + 1; a*a \neq 2)$$

$$\text{def}(A[i] + 1) \wedge (A[i] + 1) \neq 2$$

$$0 \leq i < |A| \wedge (A[i] + 1) \neq \sqrt{2}$$

$$0 \leq i < |A| \wedge A[i] \neq \sqrt{2} - 1$$

$$\begin{aligned} & c. \text{Aux} \\ & wp(b := a*a, b \neq 2) \\ & \text{def}(a*a) \wedge a*a \neq 2 \\ & \text{True} \wedge aa \neq 2 \end{aligned}$$

- c) $wp(a := A[i] + 1; a := b \cdot b, a \geq 0)$
d) $wp(a := a - b; b := a + b, a \geq 0 \wedge b \geq 0)$

$$c) wp(a := A[i] + 1; a := b \cdot b, a \geq 0)$$

$$wp(a := b^2, a \geq 0)$$

$$wp(a := A[i] + 1; wp(a := b^2, a \geq 0))$$

$$\begin{array}{l} \text{def}(b^2) \wedge b^2 \geq 0 \\ \text{True} \wedge b \geq 0 \end{array}$$

$$wp(a := A[i] + 1; b \geq 0)$$

$$\begin{array}{l} \text{def}(A[i] + 1) \wedge A[i] + 1 \geq 0 \\ 0 \leq i < |A| \wedge A[i] \geq -1 \end{array}$$

d) $wp(a := a - b; b := a + b, a \geq 0 \wedge b \geq 0)$

$$wp(a := a - b; wp(b := a + b, a \geq 0 \wedge b \geq 0))$$

$$\begin{array}{l} \text{def}(a - b) \wedge a - b \geq 0 \wedge a - b \geq -b \\ \text{True} \wedge a \geq b \wedge a \geq 0 \end{array}$$

$(a \geq b \wedge a \geq 0) \rightarrow \text{comparar resultados.}$

$$wp(b := a + b, a \geq 0 \wedge b \geq 0)$$

$$\text{def}(a + b) \wedge (a \geq 0 \wedge a + b \geq 0)$$

$$\text{True} \wedge a \geq 0 \wedge a \geq -b$$

Ejercicio 3. Sea $Q \equiv (\forall j \in \mathbb{Z})(0 \leq j < |A| \rightarrow_L A[j] \geq 0)$. Calcular las siguientes precondiciones más débiles, donde i es una variable entera y A es una secuencia de enteros.

a) $wp(A[i] := 0, Q)$

$$wp(b[i] := E, Q)$$

b) $wp(A[i+2] := -1, Q)$

$$wp(\text{setAt}(b, i, E), Q_{\text{setAt}(b, i, E)}^b)$$

c) $wp(A[i] := A[i-1], Q)$. (len close)

$$\text{setAt}(b, i, E) \left\{ \begin{array}{l} E \text{ si } i = j \\ b[j] \text{ si } i \neq j \end{array} \right.$$

a) $wp(A[i] := 0, Q)$

$$\text{def}(\text{setAt}(A, i, 0)) \wedge Q_{\text{setAt}(A, i, 0)}^{A[i]}$$

$$\text{def}(A) \wedge \text{def}(i) \wedge \text{def}(0) \wedge Q_{\text{setAt}(A, i, 0)}^A$$

$$\text{True} \wedge \text{True} \wedge \text{True} \wedge Q_{\text{setAt}(A, i, 0)}^A$$

$$(\forall j \in \mathbb{Z})(0 \leq j < |A| \rightarrow_L \text{setAt}(A, i, 0)[j] \geq 0)$$

$$\rightarrow_L [(i \neq j \wedge A[j] \geq 0) \vee (i = j \wedge 0 \geq 0)]$$

$$(\forall j \in \mathbb{Z})(0 \leq j < |A| \rightarrow_L (i \neq j \wedge A[j] \geq 0) \vee (i = j \wedge 0 \geq 0))$$

$$b) \text{wp}(A[i+2] := -1, Q)$$

$$\text{wp}(\text{setAt}(A, i+2, -1), Q)$$

$$\text{def}(\text{setAt}(A, i+2, -1)) \wedge Q^{\text{setAt}(A, i+2, -1)}$$

$$\text{def}(\text{setAt}(A, i+2, -1)) \equiv \text{def}(A) \wedge \text{def}(i+2) \wedge \text{def}(-1) \equiv \text{True}$$

$$Q^{\text{setAt}(A, i+2, -1)} \equiv (\forall j \in \mathbb{Z}) (0 \leq j < |A| \rightarrow \text{setAt}(A, i+2, -1)[j] \geq 0)$$

$$\rightarrow_L (i+2 = j \wedge -1 \geq 0) \vee \\ \text{False porque no vale } -1 \geq 0 \\ (i+2 + j \wedge A[j] \geq 0)$$

el
i+2 influye
en algo más?

$$(\forall j \in \mathbb{Z}) (0 \leq j < |A| \wedge i+2 + j \rightarrow_L A[j] \geq 0)$$

Ejercicio 4. Para los siguientes pares de programas S y postcondiciones Q

- Escribir la precondición más débil $P = \text{wp}(S, Q)$
- Mostrar formalmente que la P elegida es correcta

a) $S \equiv$

```
if( a < 0 )
    b := a
else
    b := -a
endif
```

$$Q \equiv (b = -|a|)$$

c) $S \equiv$

```
if( i > 1 )
    s[i] := s[i-1]
else
    s[i] := 0
endif
```

$$Q \equiv (\forall j \in \mathbb{Z}) (1 \leq j < |s| \rightarrow_L s[j] = s[j-1])$$

$$P = \{\text{True}\}$$

$$\text{wp}(S, Q) \equiv \text{def}(a < 0) \wedge_L ((a < 0 \wedge \text{wp}(b := a; b = -|a|)) \vee$$

$$(a \geq 0 \wedge \text{wp}(b := -a; b = -|a|)))$$

$$\text{True} \wedge_L ((a < 0 \wedge a = -|a|) \vee (a \geq 0 \wedge a = -|a|))$$

$$((a < 0 \wedge a = a) \vee (a \geq 0 \wedge a = -a))$$

True

$$\text{wp}(b := a; b = -|a|) = \text{def}(a) \wedge a = -|a|$$

$$(\text{True} \wedge a = -|a|) \equiv (a = -|a|) \equiv (a = -a)$$

$$\text{wp}(b := -a; b = -|a|) = \text{def}(-a) \wedge a = -|a| \equiv (a = -|a|) \equiv (a = -a)$$

b) $S \equiv$

```
if( i > 0 )
    s[i] := 0
else
    s[0] := 0
endif
```

$$Q \equiv (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L s[j] \geq 0)$$

$$\text{wp}(s, Q) = \underbrace{\text{def}(i > 0)}_{\text{True}} \wedge ((i > 0 \wedge \text{wp}(s[i] := 0, Q)) \vee \\ i \leq 0 \wedge \text{wp}(s[0] := 0, Q))$$

sole de $\leftarrow 0 \leq i < |s| \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L i \neq j \wedge s[j] \geq 0)\right) \vee$

unificar $i > 0,$

$$0 \leq i < |s| \wedge 0 \leq |s| \quad (i \leq 0 \quad (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L (0 \neq j \wedge s[j] \geq 0)))$$

c. Aux :

$$\text{wp}(s[i] := 0, Q) \equiv \text{wp}(\text{setAt}(s, i, 0), Q)$$

↳ sería el resultado final.

$$\equiv \text{def}(s) \wedge \text{def}(i) \wedge \text{def}(0) \wedge (0 \leq i < |s|) \wedge \text{Q}_{\text{setAt}(s, i, 0)}^s$$

$$\equiv \text{True} \wedge \text{True} \wedge \text{True} \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L \text{setAt}(s, i, 0)[j] \geq 0)$$

$$\equiv 0 \leq i < |s| \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L \underbrace{[(i = j \wedge 0 \geq 0) \vee (i \neq j \wedge s[j] \geq 0)]}_{\text{tautología}})$$

$$\text{wp}(s[0] := 0, Q) \equiv \text{wp}(\text{setAt}(s, 0, 0), Q) \quad \begin{cases} 0 & 0 = j \\ s[j] & 0 \neq j \end{cases}$$

$$\equiv \text{def}(s) \wedge \text{def}(0) \wedge \text{def}(0) \wedge 0 < |s| \wedge \text{Q}_{\text{setAt}(s, 0, 0)}^s$$

$$\equiv 1 \quad 0 < |s| \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L \underbrace{(0 = j, 0 \geq 0) \vee (0 \neq j, s[j] \geq 0)}_{\text{tautología!}})$$

(puedo dividirlo)

c) $S \equiv$

```
if( i > 1 )
  s[i] := s[i-1]
else
  s[i] := 0
endif
```

$$B = i > 1$$

$$Q \equiv (\forall j : \mathbb{Z})(1 \leq j < |s| \rightarrow_L s[j] = s[j-1])$$

$$\begin{aligned} wp(s, Q) = & \text{def}(i > 1) \wedge ((i > 1 \wedge wp(s_1, Q)) \vee (i \leq 1 \wedge wp(s_2, Q))) \\ & \text{True} \wedge ((i > 1 \wedge wp(s[i] := s[i-1], Q)) \vee (i \leq 1 \wedge wp(s[i] := 0, Q))) \\ & (i > 1 \wedge wp(\text{setAt}(s, i, s[i-1]), Q)) \vee (i \leq 1 \wedge wp(\text{setAt}(s, i, 0), Q)) \\ & \left[(1 < i < |s| \wedge (\forall j : \mathbb{Z})(1 \leq j < |s| \wedge i \neq j \rightarrow_L s[j] = s[j-1])) \vee \right. \\ & \left. (0 \leq i < |s| \wedge (\forall j : \mathbb{Z})(1 \leq j < |s| \wedge i \neq j \rightarrow_L s[j] = s[j-1])) \right] \end{aligned}$$

c. Aux :

1.

$$\begin{aligned} wp(\text{setAt}(s, i, s[i-1]), Q) &= \text{def}(s) \wedge \text{def}(i) \wedge \text{def}(s[i-1]) \wedge 0 \leq i < |s| \wedge Q \text{ setAt}(s, i, s[i-1]). \\ \exists \text{True} \wedge \text{true} \wedge (1 \leq i < |s|) \wedge (\forall j : \mathbb{Z})(1 \leq j < |s| \rightarrow_L \text{setAt}(s, i, s[i-1])[j] = \text{setAt}(s, i, s[i-1])[j-1]) \\ & (1 \leq i < |s|) \wedge (\forall j : \mathbb{Z})(1 \leq j < |s| \rightarrow_L [(i=j \wedge s[i-1] = s[j-1]) \vee (i \neq j \wedge s[j] = s[j-1])]) \quad \text{tautologica} \\ & (1 \leq i < |s|) \wedge (\forall j : \mathbb{Z})(1 \leq j < |s| \wedge i \neq j \rightarrow_L s[j] = s[j-1]) \quad \text{True siempre} \end{aligned}$$

$$i > 1 \wedge (1 \leq i < |s|) \equiv 1 < i < |s|$$

2. ?

$$\begin{aligned} (i \leq 1 \wedge wp(\text{setAt}(s, i, 0), Q)) &\equiv (i \leq 1 \wedge \text{def}(s) \wedge \text{def}(i) \wedge \text{def}(0) \wedge 0 \leq i < |s| \wedge Q \text{ setAt}(s, i, 0)) \\ &\equiv (i \leq 1) \wedge (0 \leq i < |s|) \wedge (\forall j : \mathbb{Z})(1 \leq j < |s| \rightarrow_L \text{setAt}(s, i, 0)[j] = \text{setAt}(s, i, 0)[j-1]) \\ & 0 \leq i < |s| \wedge (\forall j : \mathbb{Z})(1 \leq j < |s| \rightarrow_L [(i=j \wedge 0=0) \vee (i \neq j \wedge s[j] = s[j-1])]) \quad \text{tautologica} \end{aligned}$$

d) $S \equiv$

```
if( s[i] > 0 )
    s[i] := -s[i] → S1
else
    skip
endif
```

$$Q \equiv (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L s[j] \geq 0)$$

¿Qué hace el código

Si el elemento de s ($s[i]$) es positivo, entonces a ese elemento se le asigna su opuesto aditivo ($-s[i]$). En el caso contrario, el código no hace nada.

Axioma setAt : $b[i] := E \equiv \text{setAt}(b, i, E)$

$$\text{def}(\text{setAt}(b, i, E)) = \text{def}(E) \wedge \text{def}(b) \wedge \text{def}(i) \wedge 0 \leq i < |b|$$

$$\text{Dados } 0 \leq i, j < |b|: \text{setAt}(b, i, E)[j] = \begin{cases} E & i=j \\ b[j] & i \neq j \end{cases}$$

$$\text{wp}(S, Q) \equiv \text{def}(s[i] > 0) \wedge ((s[i] > 0 \wedge \text{wp}(s_1, Q)) \vee (s[i] \leq 0 \wedge \text{wp}(s_2, Q)))$$

$$\equiv (0 \leq i < |s|) \wedge ((s[i] > 0 \wedge \text{wp}(s[i] := -s[i], Q)) \vee (s[i] \leq 0 \wedge \text{wp}(\text{skip}, Q)))$$

$$\equiv (0 \leq i < |s|) \wedge (s[i] > 0 \wedge \text{wp}(\text{setAt}(s, i, -s[i]), Q)) \vee (s[i] \leq 0 \wedge \text{wp}(\text{skip}, Q))$$

$$\equiv (0 \leq i < |s|) \wedge (s[i] \leq 0 \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow s[j] \geq 0)) \vee (s[i] > 0 \wedge \text{wp}(\text{setAt}(s, i, -s[i]), Q))$$

$$\equiv (0 \leq i < |s|) \wedge [(s[i] \leq 0 \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow s[j] \geq 0)) \vee$$

$$(s[i] > 0 \wedge 0 \leq i < |s| \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow (i=j \wedge s[j] \leq 0) \vee (i \neq j \wedge s[j] \geq 0)))]$$

C.AUX

$$\text{wp}(\text{setAt}(s, i, -s[i]), Q) \equiv \text{def}(\text{setAt}(s, i, -s[i])) \wedge Q_{\text{setAt}(s, i, -s[i])}^s$$

$$\equiv \text{def}(s) \wedge \text{def}(i) \wedge \text{def}(-s[i]) \wedge 0 \leq i < |s| \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow \text{setAt}(s, i, -s[i])[j] \geq 0)$$

$$\equiv \text{True} \wedge \text{True} \wedge 0 \leq i < |s| \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow (i=j \wedge -s[j] \geq 0) \vee (i \neq j \wedge s[j] \geq 0))$$

$$\equiv 0 \leq i < |s| \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow (i=j \wedge s[j] \leq 0) \vee (i \neq j \wedge s[j] \geq 0))$$

Ejercicio 5. Para las siguientes especificaciones:

- Poner nombre al problema que resuelven
- Escribir un programa S sencillo en SmallLang, sin ciclos, que lo resuelva
- Dar la precondition más débil del programa escrito con respecto a la postcondición de su especificación

a) proc problema1 (in $s: seq(\mathbb{Z})$, in $i: \mathbb{Z}$, inout $a: \mathbb{Z}$) **'sumarElementos'**

requiere $\{0 \leq i < |s| \wedge_L a = \sum_{j=0}^{i-1} s[j]\}$
asegura $\{a = \sum_{j=0}^i s[j]\}$

b) proc problema2 (in $s: seq(\mathbb{Z})$, in $i: \mathbb{Z}$) : Bool **'subsecuencia De Elementos Positivos'**

requiere $\{0 \leq i < |s| \wedge_L (\forall j : \mathbb{Z})(0 \leq j < i \rightarrow_L s[j] \geq 0)\}$
asegura $\{res = true \leftrightarrow (\forall j : \mathbb{Z})(0 \leq j \leq i \rightarrow_L s[j] \geq 0)\}$

c) proc problema3 (inout $s: seq(\mathbb{Z})$, in $i: \mathbb{Z}$) **'es SucesionDeFibonacci'**

requiere $\{(0 \leq i < |s|) \wedge_L (\forall j : \mathbb{Z})(0 \leq j < i \rightarrow s[j] = fibonacci(j))\}$
asegura $\{(\forall j : \mathbb{Z})(0 \leq j \leq i \rightarrow s[j] = fibonacci(j))\}$

a) $S \equiv$
if $i > 0$:

$$a = a + s[i]$$

else :

$$a = s[0]$$

$$Q = \left\{ a = \sum_{j=0}^i s[j] \right\}$$

$$wp(s, a = \sum_{j=0}^i s[j]) = \text{def}(i > 0) \wedge (i > 0 \wedge wp(a := a + s[i]; a = \sum_{j=0}^{i-1} s[j])) \vee$$

$$(i \leq 0 \wedge wp(a := s[0]; a = \sum_{j=0}^i s[j]))$$

$$\text{True} \wedge (i > 0 \wedge (a = \sum_{j=0}^{i-1} s[j])) \vee (i = 0 \wedge s[0] = s[i])$$

$$wp(s, Q) \equiv (0 < i < |s| \wedge a = \sum_{j=0}^{i-1} s[j])$$

. $i > 0$:

$$wp(s_1, Q) \equiv \text{def}(a + s[i]) \wedge a + s[i] = \sum_{j=0}^{i-1} s[j]$$

$$\text{True} \wedge a = \sum_{j=0}^{i-1} s[j] - s[i]$$

$$a = \sum_{j=0}^{i-1} s[j]$$

. $i \leq 0$ y además $0 \leq i < |s|$ (por el requiere) $\Rightarrow i = 0$

$$wp(s_2, Q) \equiv \text{def}(s[0]) \wedge s[0] = \sum_{j=0}^0 s[j] = s[0]$$

Ejercicio 6. Dado el siguiente código y postcondición

```

if (i mod 3 = 0) → si i es divisible por 3
    s[i] := s[i] + 6 → entonces a s[i] sumale 6
else
    s[i] := i → si i no es divisible por 3, entonces asignale i a s[i]
endif

```

$$Q \equiv \{(\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L s[j] \text{ mod } 2 = 0)\}$$

Mostrar que las siguientes WPs son incorrectas, dando un contraejemplo de ser posible

- a) $P \equiv \{0 \leq i \leq |s| \wedge_L i \text{ mod } 3 = 0 \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L s[j] \text{ mod } 2 = 0)\} \rightarrow$ falta ver qué pasa para los $i \text{ mod } 3 \neq 0$
- b) $P \equiv \{0 \leq i < |s| \wedge_L i \text{ mod } 3 \neq 0 \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L s[j] \text{ mod } 2 = 0)\} \rightarrow$ falta ver qué pasa para los $i \text{ mod } 3 = 0$
- c) $P \equiv \{0 \leq i < |s| \wedge_L (i \text{ mod } 3 = 0 \vee i \text{ mod } 2 = 0) \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L s[j] \text{ mod } 2 = 0)\}$ (*) → Porque no es la más débil?
- d) $P \equiv \{i \text{ mod } 3 = 0 \wedge_L (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L s[j] \text{ mod } 2 = 0)\} \rightarrow$ no se acota el rango de i
- e) $P \equiv \{0 \leq i < |s|/2 \wedge_L i \text{ mod } 3 = 0 \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L s[j] \text{ mod } 2 = 0)\} \rightarrow$ acoto el rango de i a la mitad de s ,

(*) Para este inciso no se puede dar un contraejemplo, aunque es una WP incorrecta. Explicar por qué.

$$\begin{aligned}
wp(s, Q) \equiv & \text{def}(i \text{ mod } 3 = 0) \wedge \left[(i \text{ mod } 3 = 0 \wedge wp(s[i] := s[i] + 6, Q)) \vee \right. \\
& \left. (i \text{ mod } 3 \neq 0 \wedge wp(s[i] := i, Q)) \right] \\
0 \leq i < |s| \wedge & \left[(i \text{ mod } 3 = 0 \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L s[j] \text{ mod } 2 = 0)) \vee \right. \\
& \left. (i \text{ mod } 3 \neq 0 \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L (i = j \wedge j \text{ mod } 2 = 0) \vee (i \neq j \wedge s[j] \text{ mod } 2 = 0))) \right] \\
& \text{no sé qué pasa con este término.}
\end{aligned}$$

$$i \text{ mod } 3 = 0$$

$$\begin{aligned}
wp(s_1, Q) \equiv & \text{def}(\text{setAt}(s, i, s[i] + 6)) \wedge Q_{\text{setAt}(s, i, s[i] + 6)}^s \\
\equiv & \text{def}(s) \wedge \text{def}(i) \wedge \text{def}(s[i] + 6) \wedge 0 \leq i < |s| \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L \text{setAt}(s, j, s[j] \text{ mod } 2 = 0)) \\
\equiv & 0 \leq i < |s| \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L (i = j \wedge s[j] + 6 \text{ mod } 2 = 0) \vee (i \neq j \wedge s[j] \text{ mod } 2 = 0) \\
& \quad (i = j \wedge s[j] \text{ mod } 2 = 0) \vee (i \neq j \wedge s[j] \text{ mod } 2 = 0)) \\
\equiv & 0 \leq i < |s| \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L s[j] \text{ mod } 2 = 0)
\end{aligned}$$

$$i \text{ mod } 3 \neq 0$$

$$\text{setAt} = \begin{cases} i & i=j \\ s[j] & i \neq j \end{cases}$$

$$\begin{aligned}
wp(s_2, Q) \equiv & \text{def}(\text{setAt}(s, i, i)) \wedge Q_{\text{setAt}(s, i, i)}^s \\
\equiv & 0 \leq i < |s| \wedge (\forall j : \mathbb{Z})(0 \leq j < |s| \rightarrow_L (i = j \wedge j \text{ mod } 2 = 0) \vee (i \neq j \wedge s[j] \text{ mod } 2 = 0))
\end{aligned}$$