

$$f(x) = \sum_{i=0}^5 B_{i,2}(x) \beta_i \quad 5 \text{ knots}$$

$$B_{i,0}(x) = \begin{cases} 1, & \tau_i \leq x < \tau_{i+1} \\ 0, & \text{else} \end{cases}$$

$$B_{i,j}(x) = \frac{x - \tau_i}{\tau_{i+j} - \tau_i} B_{i,j-1}(x) + \frac{\tau_{i+j+1} - x}{\tau_{i+j+1} - \tau_{i+1}} B_{i+1,j-1}(x)$$

$$X = \{ \tau_0, \tau_1, \tau_2, \tau_3, \tau_4, \tau_5 \}$$

$$= \{ 0, 1, 2, 3, 4, 5 \}$$

for  $B_{0,2}$  need  $B_{0,1} + B_{1,1}$

$B_{0,1}$  need  $B_{0,0} + B_{1,0}$

$B_{1,1}$  need  $B_{1,0} + B_{2,0}$  ✓

$$B_{0,0}(x) = \begin{cases} 1, & 0 \leq x < 1 \\ 0, & \text{else} \end{cases}$$

$$B_{1,0}(x) = \begin{cases} 1, & 1 \leq x < 2 \\ 0, & \text{else} \end{cases}$$

$$B_{2,0}(x) = \begin{cases} 1, & 2 \leq x < 3 \\ 0, & \text{else} \end{cases}$$

⋮

$B_{1,2}$  need  $B_{1,1} + B_{2,1}$

$B_{2,1}$  need  $B_{2,0} + B_{3,0}$  ✓

$B_{2,2}$  need  $B_{2,1} + B_{3,1}$

$B_{3,1}$  need  $B_{3,0} + B_{4,0}$  ✓

$$B_{0,1}(x) = \frac{x-0}{1-0} B_{0,0} + \frac{2-x}{2-1} B_{1,0} = x B_{0,0} + (2-x) B_{1,0}$$

$$B_{1,1}(x) = \frac{x-1}{2-1} B_{1,0} + \frac{3-x}{3-2} B_{2,0} = (x-1) B_{1,0} + (3-x) B_{2,0}$$

$$B_{0,2}(x) = \frac{x-0}{2-0} B_{0,1} + \frac{3-x}{3-1} B_{1,1} = \frac{x}{2} B_{0,1} + \left(\frac{3-x}{2}\right) B_{1,1}$$

$$B_{2,1}(x) = \frac{x-2}{3-1} B_{2,0} + \frac{4-x}{4-3} B_{3,0} = \left(\frac{x-2}{2}\right) B_{2,0} + (4-x) B_{3,0}$$

$$B_{1,2}(x) = \frac{x-1}{3-1} B_{1,1} + \frac{3-x}{4-2} B_{2,1} = \left(\frac{x-1}{2}\right) B_{1,1} + \left(\frac{3-x}{2}\right) B_{2,1}$$

$$B_{3,1}(x) = \frac{x-3}{4-1} B_{3,0} + \frac{5-x}{5-4} B_{4,0} = (x-3) B_{3,0} + (5-x) B_{4,0}$$

$$B_{2,2}(x) = \frac{x-2}{3-2} B_{2,1} + \frac{5-x}{5-3} B_{3,1} = (x-2) B_{2,1} + \left(\frac{5-x}{2}\right) B_{3,1}$$