



Finding Market Regimes in Equity Returns Using Hidden Markov Models



Tools & Resources

Software:

- 1** Python
- 1.1** Yfinance (stock data)
- 1.2** Numpy/Pandas (data manipulation)
- 1.3** Matplotlib (plotting)
- 1.4** HmmLearn (HMM)
- 2** Github (Version Control)

Hardware:

Personal Laptop

Advisor/

Consultant: Professor M. Wade &
Professor M. Gee

About Me



■ BACKGROUND

Interest: Quantitative Finance and Machine Learning

Major: Applied Mathematics concentration in Computer Science

Relevant coursework: Mathematical Models, Optimal Control, Probability, Applied Linear Algebra, Stats (106 & 206)

School Experience: (Tutor/TA for COMP 118 & 218)

Professional Experience: 3 Data Science Internships; 2 of which were at JPMorgan Chase

From Data Science → Quant Research





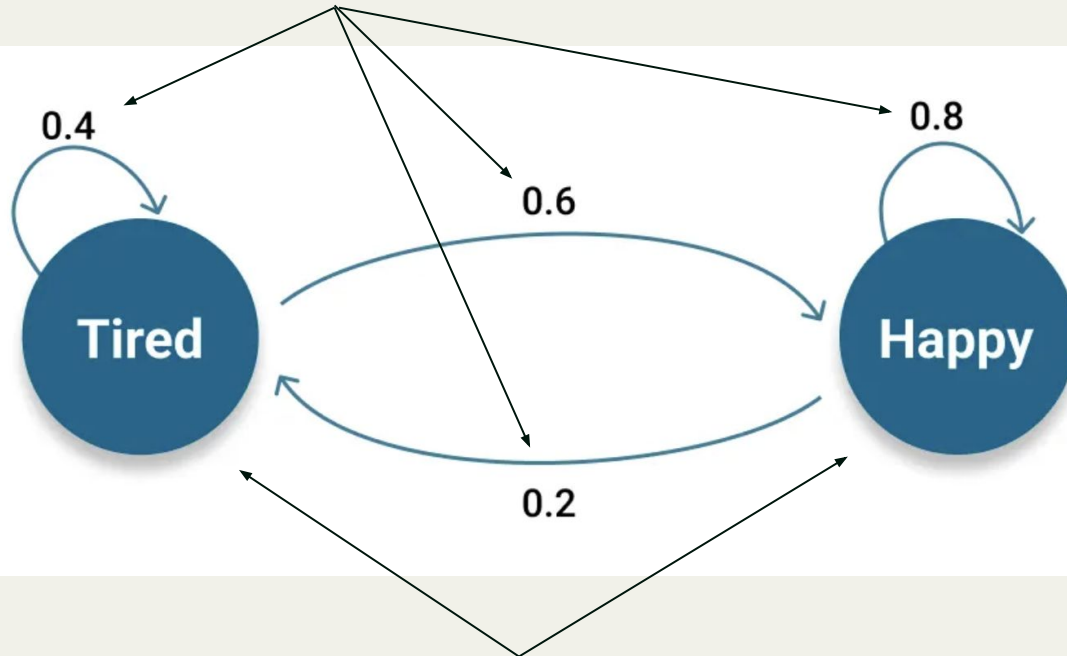
Research Question without Jargon

Can we automatically detect when the market is in a “calm” period versus a “volatile” period by only looking at daily price changes?”



Markov Chains

Transition Probabilities: from a current state to a next state



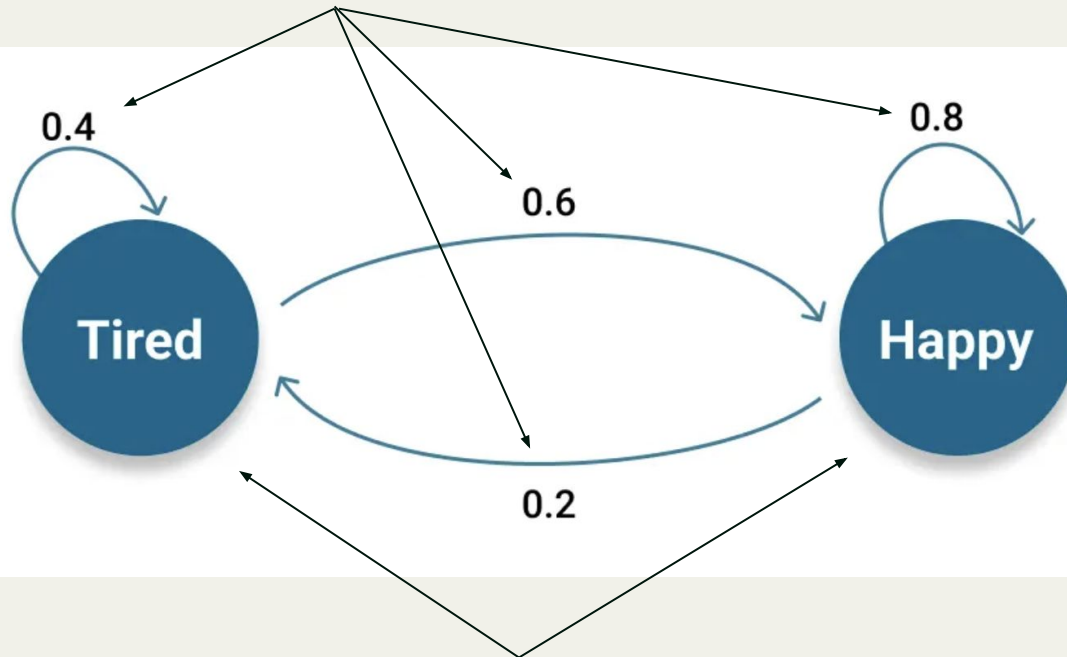
States: the environment/system

Example:

Imagine being **Tired** you then have a **60% chance** of becoming happy, and a **40% chance** of staying tired.

Markov Chains

Transition Probabilities: from a current state to a next state

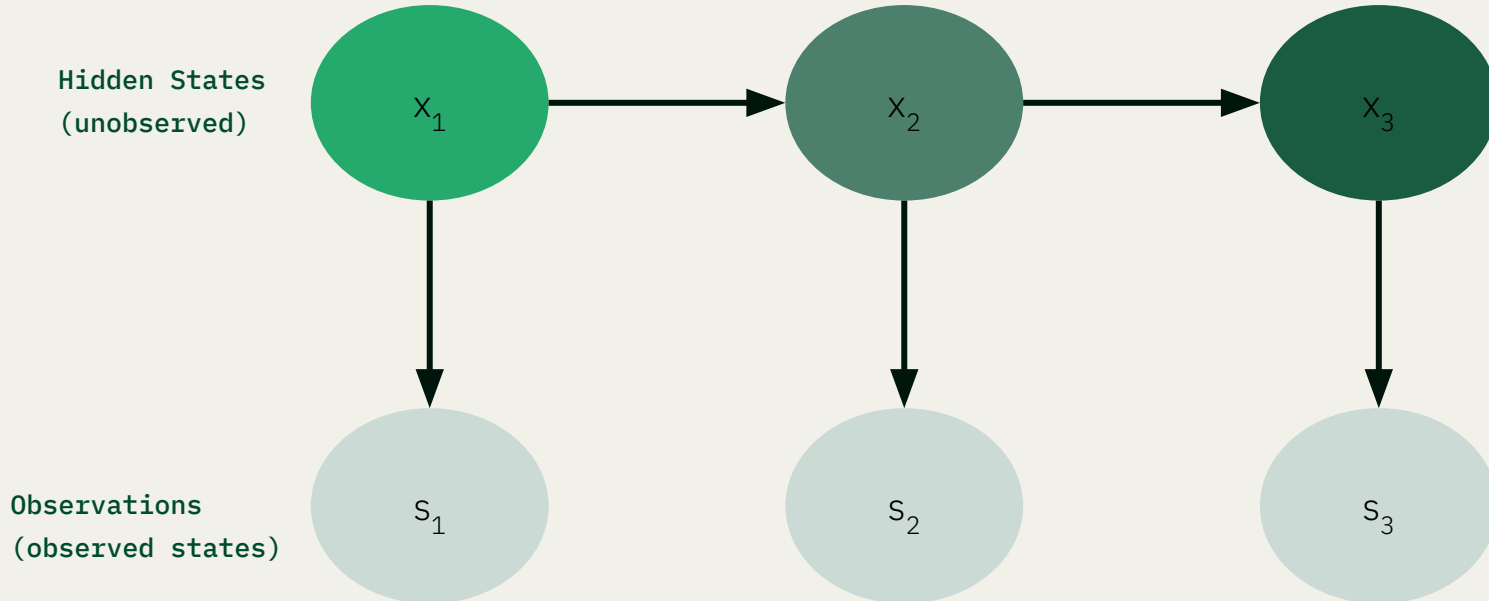


States: the environment/system

- stochastic process
- moves between states over time
- **“Memoryless,”** The next state only depends on the current state. This is what’s called the **Markov Property**

Hidden Markov Model

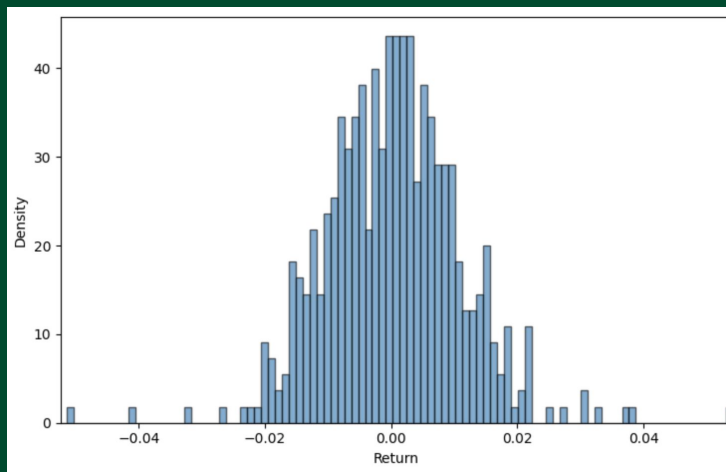
The Claim: There exists an underlying, unobserved processes x_t that governs how s_t are generated.



Stock Returns

n : the number of samples ($n=500$)

s_t : observed return at time t



This histogram shows the **empirical distribution of observed returns**.

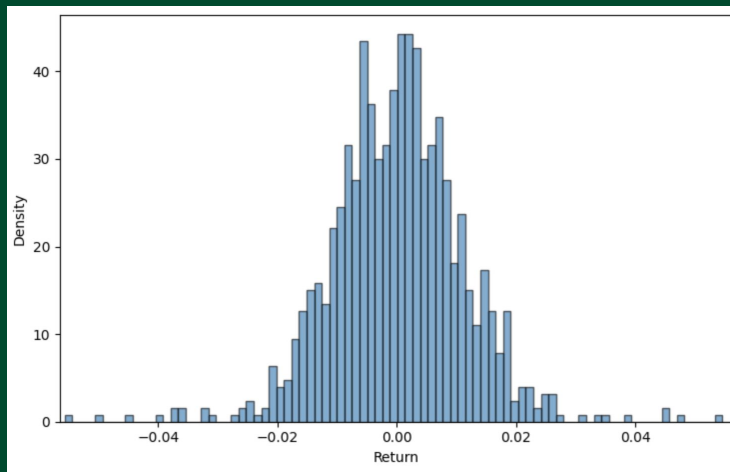
Each **return is a sample** drawn from an **unknown underlying distribution**.

With a **small number of samples**, the shape of the distribution is noisy and difficult to identify, so let's **increase the number of samples**.

Goal: Find the distribution generating these observations (**Find x_t**)

Stock Returns

$n = 1000$



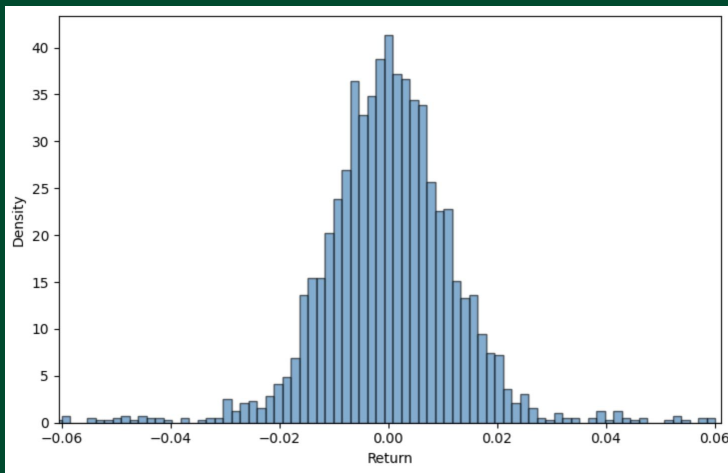
We are starting to get **more density** around $\pm [0.02, 0.04]$

Let's keep increasing the sample count..

Goal: Find the distribution generating these observations (**Find x_t**)

Stock Returns

n = 2500



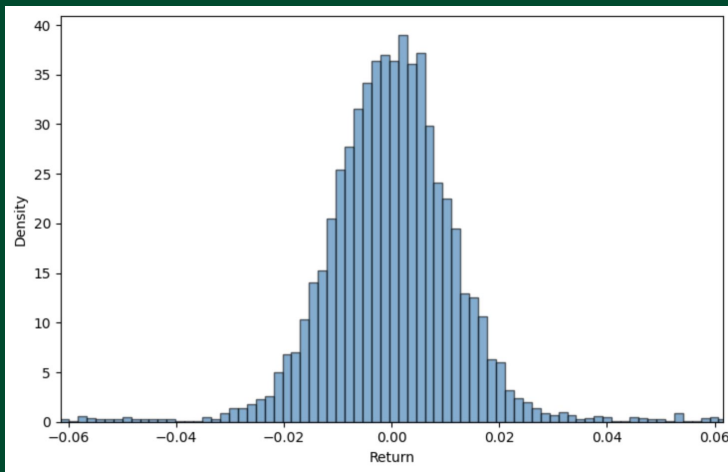
Again, we are getting **more density around $\pm [0.02, 0.04]$** and also **less gaps in our structure**

Let's keep increasing the sample count..

Goal: Find the distribution generating these observations (**Find x_t**)

Stock Returns

$n = 5000$



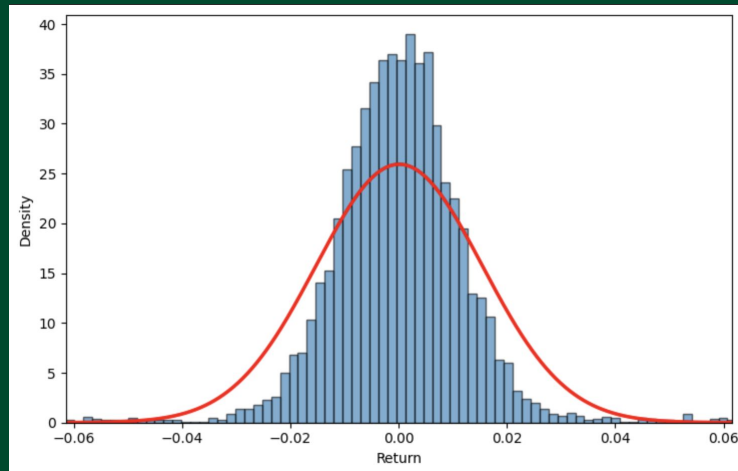
We have 10x our sample size (n)

Our data, now looks **continuous**, meaning **no holes or gaps**.

So, let's try fitting this to a familiar **probability distribution**

Goal: Find the distribution generating these observations (**Find x_t**)

Distribution Generating Returns



Each day's a return (s_t) is a randomly drawn from a Normal (Gaussian) distribution (x_t)

This distribution determines:

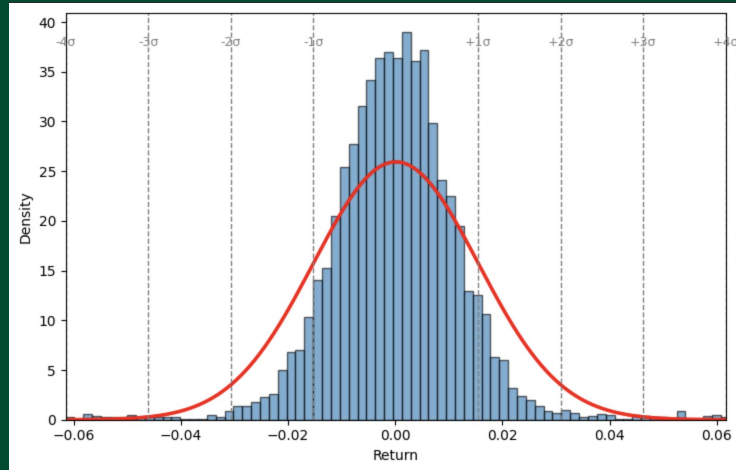
- The **probability** of observing different returns
- The **spread** of returns (volatility)
- The **likelihood** of extreme market moves

Relationship: $S \sim N(\mu, \sigma^2)$

μ : mean (the center of the curve)

σ : standard deviation (volatility)

68-95-99.7 Rule



In a Normal distribution:

~68% of observations fall within $\pm 1\sigma$

95% fall within $\pm 2\sigma$

99.7% fall within $\pm 3\sigma$

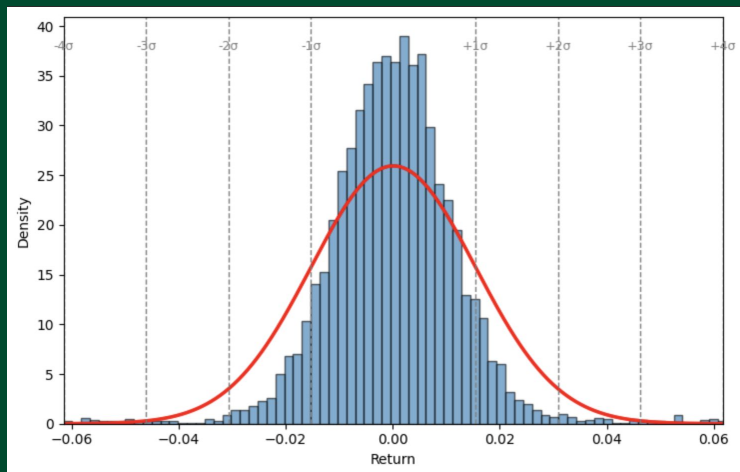
This **Empirical Rule** saves us a lot of time, and tells us that this is **not satisfying our goal**

Relationship: $S \sim N(\mu, \sigma^2)$

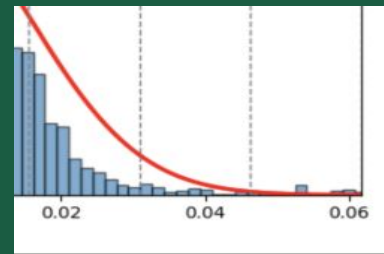
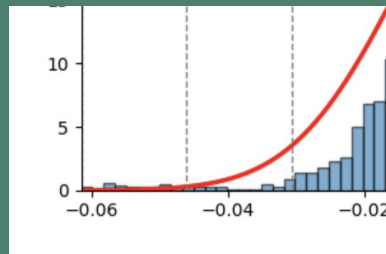
μ : mean (the center of the curve)

σ : standard deviation (volatility)

What's the big deal?



Yes, we may be misfitting the center of the distribution. However, to a **portfolio manager**, the **main concern is risk** not the **average return**



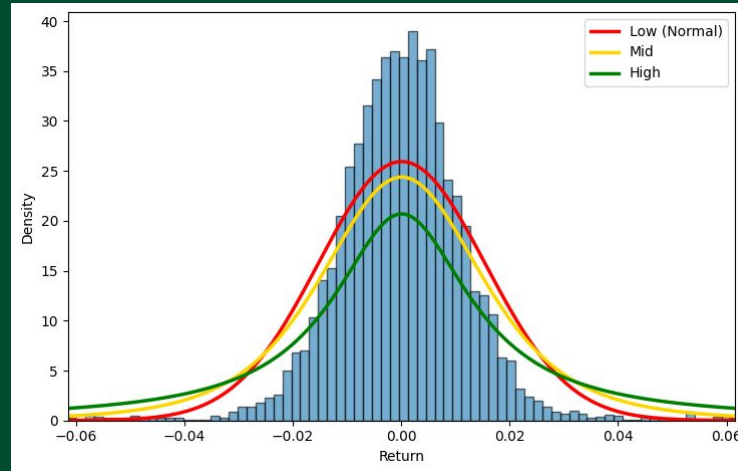
What's happening at the tails:

Extreme returns occur far more **frequently** than a single **Gaussian distribution predicts**

Volatility Regimes

New Claim:

Returns are generated from different **Gaussian** distributions depending on the underlying **hidden volatility regime**



Old Claim $S \sim N(\mu, \sigma^2) \rightarrow$ New Claim $S \sim N(\mu, \sigma_{x_t}^2)$

Where:

μ : mean (fixed)

σ_{x_t} : standard deviation (regime-dependent **volatility**)

Observed Data: Returns (s_t)

Hidden States: Regimes (x_t)

Model: Hidden Markov Model



Can a 3-state Hidden Markov Model fitted to daily equity returns identify underlying volatility regimes?

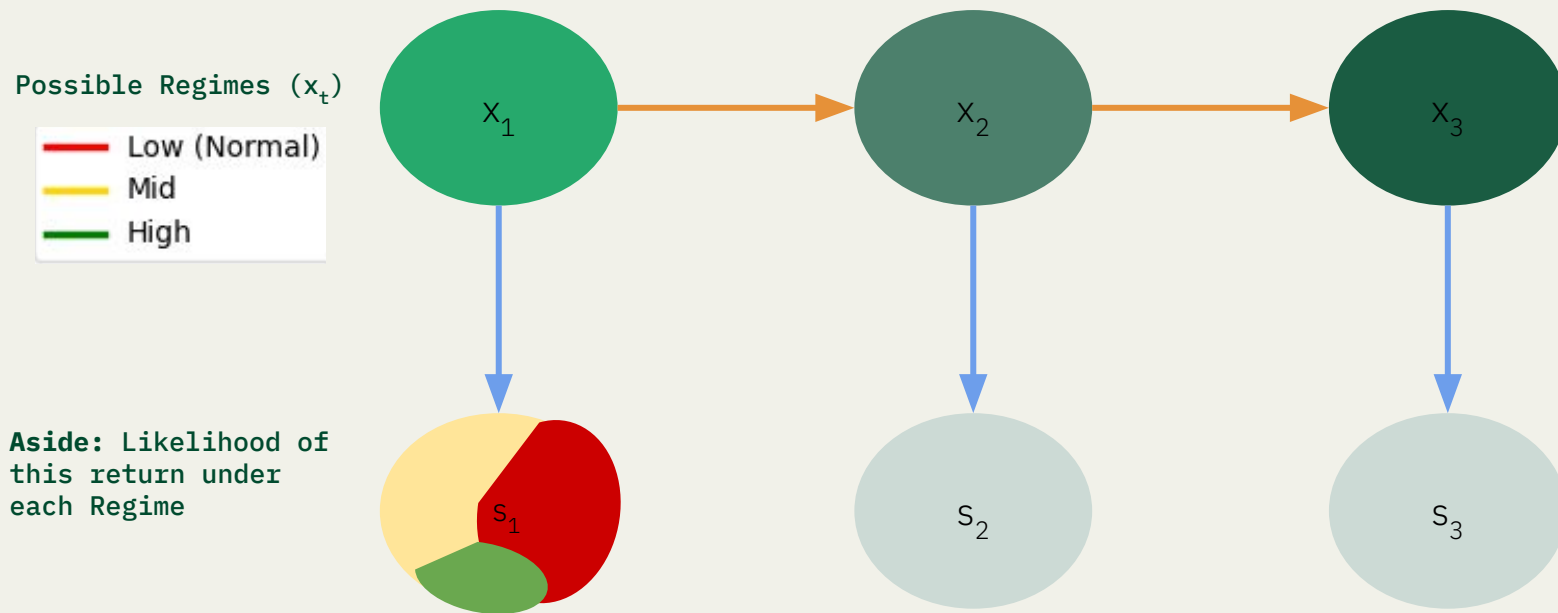
Do those regimes have meaningfully different risk characteristics and "realistic" transition dynamics?



What I've Done So Far

Transition Probability: Probability the Regime change from x_t to x_{t+1}

Emission Probability: Distribution of Returns generated by regime x_t



Anticipated Challenges / Potential Future Steps

Challenges:

- 01 Choose number of regimes
- 02 Sensitivity to initializations
- 03 Interpreting regimes economically

Next Steps:

Examine, for each day, which hidden state the model believes the market was most likely in
(Viterbi Algorithm)



COMP_s

Timeline

Now - Feb
16th

Experiment with
number of regimes
($K = 2, 3, 4$)

Evaluate Model
strength
(precision/recall)

Feb 17th -
Mar 19th

Refine HMM
implementation

Create more HMM
models using
other volatility
techniques or
distributions

Mar 20th -
Mar 25th

Results & model
comparison
results

Start writing up
a report on
findings

Mar 26th -
Apr 7th

Improve
visualizations
and storytelling

Interpret
economic meaning
of regimes

Apr 6th -
Apr 28th

Is this Viable...
Finalized
analysis &
conclusions

Cleaning up
Github repo(s)



Questions?