



# Finding Market Regimes in Equity Returns Using Hidden Markov Models



# Tools & Resources

## Software:

- 1** Python
- 1.1** Yfinance (stock data)
- 1.2** Numpy/Pandas (data manipulation)
- 1.3** Matplotlib (plotting)
- 1.4** HmmLearn (HMM)
- 2** Github (Version Control)

## Hardware:

Personal Laptop

## Advisor/

**Consultant:** Professor M. Wade &  
Professor M. Gee

# About Me



## ■ BACKGROUND

**Interest:** Quantitative Finance and Machine Learning

**Major:** Applied Mathematics concentration in Computer Science

**Relevant coursework:** Mathematical Models, Optimal Control, Probability, Applied Linear Algebra, Stats (106 & 206)

**School Experience:** (Tutor/TA for COMP 118 & 218)

**Professional Experience:** 3 Data Science Internships; 2 of which were at JPMorgan Chase



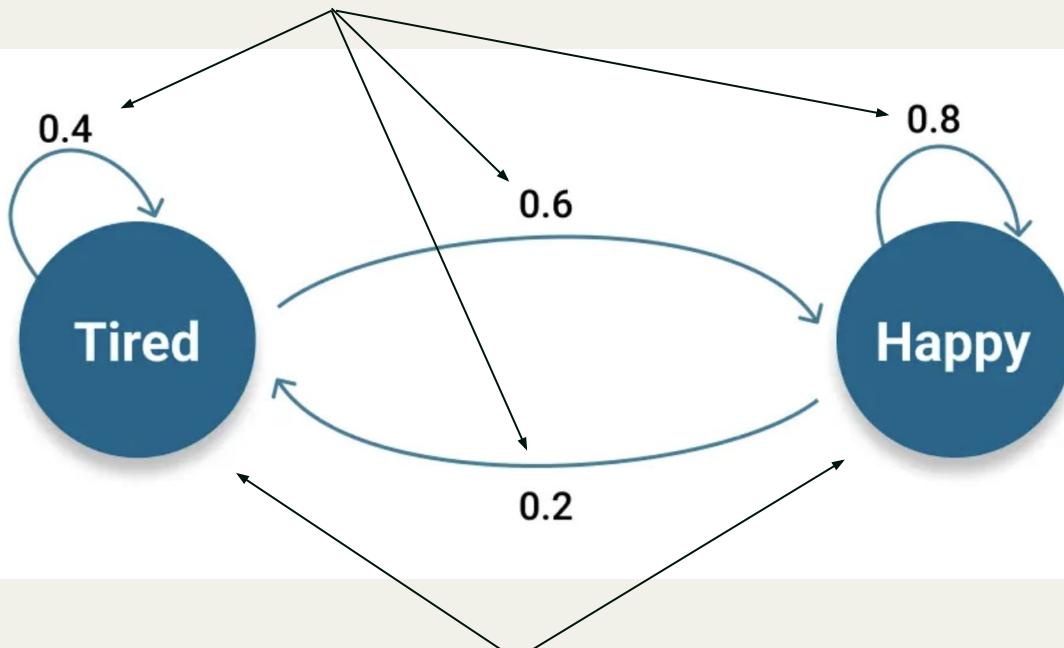
## **Research Question without Jargon**

Can we automatically detect when the market is in a “calm” period versus a “volatile” period by only looking at daily price changes?”

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# Markov Chains

**Transition Probabilities:** from a current state to a next state



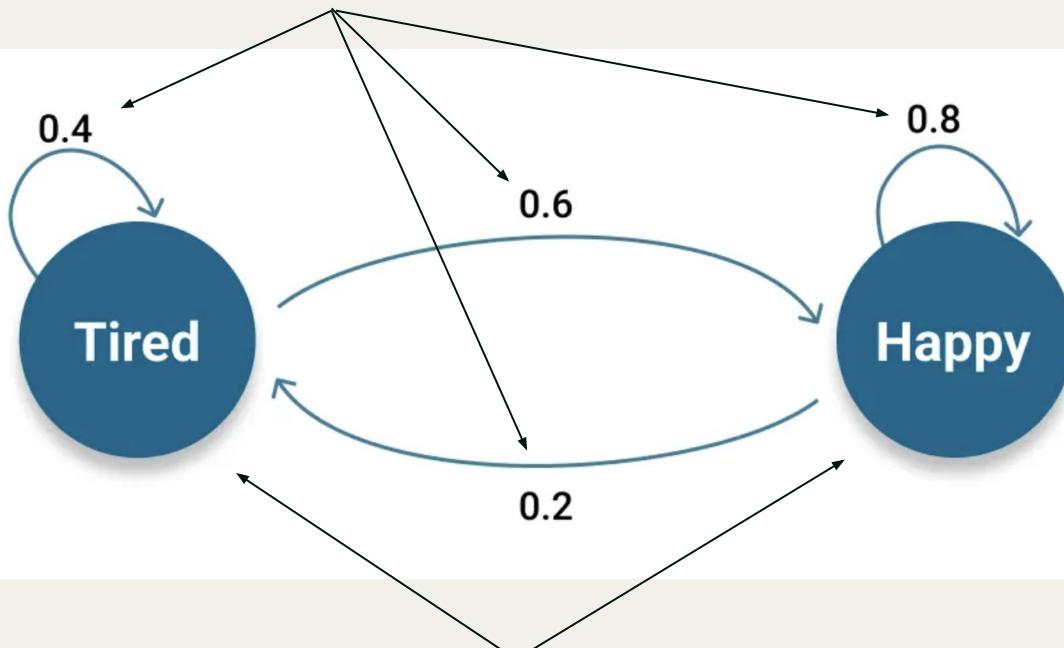
**States:** the environment/system

**Example:**

Imagine being **Tired** you then have a **60% chance** of becoming happy, and a **40% chance** of staying tired.

# Markov Chains

**Transition Probabilities:** from a current state to a next state

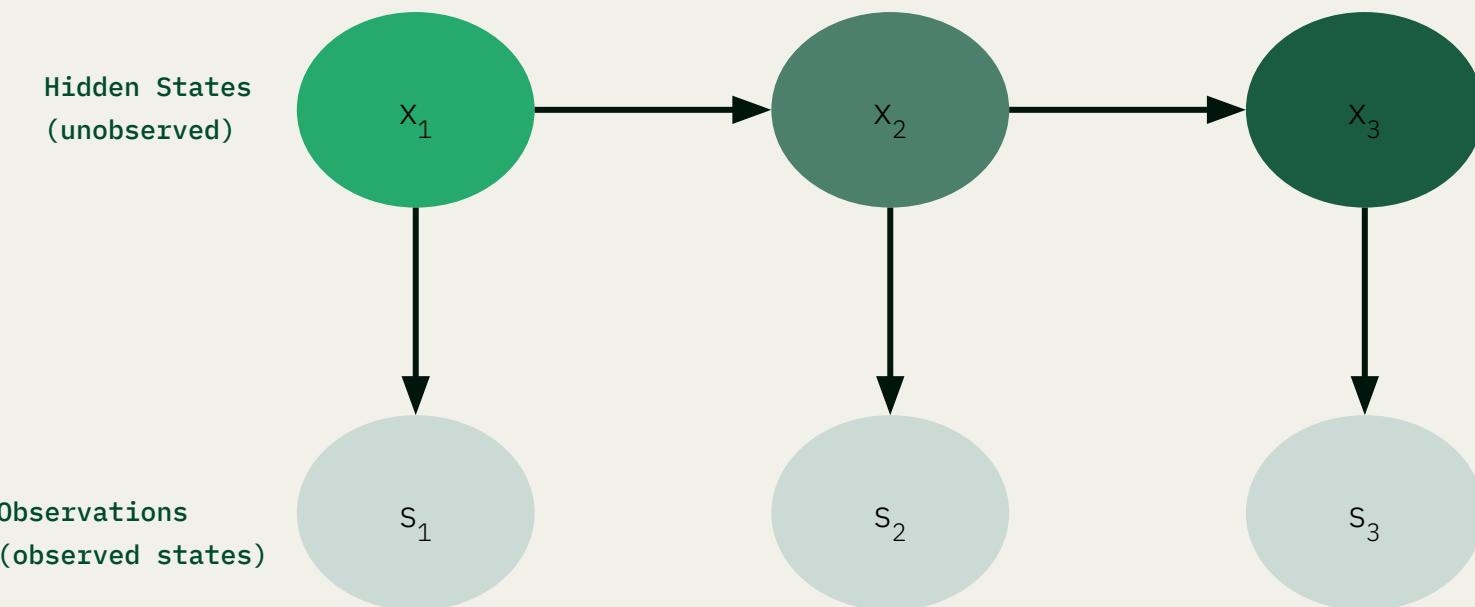


**States:** the environment/system

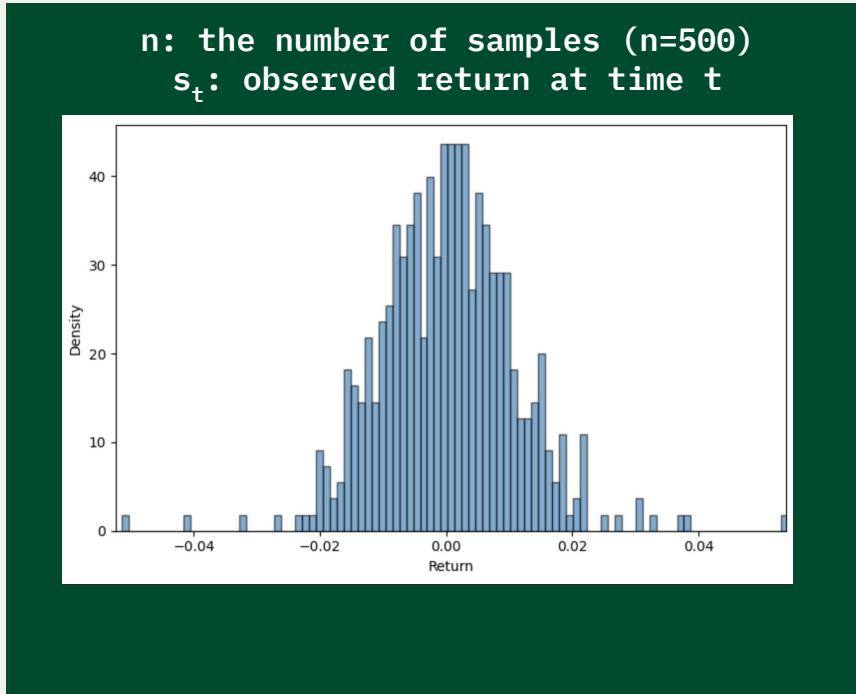
- stochastic process
- moves between states over time
- **“Memoryless,”** The next state only depends on the current state. This is what's called the **Markov Property**

# Hidden Markov Model

The Claim: There exists an underlying, unobserved processes  $x_t$  that governs how  $s_t$  are generated.



# Stock Returns



This histogram shows the **empirical distribution of observed returns**.

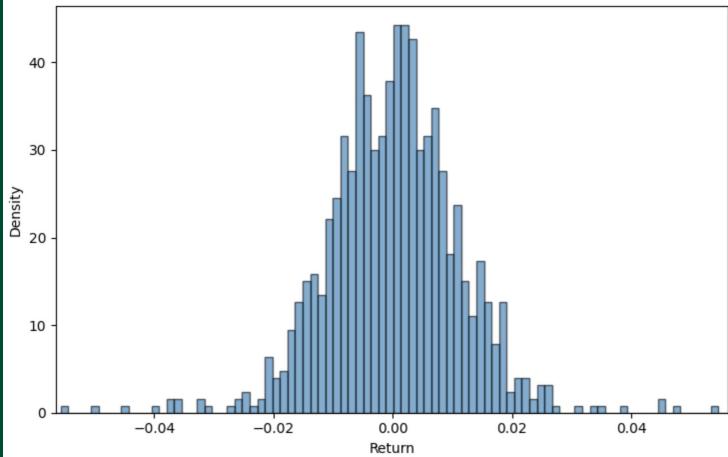
Each **return is a sample** drawn from an **unknown underlying distribution**.

With a **small number of samples**, the shape of the distribution is noisy and difficult to identify, so let's **increase the number of samples**.

**Goal:** Find the distribution generating these observations (**Find  $x_t$** )

# Stock Returns

n = 1000

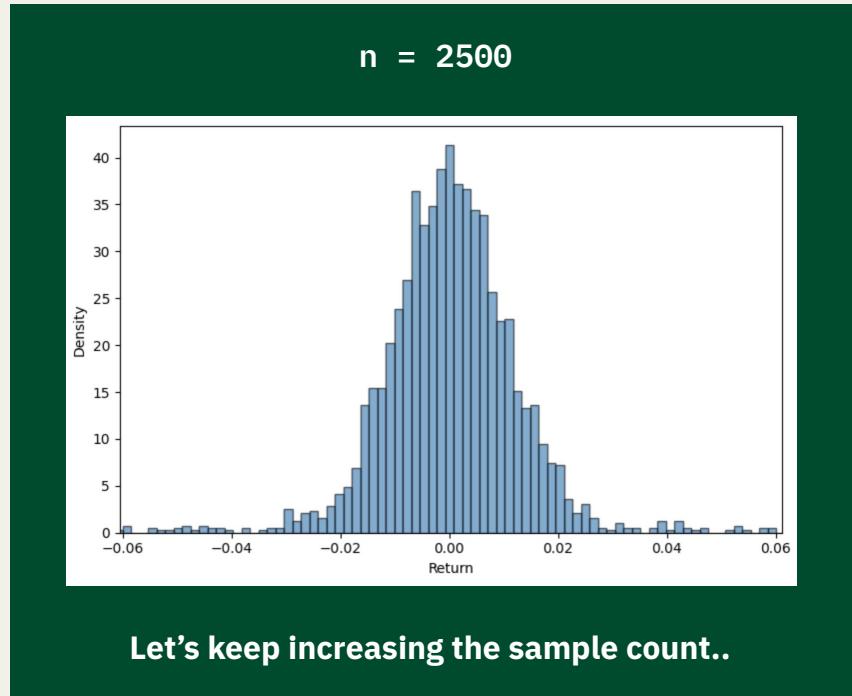


We are starting to get **more density around  $\pm [0.02, 0.04]$**

Let's keep increasing the sample count..

**Goal:** Find the distribution generating these observations (**Find  $x_t$** )

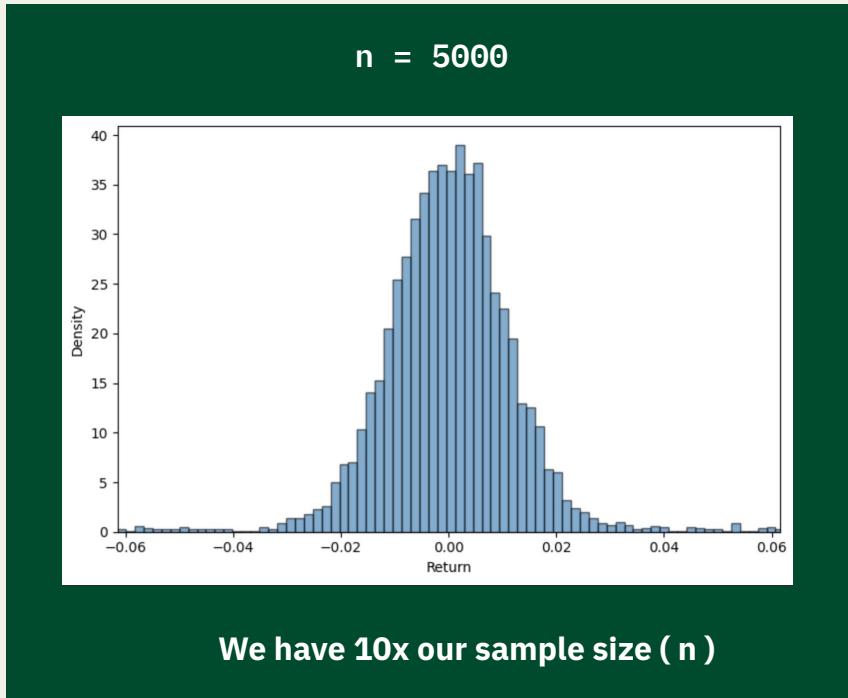
# Stock Returns



Again, we are getting **more density around  $\pm [0.02, 0.04]$**  and also **less gaps in our structure**

**Goal:** Find the distribution generating these observations (**Find  $x_t$** )

# Stock Returns

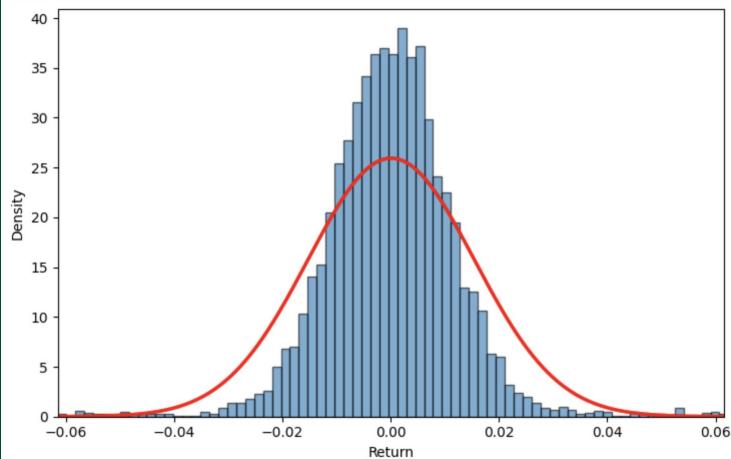


Our data, now looks **continuous**, meaning **no holes or gaps**.

So, let's try fitting this to a familiar **probability distribution**

**Goal:** Find the distribution generating these observations (**Find  $x_t$** )

# Distribution Generating Returns



Each day's a return ( $s_t$ ) is a randomly drawn from a Normal (Gaussian) distribution ( $x_t$ )

This distribution determines:

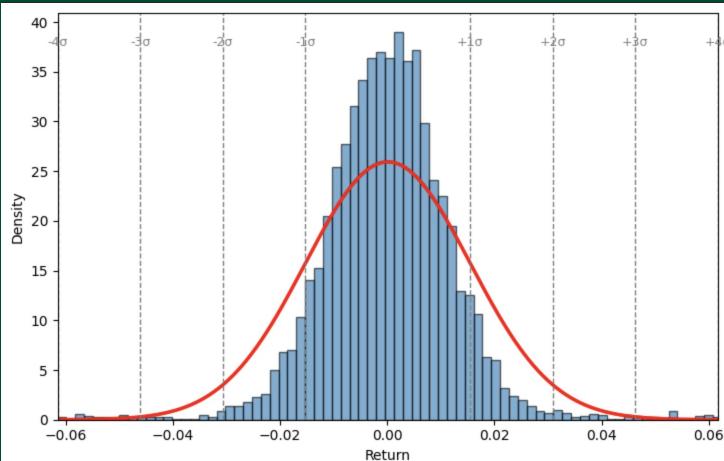
- The **probability** of observing different returns
- The **spread** of returns (volatility)
- The **likelihood** of extreme market moves

**Relationship:**  $S \sim N(\mu, \sigma^2)$

$\mu$  : mean (the center of the curve)

$\sigma$  : standard deviation (volatility)

# 68-95-99.7 Rule



In a **Normal distribution**:

~68% of observations fall within  $\pm 1\sigma$

95% fall within  $\pm 2\sigma$

99.7% fall within  $\pm 3\sigma$

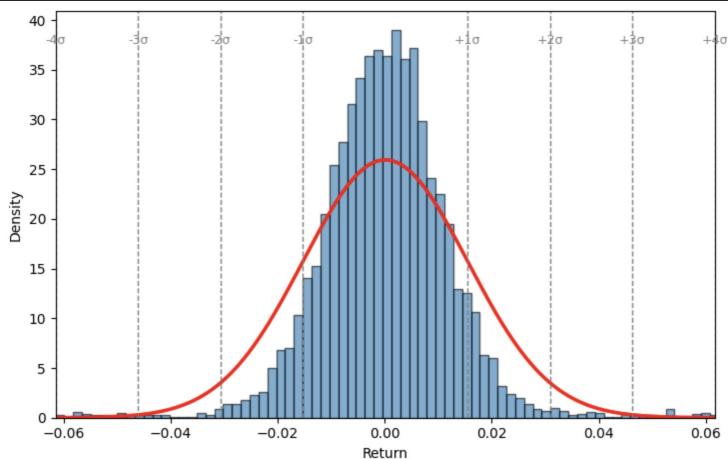
This **Empirical Rule** saves us a lot of time, and tells us that this is **not satisfying our goal**

**Relationship:**  $S \sim N(\mu, \sigma^2)$

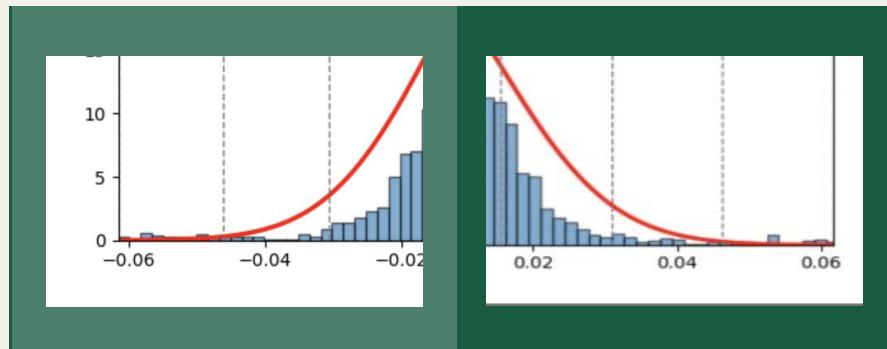
$\mu$  : mean (the center of the curve)

$\sigma$  : standard deviation (volatility)

# What's the big deal?



Yes, we may be misfitting the center of the distribution. However, to a **portfolio manager**, the **main concern is risk** not the **average return**



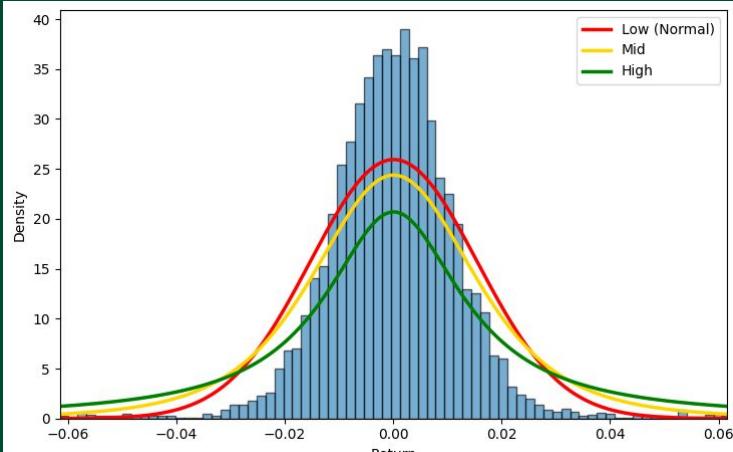
What's happening at the tails:

**Extreme returns** occur far more **frequently** than a single **Gaussian distribution predicts**

# Volatility Regimes

New Claim:

Returns are generated from different Gaussian distributions depending on the underlying hidden volatility regime



$$\text{Old Claim } S \sim N(\mu, \sigma^2) \rightarrow \text{New Claim } S \sim N(\mu, \sigma_{x_t}^2)$$

Where:

$\mu$  : mean (fixed)

$\sigma_{x_t}$  : standard deviation (regime-dependent volatility )

Observed Data: Returns ( $s_t$ )

Hidden States: Regimes ( $x_t$ )

Model: Hidden Markov Model



# Can a 3-state Hidden Markov Model fitted to daily equity returns identify underlying volatility regimes?

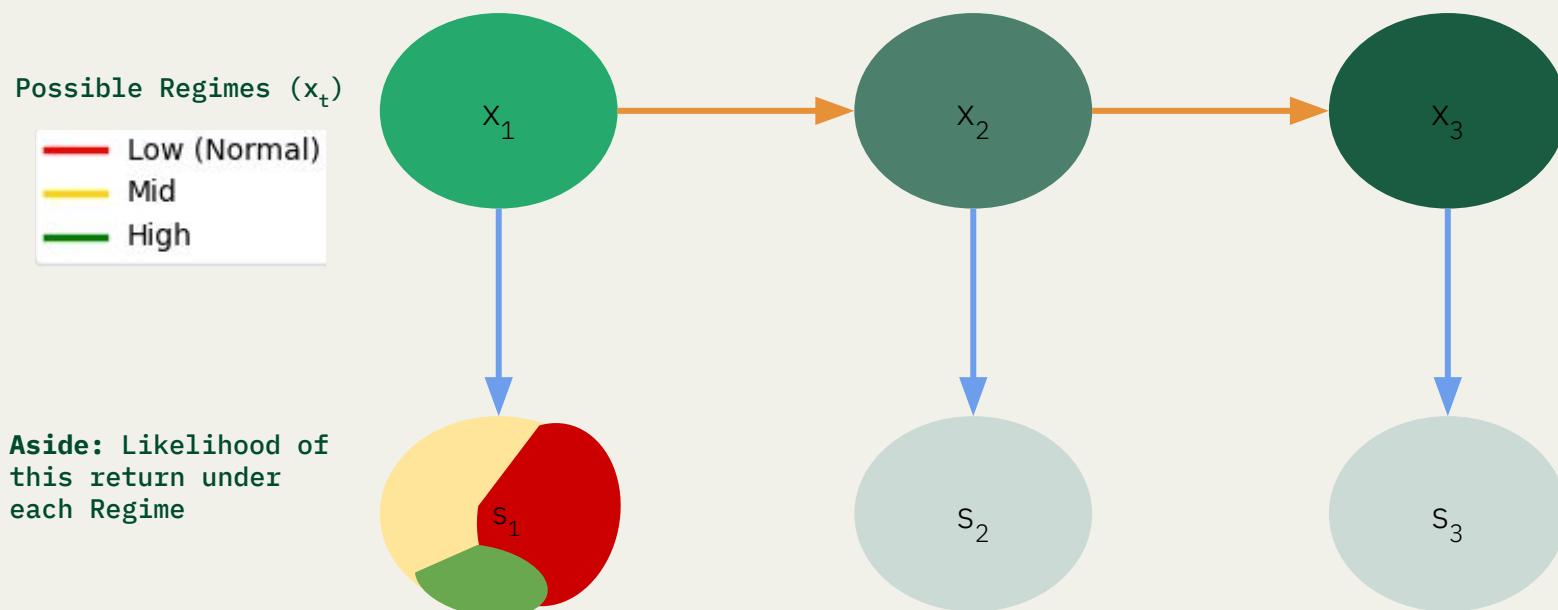
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Do those regimes have meaningfully different risk characteristics and "realistic" transition dynamics?

# What I've Done So Far

Transition Probability: Probability the Regime change from  $x_t$  to  $x_{t+1}$

Emission Probability: Distribution of Returns generated by regime  $x_t$



# Anticipated Challenges / Potential Future Steps

## **Challenges:**

- 01 Choose number of regimes
- 02 Sensitivity to initializations
- 03 Interpreting regimes economically

## **Next Steps:**

Examine, for each day, which hidden state the model believes the market was most likely in  
**(Viterbi Algorithm)**

# COMPs

## Timeline

Now - Feb 16th	Feb 17th - Mar 19th	Mar 20th - Mar 25th	Mar 26th - Apr 7th	Apr 6th- Apr 28th
<p>Experiment with number of regimes (<math>K = 2, 3, 4</math>)</p> <p>Evaluate Model strength (precision/recall)</p>	<p>Refine HMM implementation</p> <p>Create more HMM models using other volatility techniques or distributions</p>	<p>Results &amp; model comparison results</p> <p>Start writing up a report on findings</p>	<p>Improve visualizations and storytelling</p> <p>Interpret economic meaning of regimes</p>	<p>Is this Viable... Finalized analysis &amp; conclusions</p> <p>Cleaning up Github repo(s)</p>



# Questions?