



# Finding Market Regimes in Equity Returns Using Hidden Markov Models

---



# Tools & Resources

## **Software:**

- 1** Python
- 1.1** Yfinance (stock data)
- 1.2** Numpy/Pandas (data manipulation)
- 1.3** Matplotlib (plotting)
- 1.4** HmmLearn (HMM)
- 2** Github (Version Control)

## **Hardware:**

Personal Laptop

## **Advisor/**

**Consultant:** Professor M. Wade &  
Professor M. Gee

# About Me



## ■ BACKGROUND

**Interest:** Quantitative Finance and Machine Learning

**Major:** Applied Mathematics concentration in Computer Science

**Relevant coursework:** Mathematical Models, Optimal Control, Probability, Applied Linear Algebra, Stats (106 & 206)

**School Experience:** (Tutor/TA for COMP 118 & 218)

**Professional Experience:** 3 Data Science Internships; 2 of which were at JPMorgan Chase

**From Data Science → Quant Research**





## **Research Question without Jargon**

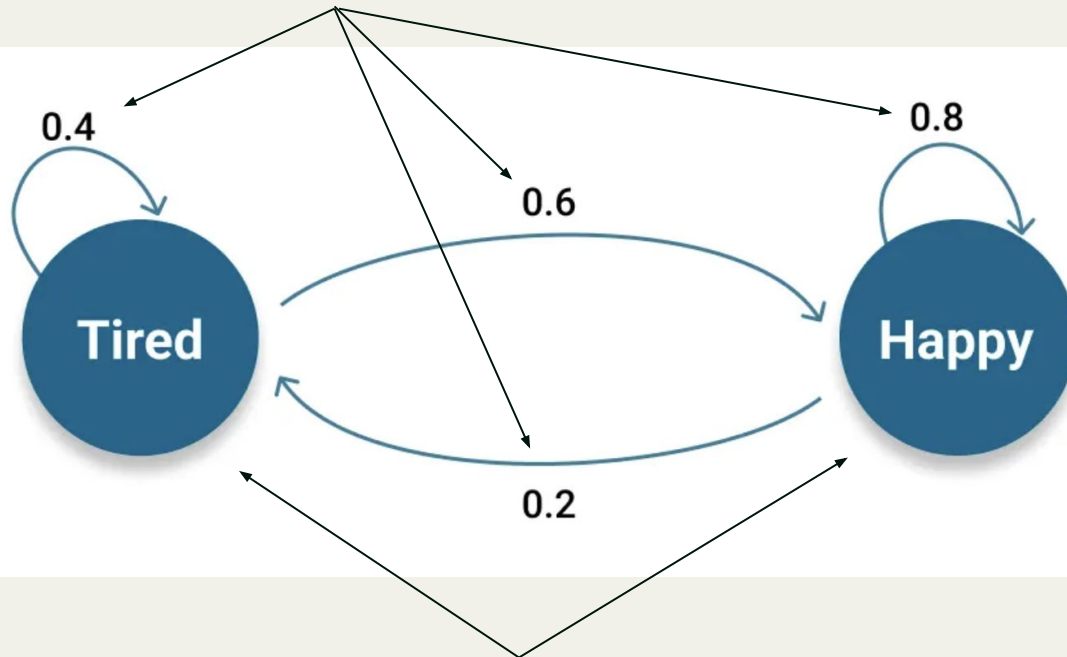
Can we automatically detect when the market is in a “calm” period versus a “volatile” period by only looking at daily price changes?”

---



# Markov Chains

**Transition Probabilities:** from a current state to a next state



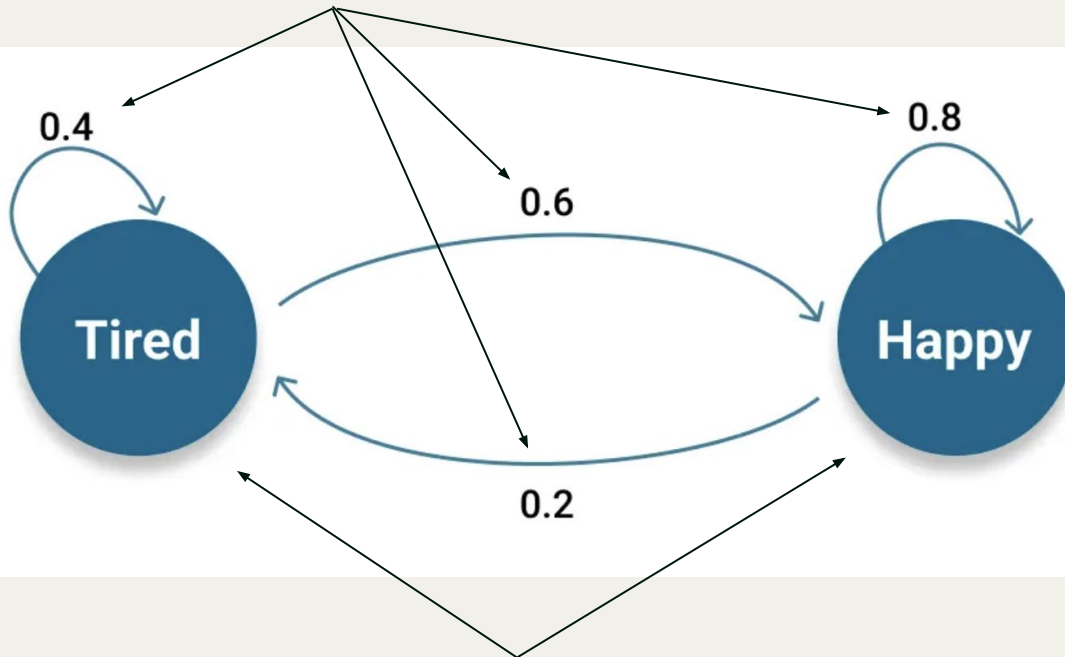
**States:** the environment/system

## Example:

Imagine being **Tired** you then have a **60% chance** of becoming happy, and a **40% chance** of staying tired.

# Markov Chains

**Transition Probabilities:** from a current state to a next state



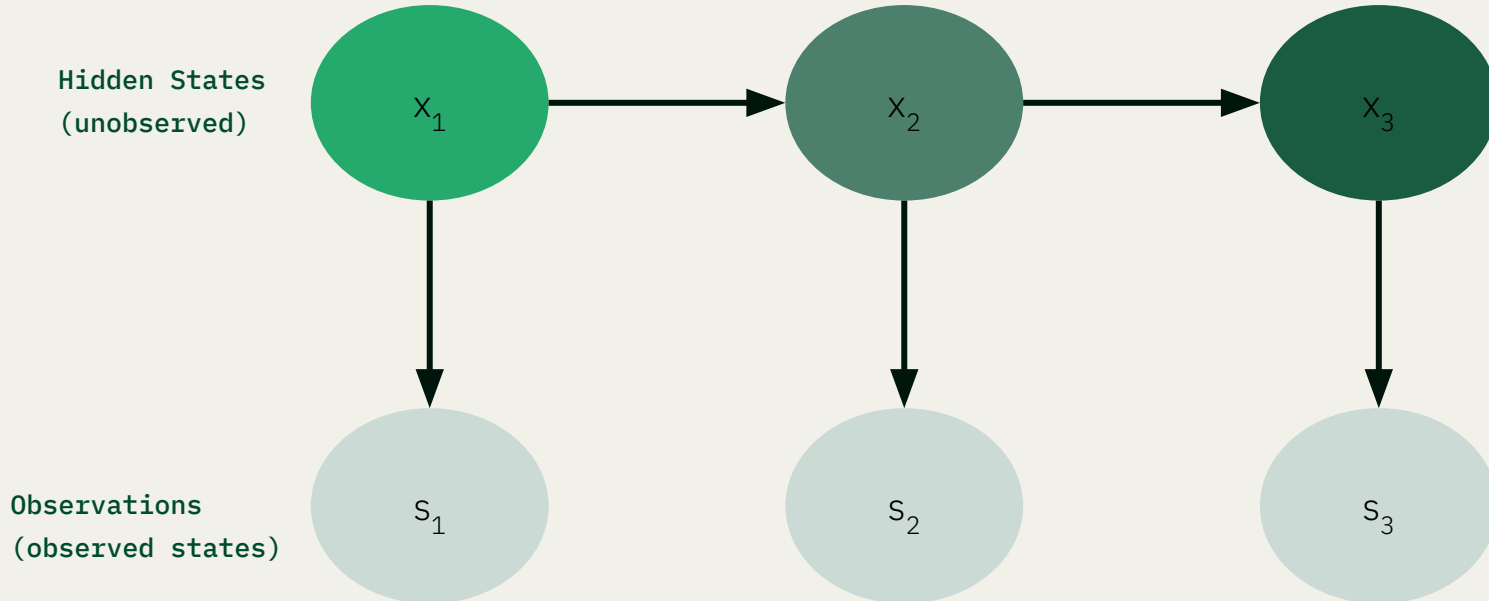
**States:** the environment/system

- stochastic process
- moves between states over time
- **“Memoryless,”** The next state only depends on the current state. This is what’s called the **Markov Property**



# Hidden Markov Model

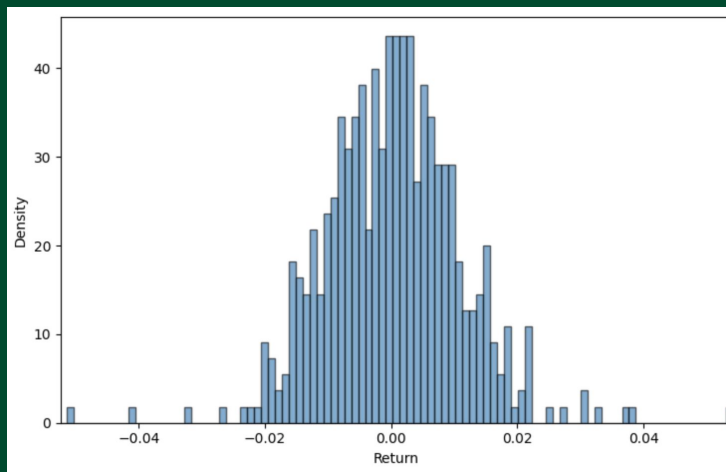
**The Claim:** There exists an underlying, unobserved processes  $x_t$  that governs how  $s_t$  are generated.



# Stock Returns

$n$ : the number of samples ( $n=500$ )

$s_t$ : observed return at time  $t$



This histogram shows the **empirical distribution of observed returns**.

Each **return is a sample** drawn from an **unknown underlying distribution**.

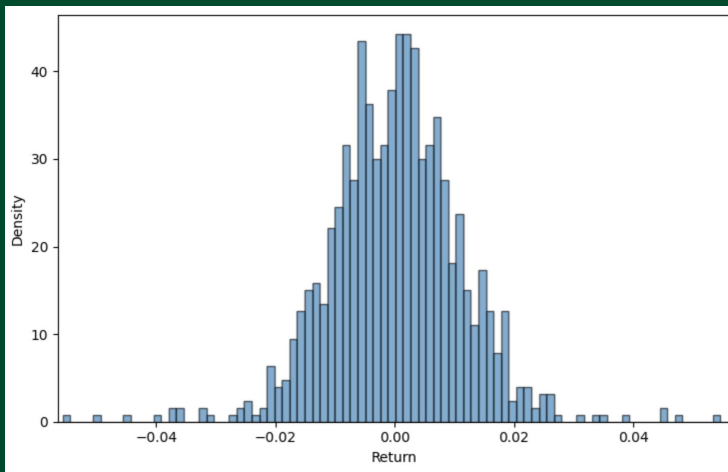
With a **small number of samples**, the shape of the distribution is noisy and difficult to identify, so let's **increase the number of samples**.

**Goal:** Find the distribution generating these observations (**Find  $x_t$** )



# Stock Returns

$n = 1000$



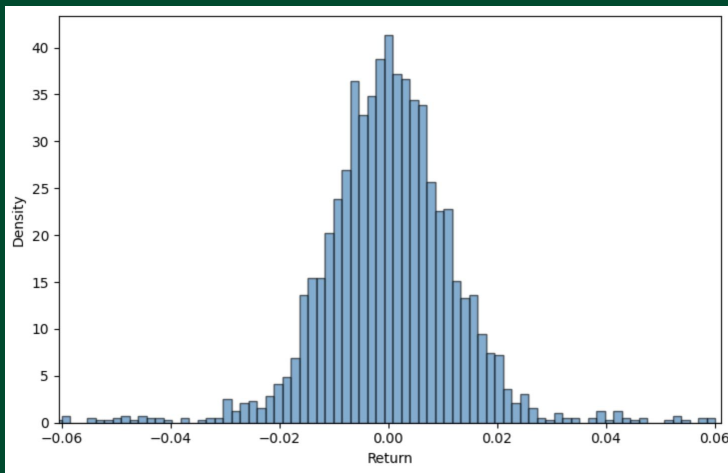
We are starting to get **more density** around  $\pm [0.02, 0.04]$

**Let's keep increasing the sample count..**

**Goal:** Find the distribution generating these observations ( **Find  $x_t$**  )

# Stock Returns

n = 2500



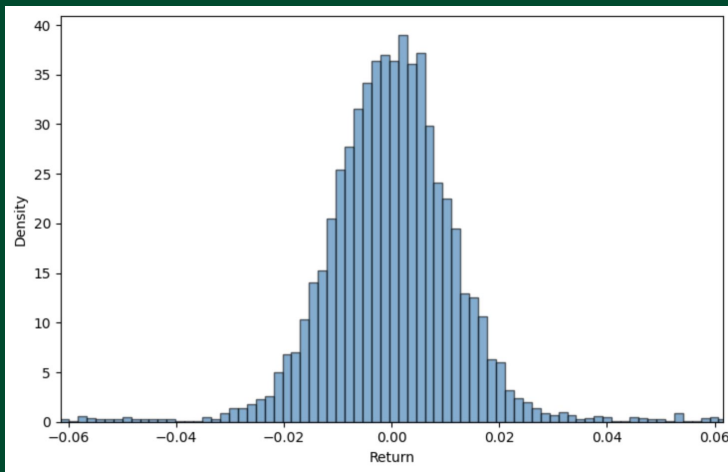
Again, we are getting **more density around  $\pm [0.02, 0.04]$**  and also **less gaps in our structure**

**Let's keep increasing the sample count..**

**Goal:** Find the distribution generating these observations (**Find  $x_t$** )

# Stock Returns

$n = 5000$



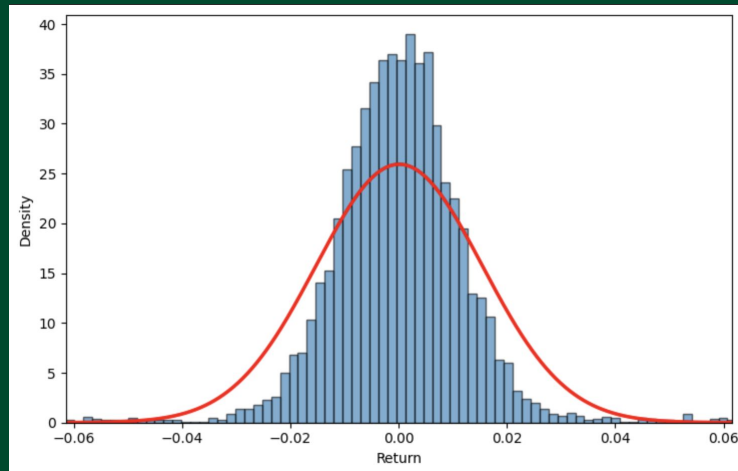
We have 10x our sample size (  $n$  )

Our data, now looks **continuous**, meaning **no holes or gaps**.

So, let's try fitting this to a familiar **probability distribution**

**Goal:** Find the distribution generating these observations ( **Find  $x_t$**  )

# Distribution Generating Returns



Each day's a return ( $s_t$ ) is a randomly drawn from a Normal (Gaussian) distribution ( $x_t$ )

**This distribution determines:**

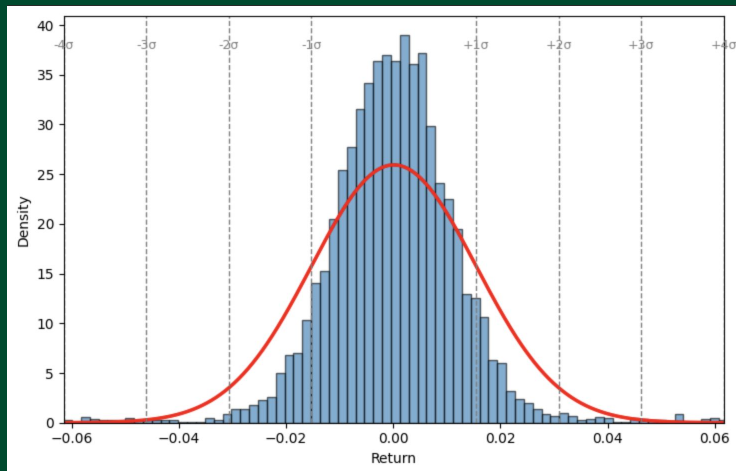
- The **probability** of observing different returns
- The **spread** of returns (volatility)
- The **likelihood** of extreme market moves

**Relationship:**  $S \sim N(\mu, \sigma^2)$

$\mu$  : mean (the center of the curve)

$\sigma$  : standard deviation (volatility)

# 68-95-99.7 Rule



## In a Normal distribution:

~68% of observations fall within  $\pm 1\sigma$

95% fall within  $\pm 2\sigma$

99.7% fall within  $\pm 3\sigma$

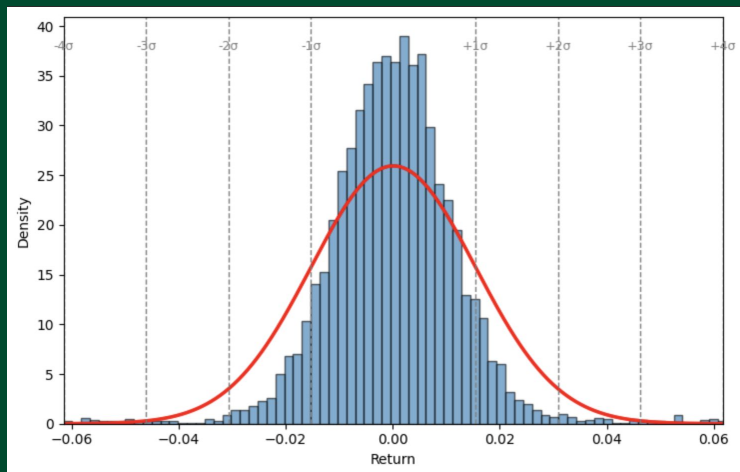
This **Empirical Rule** saves us a lot of time, and tells us that this is **not satisfying our goal**

**Relationship:**  $S \sim N(\mu, \sigma^2)$

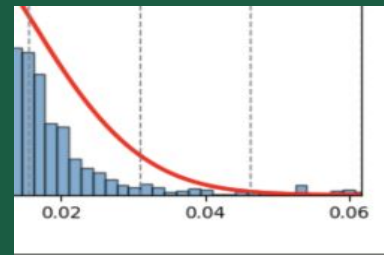
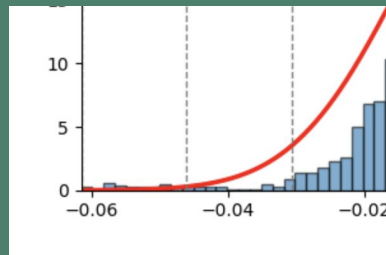
$\mu$  : mean (the center of the curve)

$\sigma$  : standard deviation (volatility)

# What's the big deal?



Yes, we may be misfitting the center of the distribution. However, to a **portfolio manager**, the **main concern is risk** not the **average return**



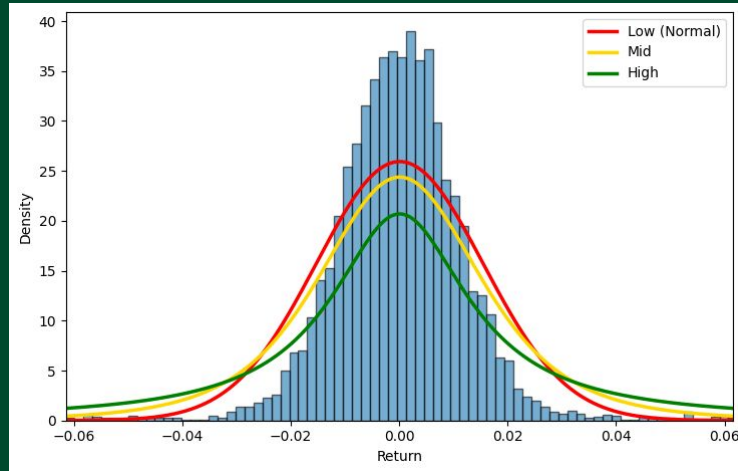
What's happening at the tails:

**Extreme returns** occur far more **frequently** than a single **Gaussian distribution predicts**

# Volatility Regimes

## New Claim:

**Returns** are generated from different **Gaussian** distributions depending on the underlying **hidden volatility regime**



Old Claim  $S \sim N(\mu, \sigma^2) \rightarrow$  New Claim  $S \sim N(\mu, \sigma_{x_t}^2)$

## Parameters with New Claim:

$\mu$  : (fixed),  $\sigma_{x_t}$  : (regime-dependent **volatility**)

**Observed Data:** Returns ( $s_t$ )

**Hidden States:** Regimes ( $x_t$ )

**Model:** Hidden Markov Model



Can a 3-state Hidden Markov Model fitted to daily equity returns identify underlying volatility regimes?

---

Do those regimes have meaningfully different risk characteristics and "realistic" transition dynamics?

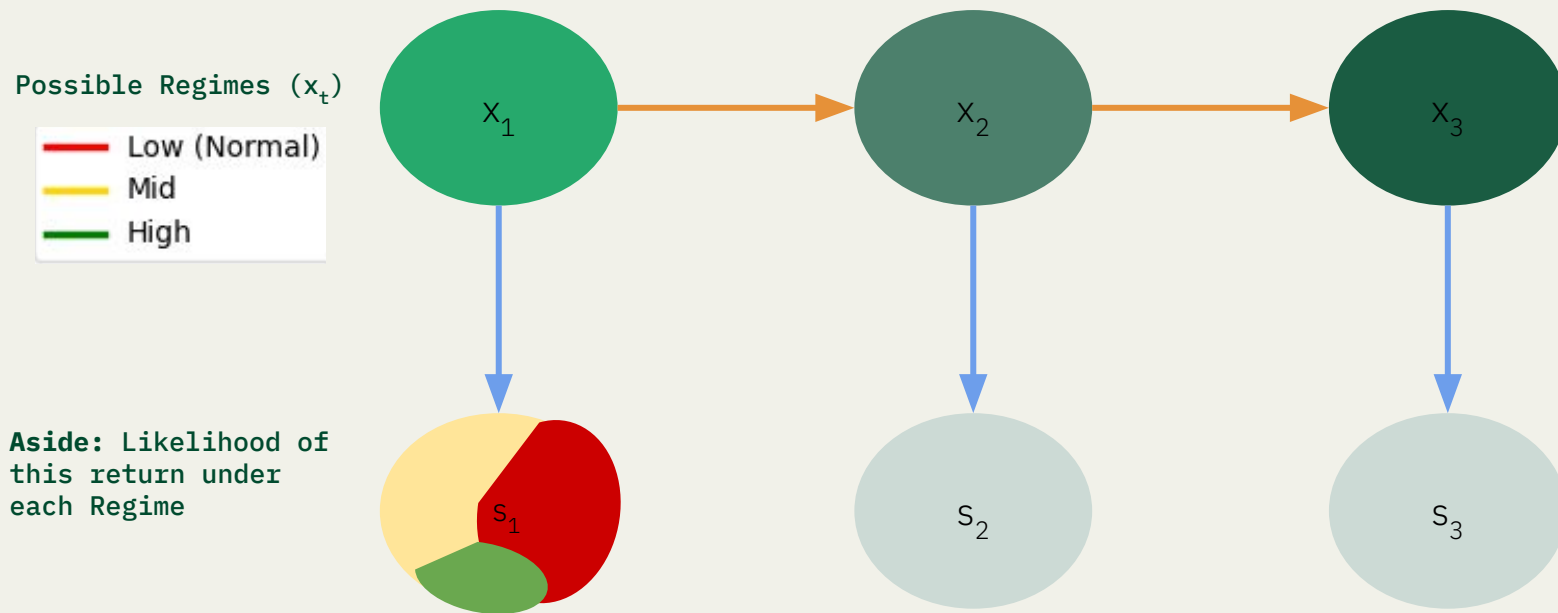




# What I've Done So Far

**Transition Probability:** Probability the Regime change from  $x_t$  to  $x_{t+1}$

**Emission Probability:** Distribution of Returns generated by regime  $x_t$



# Anticipated Challenges / Potential Future Steps

## Challenges:

- 01 Choose number of regimes
- 02 Sensitivity to initializations
- 03 Interpreting regimes economically

## Next Steps:

Examine, for each day, which hidden state the model believes the market was most likely in  
**(Viterbi Algorithm)**



---

# COMP<sub>s</sub>

## Timeline

Now - Feb  
16th

Experiment with  
number of regimes  
( $K = 2, 3, 4$ )

Evaluate Model  
strength  
(precision/recall)

Feb 17th -  
Mar 19th

Refine HMM  
implementation

Create more HMM  
models using  
other volatility  
techniques or  
distributions

Mar 20th -  
Mar 25th

Results & model  
comparison  
results

Start writing up  
a report on  
findings

Mar 26th -  
Apr 7th

Improve  
visualizations  
and storytelling

Interpret  
economic meaning  
of regimes

Apr 6th -  
Apr 28th

Is this Viable...  
Finalized  
analysis &  
conclusions

Cleaning up  
Github repo(s)



Questions?