

```
1: // $Id: powerint.cpp,v 1.15 2022-01-07 12:53:31-08 - - $
2:
3: //
4: // NAME
5: //     powerint - power function raising a double to an int power
6: //
7: // SYNOPSIS
8: //     double powi (double base, int exponent);
9: //
10: // DESCRIPTION
11: //     The powi() function computes the value of base raised to the
12: //     power exponent.
13: //
14: // RETURN VALUES
15: //     Upon successful completion, powi() returns the value of base
16: //     raised to the power of exponent.  If exponent is 0, 1.0 is
17: //     returned regardless of the value of base (a number, 0, NaN,
18: //     or +-Infinity).  Otherwise multiplication and division are
19: //     subject to the rules of IEEE-754 floating point arithmetic,
20: //     for CPUs which support that.
21: //
22: // MATHEMATICS USED
23: //
24: //     powi (x, - n)    => powi (1 / x, n)
25: //     powi (x, 2 n)    => powi (x ** 2, n / 2)
26: //     powi (x, n + 1) => x * powi (x, n)
27: //
28: //     .EQ
29: //     x sup { - n }    = { ( 1 / x ) } sup n
30: //     x sup { 2 n }    = ( x sup 2 ) sup { n / 2 }
31: //     x sup { n + 1 } = x ( x sup n )
32: //     .EN
33: //
34: //     $$
35: //     x ^ { - n }      = { ( 1 / x ) } ^ n
36: //     x ^ { 2 n }      = ( x ^ 2 ) ^ ( n / 2 )
37: //     x ^ { n + 1 }    = x ( x ^ n )
38: //     $$
39: //
40: //
41:
42: #include <cstdlib>
43: #include <iomanip>
44: #include <iostream>
45: #include <libgen.h>
46: #include <limits>
47: #include <sstream>
48: #include <string>
49: #include <typeinfo>
50: #include <vector>
51:
52: using namespace std;
53:
54: const int DIGITS = numeric_limits<double>::digits10 + 6;
```

```
55:
56: template <typename item_t>
57: item_t from_string (const string& arg) {
58:     stringstream stream {arg};
59:     item_t result;
60:     stream >> result;
61:     return result;
62: }
63:
64: void print_powi (double base, int exponent, double result) {
65:     cout << "powi: " << base << " ** " << exponent << " * "
66:         << result << endl;
67: }
68:
69: double powi (double base, int exponent) {
70:     double result = 1.0;
71:     print_powi (base, exponent, result);
72:     if (exponent < 0) {
73:         base = 1.0 / base;
74:         exponent = - exponent;
75:         print_powi (base, exponent, result);
76:     }
77:     while (exponent > 0) {
78:         if (exponent % 2 == 0) { /* is even */
79:             base *= base;
80:             exponent /= 2;
81:         } else {
82:             result *= base;
83:             --exponent;
84:         }
85:         print_powi (base, exponent, result);
86:     }
87:     return result;
88: }
89:
90: int main (int argc, char** argv) {
91:     vector<string> args (&argv[1], &argv[argc]);
92:     for (auto arg = args.cbegin(); arg != args.cend(); ++arg) {
93:         double base = from_string<double> (*arg);
94:         if (++arg == args.cend()) break;
95:         int exponent = from_string<int> (*arg);
96:         cout << endl << setprecision (DIGITS);
97:         double result = powi (base, exponent);
98:         cout << "ANSWER: " << base << " ** " << exponent
99:             << " == " << result << endl;
100:     }
101:     return 0;
102: }
103:
104: /*
105: //TEST// valgrind --leak-check=full --show-reachable=yes \
106: //TEST//      --log-file=powerint.out.grind \
107: //TEST//      powerint 2 2 2 9 2 15 2 16 2 24 \
108: //TEST//      >powerint.out 2>&1
109: //TEST// mkpspdf powerint.ps powerint.cpp powerint.out*
110: */
111:
```

```
1:
2: powi: 2 ** 2 * 1
3: powi: 4 ** 1 * 1
4: powi: 4 ** 0 * 4
5: ANSWER: 2 ** 2 == 4
6:
7: powi: 2 ** 9 * 1
8: powi: 2 ** 8 * 2
9: powi: 4 ** 4 * 2
10: powi: 16 ** 2 * 2
11: powi: 256 ** 1 * 2
12: powi: 256 ** 0 * 512
13: ANSWER: 2 ** 9 == 512
14:
15: powi: 2 ** 15 * 1
16: powi: 2 ** 14 * 2
17: powi: 4 ** 7 * 2
18: powi: 4 ** 6 * 8
19: powi: 16 ** 3 * 8
20: powi: 16 ** 2 * 128
21: powi: 256 ** 1 * 128
22: powi: 256 ** 0 * 32768
23: ANSWER: 2 ** 15 == 32768
24:
25: powi: 2 ** 16 * 1
26: powi: 4 ** 8 * 1
27: powi: 16 ** 4 * 1
28: powi: 256 ** 2 * 1
29: powi: 65536 ** 1 * 1
30: powi: 65536 ** 0 * 65536
31: ANSWER: 2 ** 16 == 65536
32:
33: powi: 2 ** 24 * 1
34: powi: 4 ** 12 * 1
35: powi: 16 ** 6 * 1
36: powi: 256 ** 3 * 1
37: powi: 256 ** 2 * 256
38: powi: 65536 ** 1 * 256
39: powi: 65536 ** 0 * 16777216
40: ANSWER: 2 ** 24 == 16777216
```

```
1: ==18774== Memcheck, a memory error detector
2: ==18774== Copyright (C) 2002-2017, and GNU GPL'd, by Julian Seward et al
.
3: ==18774== Using Valgrind-3.17.0 and LibVEX; rerun with -h for copyright
info
4: ==18774== Command: powerint 2 2 2 9 2 15 2 16 2 24
5: ==18774== Parent PID: 18772
6: ==18774==
7: ==18774==
8: ==18774== HEAP SUMMARY:
9: ==18774==      in use at exit: 0 bytes in 0 blocks
10: ==18774==    total heap usage: 26 allocs, 26 frees, 891 bytes allocated
11: ==18774==
12: ==18774== All heap blocks were freed -- no leaks are possible
13: ==18774==
14: ==18774== For lists of detected and suppressed errors, rerun with: -s
15: ==18774== ERROR SUMMARY: 0 errors from 0 contexts (suppressed: 0 from 0)
```