

Greenhouse Gas Emissions

A Case Study On The Calibration Of An L-pitot Static Tube

Eric Harman
CEESI



RATA Tests are often based on “S” Pitot Tubes

Advantages:

- Cheap
- Simple design
- Doesn't plug



Disadvantages:

- Questionable accuracy
- Problems with swirl

3-D Pitot Tubes

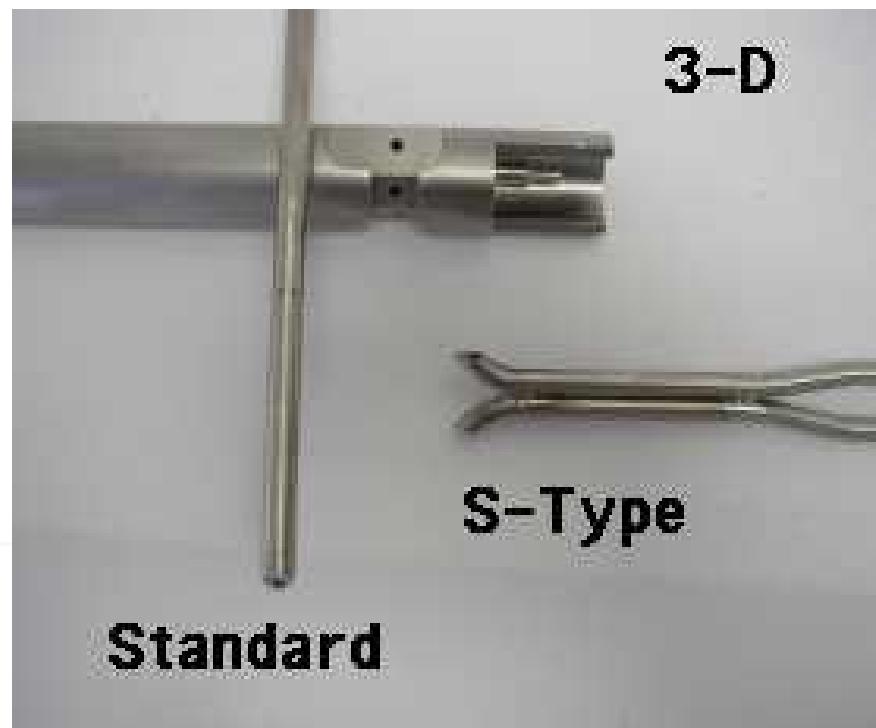
Advantages:

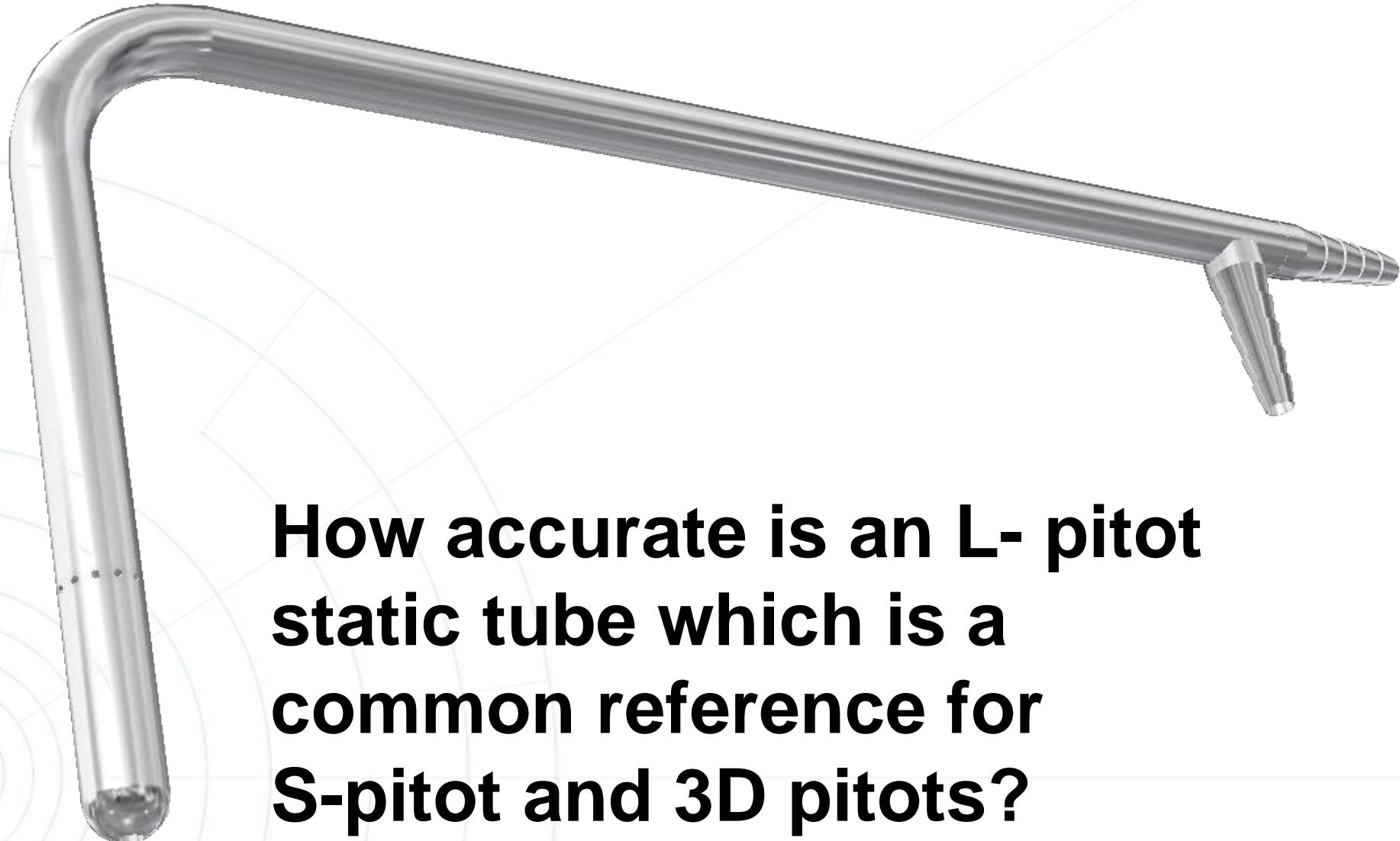
- Can measure swirl vectors (yaw)
- Can measure radial vectors (pitch)

Problems:

- Requires calibration

EPA adds wind tunnel calibration requirements which are often based on L-pitot static tubes



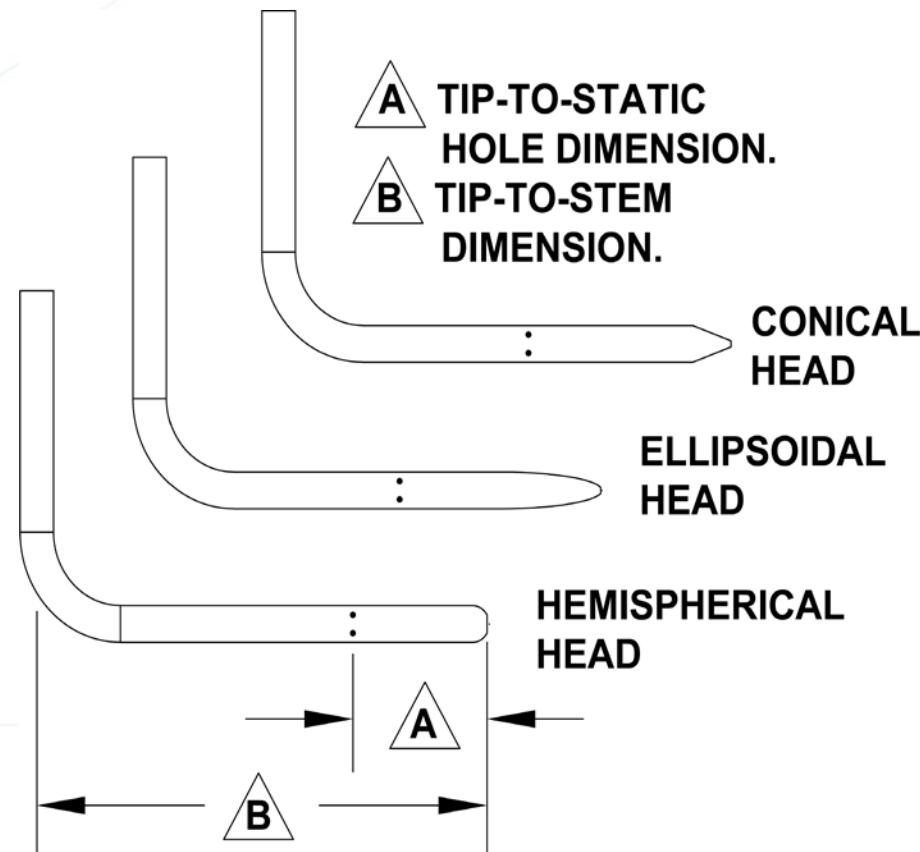
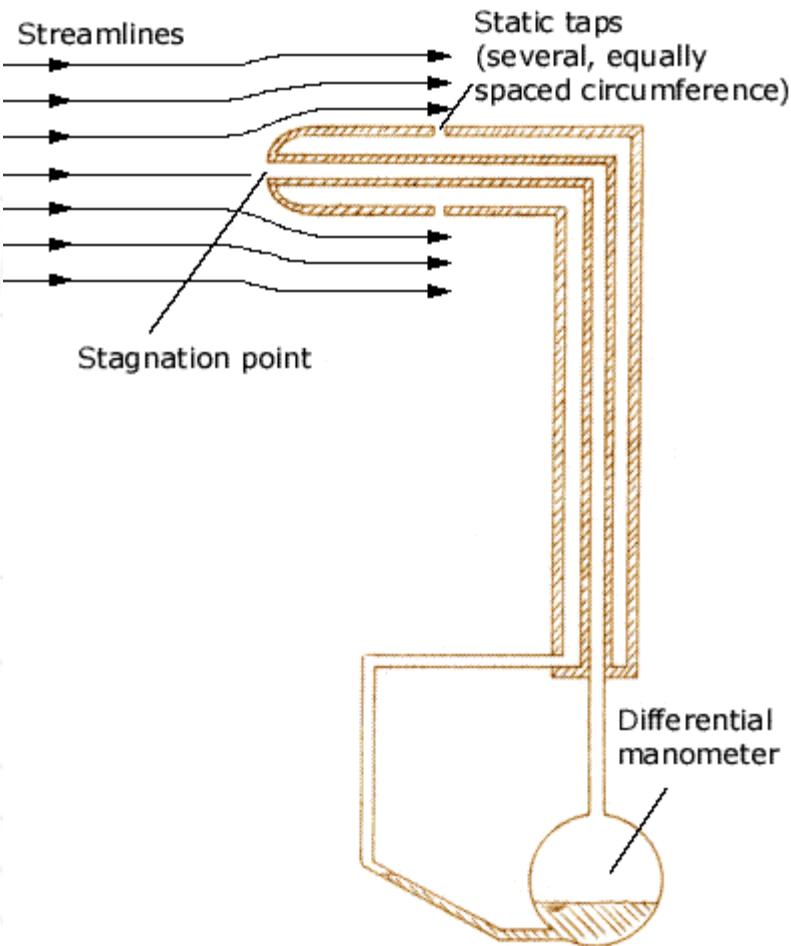


How accurate is an L- pitot static tube which is a common reference for S-pitot and 3D pitots?

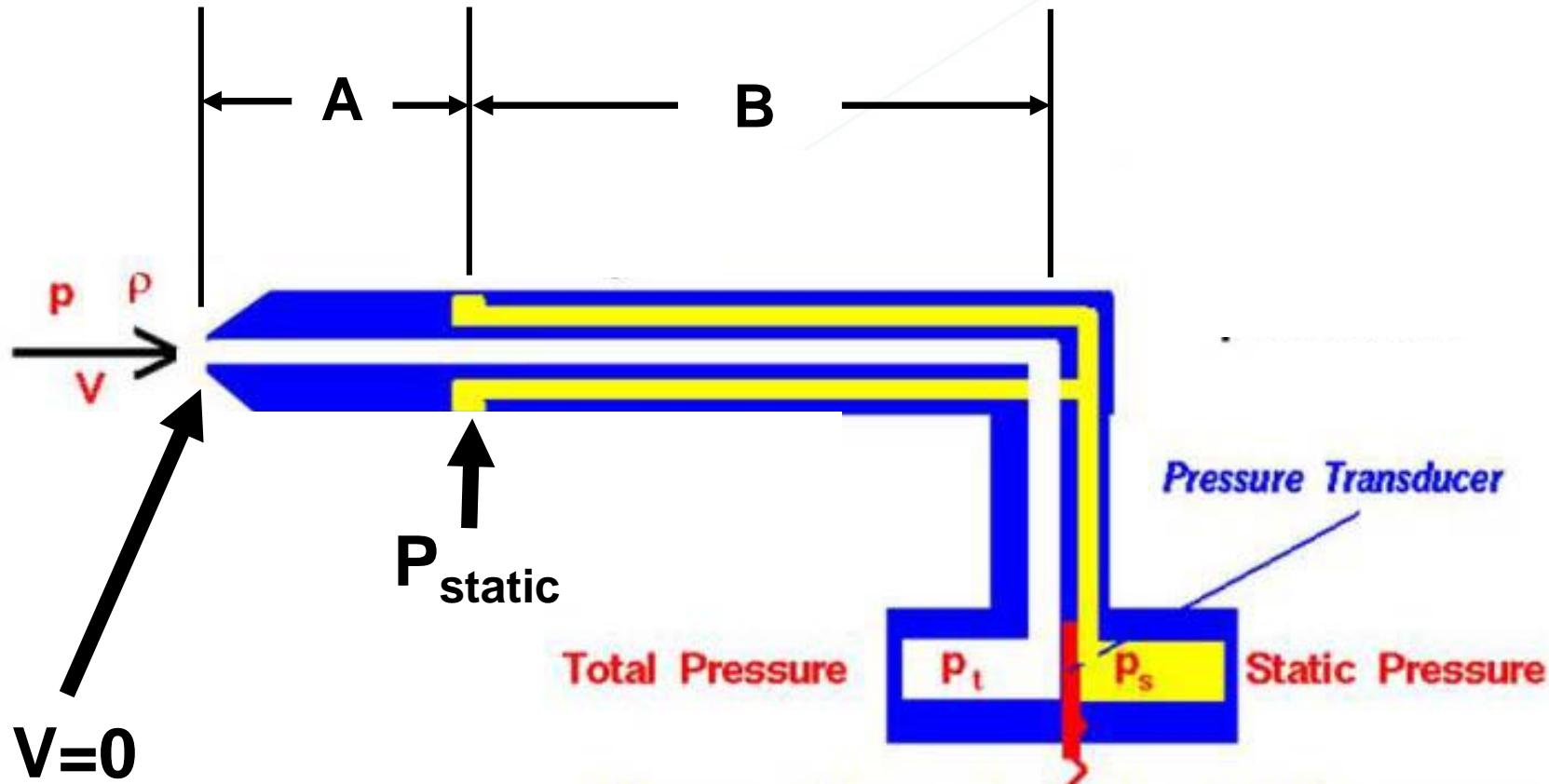
Alternate Calibration Methodology For Point-Velocity Devices (Pitot-Tubes, Anemometers, Hot-Wire Devices) Using NIST Traceable Mass Flow Measurement Standards



Pitot-static In A Flow Stream



Pitot-Static Tube Physics



**Isentropic
Compression**

Not All Static Pitot Tubes are the same

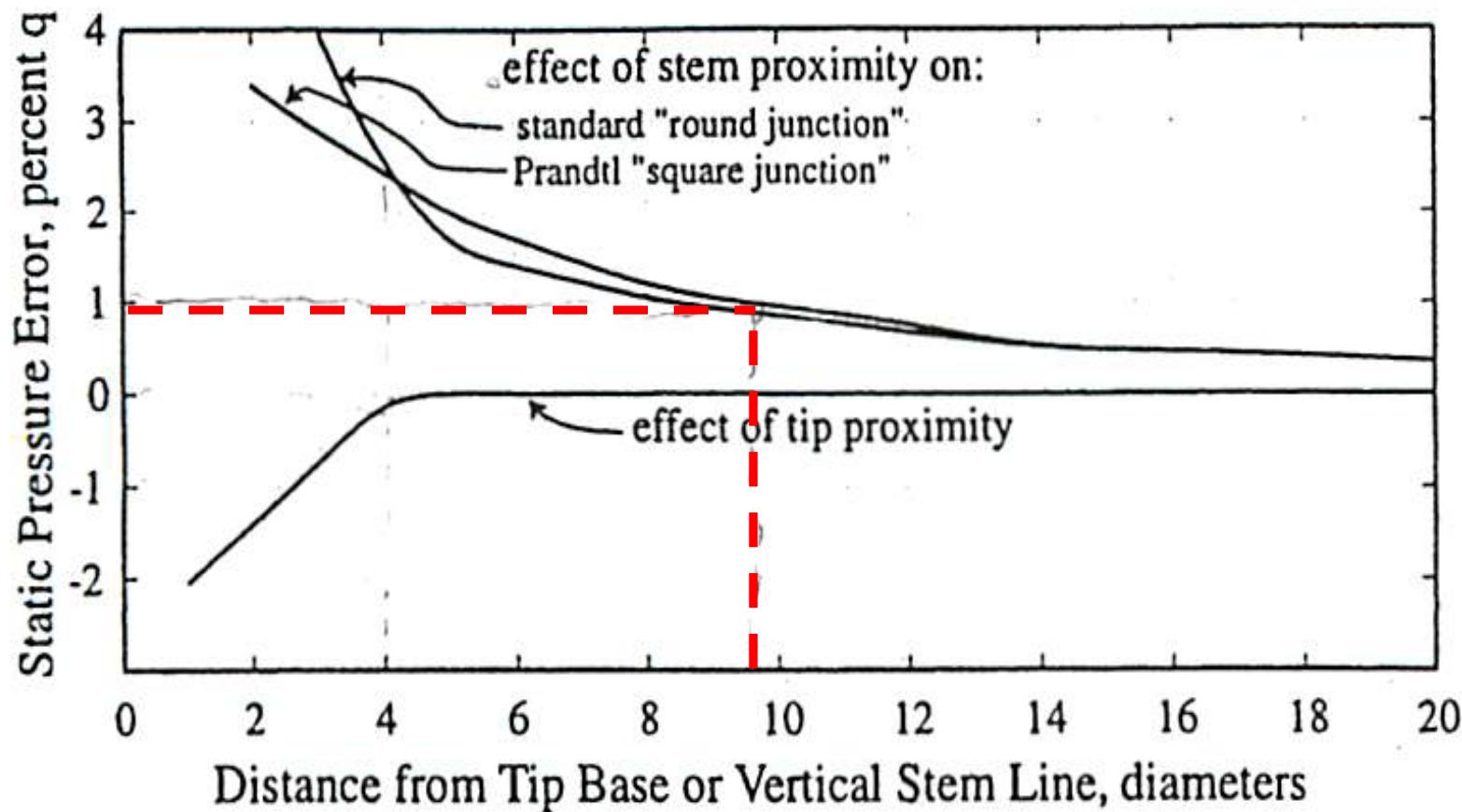


FIGURE 4.9 Effect of static orifice distance from tip or from stem: see Example 4.1.

Point-Velocity Calibration

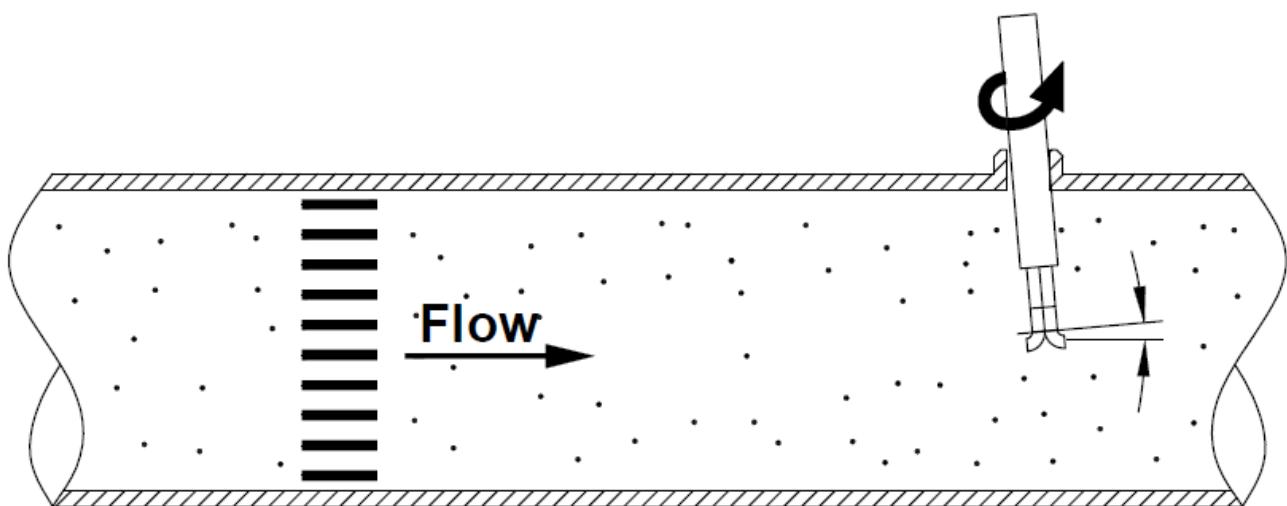
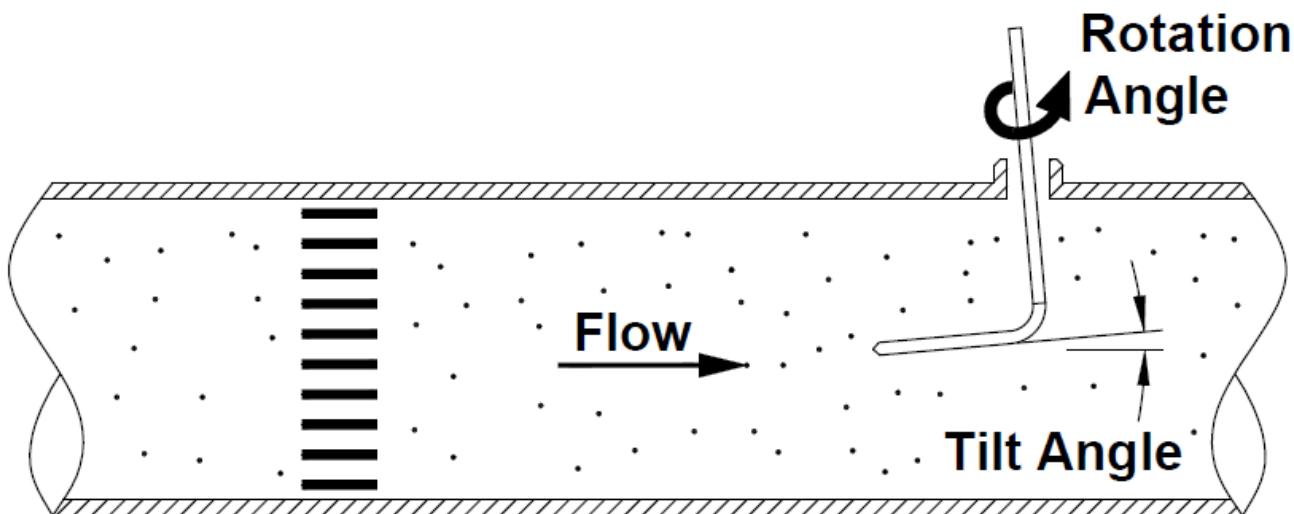


$$V = K_{factor} \text{ (output)}$$

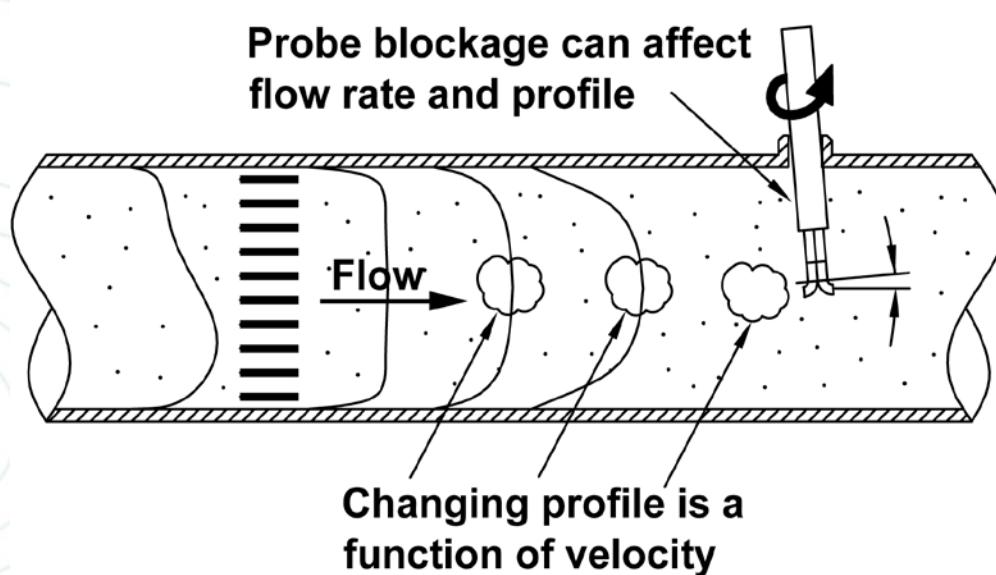
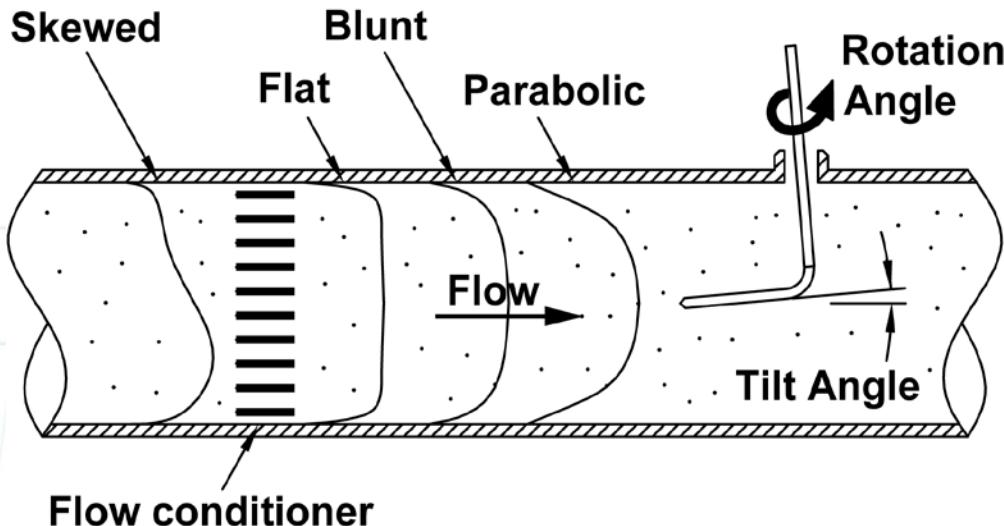
From Lab

Measured

Traditional Method



Traditional Calibration Methodology Pitfalls



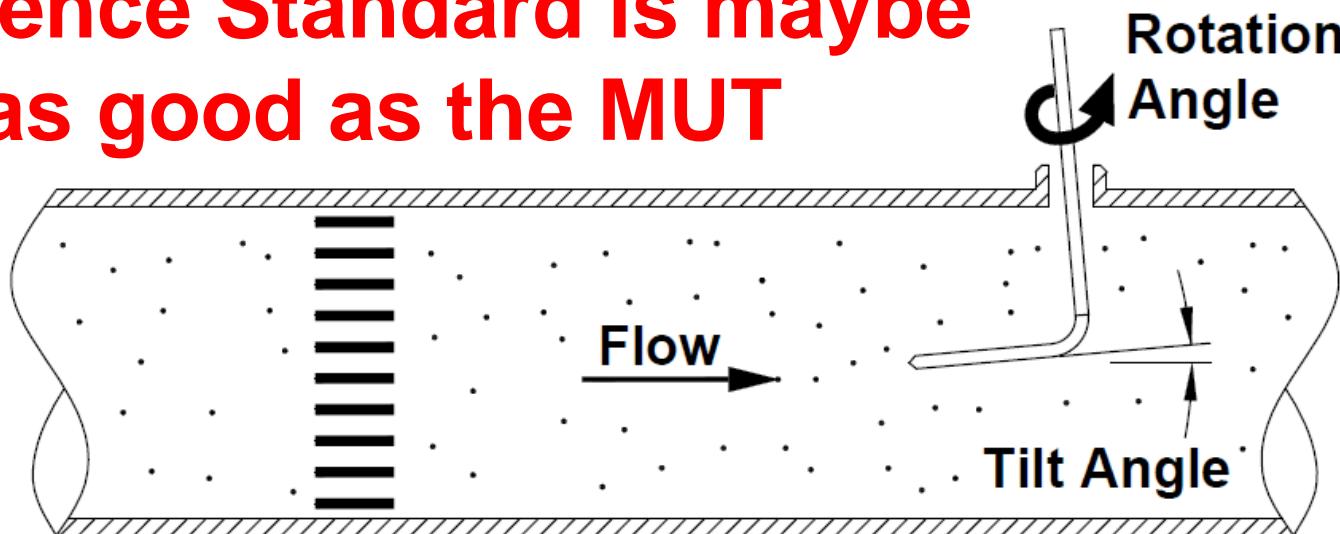
STEP 1.

- Set flow and record velocity with Pitot-Static Tube that has a known Pressure Coefficient (C_p).
- Avoid Tilt & Rotation Errors.

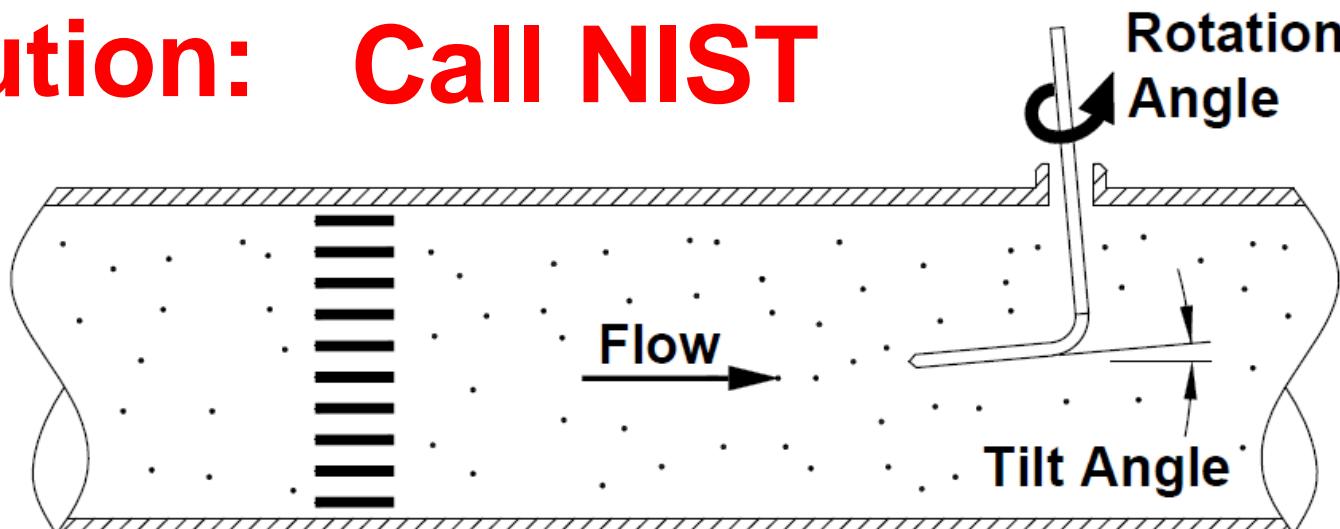
STEP 2.

- Maintain identical flow rate.
- Remove the Pitot-Static Tube.
- Position the Point Velocity Device in the exact same location.
- Make sure the blockage of Point Velocity Device does not alter the fluid velocity by reducing the flow area or increasing the pressure drop causing a lower fan output.
- Make sure velocity range does not cause an adverse localized velocity gradient.
- Avoid Tilt & Rotation Errors.

**Reference Standard is maybe
only as good as the MUT**



Solution: Call NIST



Alternate Point-Velocity Calibration

NIST Fluid Metrology Group

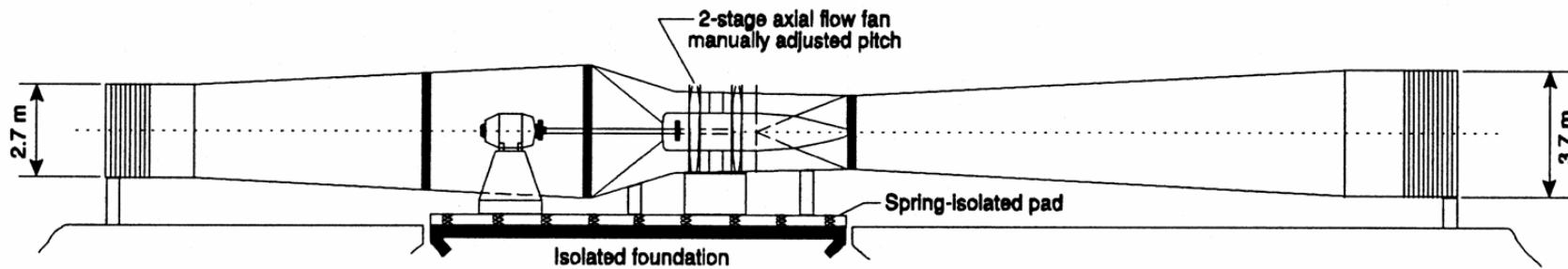
Iosif I. Shinder, Aaron Johnson



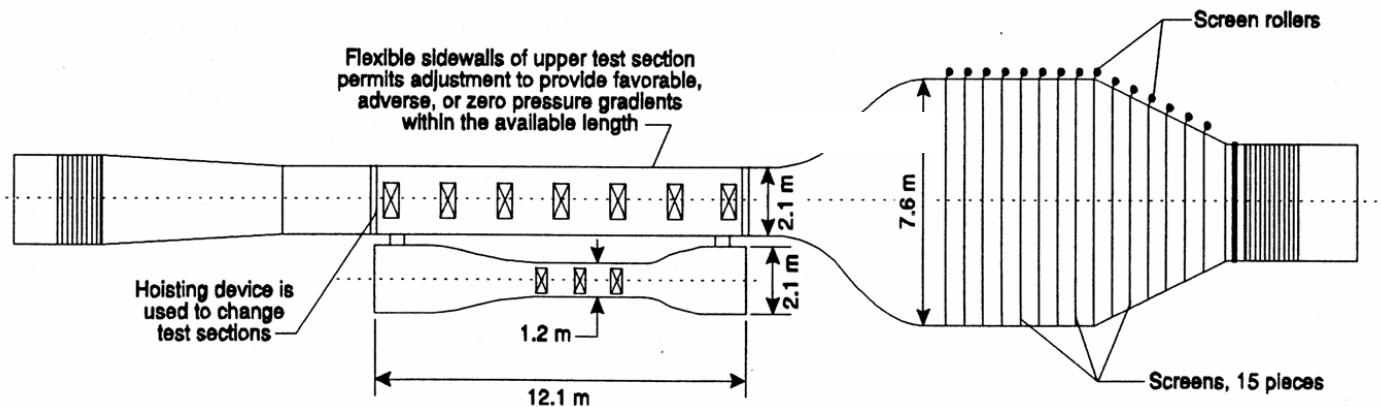
NIST Dual Test-Section Wind Tunnel



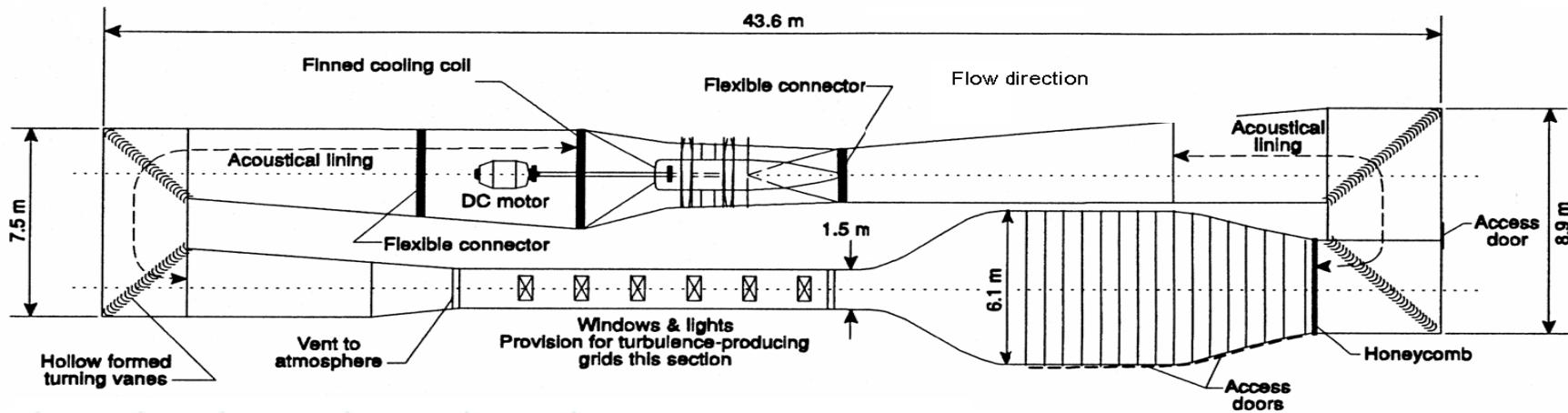
Return
Section
Side
View



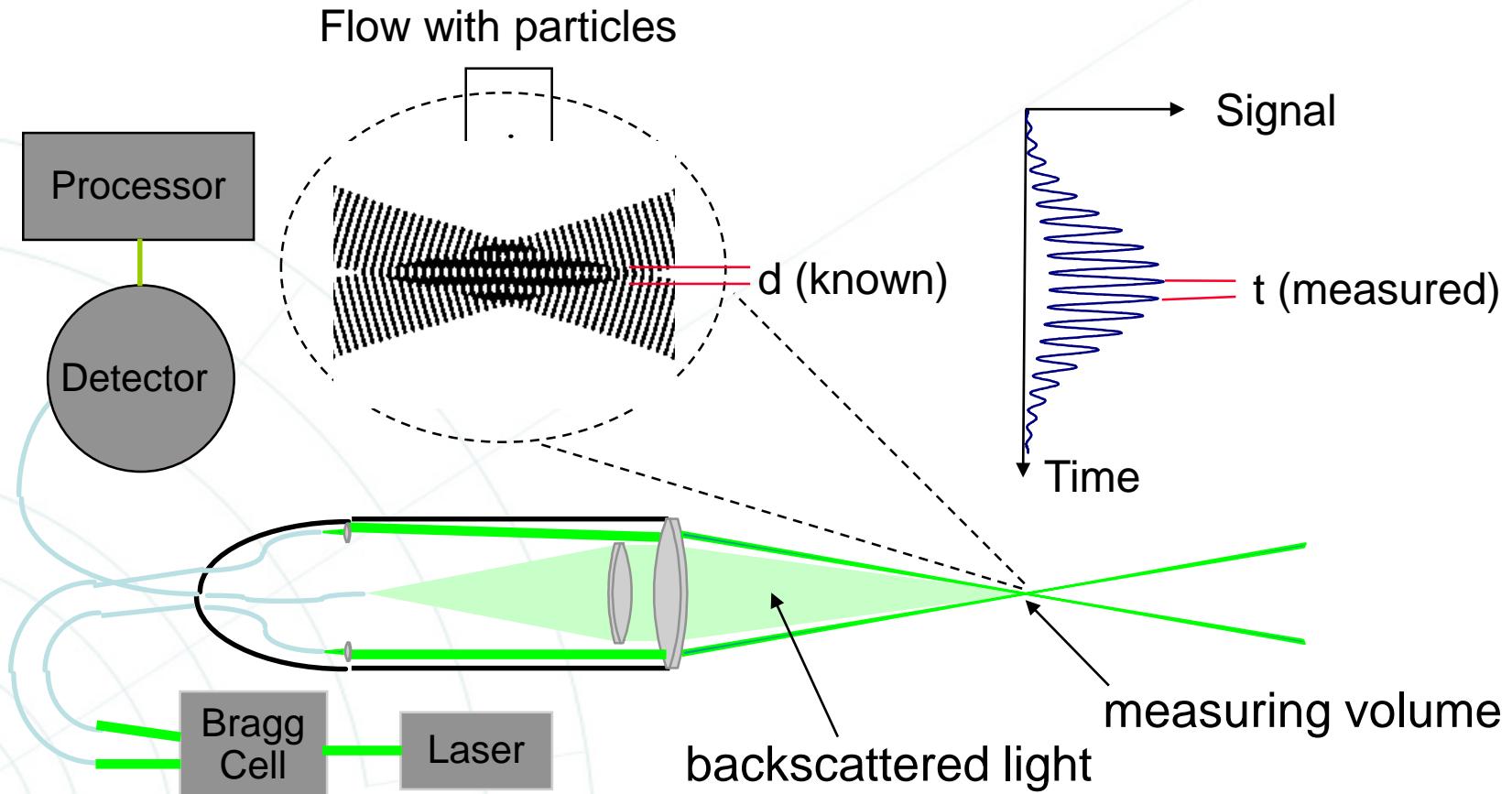
Test
Section
Side
View



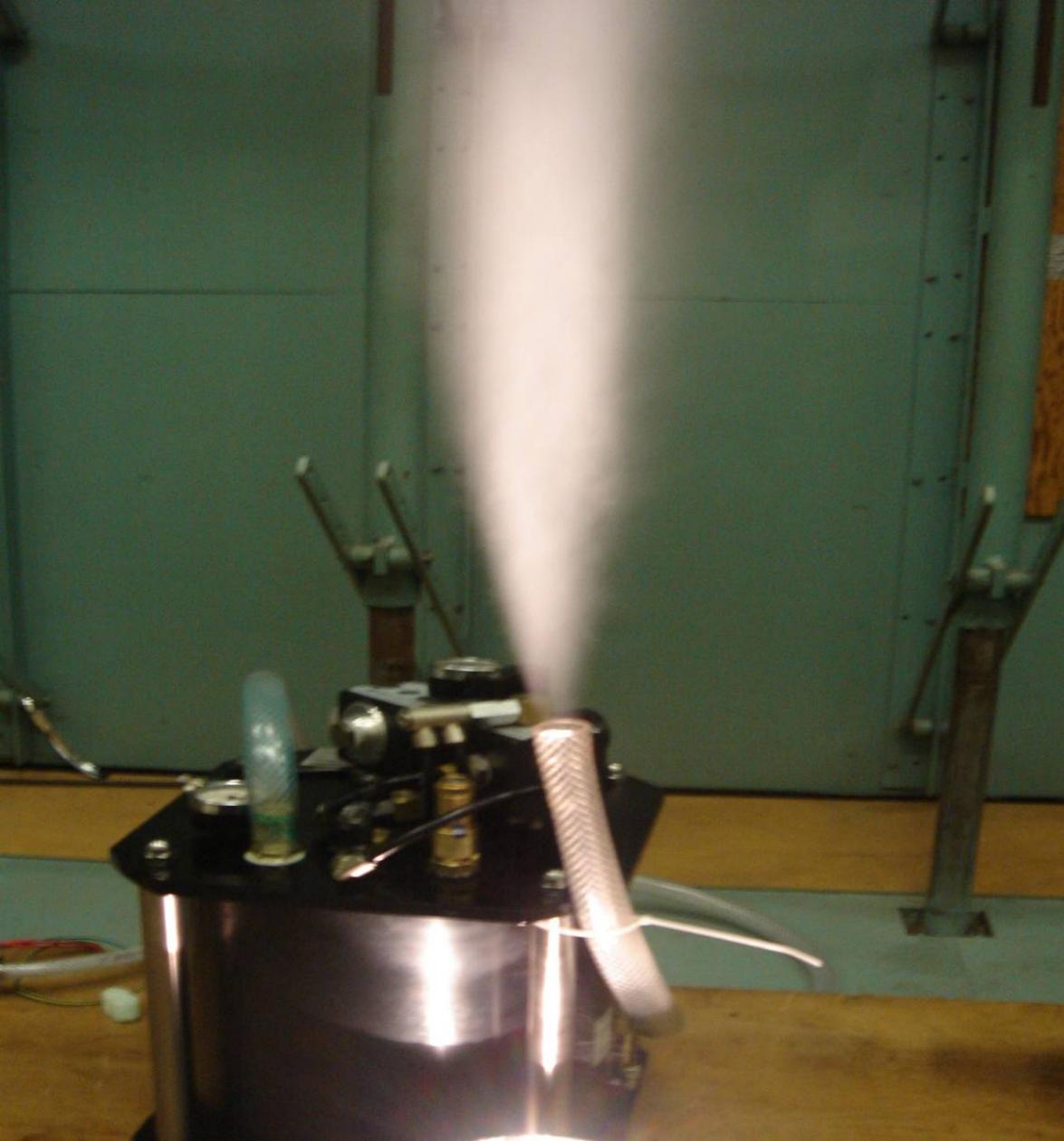
Top
View



Primary Standard. Differential LDV



Oil Seeding



Lasers & Seeding

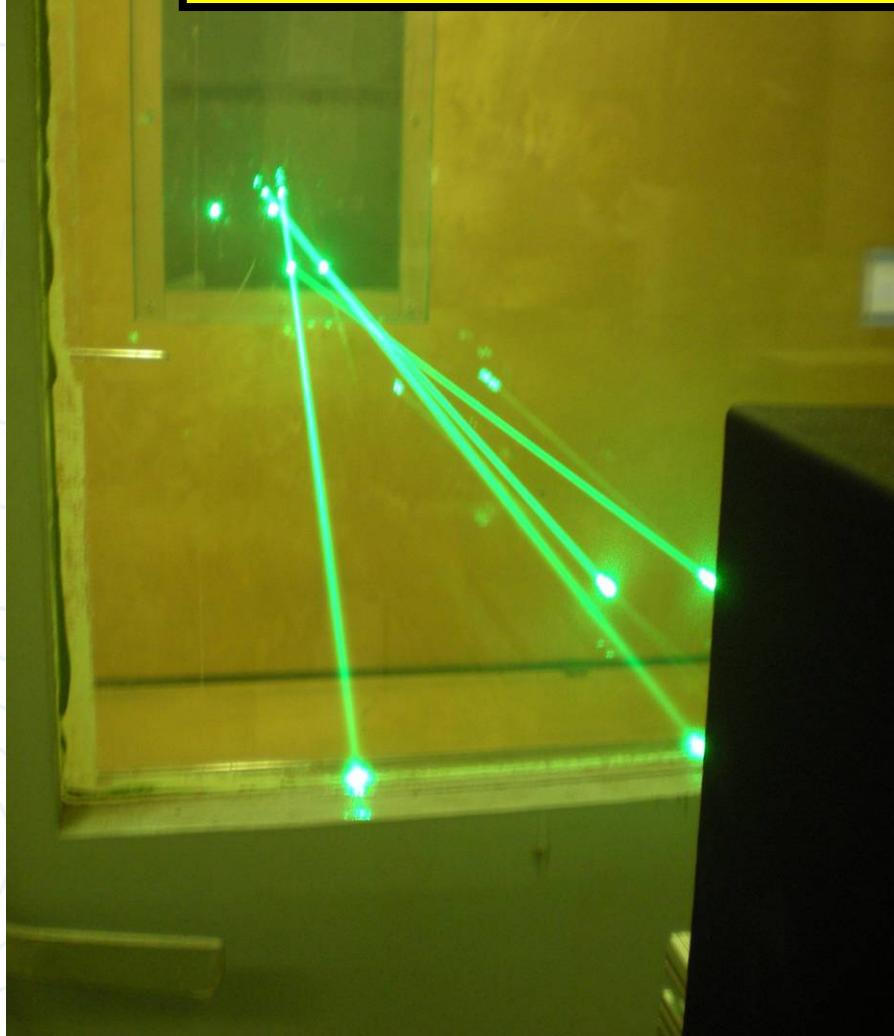
Oil Seeding

3 gm/hr

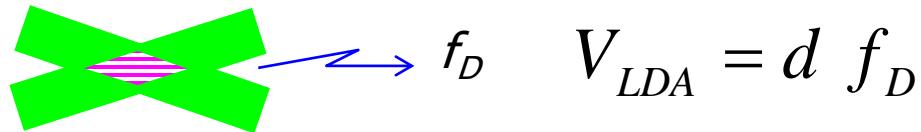
vs

Water Seeding

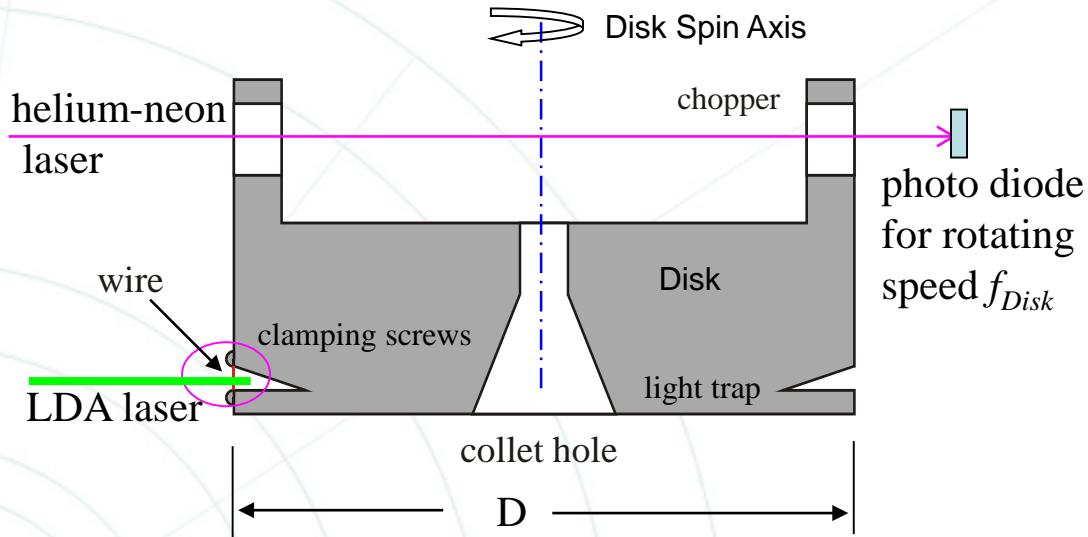
10000 gm/hr



Spinning disk



$$V_{Disk} = f_{Disk} \ D / 2$$



$$C_{LDA} = \frac{V_{Disk}}{V_{LDA}} = \frac{D}{2} \frac{f_{Disk}}{f_D^C d}$$

$$V_{NIST} = C_{LDA} \ V_{LDA} = \frac{D}{2} f_{Disk} \frac{f_D}{f_D^C}$$

Length D and Time f_{Disk}

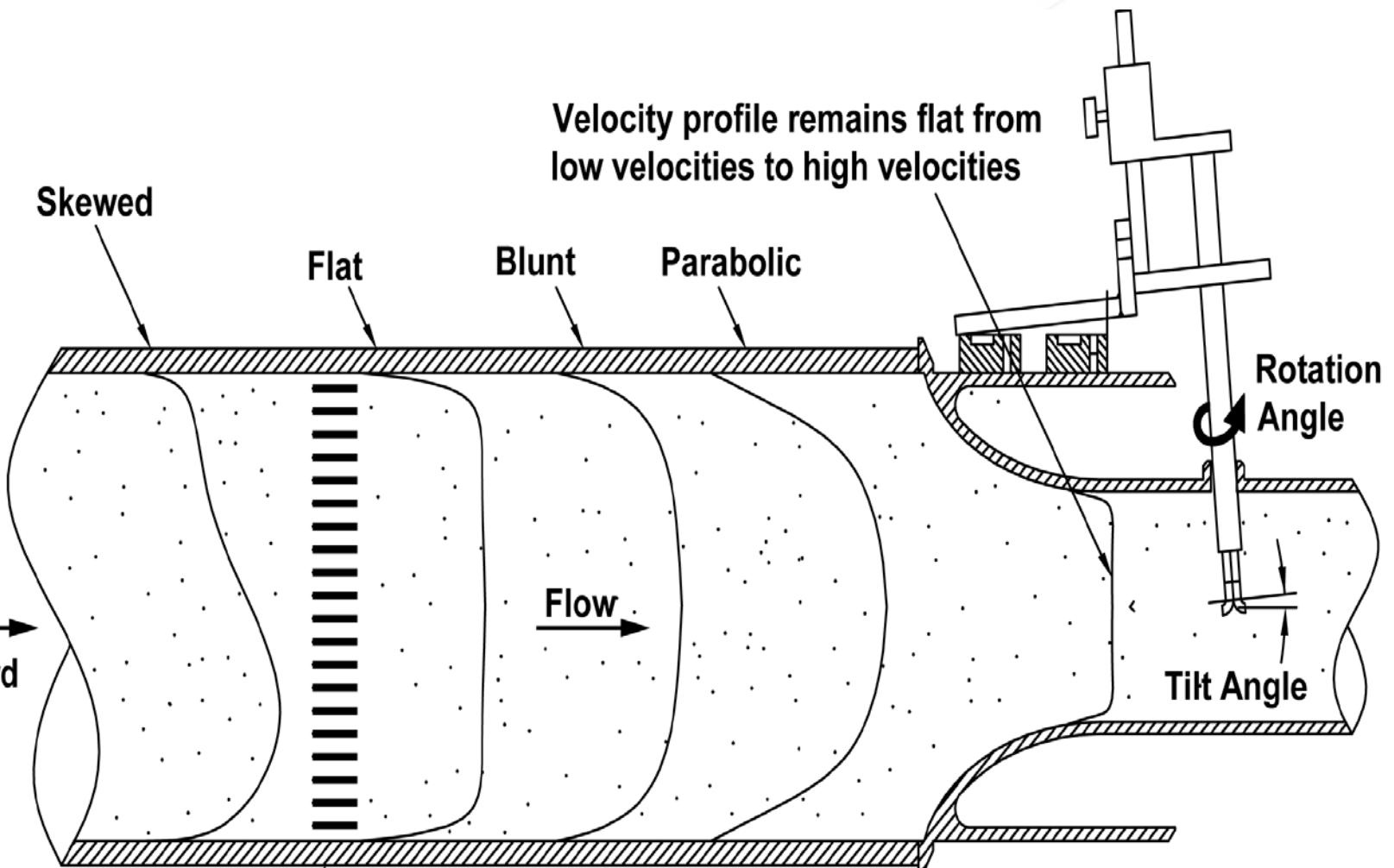
NIST Wind Tunnel Capabilities



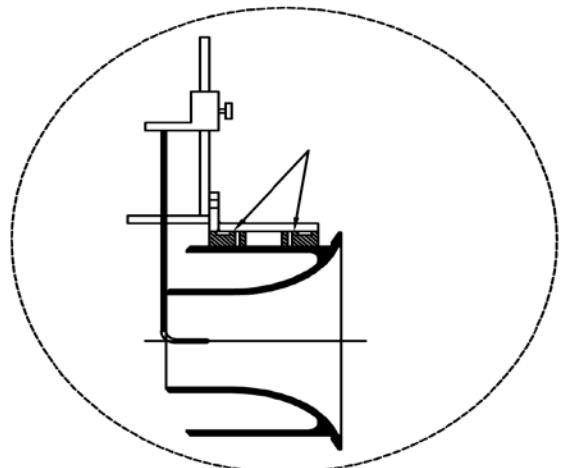
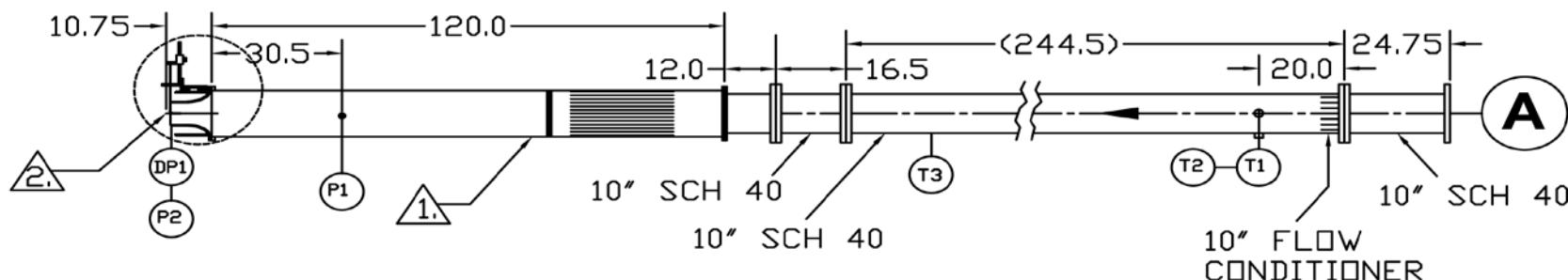
- Two test sections:
- High speed: to 75 m/s (246 ft/sec) 1.2 m high
- Low speed: to 45 m/s (147 ft/sec) 2.1 m high
- Uncertainties – 0.25% increasing to 2% at low speeds

NASA's Requirements:
7.6 to 122 m/sec (25 to 400 FPS)

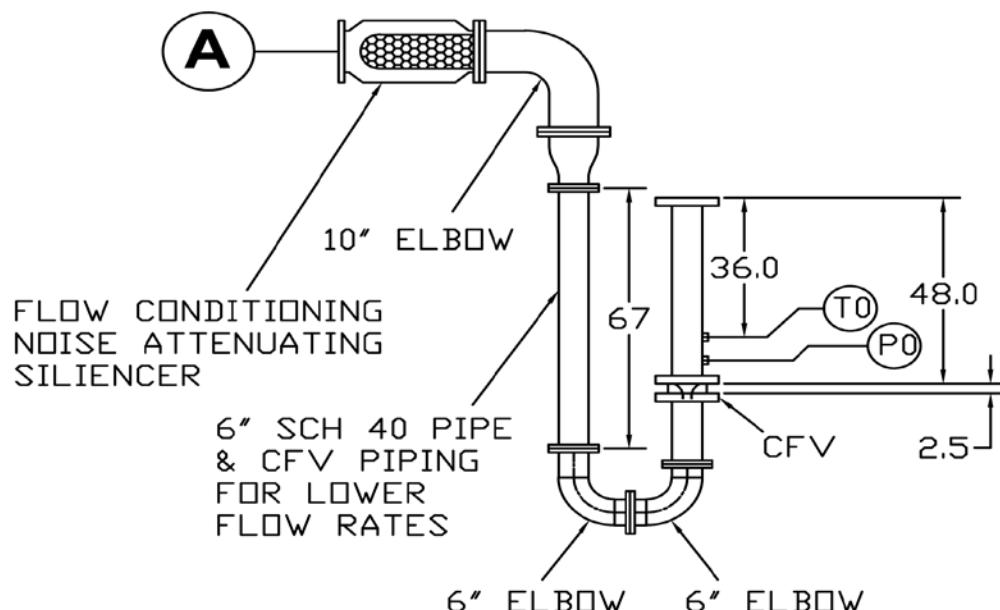
Alternate Point-Velocity Calibration Methodology



Test Configuration



4X MAGNIFICATION BUBBLE



NOTES:

1. 12" SCH 10S CONDITIONING SPOOL WITH TUBE BUNDLE & HONEYCOMB
2. FLOW CONDITIONING SUB-SONIC VENTURI
3. T3 INSERTED AT 0.5D FROM TOP, T2 INSERTED AT 0.25D FROM BOTTOM, T1 INSERTED AT 0.25D. P2 MEASURING STAGNATION PRESSURE, ON HIGH SIDE OF PITOT TUBE.

UNLESS OTHERWISE SPECIFIED
DIMENSIONS IN INCHES
TOLERANCES:
FRACTIONAL: $\pm 1/32"$
ANGULAR: $\pm 1^{\circ}$
1-PLACE DECIMAL: ± 0.03
2-PLACE DECIMAL: ± 0.01
3-PLACE DECIMAL: ± 0.005



Piping Configuration for Point-Velocity Calibration

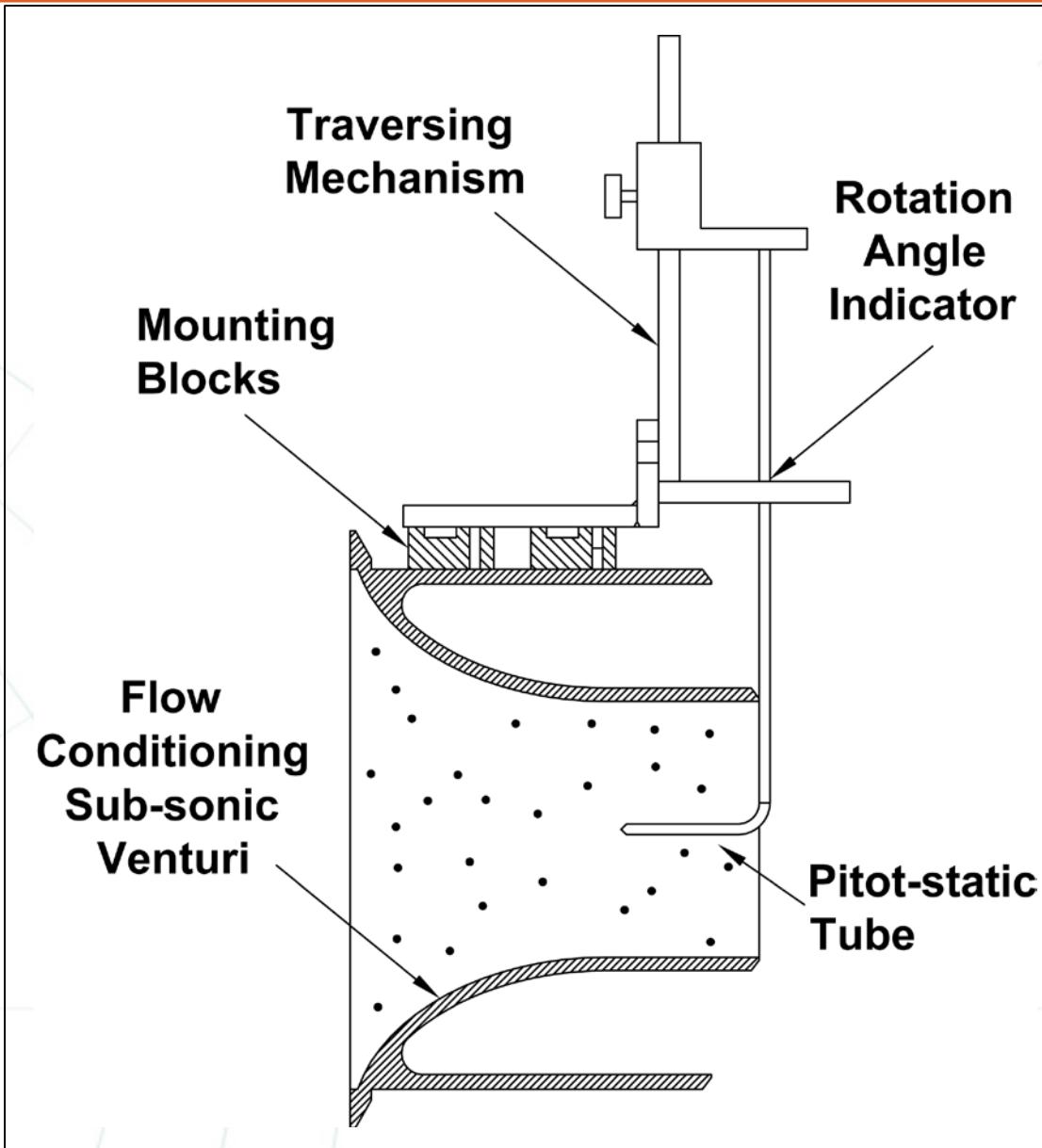
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The Hardware



The Hardware



Step-by-step Alternate Methodology



1. Determine the mass flowrate (\dot{m}) from an upstream NIST traceable flow standard.
2. Determine the gas density (ρ) at the calibration location from temperature and pressure measurements.
3. Divide the mass flowrate by the gas density and the throat area (A_{throat}) of the sub-sonic venturi to determine the bulk (average) velocity in the calibration location.

$$V_{Average} = \frac{\dot{m}}{\rho \cdot A_{throat}}$$

4. Correct the average velocity by the projected area of the Pitot-static tube. Note, this does not include the Pitot-static's stem area.

$$V_{Ave-corrected} = V_{Average} \cdot \frac{A_{throat}}{(A_{throat} - A_{Pitot})}$$

5. Using an uncalibrated Pitot-static tube, perform a pitot traverse at the calibrating velocity ranges, while monitoring the flow standard. Apply the equation below to determine individual velocities at each traverse location. If slight variations occur in the flowrate during the pitot traverse, the velocities can be normalized by multiplying by the average mass flow rate during the testing, and by dividing the mass flowrate during the individual traverse point as shown below.

$$V_i = N \cdot K_{initial} \sqrt{\frac{h_{w-i}}{\rho_i}} \left(\frac{\dot{m}_{average}}{\dot{m}_i} \right)$$

6. Determine a Profile Factor (PF) that relates the average velocity in the throat of the sub-sonic venturi to the velocity in the center. Notice how the initial Pitot-static flow coefficient ($K_{initial}$) drops out of the equation.

$$PF = \frac{\frac{N \cdot K_{initial} \sqrt{\frac{h_{W-center}}{\rho_{center}}} \left(\frac{\dot{m}_{average}}{\dot{m}_{center}} \right)}{\sum \left[\sqrt{\frac{h_{W-i}}{\rho_i}} \left(\frac{\dot{m}_{average}}{\dot{m}_i} \right) \right]}}{N \cdot K_{initial} \frac{n}{n}} = \frac{\sqrt{\frac{h_{W-center}}{\rho_{center}} \left(\frac{\dot{m}_{average}}{\dot{m}_{center}} \right)}}{\sum \left[\sqrt{\frac{h_{W-i}}{\rho_i}} \left(\frac{\dot{m}_{average}}{\dot{m}_i} \right) \right]}$$

7. Profile Factors (PF) can be calculated for different velocities, and curve fit to different Throat Reynolds Numbers.

$$PF = f(Re_{throat})$$

8. The Point Velocity Device can be inserted into the center of the sub-sonic venturi, and its flow coefficient can be determined by the following equation.

$$K = \frac{PF}{N \cdot (A_{throat} - A_{Pitot})} \cdot \frac{\dot{m}}{\sqrt{\rho \cdot h_w}}$$

- Three Pitot-static tubes were tested using the Alternative Methodology.
- The Pitot-static tubes were positioned in the center of the nozzle, and tested from 10 to 115 m/sec.
- The percent deviation between the experimentally determined flow coefficients (K) and theory was determined where:

$$K_{theory} = \left\{ \left(\frac{\gamma}{\gamma - 1} \right) \left(\frac{P_1}{P_t - P_1} \right) \left[\left(\frac{P_t}{P_1} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right] \right\}^{\frac{1}{2}}$$

Experimental K-factors vs. Theory



Summary of the Percent Deviation between Experimentally determined Flow Coefficients and Theroetical Flow Coefficients

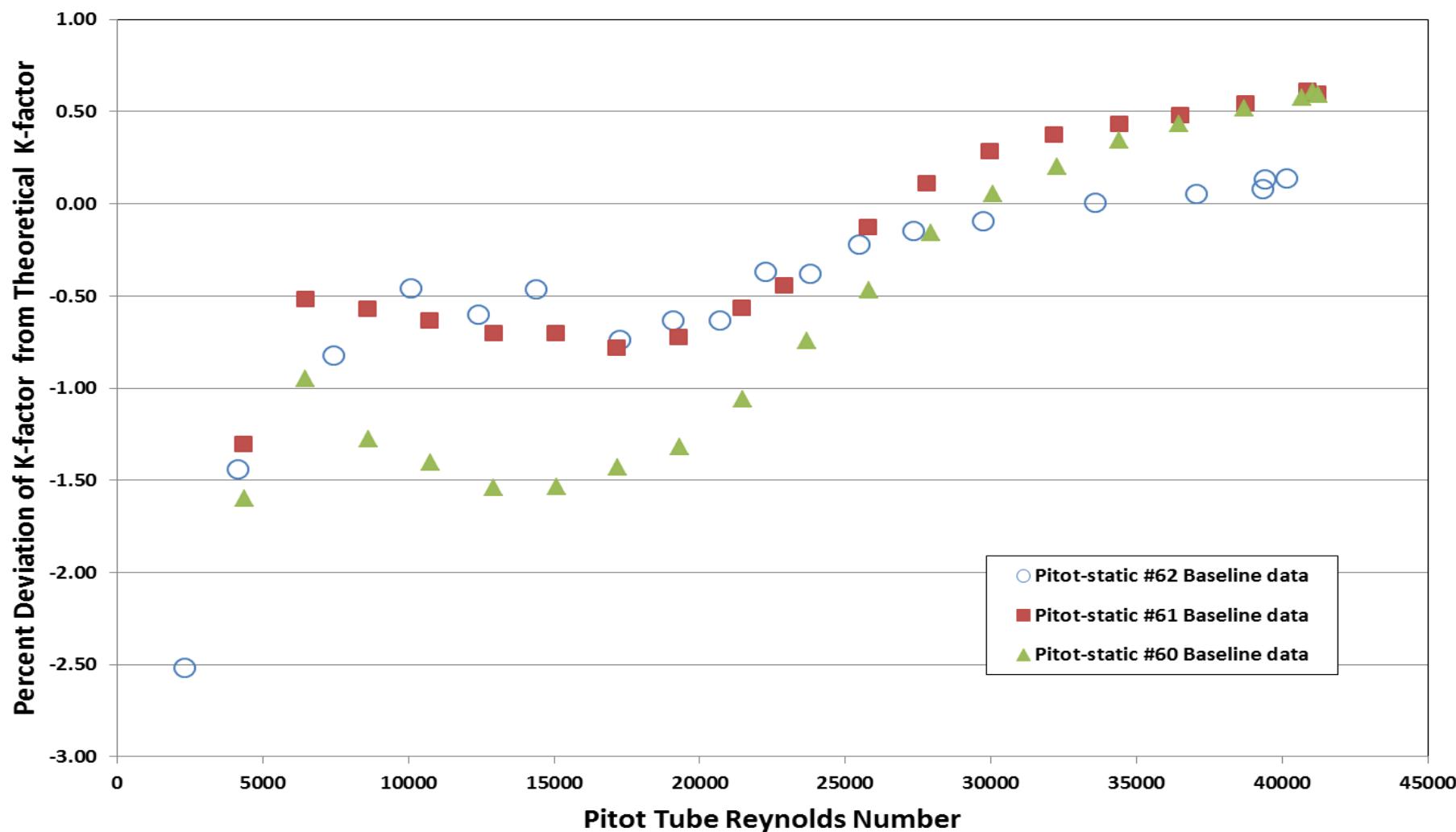
Pitot-static Tube No.	Perent Average Deviation*	Percent Standard Deviation*
#60	-0.5	0.84
#61	-0.2	0.58
#62	-0.5	0.62
Averages:	<hr/> -0.4	<hr/> 0.7

* Over the entire velocity range tested

K-factor vs. Pitot Tube Reynolds Number

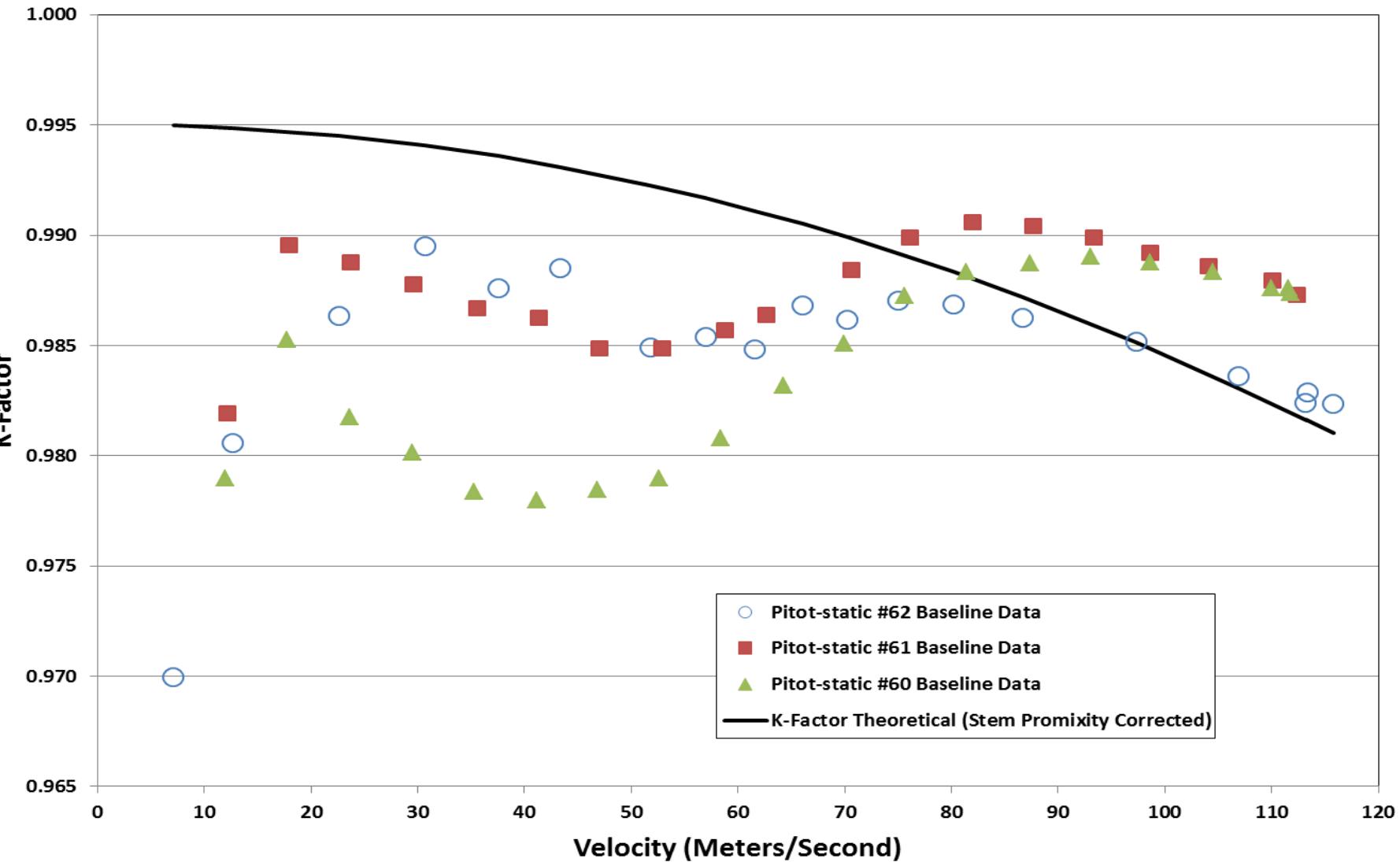


Three Hemispherical Pitot Tubes
Percent Deviation From Theoretical K-Factor (Stem Proximity Corrected)
vs. Pitot Tube Reynolds Number



K-Factor vs. Velocity

Three Hemispherical Pitot Tubes
K-Factor vs. Centerline Velocity



The following equation was used to determine the Pitot-static Tube's flow coefficient (K) uncertainty.

$$\frac{U_e(K)}{K} = \sqrt{\left[\left(\frac{\partial K}{\partial \dot{m}} \right) \frac{U(\dot{m})}{\dot{m}} \right]^2 + \left[\left(\frac{\partial K}{\partial V_{pf}} \right) \frac{U(V_{pf})}{V_{pf}} \right]^2 + \left[\left(\frac{\partial K}{\partial P_1} \right) \frac{U(P_1)}{P_1} \right]^2 + \left[\left(\frac{\partial K}{\partial T_1} \right) \frac{U(T_1)}{T_1} \right]^2 + \left[\left(\frac{\partial K}{\partial h_w} \right) \frac{U(h_w)}{h_w} \right]^2}$$

Where:

\dot{m} =mass flow rate from the Critical Flow Venturi, pounds-mass/sec

V_{pf} = Velocity profile factor in the sub-sonic venturi

P_1 = Static pressure in the sub-sonic venturi, psia

T_1 = Absolute sub-sonic venturi temperature, °R

h_w = Differential pressure produced by the Pitot-static tube, "H₂O

Applying the appropriate sensitivity coefficients the equation above yields.

$$\frac{U_e(K)}{K} = \sqrt{\left[\frac{U(\dot{m})}{\dot{m}}\right]^2 + \left[\frac{U(V_{pf})}{V_{pf}}\right]^2 + \left[\frac{1}{2} \frac{U(P_1)}{P_1}\right]^2 + \left[\frac{1}{2} \frac{U(T_1)}{T_1}\right]^2 + \left[\frac{1}{2} \frac{U(h_w)}{h_w}\right]^2}$$

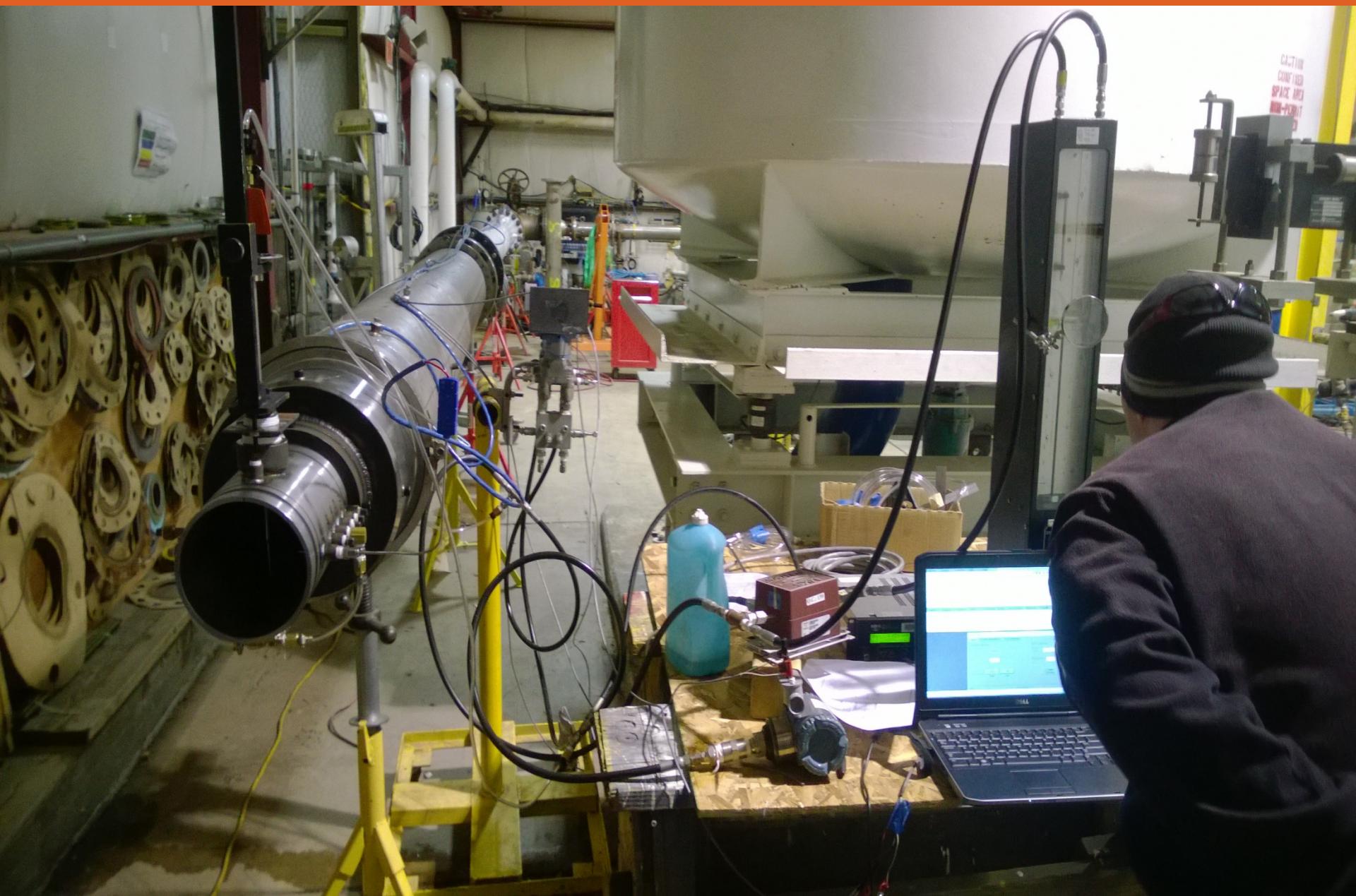
Applying the test uncertainties the equation above yields.

$$\frac{U_e(K)}{K} = \sqrt{[0.35]^2 + [0.1]^2 + \left[\frac{1}{2} \cdot 0.1\right]^2 + \left[\frac{1}{2} \cdot 0.1\right]^2 + \left[\frac{1}{2} \cdot 1.0\right]^2} = 0.62\%$$

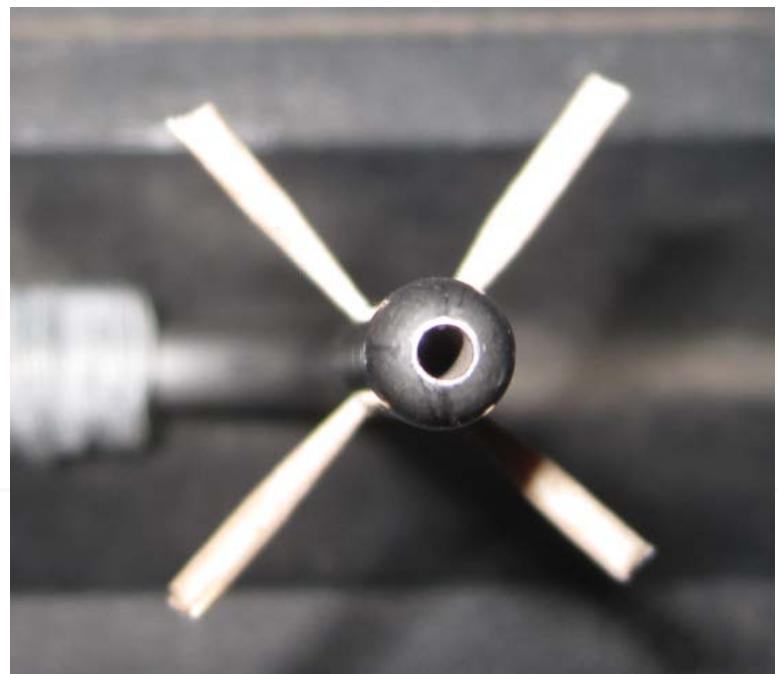
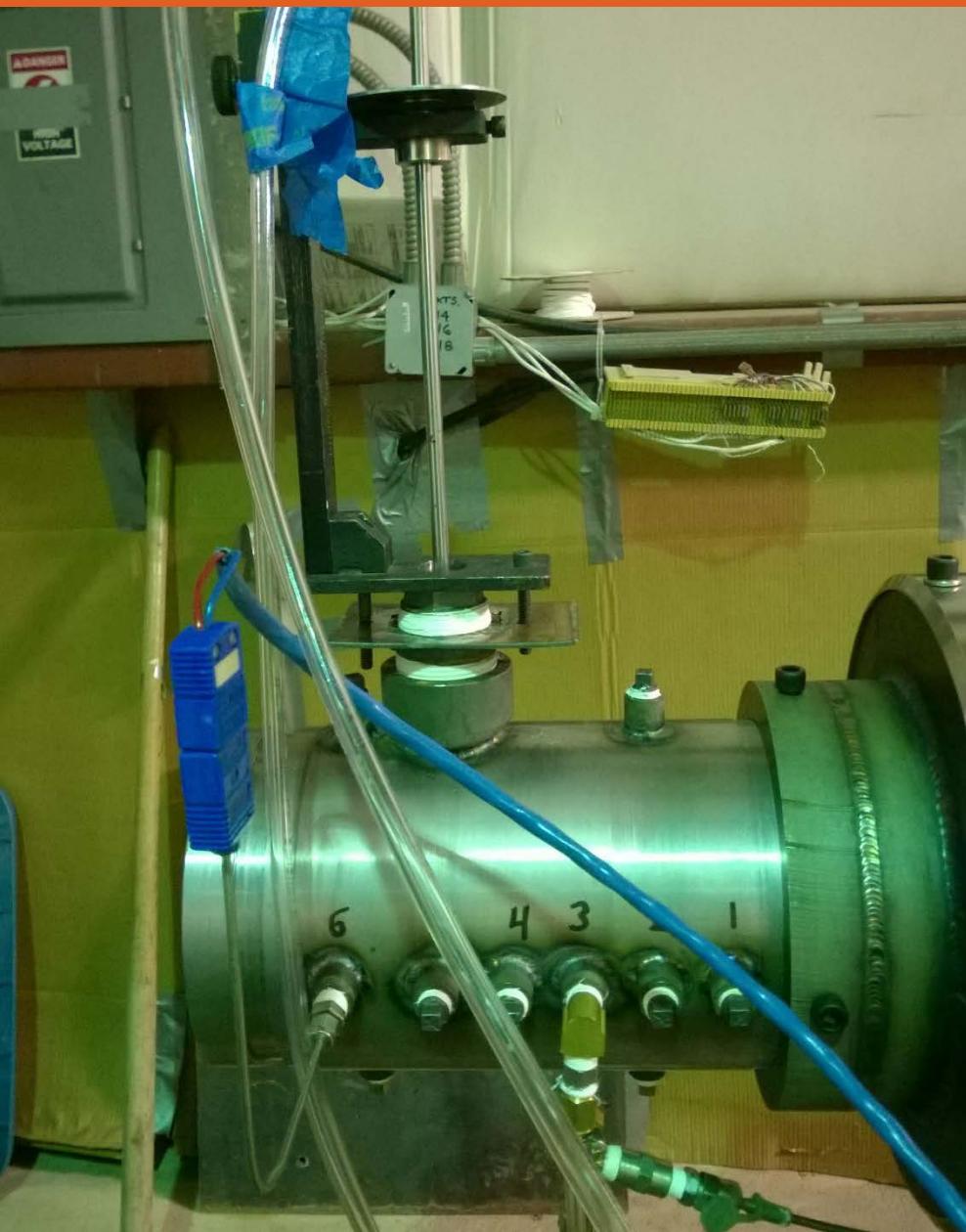
The expanded uncertainty of the Pitot-static flow coefficient (K) at two-sigma is 1.24%

- Individual averages of all three experimentally determined flow coefficients were within the estimated uncertainty of 0.62% at one sigma of the theoretically calculated flow coefficient.
- Flow coefficient deviations were likely a result of imperfections in the Pitot-static tube's surfaces and geometry, and the turbulence levels during testing.
- Better uncertainty could be achieved using more accurate DP transducers which contributed greatly to the uncertainty budget.
- $\pm 0.5\%$ DP transducers would have produced a 0.9 % uncertainty at two sigma.

Similar Testing (Added a Throat Extension)



Extended Throat & Close-up of Pitot Tubes



Checking For Leaks

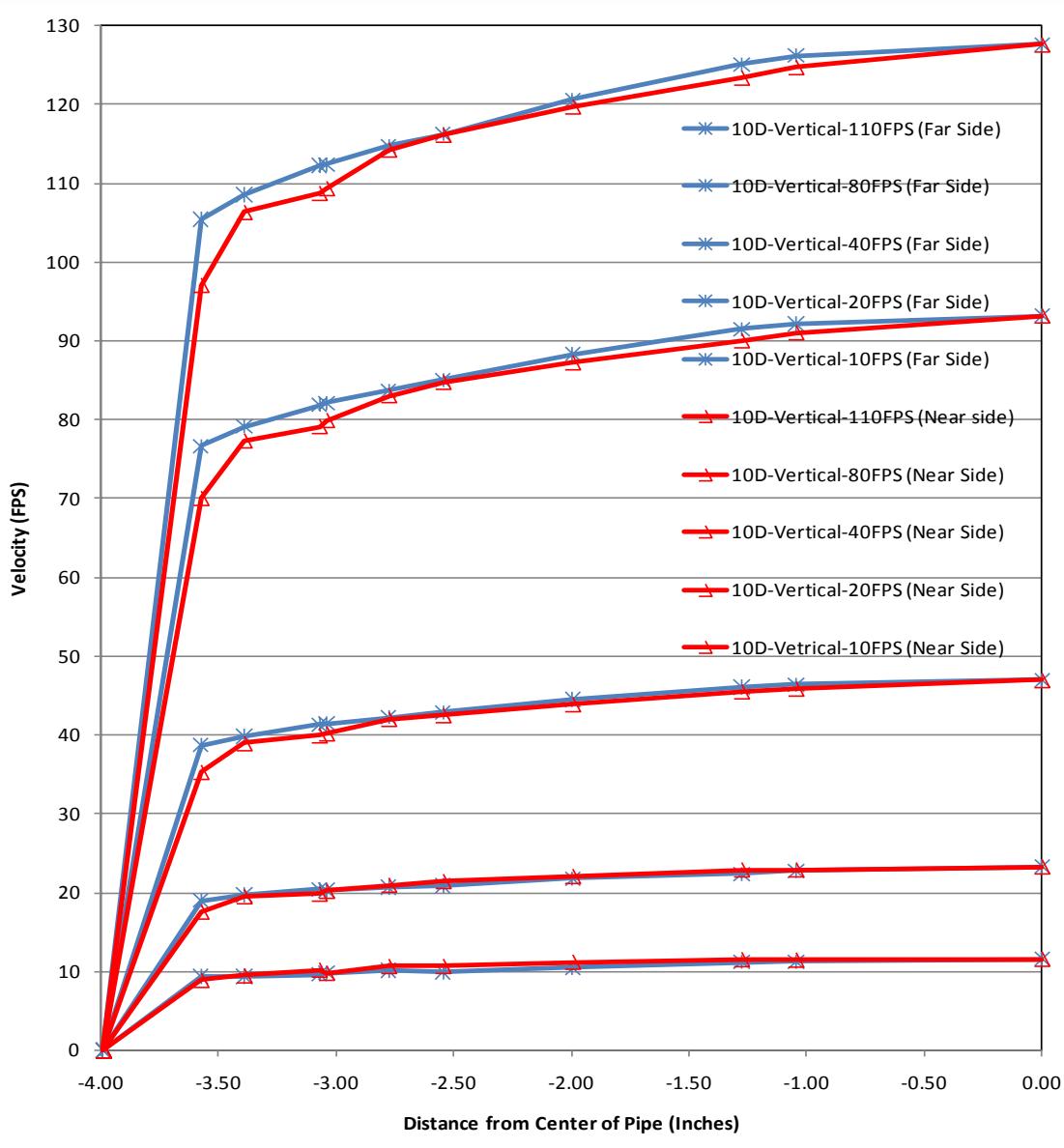


Checking For Leaks

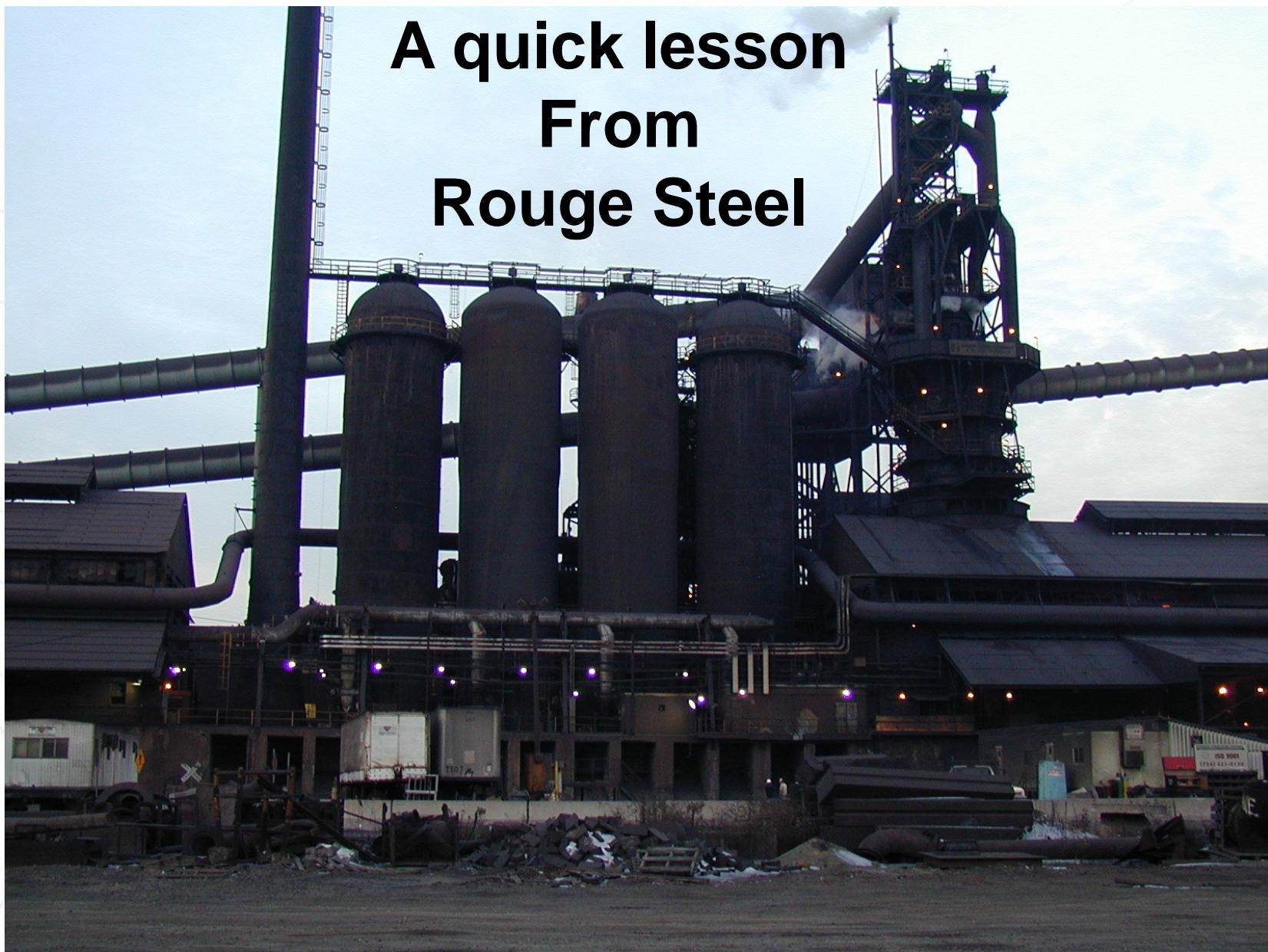


Eureka A Leak !

Don't Forget about Blockage



A quick lesson From Rouge Steel



Flare Gas



Stack Flow Measurement



Stack Flow Measurement

OOPS!



Stack Flow Measurement



Questions?



CEESI
54043 WCR 37
Nunn, CO 80648

Eric Harman
eharman@ceesi.com
970-897-2711 work
303-638-1384 cell

