

ES155 P7

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Problem 3

3.a

```
P = tf(1, [1 10 3 10])
S = 1000 * tf([1 1], [1 10])

L = P*S

figure(1); clf;
subplot(1,2,1)
bode(L)
subplot(1,2,2)
nyquist(L)

saveas(gcf, "ES155P7_3a.jpg")

pole(L)
[GainMargin, PhaseMargin, Wcg, Wcp] = margin(L)
```

P =

$$\frac{1}{s^3 + 10s^2 + 3s + 10}$$

Continuous-time transfer function.

S =

$$\frac{1000s + 1000}{s + 10}$$

Continuous-time transfer function.

L =

$$\frac{1000s + 1000}{s^4 + 20s^3 + 103s^2 + 40s + 100}$$

Continuous-time transfer function.

ans =

```
-10.0000 + 0.0000i
-9.7980 + 0.0000i
-0.1010 + 1.0052i
-0.1010 - 1.0052i
```

GainMargin =

```
1.6047
```

PhaseMargin =

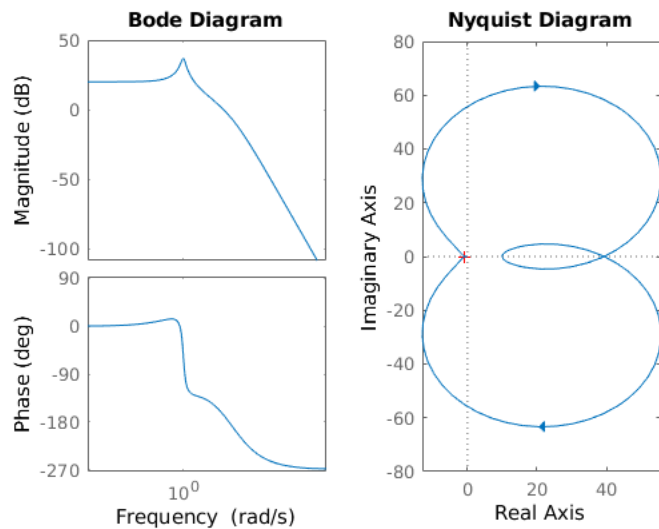
```
12.9616
```

Wcg =

```
9.0682
```

Wcp =

```
7.0090
```



3.b

```
P = tf(100, [100, 101, 1])
S = tf([1 10], 1)

L = P*S

figure(2); clf;
subplot(1,2,1)
bode(L)
subplot(1,2,2)
nyquist(L)

saveas(gcf, "ES155P7_3b.jpg")

pole(L)
[GainMargin, PhaseMargin, Wcg, Wcp] = margin(L)
```

```
P =
      100
-----
100 s^2 + 101 s + 1
Continuous-time transfer function.
```

```
S =
      s + 10
Continuous-time transfer function.
```

```
L =
      100 s + 1000
-----
100 s^2 + 101 s + 1
Continuous-time transfer function.
```

```
ans =
-1.0000
-0.0100
```

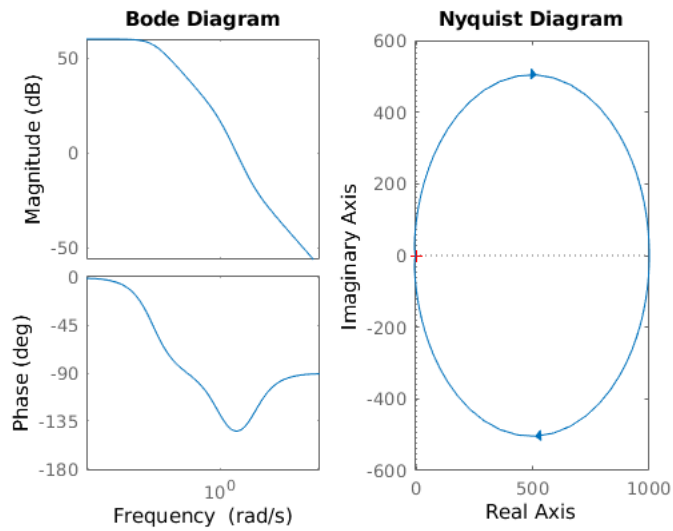
```
GainMargin =
Inf
```

```
PhaseMargin =
35.2780
```

```
Wcg =
NaN
```

Wcp =

3.1623



Problem 4

```
% Constants
a = 0.2
b = 25
c = 50
T = 200
m = 1000

P = tf(T*b*a, [m, a*m + c, a*c])
```

```
a =
    0.2000

b =
    25

c =
    50

T =
    200

m =
    1000

P =
    1000
-----
 1000 s^2 + 250 s + 10

Continuous-time transfer function.
```

4.a

```
table = zeros(4,8);

figure(3); clf;
figure(4); clf;

Kp = [0.5, 0.05, 0.05, 0.005]
```

```

Ki = [0.1, 1, 0.001, 0.001]

for i = 1:4
    figure(3)
    kp = Kp(i)
    ki = Ki(i)

    table(i,1) = kp;
    table(i,2) = ki;

    C = tf([kp, ki], 1)
    G = feedback(P*C, 1)

    L = P*C
    sysL = ss(L)

    sys = ss(G);

    table(i,3) = isstable(sys);

    [GainMargin, PhaseMargin, Wcg, Wcp] = margin(sysL)

    table(i,4) = GainMargin;
    table(i,5) = PhaseMargin;

    [y, t] = step(sys);
    if y(length(t)) == y(length(t-2))
        error_SS = 1 - y(length(t))
    else
        error("Steady State not reached")
    end

    table(i,6) = error_SS;

    S = stepinfo(sys)

    table(i,7) = S.RiseTime;
    table(i,8) = S.Overshoot;

    subplot(2,4,i)
    pzmap(sys)

    subplot(2,4,i+4)
    step(sys, S.RiseTime*10)

    figure(4)
    subplot(2,4,i)
    bode(sys)
    subplot(2,4,i+4)
    nyquist(sys)

    % plot the unit circle on the nyquist plot
    theta = 0:0.1:2*pi;
    x = cos(theta);
    y = sin(theta);
    hold on;
    plot(x,y,'-');
    hold off;
end

table

```

```

Kp =

    0.5000    0.0500    0.0500    0.0050

```

```

Ki =

    0.1000    1.0000    0.0010    0.0010

```

```

kp =

    0.5000

```

```

ki =

    0.1000

```

```

C =

    0.5 s + 0.1

```

Continuous-time transfer function.

```

G =

```

$$\frac{500 s + 100}{1000 s^2 + 750 s + 110}$$

Continuous-time transfer function.

L =

$$\frac{500 s + 100}{1000 s^2 + 250 s + 10}$$

Continuous-time transfer function.

sysL =

$$A = \begin{bmatrix} & x1 & x2 \\ x1 & -0.25 & -0.08 \\ x2 & 0.125 & 0 \end{bmatrix}$$

B =

$$\begin{bmatrix} u1 \\ x1 & 1 \\ x2 & 0 \end{bmatrix}$$

C =

$$\begin{bmatrix} x1 & x2 \\ y1 & 0.5 & 0.8 \end{bmatrix}$$

D =

$$\begin{bmatrix} u1 \\ y1 & 0 \end{bmatrix}$$

Continuous-time state-space model.

GainMargin =

Inf

PhaseMargin =

95.7406

Wcg =

NaN

Wcp =

0.4974

error_SS =

0.0910

S =

struct with fields:

```
RiseTime: 3.9946
SettlingTime: 7.1129
SettlingMin: 0.8223
SettlingMax: 0.9091
Overshoot: 0
Undershoot: 0
Peak: 0.9091
PeakTime: 19.1743
```

kp =

0.0500

ki =

1

C =

0.05 s + 1

Continuous-time transfer function.

G =

$$\frac{50 s + 1000}{1000 s^2 + 300 s + 1010}$$

Continuous-time transfer function.

L =

$$\frac{50 s + 1000}{1000 s^2 + 250 s + 10}$$

Continuous-time transfer function.

sysL =

$$A = \begin{array}{cc} & \begin{array}{c} x1 \quad x2 \end{array} \\ \begin{array}{c} x1 \\ x2 \end{array} & \begin{bmatrix} -0.25 & -0.08 \\ 0.125 & 0 \end{bmatrix} \end{array}$$

B =

$$\begin{array}{c} u1 \\ \begin{array}{c} x1 \quad x2 \end{array} \end{array} \begin{bmatrix} 4 \\ 0 \end{bmatrix}$$

C =

$$\begin{array}{cc} & \begin{array}{c} x1 \quad x2 \end{array} \\ \begin{array}{c} y1 \end{array} & \begin{bmatrix} 0.0125 & 2 \end{bmatrix} \end{array}$$

D =

$$\begin{array}{c} u1 \\ \begin{array}{c} y1 \end{array} \end{array} \begin{bmatrix} 0 \end{bmatrix}$$

Continuous-time state-space model.

GainMargin =

Inf

PhaseMargin =

17.1460

Wcg =

NaN

Wcp =

0.9900

error_SS =

0.0047

S =

struct with fields:

```
RiseTime: 1.1611
SettlingTime: 25.7136
SettlingMin: 0.6095
SettlingMax: 1.6066
Overshoot: 62.2638
Undershoot: 0
Peak: 1.6066
PeakTime: 3.0701
```

kp =

0.0500

ki =

1.0000e-03

C =

0.05 s + 0.001

Continuous-time transfer function.

G =

$$\frac{50 s + 1}{1000 s^2 + 300 s + 11}$$

Continuous-time transfer function.

L =

$$\frac{50 s + 1}{1000 s^2 + 250 s + 10}$$

Continuous-time transfer function.

sysL =

A =

	x1	x2
x1	-0.25	-0.08
x2	0.125	0

B =

	u1
x1	0.25
x2	0

C =

	x1	x2
y1	0.2	0.032

D =

	u1
y1	0

Continuous-time state-space model.

GainMargin =

Inf

PhaseMargin =

Inf

Wcg =

NaN

Wcp =

NaN

error_SS =

0.9089

S =

struct with fields:

RiseTime: 2.0130
 SettlingTime: 98.7607
 SettlingMin: 0.0896
 SettlingMax: 0.1557
 Overshoot: 71.3097
 Undershoot: 0
 Peak: 0.1557
 PeakTime: 11.0995

```
kp =
    0.0050
```

```
ki =
    1.0000e-03
```

```
C =
    0.005 s + 0.001
```

Continuous-time transfer function.

```
G =
    5 s + 1
    -----
    1000 s^2 + 255 s + 11
```

Continuous-time transfer function.

```
L =
    5 s + 1
    -----
    1000 s^2 + 250 s + 10
```

Continuous-time transfer function.

```
sysL =
A =
      x1      x2
x1  -0.25  -0.08
x2   0.125    0
```

```
B =
      u1
x1   0.125
x2    0
```

```
C =
      x1      x2
y1   0.04   0.064
```

```
D =
      u1
y1    0
```

Continuous-time state-space model.

```
GainMargin =
    Inf
```

```
PhaseMargin =
    Inf
```

```
Wcg =
    NaN
```

```
Wcp =
    NaN
```

```
error_SS =
    0.9091
```

```
S =
struct with fields:
    RiseTime: 39.9456
    SettlingTime: 71.1286
    SettlingMin: 0.0822
    SettlingMax: 0.0909
```


Overshoot: 0
Undershoot: 0
Peak: 0.0909
PeakTime: 191.7425

table =

Columns 1 through 7

0.5000	0.1000	1.0000	Inf	95.7406	0.0910	3.9946
0.0500	1.0000	1.0000	Inf	17.1460	0.0047	1.1611
0.0500	0.0010	1.0000	Inf	Inf	0.9089	2.0130
0.0050	0.0010	1.0000	Inf	Inf	0.9091	39.9456

Column 8

0
62.2638
71.3097
0

