



Data Intensive Systems (DIS)

KBH-SW7 E25

9. Association Rules

A Real Application of Association Rules

- Amazon's recommendation
 - 90% buyers who bought A also bought B.
 - Since you've bought A, you may also want B.

Make recommendations based on rules of high support, confidence and lift.

Frequently Bought Together

Price for all three: **\$67.41**

[Add all three to Cart](#)

[Add all three to Wish List](#)

[Show availability and shipping details](#)


[Add to Wish List](#)

[Have one to sell?](#) [Sell on Amazon](#)

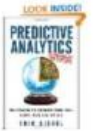
- ☒ **This item:** Big Data: A Revolution That Will Transform How We Live, Work, and Think by Viktor Mayer-Schönberger Paperback **\$10.61**
- ☒ **Data Science for Business: What you need to know about data mining and data-analytic thinking** by Foster Provost Paperback **\$37.99**
- ☒ **Predictive Analytics: The Power to Predict Who Will Click, Buy, Lie, or Die** by Eric Siegel Hardcover **\$18.81**

Customers Who Bought This Item Also Bought


Page




Data Science for Business:
What you need...
by Foster Provost
★★★★☆ 103
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★★★★☆ 235
Hardcover
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Big Data: Understanding How Data Powers Big...
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Paperback
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Big Data For Dummies
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★★★★☆ 31
Paperback
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Digital Sociology
by Deborah Lupton
Paperback
\$46.95 ✓Prime



Big Data: Using SMART Big Data, Analytics...
by Bernard Marr
★★★★☆ 9
Paperback
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Agenda

- Problem definition
 - Support, confidence, lift, and association rule
 - Frequent itemsets
 - Steps for association rule mining
- Apriori principle, Apriori algorithm
- Deriving association rules from frequent itemsets
- Reflection on Apriori algorithm

Market Basket Data

- ▶ Large set of *items*, i.e., things sold in a supermarket
- ▶ Large set of *baskets*, each a small subset of items, i.e., things that one customer buys in one **transaction**
- ▶ Transaction table **T**: market-basket data
 - ▶ Each record is a transaction, containing a set of items
 - ▶ Many-to-many mapping (association) between items and baskets
- ▶ What can we do with this type of data?
 - ▶ E.g., counting whether the combination {Milk, Bread} is **frequent** or not

TID	Items
1	{Milk, Bread, Beer, Diapers}
2	{Bread, Eggs}
3	{Bread, Diapers}
4	{Milk, Bread, Cola}
5	{Milk, Bread, Diapers}

Transaction table

What Is Association Rule Mining?

- ▶ Finding **frequent patterns** and **associations** (rules) among sets of items in a transaction table
- ▶ Motivation (market basket analysis):
 - ▶ How likely is that the customers buying *milk* are also buying *bread*?
 - ▶ Such rules help retailers making decisions
 - › Plan the shelf space: placing milk close to bread, more convenient for the customers
 - › Offer promotions/discounts for those products together

What Is an Association Rule?

- An **association rule** correlates (associates) the presence of one set of items with that of another set of items
- Examples
 - Rule form: **Body** \Rightarrow **Head** [support, confidence]
 - milk \Rightarrow bread [5%, 70%]
 - › 5% of transactions buy both milk and bread
 - › transactions that buy milk have 70% chance of buying also bread
- Applications: basket data analysis, catalog design
 - * \Rightarrow **chocolate** (How to boost the sales of chocolate)
 - **Home Electronics** \Rightarrow * (What other products should the store stock up?)

Rule Components

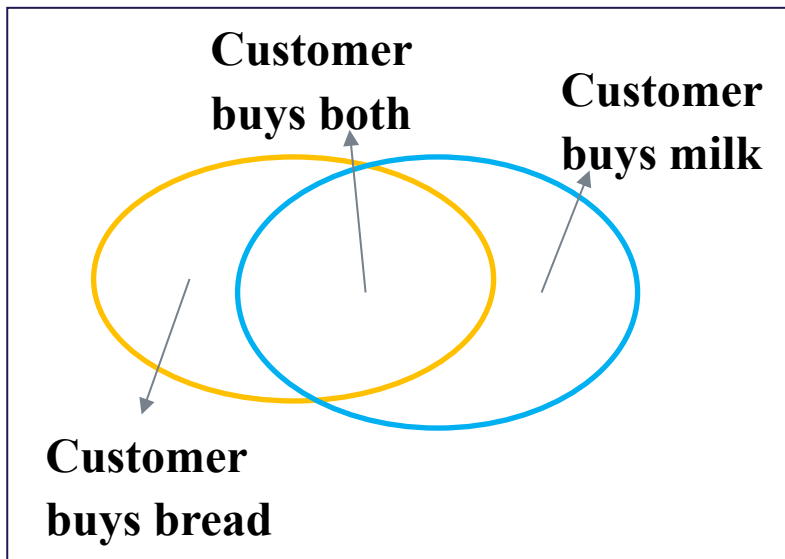
- ▶ An **itemset** means a set of items
 - ▶ E.g., {a, b, c}
- ▶ Let T be a collection of transactions
 - ▶ E.g., $T = \{\text{TID 1, TID 2, TID 3, TID 4}\}$
- ▶ Let I be the set of items that appear in the database, e.g., $I = \{a, b, c, g, e, f\}$
- ▶ A rule is defined by $X \Rightarrow Y$, where $X \subset I$, $Y \subset I$, and $X \cap Y = \emptyset$
 - ▶ E.g., $\{b, c\} \Rightarrow \{e\}$ is a rule. We may simplify it as $bc \Rightarrow e$ if the context is clear.
 - ▶ E.g., $\{b, c\} \Rightarrow \{c, e\}$ is not a rule

TID	Items
1	a,b,c
2	a,c
3	a,g
4	b,e,f

Interesting Rules

- ▶ A rule is said to be **interesting** (or valid) when:
 - ▶ Its items appear frequently in the transaction table (**support**)
 - ▶ It holds with a high probability (**confidence**)

Example: $milk \Rightarrow bread$



NB: X and Y are itemsets.

Find all the rules $X \Rightarrow Y$ with confidence and support above given thresholds

- **support s** , probability that a transaction contains $X \cup Y$
- **confidence c** , conditional probability that a transaction having X also contains Y

Example (1)

► Find the **support** and **confidence** of the rule: $\{B,D\} \Rightarrow \{A\}$

► Support value of $sup(ABD)$:

- percentage of tuples with $\{A,B,D\}$
 $= (3/4) * 100\% = 75\%$

TID	items bought
100	{F,A,D,B}
200	{D,A,C,E,B}
300	{C,A,B,E}
400	{B,A,D}

► Confidence value of $conf(BD \Rightarrow A)$

$$\frac{\text{number of transactions that contain } \{A, B, D\}}{\text{number of transactions that contain } \{B, D\}} = \frac{3}{3} = 100\%$$

$$\begin{aligned} \text{prob}(Y | X) &= \frac{\text{prob}(X \cup Y)}{\text{prob}(X)} \\ \text{conf}(X \Rightarrow Y) &= \frac{\text{sup}(X \cup Y)}{\text{sup}(X)} = \frac{\text{frequency}(X \cup Y)}{\text{frequency}(X)} \end{aligned}$$

Example (1)

- Find interesting rules

Transaction ID	Items Bought
2000	A,B,C
1000	A,C
4000	A,D
5000	B,E,F

Thresholds:

Min. support 50%
Min. confidence 50%

Frequent Itemset	Support
{A}	75%
{B}	50%
{C}	50%
{A,C}	50%

“ $A \Rightarrow C$ ” is a valid rule because:

support = $\text{support}(\{A \cup C\}) = 2/4 = 50\%$

confidence = $\text{support}(\{A \cup C\}) / \text{support}(\{A\}) = 50\% / 75\% = 66.6\%$

Lift of A Rule

- ▶ **Lift**($X \Rightarrow Y$) = $\text{confidence}(X \Rightarrow Y) / \text{support}(Y)$
= $\text{support}(X \cup Y) / (\text{support}(X) * \text{support}(Y))$
= $(\text{frequency}(X \cup Y) * |T|) / (\text{frequency}(X) * \text{frequency}(Y))$
- ▶ **Lift**($X \Rightarrow Y$) refers to **the increase in the ratio of sale of Y when X is sold**
 - ▶ **Lift = 1**: No association between products X and Y.
 - ▶ **Lift > 1**: Products X and Y are more likely to be bought together.
 - ▶ **Lift < 1**: The two products are unlikely to be bought together.

Example of Lift

Transaction ID	Items Bought
2000	A,B,C
1000	A,C
4000	A,D
5000	B,E,F

Frequent Itemset	Support
{A}	75%
{B}	50%
{C}	50%
{A,C}	50%

Rule $A \Rightarrow C$:

support = $\text{support}(\{A \cup C\}) = 2/4 = 50\%$

confidence = $\text{support}(\{A \cup C\})/\text{support}(\{A\}) = 50\%/75\% = 66.6\%$

lift = $\text{confidence}(A \Rightarrow C)/\text{support}(C) = 66.6\%/50\% = 1.333$

Lift's meaning: the likelihood of buying a A and C *together* is 1.33 times more than the likelihood of just buying the C.

Recommendation in Amazon

- Two types of recommendation
 - 90% buyers who bought A also bought B.
 - Since you've bought A, you may also want B.

The screenshot displays the Amazon product page for the book 'Big Data: A Revolution That Will Transform How We Live, Work, and Think' by Viktor Mayer-Schönberger. The page features two main recommendation sections:

- Frequently Bought Together:** This section, highlighted with a red oval and a green box labeled 'Frequent itemset', shows three books: 'Big Data', 'Data Science for Business', and 'Predictive Analytics'. It includes buttons to 'Add all three to Cart' and 'Add all three to Wish List', along with a link to 'Show availability and shipping details'.
- Customers Who Bought This Item Also Bought:** This section, also highlighted with a red oval and a green box labeled 'Association rules', displays a grid of related books. Each book entry includes its title, author, star rating, number of reviews, and price. For example, 'Data Science for Business' is priced at \$37.99 and is marked as a '#1 Best Seller' in Database Storage & Design.

Additional UI elements visible on the page include an 'Add to Wish List' button, a 'Have one to sell?' link, and a 'Sell on Amazon' button.

Causality vs. Correlation

- Causality
 - From the very first day, humans are curious about *why*.
 - With big data, it may be very hard to see the exact reasons.
- Correlation
 - Instead, we can find interesting patterns or associations of different things from big data.
 - Probability instead of certainty (not totally random).
 - Association rule mining.
- **NB:** Association rules are empiricism! What they tell may not be the true cause and effect.

Steps of Association Rule Mining

1. Find the *frequent itemsets*

- ▶ The sets of items that have minimum support
- ▶ How to do this efficiently?

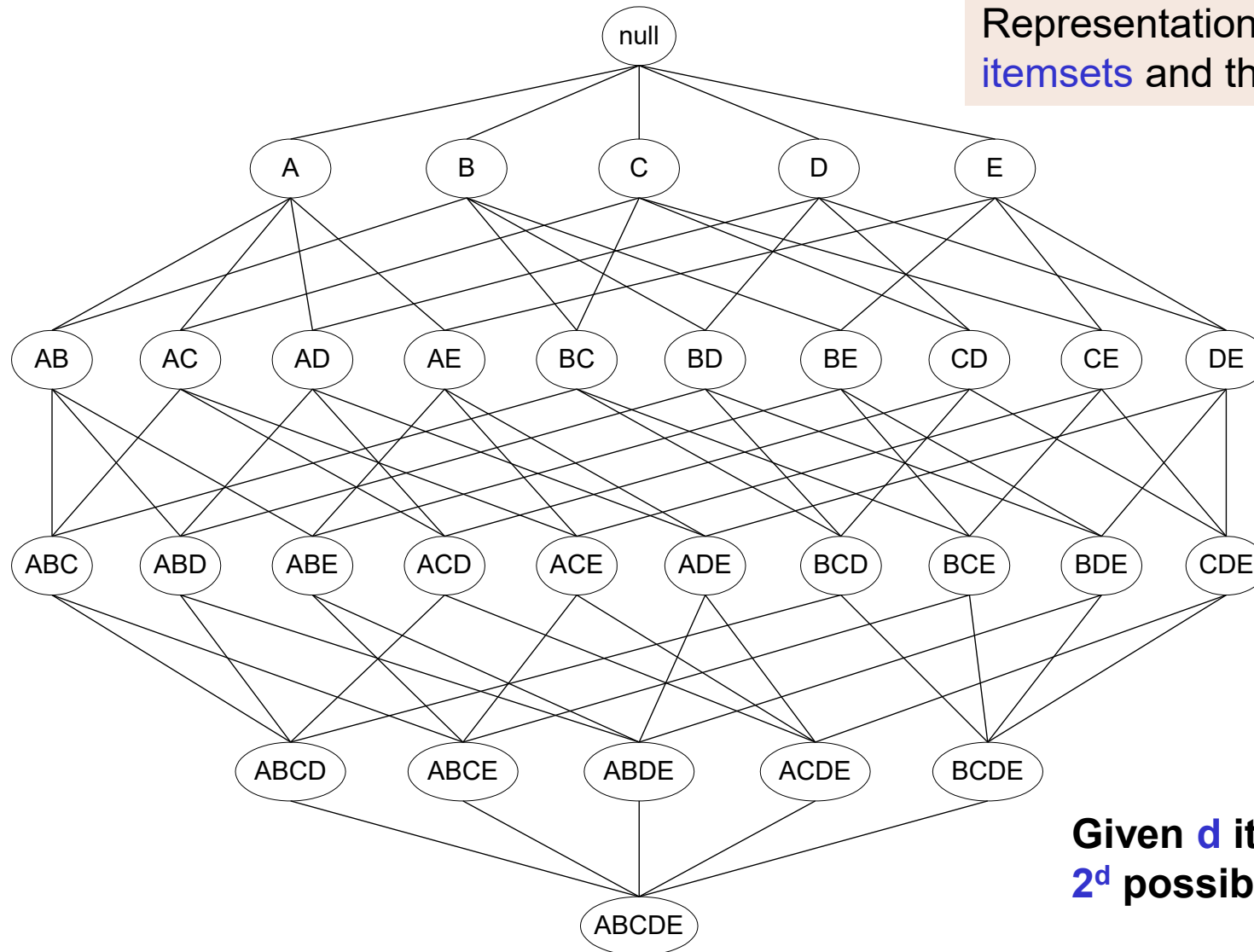
2. Use the *frequent itemsets* to generate association rules

Mining Frequent Itemsets

- **Input:** A set of transactions T , over a set of items I
- **Output:** All itemsets with items in I having
 - $\text{support} \geq \text{minsup}$ (support threshold)
- Problem parameters:
 - $N = |T|$: number of transactions
 - $d = |I|$: number of (distinct) items
 - w : max width of a transaction
 - Number of possible itemsets: $M = 2^d$
- Scale of the problem:
 - WalMart sells 100,000 items and can store billions of baskets.
 - The Web has billions of words and many billions of pages.

The Itemset Lattice

Representation of all possible
itemsets and their relationships



Given **d** items, there are
 2^d possible itemsets

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- Problem definition
- Apriori principle, Apriori algorithm
- Deriving association rules from frequent itemsets
- Reflection on Apriori algorithm

The Apriori Principle

- ▶ Main observations: $\forall X, Y: X \subseteq Y \Rightarrow s(X) \geq s(Y)$
 - ▶ If an itemset is frequent, so are its subsets
 - ▶ If an itemset is infrequent, so are its supersets
- ▶ The **Apriori** principle: *A subset of a frequent itemset must also be a frequent itemset*
 - ▶ E.g., if $\{AB\}$ is a frequent itemset, both $\{A\}$ and $\{B\}$ must be a frequent itemset
 - ▶ Iteratively find frequent itemsets with cardinality from 1 to m (m -itemset): Use frequent k -itemsets to explore $(k+1)$ -itemsets

Illustration of Apriori Principle

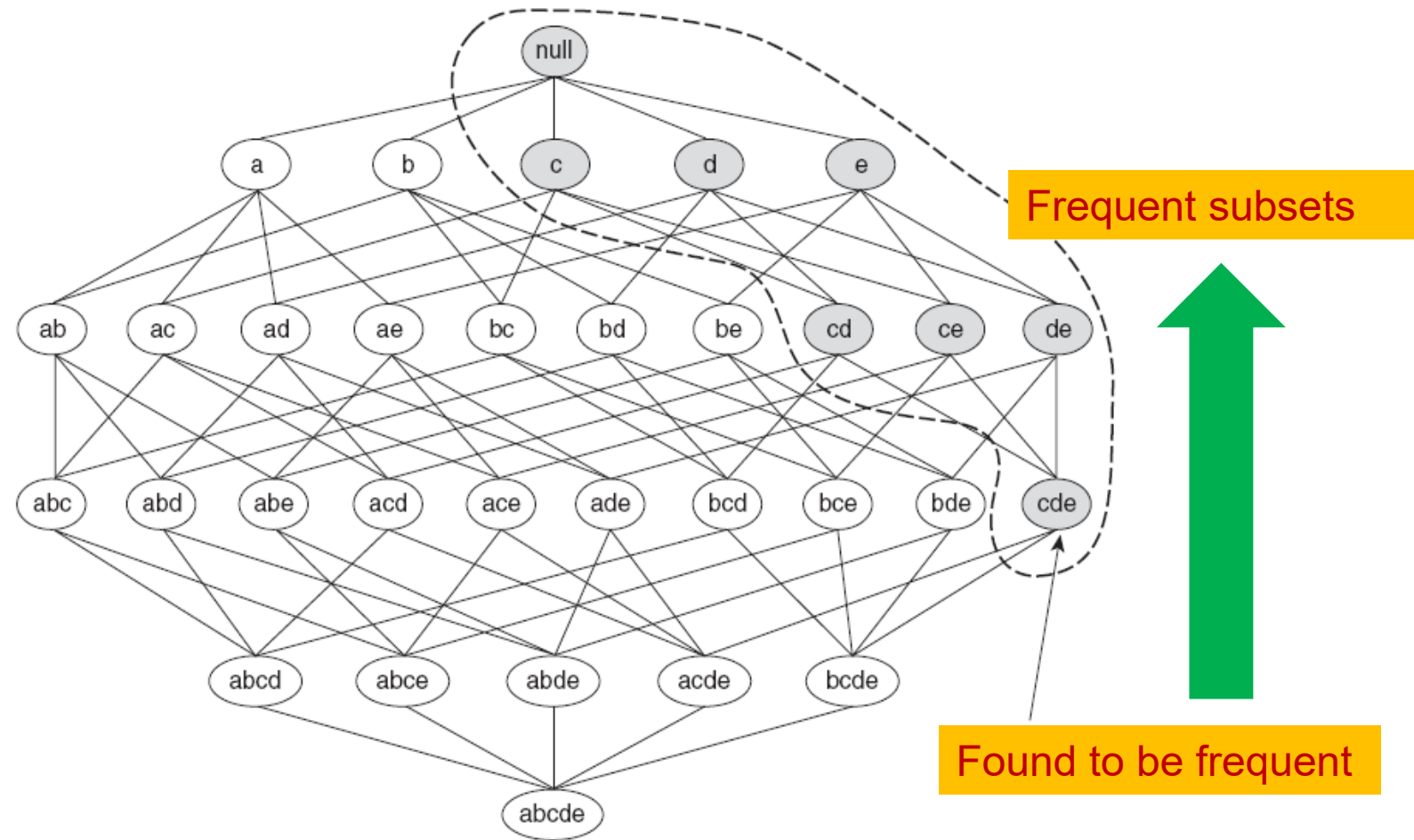
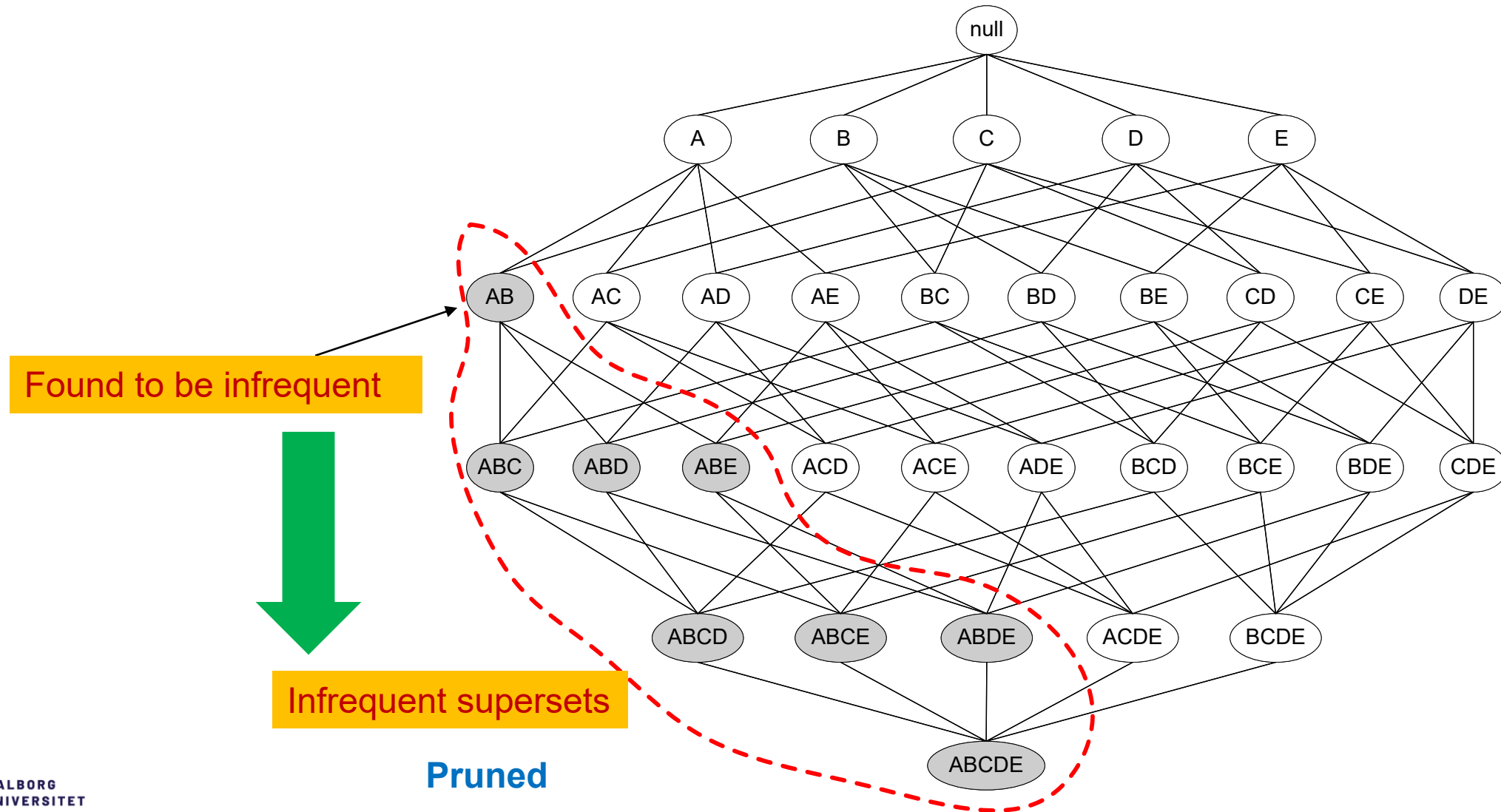


Figure 6.3. An illustration of the *Apriori* principle. If $\{c, d, e\}$ is frequent, then all subsets of this itemset are frequent.

Illustration of Apriori Principle (cont.)



Level-wise Process of Apriori Principle

Level 4 (frequent quadruples): $\{....\}$

Level 3 (frequent triplets): $\{ABD\}, \{BDF\}$

Level 2 (frequent pairs): $\{AB\}, \{AD\}, \{BD\}, \{BF\}, \{DF\}$

Level 1 (frequent items): $\{A\}, \{B\}, \{D\}, \{F\}$

Remember:

All subsets of a frequent itemset must be frequent as well

Question: Can ADF be frequent?

NO: because AF is not frequent

The Apriori Algorithm

► Notations

- C_k : Candidate itemset of size k
- L_k : Frequent itemset of size k

► Important steps in candidate generation

- **Prune Step**: Any k -itemset that is not frequent cannot be a subset of a frequent $(k+1)$ -itemset
- **Join Step**: C_{k+1} is generated by joining L_k with itself

```
 $C_I = \{\{\text{item}_1\}, \dots, \{\text{item}_N\}\};$   
for ( $k = 1$ ;  $L_k \neq \emptyset$ ;  $k++$ )  
  for each transaction  $t$  in transaction table  $T$   
    increment the count of all candidates in  $C_k$  that are contained in  $t$   
   $L_k =$  candidates in  $C_k$  with min_support (frequent)  
   $C_{k+1} =$  candidates generated from  $L_k$ ;  
return  $\cup_k L_k$ ;
```

Special self-join!

The Apriori Algorithm Example (1)

Trans. Table T

TID	Items
100	1 3 4
200	2 3 5
300	1 2 3 5
400	2 5

min_sup=2 (or 50%)

Scan T →

C_1	itemset	sup.
	{1}	2
	{2}	3
	{3}	3
	{4}	1
	{5}	3

→ L_1

L_1	itemset	sup.
	{1}	2
	{2}	3
	{3}	3
	{5}	3

↺

C_2	itemset
	{1 2}
	{1 3}
	{1 5}
	{2 3}
	{2 5}
	{3 5}

The Apriori Algorithm Example (2)


Trans. Table T

TID	Items
100	1 3 4
200	2 3 5
300	1 2 3 5
400	2 5

min_sup=2 (or 50%)


L_2

itemset	sup
{1 3}	2
{2 3}	2
{2 5}	3
{3 5}	2



C_2

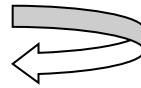
itemset	sup
{1 2}	1
{1 3}	2
{1 5}	1
{2 3}	2
{2 5}	3
{3 5}	2



C_2

itemset
{1 2}
{1 3}
{1 5}
{2 3}
{2 5}
{3 5}

Scan T



C_3

itemset
{2 3 5}

The Apriori Algorithm Example (3)

Trans. Table T

TID	Items
100	1 3 4
200	2 3 5
300	1 2 3 5
400	2 5

min_sup=2 (or 50%)



C_3	itemset
	{2 3 5}

Scan T

L_3	itemset	sup
	{2 3 5}	2

The Apriori Algorithm Example (4)

Trans. Table T

TID	Items
100	1 3 4
200	2 3 5
300	1 2 3 5
400	2 5

min_sup=2 (or 50%)

The result of frequent itemsets

itemset	sup.
{1}	2
{2}	3
{3}	3
{5}	3

itemset	sup
{1 3}	2
{2 3}	2
{2 5}	3
{3 5}	2

itemset	sup
{2 3 5}	2

$$L_1 \cup L_2 \cup L_3$$

Candidates Generation

- Suppose the items in L_k are listed in an order

- Step 1: self-joining L_k to get C_{k+1} (In SQL)

INSERT INTO C_{k+1}

SELECT $p.item_1, p.item_2, \dots, p.item_k, q.item_k$

FROM $L_k p, L_k q$

WHERE $p.item_1=q.item_1, \dots, p.item_{k-1}=q.item_{k-1}, p.item_k < q.item_k$

- Step 2: pruning frequent itemsets in C_{k+1}

forall *itemsets* c in C_{k+1} do

 forall *k-subsets* s of c do

 if (s is not in L_k) then delete c from C_{k+1}

The Previous Example

Trans. Table T

TID	Items
100	1 3 4
200	2 3 5
300	1 2 3 5
400	2 5

min_sup=2 (or 50%)

We only need
to match
{2 3} with {2 5}



L_2

itemset	sup
{1 3}	2
{2 3}	2
{2 5}	3
{3 5}	2

C_3

itemset
{2 3 5}

Example of Candidates Generation

► $L_3 = \{abc, abd, acd, ace, bcd\}$

► Self-joining: $L_3 \bowtie L_3$

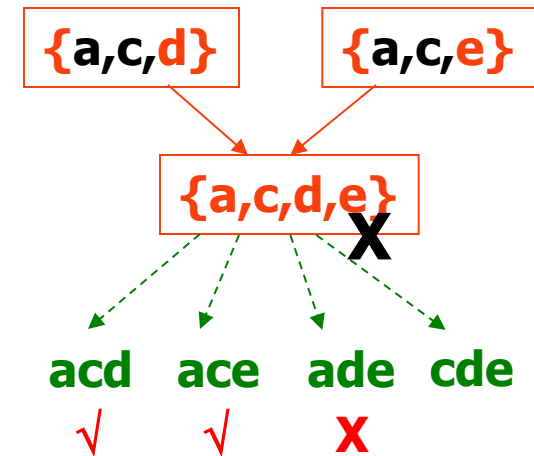
- $abcd$ from abc and abd
- $acde$ from acd and ace
- No need to match other pairs

► Pruning:

- $acde$ is removed because ade is not in L_3

► $C_4 = \{abcd\}$

- Scanning transaction table T is still needed to get the frequencies for items in C_4 (to decide the correct L_4)



Agenda

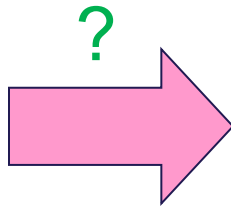
- ▶ Problem definition
- ▶ Apriori principle, Apriori algorithm
- ▶ **Deriving association rules from frequent itemsets**
- ▶ Reflection on Apriori algorithm

Generating Association Rules from Frequent Itemsets

- Assume that we have discovered the frequent itemsets and their support
- How do we generate association rules?
- Frequent itemsets:

{1}	2
{2}	3
{3}	3
{5}	3
{1,3}	2
{2,3}	2
{2,5}	3
{3,5}	2
{2,3,5}	2

$l \rightarrow$



Not a transaction table!

- For each frequent itemset l , find all nonempty subsets s .
- For each s , generate rule $s \Rightarrow l-s$, if $\text{sup}(l)/\text{sup}(s) \geq \text{min_conf}$

Example: $l = \{2,3,5\}$, $\text{min_conf} = 75\%$

$\{2,3\} \Rightarrow \{5\}$ $2/2=100\%$ ✓
 $\{2,5\} \Rightarrow \{3\}$ $2/3=66.6\%$ ✗
 $\{3,5\} \Rightarrow \{2\}$ $2/2=100\%$ ✓

do the rest as an exercise

Association Rules in Jupyter Notebook

► Library **mlxtend**

- To install the library: `pip install mlxtend` in Anaconda Prompt
- `from mlxtend.frequent_patterns import apriori: frequent itemsets`
- `from mlxtend.frequent_patterns import association_rules: rules`

► Exercises on real data

- `store_data.csv` (in Moodle)
- (7501, 20)
 - › 7501 transactions, each having at most 20 items

Agenda

- ▶ Problem definition
- ▶ Apriori principle, Apriori algorithm
- ▶ Deriving association rules from frequent itemsets
- ▶ Reflection on Apriori algorithm

Performance Bottlenecks of Apriori

- ▶ Is Apriori fast enough?
- ▶ The core of the Apriori algorithm:
 - ▶ Use frequent k -itemsets to generate **candidate** frequent $(k+1)$ -itemsets
 - ▶ Use full table scan and pattern matching to collect counts for the candidate itemsets
- ▶ The bottleneck of Apriori: **candidate generation**
 - ▶ Huge candidate sets:
 - › A 10^4 -sized frequent 1-itemset will generate 10^7 candidate 2-itemsets
 - › To discover a frequent pattern of size 100, e.g., $\{a_1, a_2, \dots, a_{100}\}$, one needs to generate $2^{100} \approx 10^{30}$ candidates.
 - ▶ Multiple scans of database table:
 - › Needs $(n + 1)$ scans, n is the length of the longest pattern

Methods to Improve Apriori's Efficiency

- Transaction reduction
 - A transaction that does not contain any frequent k -itemset is useless in subsequent scans
- Partitioning
 - Any itemset that is potentially frequent in transaction table T must be frequent in at least one of the partitions of T .

Partitioning

- ▶ Divide transaction table T into partitions T_1, T_2, \dots, T_p such that each T_i fits in the main memory
- ▶ Apply Apriori to each partition
- ▶ Any frequent itemset must be frequent in at least one partition

1. Divide T into partitions T^1, T^2, \dots, T^p ;
2. For $i = 1$ to p do
3. $L^i = \text{Apriori}(T^i)$;
4. $C = L^1 \cup \dots \cup L^p$;
5. Count C on T to generate L ;

Partitioning Example (1)

	Transaction	Items
T_1	t_1	Bread,Jelly,PeanutButter
	t_2	Bread,PeanutButter
	t_3	Bread,Milk,PeanutButter
T_2	t_4	Beer,Bread
	t_5	Beer,Milk

min_support = 10%

$L(T_1) = \{ \{ \text{Bread} \}, \{ \text{Jelly} \},$
 $\{ \text{PeanutButter} \},$
 $\{ \text{Bread,Jelly} \},$
 $\{ \text{Bread,PeanutButter} \}, \{ \text{Jelly,$
 $\text{PeanutButter} \},$
 $\{ \text{Bread,Jelly,PeanutButter} \} \}$

$L(T_2) = \{ \{ \text{Bread} \}, \{ \text{Milk} \},$
 $\{ \text{PeanutButter} \}, \{ \text{Bread,Milk} \},$
 $\{ \text{Bread,PeanutButter} \}, \{ \text{Milk,$
 $\text{PeanutButter} \},$
 $\{ \text{Bread,Milk,PeanutButter} \},$
 $\{ \text{Beer} \}, \{ \text{Beer,Bread} \},$
 $\{ \text{Beer,Milk} \} \}$

Partitioning Example (2)

Transaction	Items
t_1	Bread,Jelly,PeanutButter
t_2	Bread,PeanutButter
t_3	Bread,Milk,PeanutButter
t_4	Beer,Bread
t_5	Beer,Milk

min_support = 10%

$L(T_1) = \{\{\text{Bread}\}, \{\text{Jelly}\},$
 $\{\text{PeanutButter}\}, \{\text{Bread,Jelly}\},$
 $\{\text{Bread,PeanutButter}\}, \{\text{Jelly},$
 $\text{PeanutButter}\},$
 $\{\text{Bread,Jelly,PeanutButter}\}\}$

$L(T_2) = \{\{\text{Bread}\}, \{\text{Milk}\},$
 $\{\text{PeanutButter}\}, \{\text{Bread,Milk}\},$
 $\{\text{Bread,PeanutButter}\}, \{\text{Milk},$
 $\text{PeanutButter}\},$
 $\{\text{Bread,Milk,PeanutButter}\}, \{\text{Beer}\},$
 $\{\text{Beer,Bread}\}, \{\text{Beer,Milk}\}\}$

$C = L(T_1) \cup L(T_2)$

Count itemsets in C with respect to T ,
and prune infrequent ones.

Partitioning's Pros and Cons

► Advantages:

- It adapts to available main memory
- It can be easily parallelized
 - › Maximum number of database table scans is two (why?)
 - › One for partitioning the transaction table, and one for the final counting

► Disadvantages:

- May have many candidates for the second scan
- A countermeasure: associate the frequency to each itemset in each partition, and the final global counting can be a simple aggregation.

More Efficient Approach: FP-tree

- ▶ Using FP-tree for finding frequent items
- ▶ Compress a large database table into a compact, [Frequent-Pattern tree \(FP-tree\)](#) structure
 - ▶ highly condensed, but complete for frequent pattern mining
 - ▶ avoid costly database table scans
- ▶ Develop an efficient, FP-tree-based frequent pattern mining method
 - ▶ A divide-and-conquer methodology: decompose mining tasks into smaller ones
 - ▶ Avoid candidate generation: sub-database test only!
- ▶ FP-growth: mining frequent patterns without candidate generation

Summary

- Association rule definition
 - Support, confidence, lift and association rule
 - Frequent itemsets
 - Steps for association rule mining
- Apriori algorithm
- Deriving association rules from frequent itemsets
- Criticism on Apriori

Exercises

1. Refer to the transaction table to the right. Say $\text{sup}(ab)=100$

➤ Determine the possible values of $\text{sup}(a)$

▪ Conclusion: $\text{sup}(a)$ 100

▪ *Hint*: Is it possible that $\text{sup}(a)=70$? Why?

➤ Determine the possible values of $\text{sup}(abc)$

▪ Conclusion: $\text{sup}(abc)$ 100

▪ *Hint*: Is it possible that $\text{sup}(abc)=120$? Why?

Choose either " \leq " or " \geq "

Transaction table
(1000 rows)

TID	Items
1	a,b,c
2	a,c
3	b,e,f
...

2. Slides 33 (Hands-on, optional)

Readings

➤ Mandatory reading

- Jiawei Han, Micheline Kamber and Jian Pei. Data Mining: Concepts and Techniques (3rd edition), Elsevier Science Ltd, 2011.
 - Chapter 6

➤ Further readings

- Rakesh Agrawal, Ramakrishnan Srikant: Fast Algorithms for Mining Association Rules in Large Databases. VLDB 1994: 487-499
- Jiawei Han, Jian Pei, Yiwen Yin: Mining Frequent Patterns without Candidate Generation. SIGMOD 2000: 1-12

➤ Acknowledgment: Slides are from

- Margaret H. Dunham (Data Mining: Introductory and Advanced Topics, Prentice Hall, 2002)
- The HKP textbook
- Man Lung Yiu and Panagiotis Karras

Readings for Coding

► Mandatory readings

- Association Rule: <https://www.geeksforgeeks.org/association-rule/?ref=lbp>
- Frequent Itemsets: <https://www.geeksforgeeks.org/frequent-item-set-in-data-set-association-rule-mining/?ref=lbp>
- Apriori Algorithm: <https://www.geeksforgeeks.org/apriori-algorithm/?ref=lbp>

► Further readings

► Documentation of mlxtend's frequent

- › http://rasbt.github.io/mlxtend/user_guide/frequent_patterns/apriori/
- › http://rasbt.github.io/mlxtend/user_guide/frequent_patterns/association_rules/

► Tutorials

- › <https://www.geeksforgeeks.org/implementing-apriori-algorithm-in-python/>
- › <https://www.kaggle.com/code/annettecatherinepaul/apriori-algorithm-association-rule-mining>
- › <https://towardsdatascience.com/understand-and-build-fp-growth-algorithm-in-python-d8b989bab342> (FP-Growth, advanced)