Thevenin/Norton equivalents

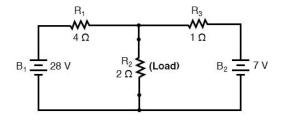
To find a Thevenin-equivalent, one usually follows the same procedure.

- 1. Open-circuit the load element.
- 2. Find voltage across the open gap.
- 3. Short-circuit voltage sources and open-circuit current sources.
- 4. Simplify to single impedance.

To illustrate this process, we load a circuit and decide to find the Thevenin-equivalent if we view R_2 as the load impendance.

```
circuit = Circuit('circuits/th_no_equivalents.txt');
circuit.list
```

```
ans =
    'V1 1 0 DC 28
    V2 3 0 DC 7
    R1 1 2 4
    R2 2 0 2
    R3 2 3 1
```



ELAB.evaluate(circuit)

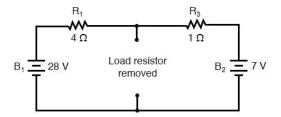
Symbolic analysis successful (0.410586 sec).

Numerical evaluation successful (0.0671006 sec).

We open-circuit the load.

```
circuit.open(circuit.Resistors(2))
circuit.list
```

```
ans =
'V1 1 0 DC 28
V2 3 0 DC 7
R1 1 2 4
R3 2 3 1
```



Then find the voltage across the gap, which is the Thevenin-equivalent voltage source.

```
ELAB.evaluate(circuit)

Symbolic analysis successful (0.280977 sec).

Numerical evaluation successful (0.0492452 sec).

circuit.numerical_node_voltages(2)

ans = v_2 = \frac{56}{5}
```

We short all the voltage sources and simplify to find the Thevenin-equivalent impedance.

```
ELAB.remove_sources(circuit);
ELAB.simplify(circuit);
circuit.Resistors(1).impedance

ans =
4
5
```

Of course, this process has also been condensed and given a high-level function.

```
circuit = Circuit('circuits/th_no_equivalents.txt');
ELAB.thevenin(circuit, circuit.Resistors(2));

Symbolic analysis successful (0.242366 sec).
Numerical evaluation successful (0.0384677 sec).

circuit.list
```

```
ans =
'Vth 1 0 DC 56/5
Rth 1 2 4/5
R2 2 0 2
```

Thevenin Equivalent Circuit $\begin{array}{c|c} R_{\text{Thevenin}} \\ \hline & 0.8 \ \Omega \\ \hline & & \\ E_{\text{Thevenin}} \end{array} = 11.2 \ V \qquad \begin{array}{c|c} R_2 \\ 2 \ \Omega \end{array} \Rightarrow \text{(Load)}$

And there is a corresponding Norton-equivalent function, as well.

```
circuit = Circuit('circuits/th_no_equivalents.txt');
ELAB.norton(circuit, circuit.Resistors(2));
```

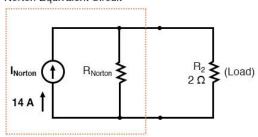
Symbolic analysis successful (0.289178 sec).

Numerical evaluation successful (0.039912 sec).

circuit.list

```
ans =
'Ino 1 0 DC 14
Rno 1 0 4/5
R2 1 0 2
```

Norton Equivalent Circuit



Both functions also handle purely symbolic or mixed circuits.

```
circuit = Circuit('circuits/th_no_equivalents_sym.txt');
ELAB.thevenin(circuit, circuit.Resistors(2));
```

Symbolic analysis successful (0.252057 sec).

Numerical evaluation successful (0.0706248 sec).

```
circuit.list
```

```
ans =
'Vth 1 0 DC (R1*V2 + R3*V1)/(R1 + R3)
Rth 1 2 (R1*R3)/(R1 + R3)
```

```
R2 2 0 R2
```

```
circuit = Circuit('circuits/th_no_equivalents_sym.txt');
ELAB.norton(circuit, circuit.Resistors(2));

Symbolic analysis successful (0.240673 sec).

Numerical evaluation successful (0.0647609 sec).
```

```
circuit.list
```

```
ans =
   'Ino 1 0 DC (R1*V2 + R3*V1)/(R1*R3)
   Rno 1 0 (R1*R3)/(R1 + R3)
   R2 1 0 R2
   '
```