

# A Spiking Independent Accumulator Model for Winner-Take-All Computation





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#### Motivation

- Investigate WTA mechanisms in the context of neurally plausible cognitive modelling
- Implement using spiking neurons
- Explore the effect of noisy inputs on stable decision making
- Allow for integration into larger scale networks

### **Neural Engineering Framework**

- Representation in spiking neurons defined by encoding  $a_i(t) = G_i \left[ a_i e_i x(t) + J_i^{\mathrm{bias}} \right]$  and decoding  $\hat{x}(t) = \sum_i d_i \left[ (a_i * h)(t) \right]$
- Transformation by decoding weights  $d_i$  minimizing  $E_{f(x)} = |f(x) \hat{x}|$
- Dynamics by recurrent transformation

$$\frac{\partial x}{\partial t} = g(x) \quad \Rightarrow \quad f(x) = \tau_s g(x) + x$$

#### Benchmarks

- Ability to provide a clear output (single output above 0.15, stable over at least 1 s)
- Correctness (output corresponds to strongest input)
- Time required to reach a decision
- Transient outputs before final decision is reached

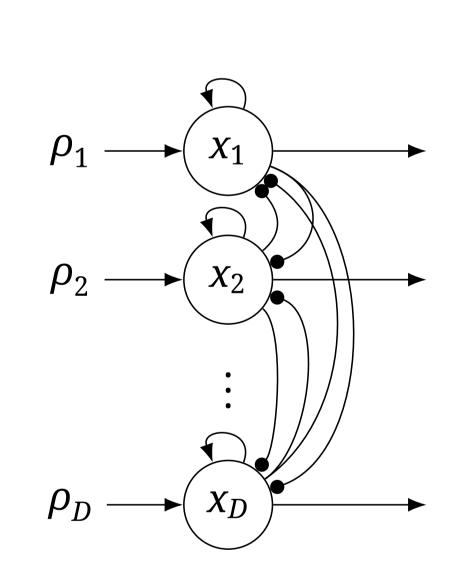
#### Conclusions

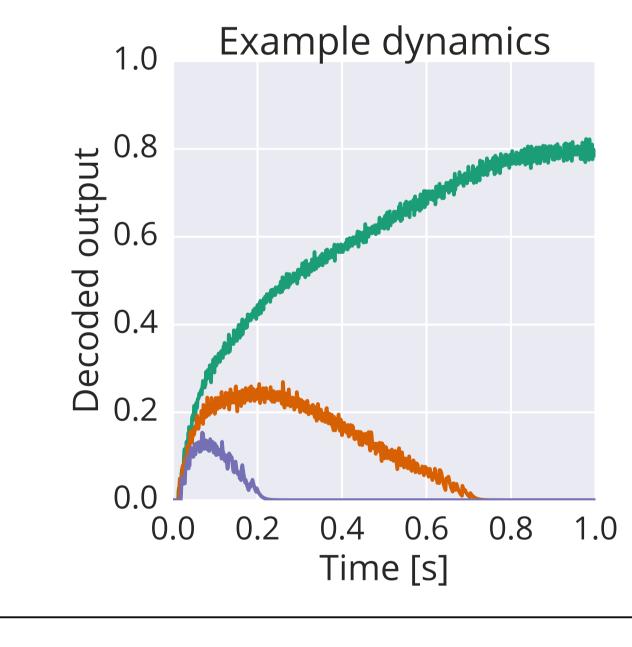
- The two WTA mechanisms are best suited for different purposes
- LCA network:
  - Reacts more quickly
  - If stable decision is reached, it will be correct
  - Output can be unstable in noisy conditions
- IA network: will eventually give a stable output, but it might not be the correct one

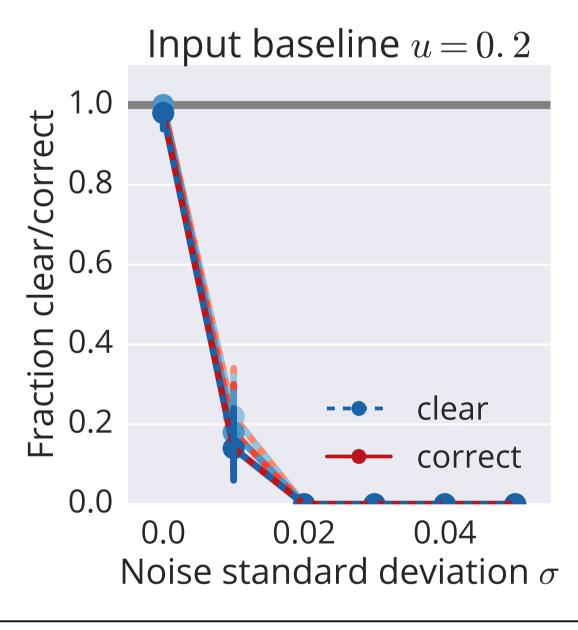
# Leaky, Competing Accumulators (LCA)

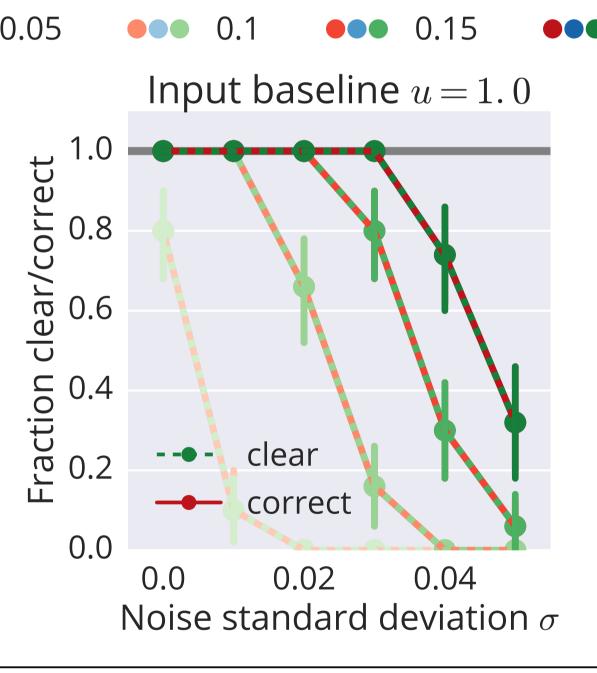
$$rac{\partial x_i}{\partial t} = \left( 
ho_i - kx_i - eta \sum_{j \neq i} x_j 
ight) rac{1}{ au},$$
 $x_i \geq 0$ 

Usher, M., & McClelland, J. L. (2001). The time course of perceptual choice: THe leaky, competing accumulator model. *Psychological Review*, 108(3), 550–592.

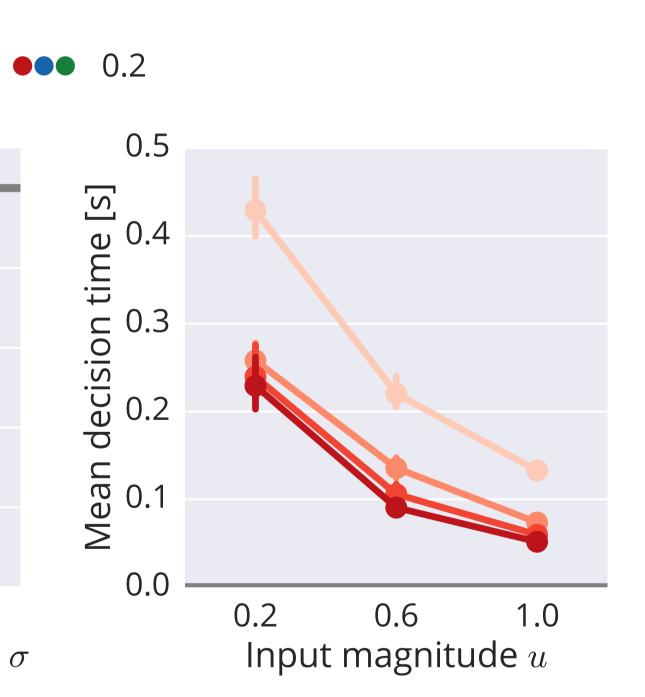


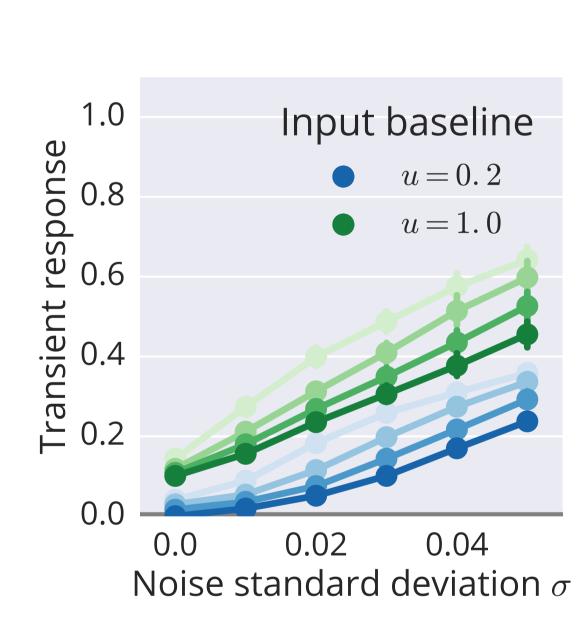






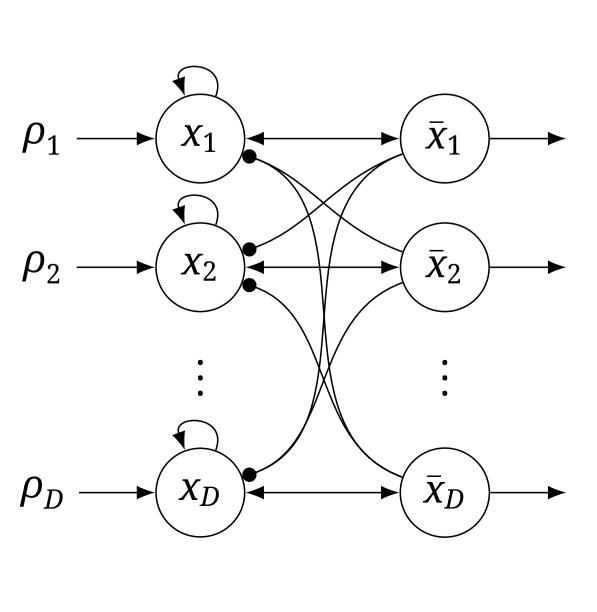
Target separation

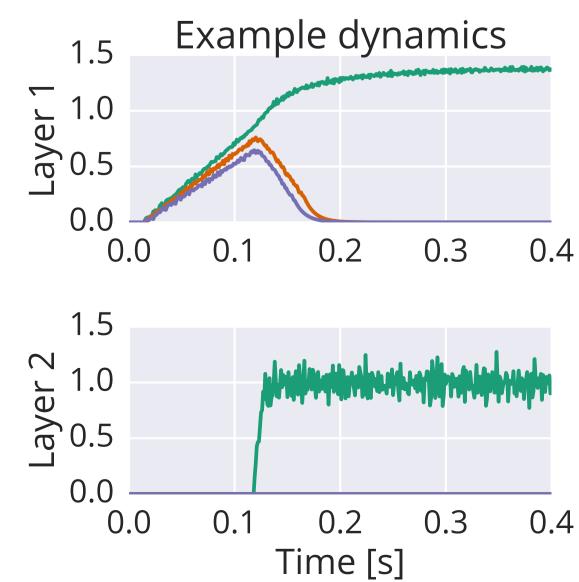


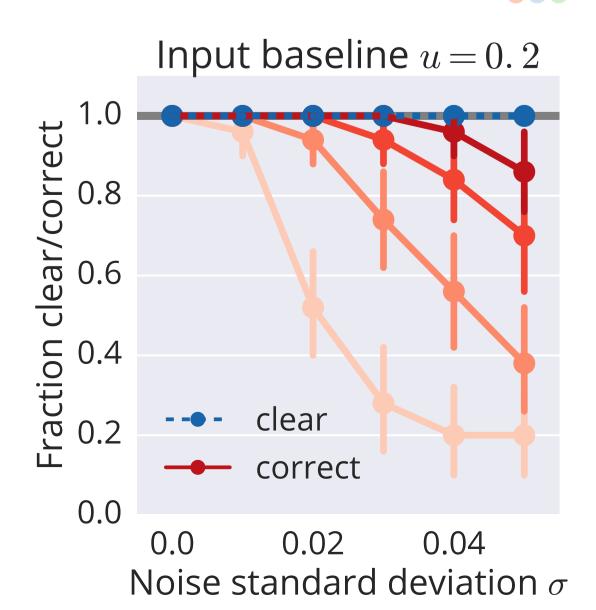


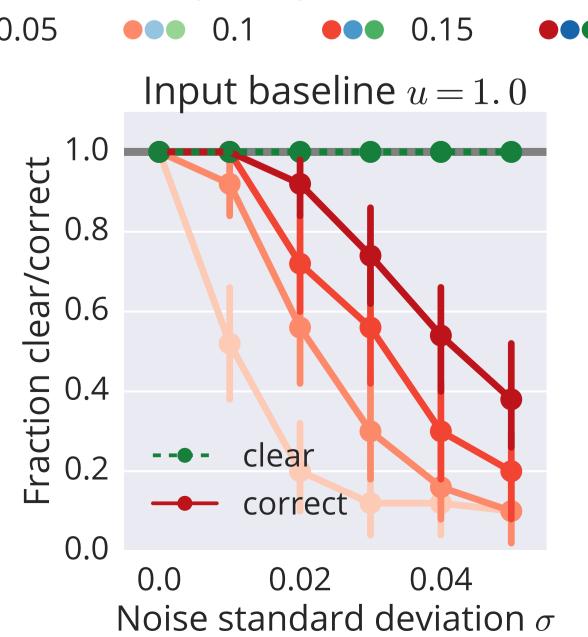
## Independent Accumulators (IA)

$$egin{aligned} ar{x}_i &:= \Theta(x_i - artheta), \ rac{\partial x_i}{\partial t} &= 
ho_i rac{1}{ au_1} + \left(ar{x}_i - ar{eta} \sum_{j 
eq i} ar{x}_j
ight) rac{1}{ au_2}, \ x_i &\geq 0 \end{aligned}$$









Target separation

