

# Analog Electronics

Fengchun Zhang

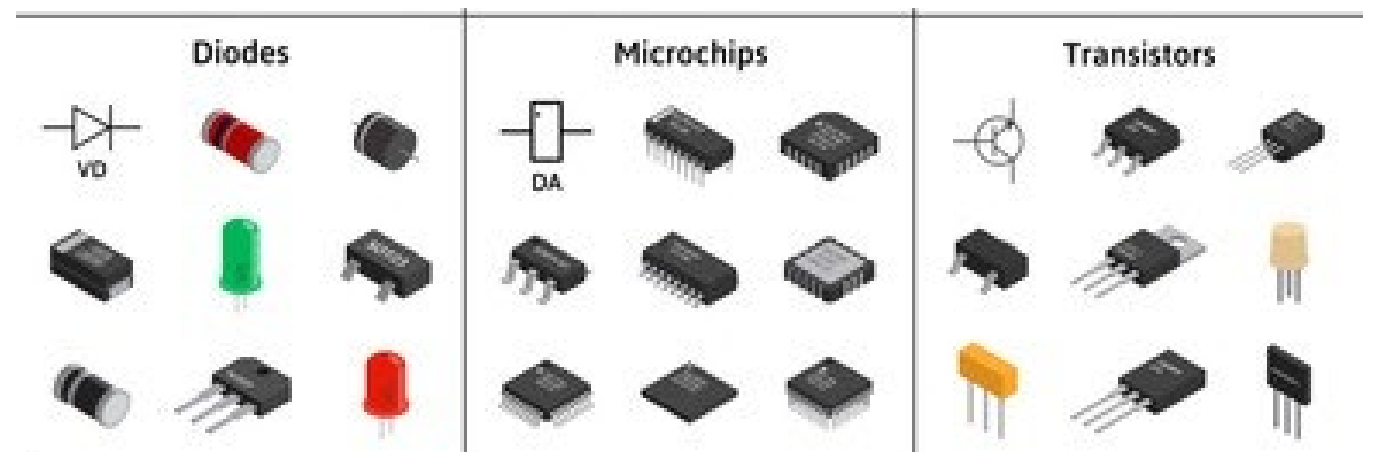
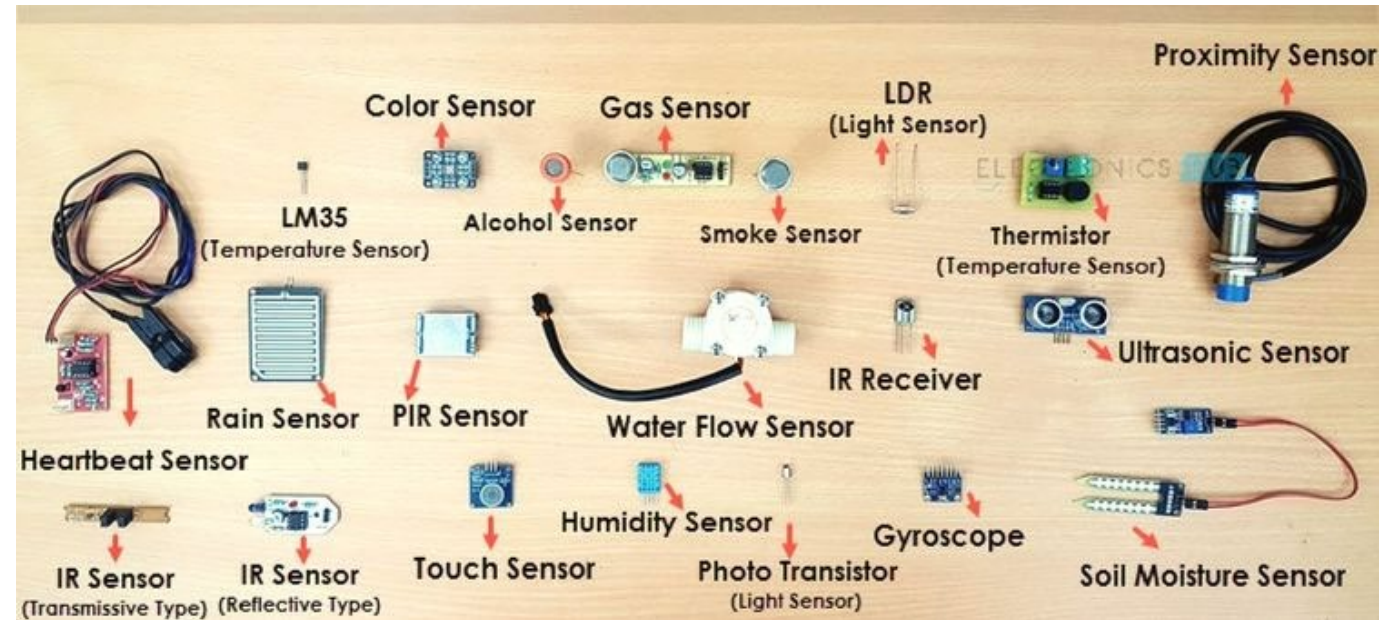
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# Agenda

- Introduction to analog electronics
- Course overview
  - Contents
  - Exam
  - Course execution
- Semiconductor & PN junction
- Diode
  - Models
  - I-V, input-output characteristics

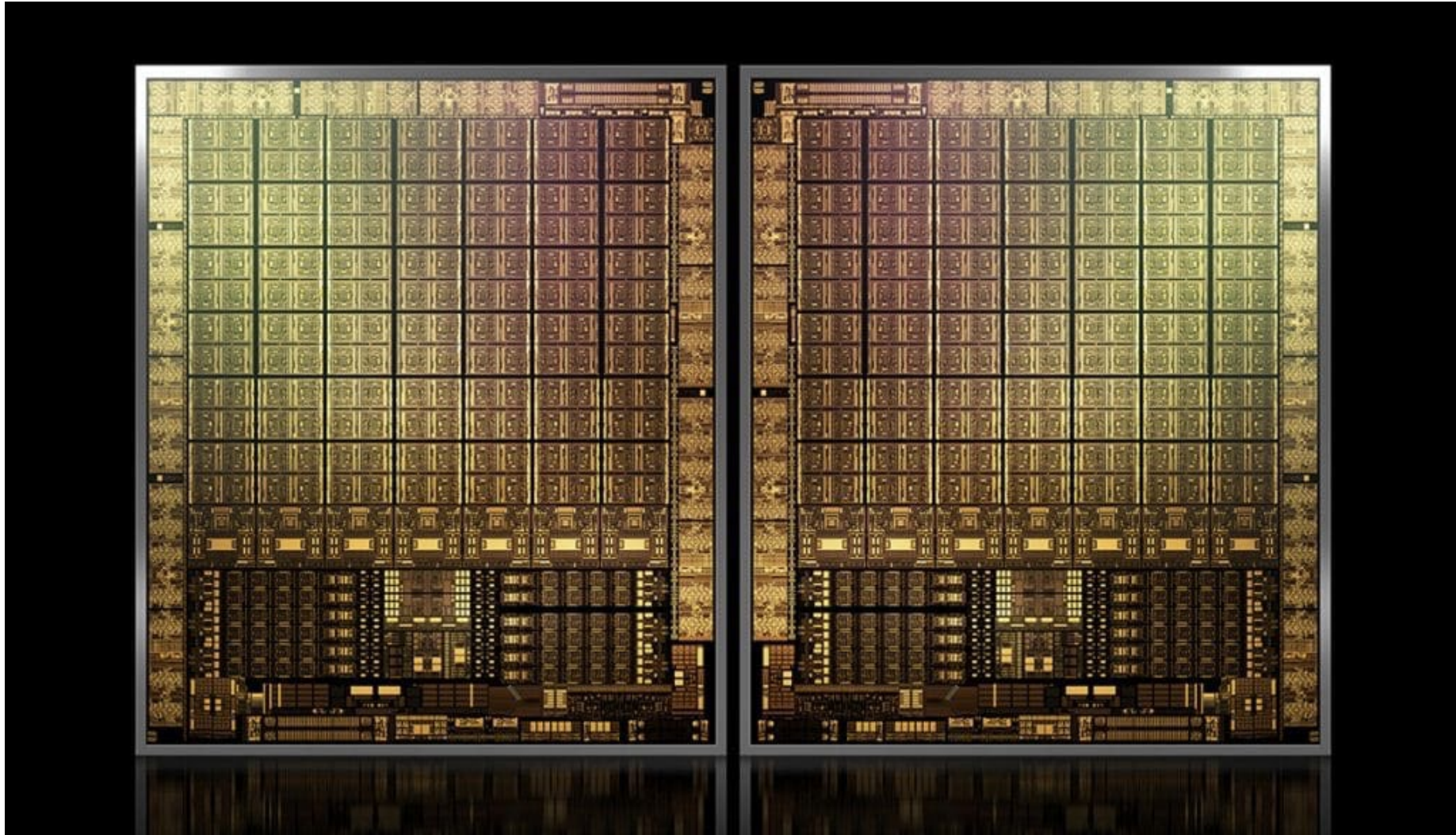
# What is Analog electronics?

- Deal with continuous signals
  - Capture, process and transmit real-world information
- Basis of many digital components in modern system design



Semiconductor devices

The two graphic processing unit (GPU) chips host 28.3 billion transistors each



# Provisional course plan

- Module 1: semiconductor, PN junction and diode
  - 1.1 Course introduction, semiconductors, PN junction, diode models
  - 1.2 Diode circuit principle, practical diode circuits
  - 1.3 Practical diode circuits, small signal model
  - 1.4 Measurement 1
- Module 2: Bipolar Junction Transistor (BJT)
  - 2.1 Structure and operation, properties in various regions, bias, large-signal & small-signal model, early effect
  - 2.2 Common-emitter stage w/o and w/ degeneration, biasing techniques
  - 2.3 Common-base stage, emitter followers
  - 2.4 Hybrid pi model
  - 2.5 Measurement 2

# Provisional course plan

- Module 3: Metal-Oxide-Semiconductor Field-Effect Transistor(MOSFET)
  - 3.1 Introduction to MOSFETs, biasing, transconductance
  - 3.2 Large-signal & small-signal operation, NMOS & PMOS
  - 3.3 Common-source stage w/o and w/ degeneration, biasing techniques
  - 3.4 Time harmonic distortion
  - 3.5 Measurement 3

# Exam

- Assessment : 7-step scale
- Written exam in June
  - Based on assignments
  - 6 tasks, 2 for each module

# Course execution

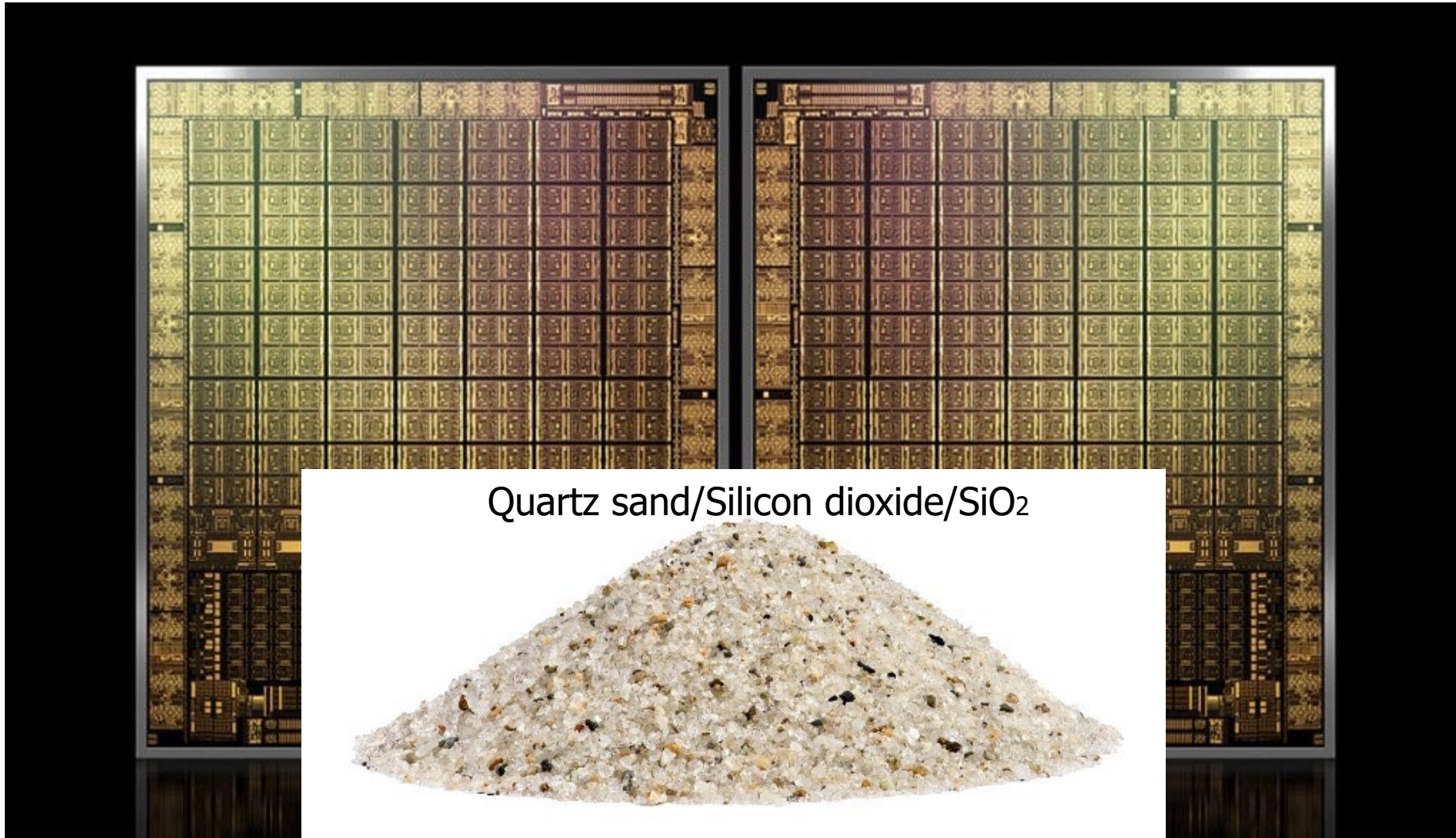
- Traditional lectures and assignments in groups:
  - Preferably calculate tasks together on the board, bring a notebook and pen.
  - Quizzes during the lecture.
  - It is not important that all assignments are calculated. BUT it is important that you understand the principles!
  - Simulations: LTspice
- Lab session:
  - Measurements
  - With simulations and measurements, you must always evaluate the results - do they make sense in relation to characteristics of the circuit.



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- **Semiconductor & PN junction**
- Diode
  - Models
  - I-V and input-output characteristics

What is the raw material for the GPU chips?



# Semiconductors devices



Germanium - Ge



Silicon - Si

Semiconductor



Semiconductor Devices



# Semiconductor

**Conductivity:** ability to allow the flow of electric current



Conductor



Germanium - Ge



Silicon - Si

Semiconductor



rubber



glass



oil



diamond



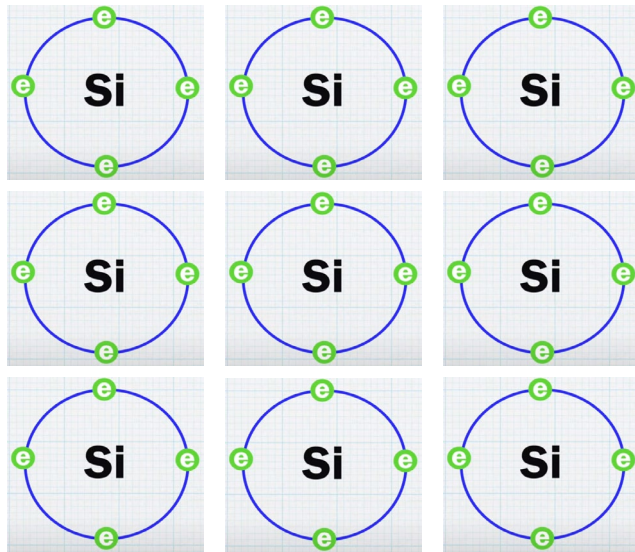
wood

Insulators



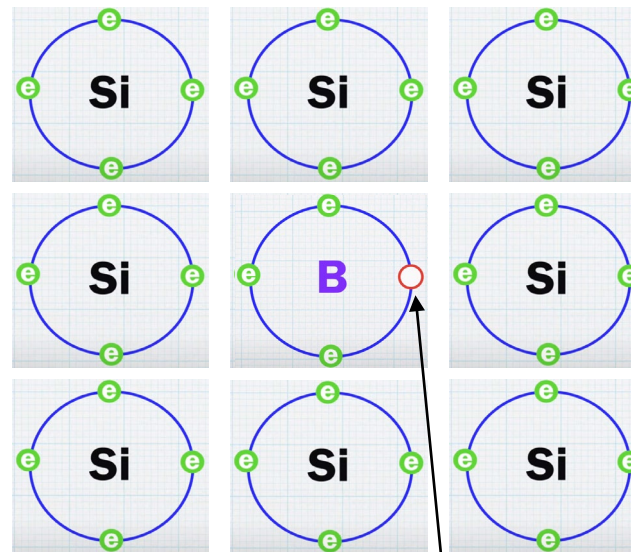
# Semiconductor

Intrinsic (Undoped)



Extrinsic (Doped)

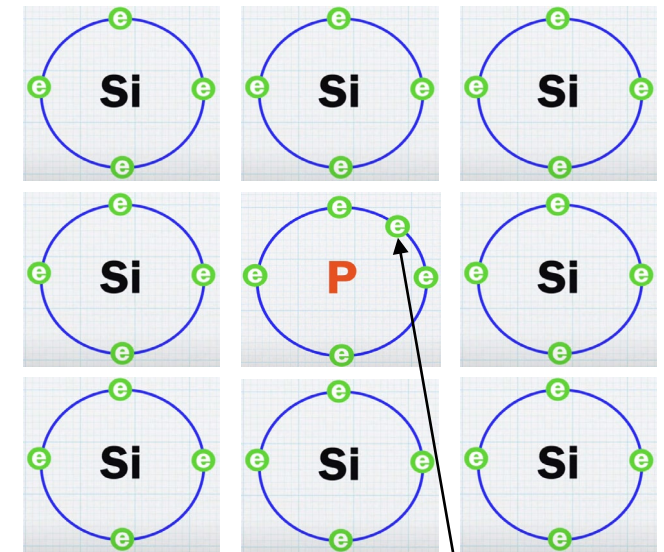
**P-Type**



**B: Boron**

extra hole

**N-Type**



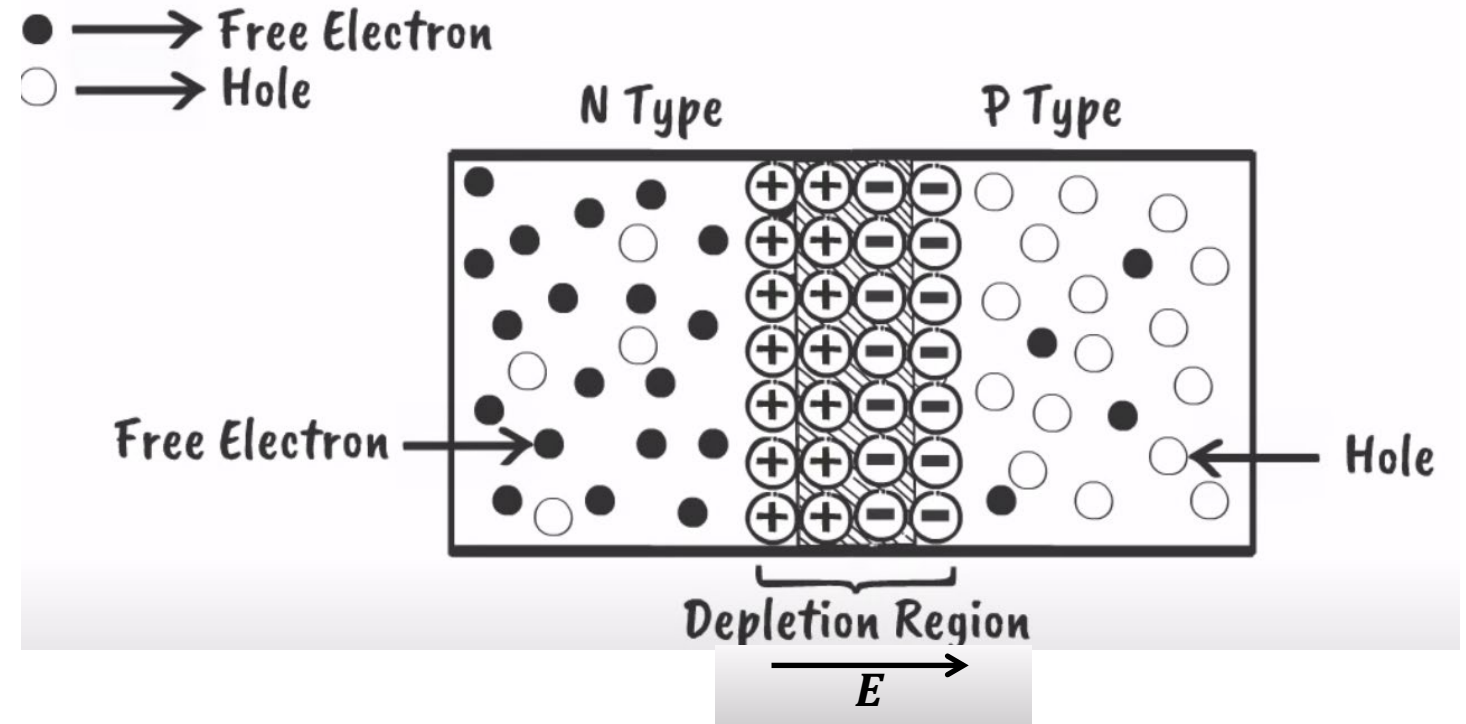
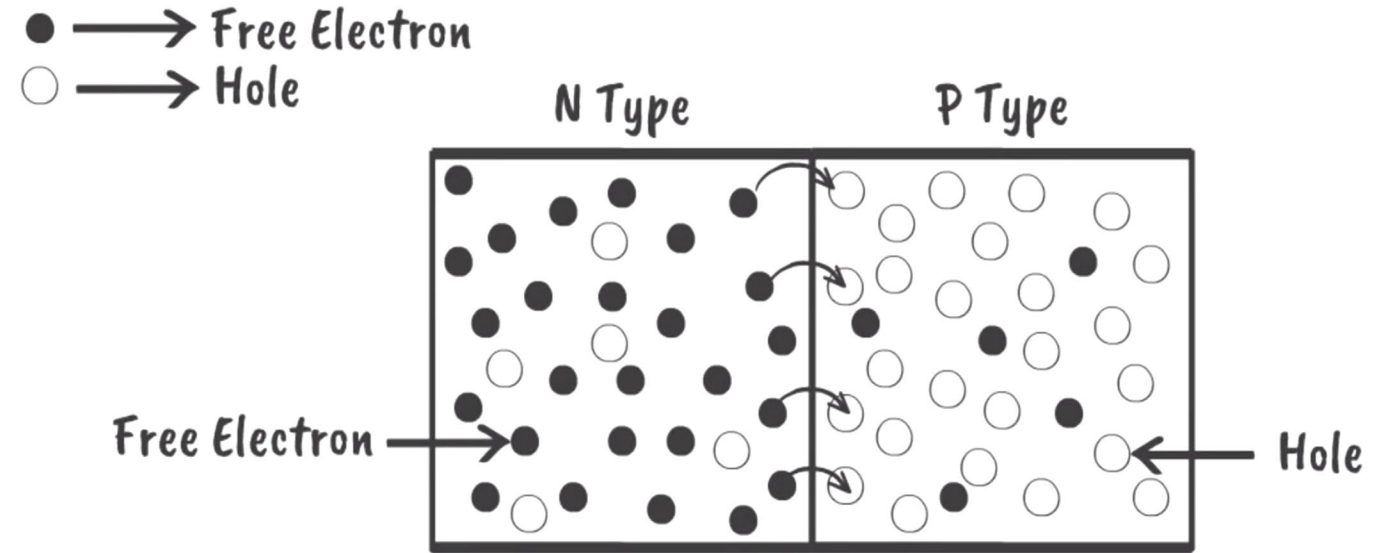
**P: Phosphorus**

extra electron

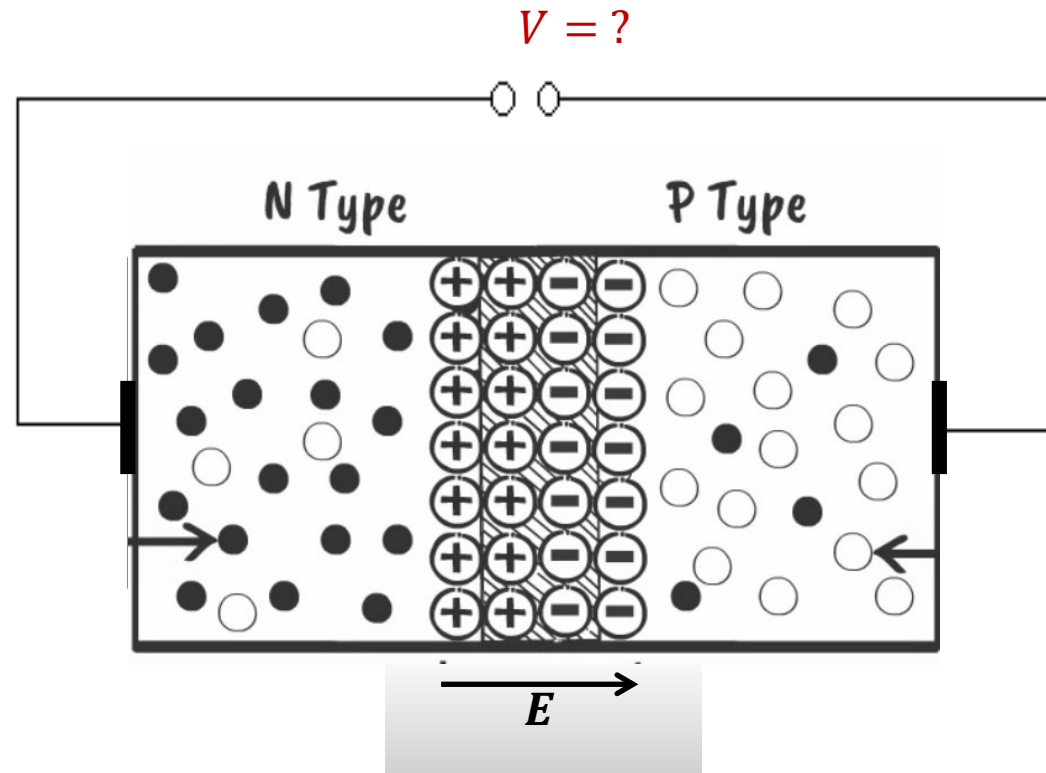
Free electrons / holes :  $10^{10} \sim 10^{12} / \text{cm}^3$  VS.  $10^{15} \sim 10^{20} / \text{cm}^3$  in room temperature.

Both n-type and p-type silicon are more electrically conductive than intrinsic silicon.

# PN junction

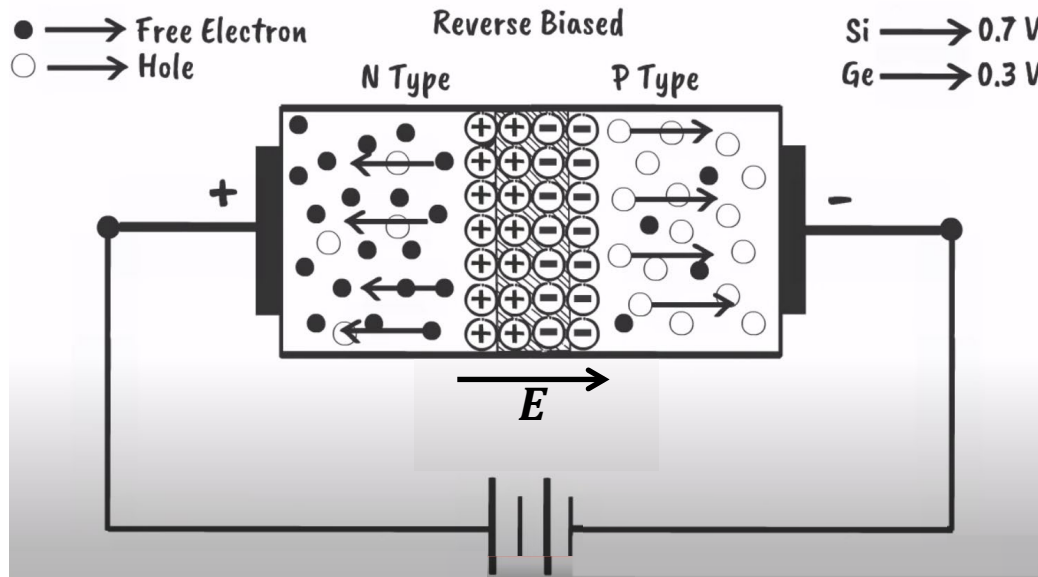


# Quiz

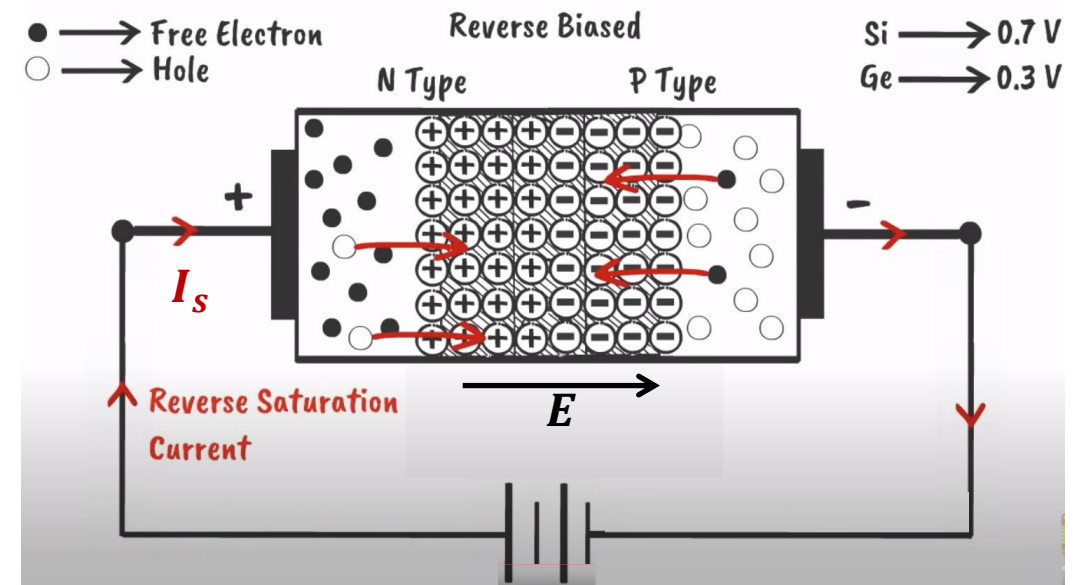
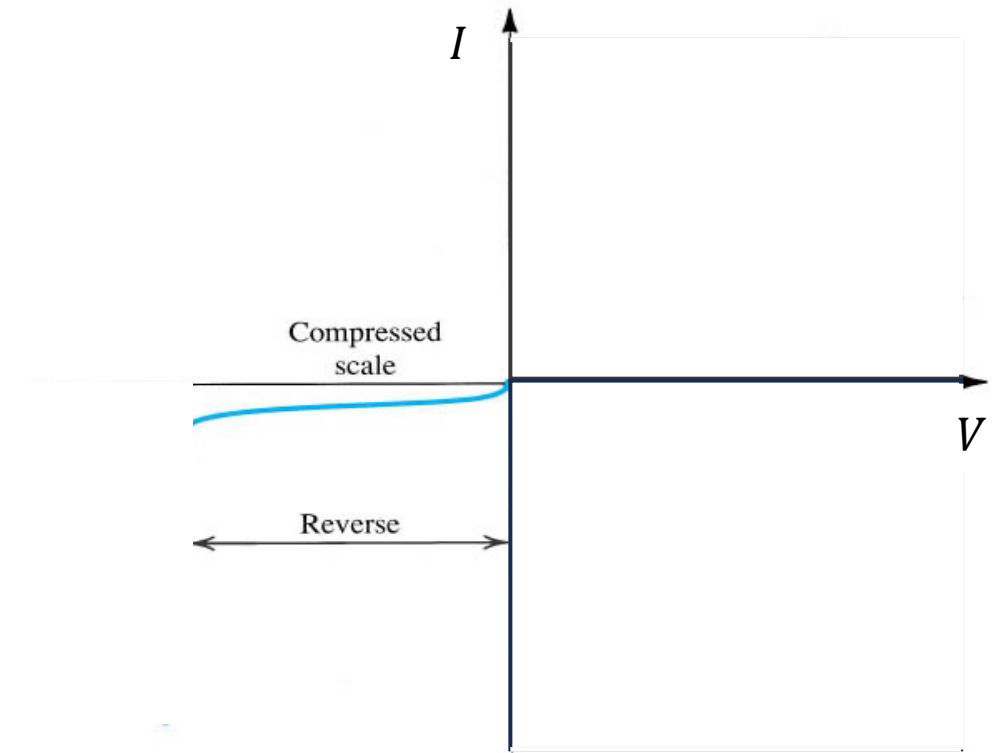


When the PN junction terminals are left open, what will  $V$  be?

# PN junction- reverse bias

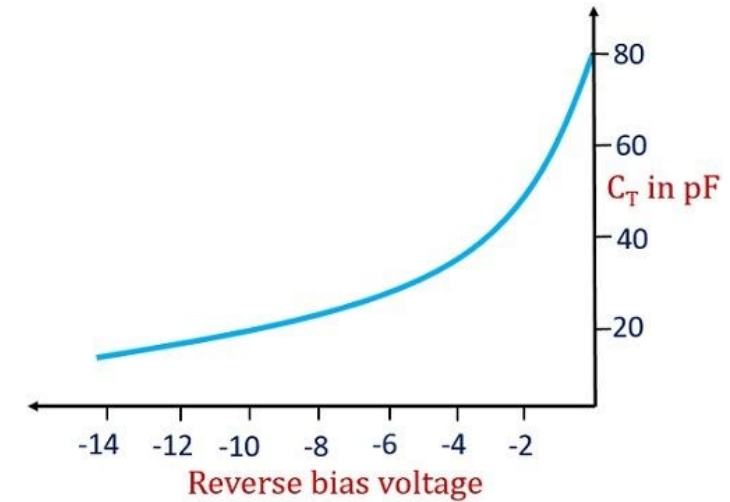
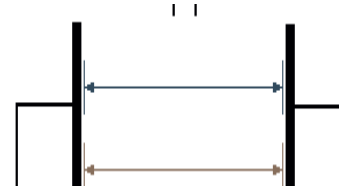
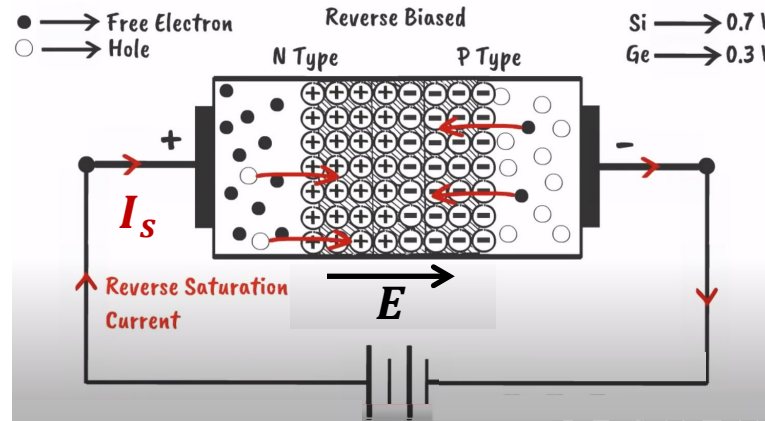
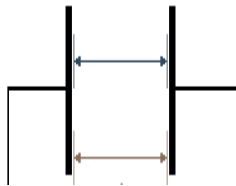
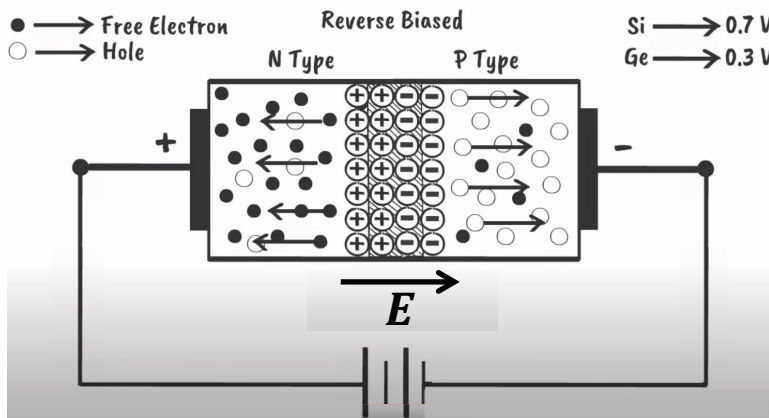


- free electrons drawn to the positive potential → more  $\oplus$  ions
- Holes drawn to the negative potential → more  $\ominus$  ions
- Wider depletion region



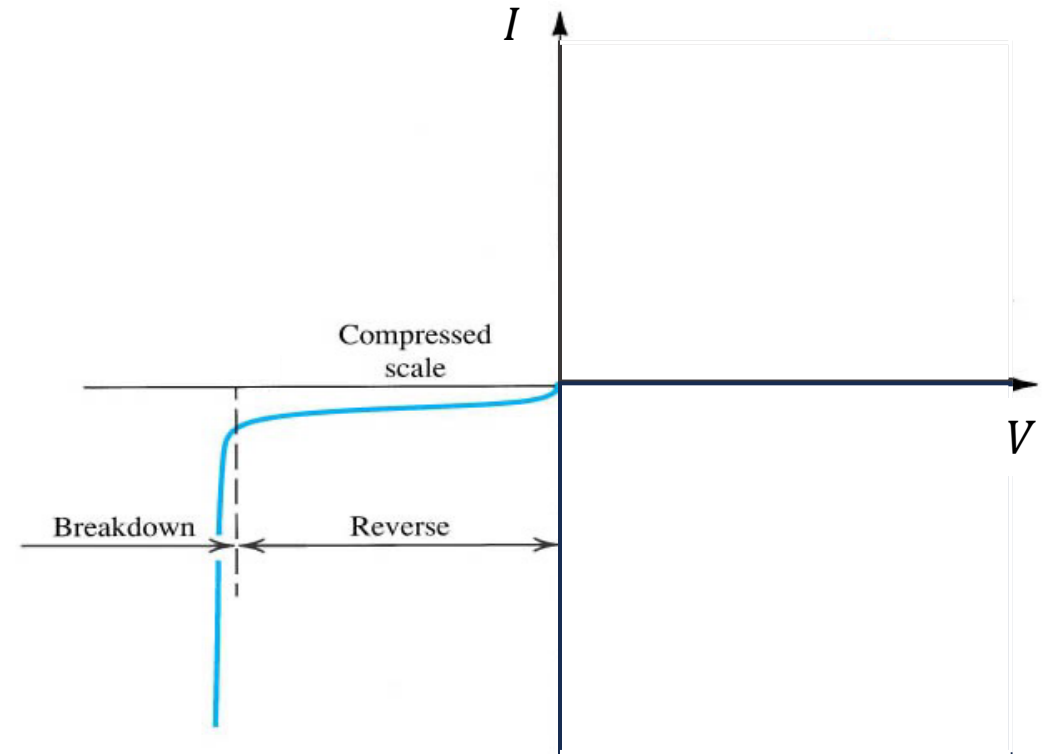
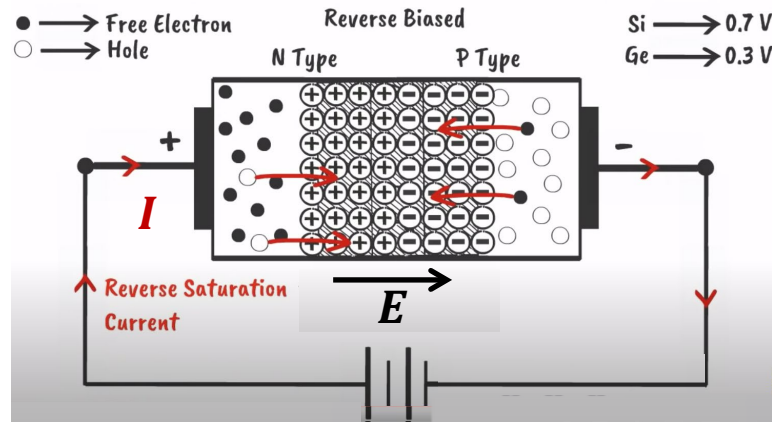


# PN junction- reverse bias



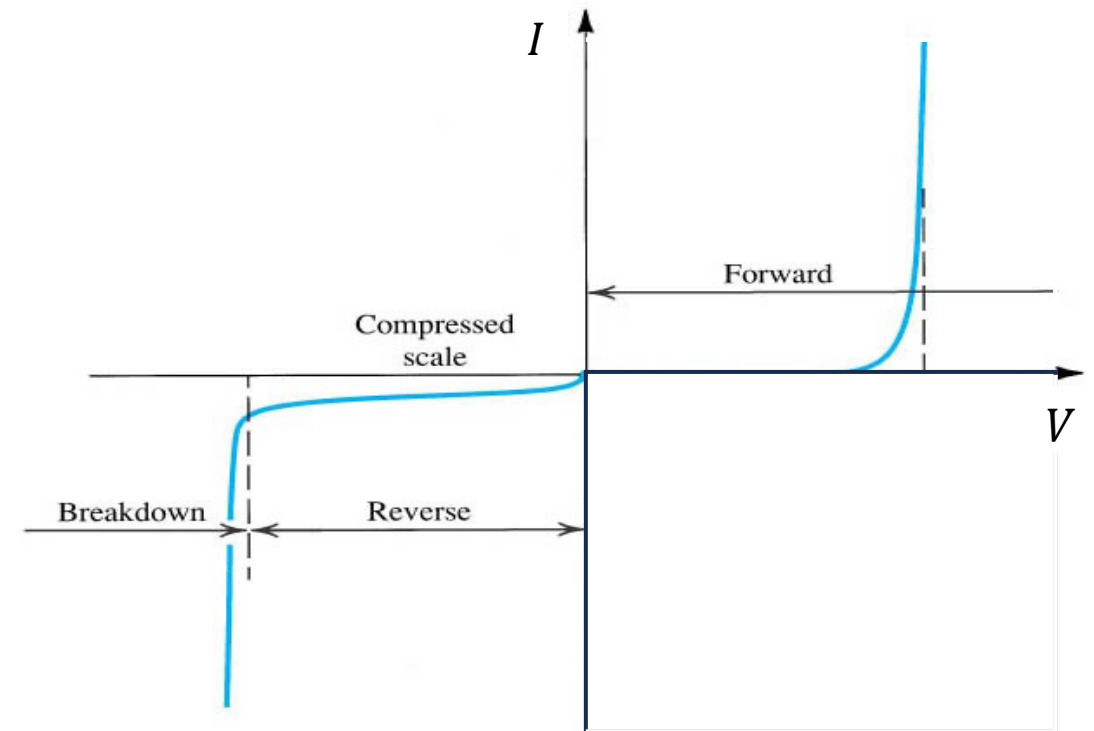
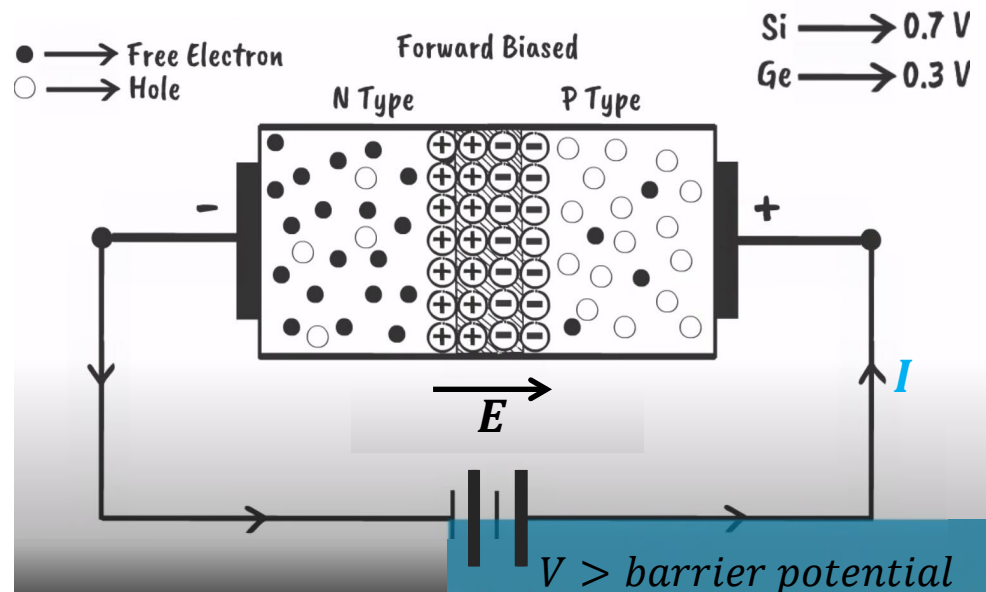
Varactor: a capacitor whose capacitance can be controlled by a voltage  
Application: oscillators

# PN junction- reverse breakdown



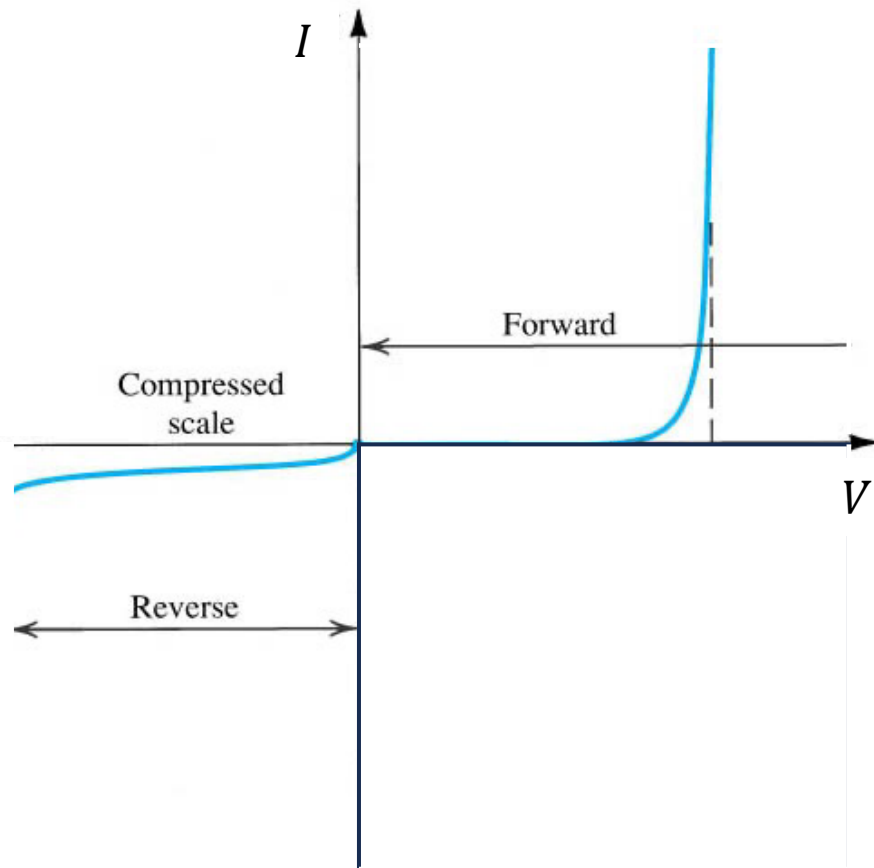
- When  $V$  becomes very negative, PN junction is broken down.
- Limit the reverse current to avoid damage
- Application: Zener diode

# PN junction- forward bias



- Battery  $V$  pushes the free electrons (majority charge carrier) from N to P.
- As long as the battery can provide current, the current can flow from P to N.
- The current increases dramatically as  $V$  increases.
- A 'fully conducting' diode  $\rightarrow$  voltage drop is  $0.6\text{ V} \sim 0.8\text{ V}$

# PN junction- Shockley's equation



$$I = I_S \left( e^{\frac{V}{nV_T}} - 1 \right) \quad \text{For anything with PN junctions}$$

$I_S$ : reverse saturation current, given in datasheet

$V$ : voltage across the junction

$n$ : ideal factor, depending on the construction of the PN junction,  $1 < n < 2$ ,  $n = 1$  for ideal PN junction

$V_T$ : thermal voltage

$$V_T = \frac{KT_K}{q}$$

$K$ : Boltzmann's constant =  $1.38 \times 10^{-23}$  J/K

$T_K$ : the absolute temperature in kelvins =  $273 + x$  °C

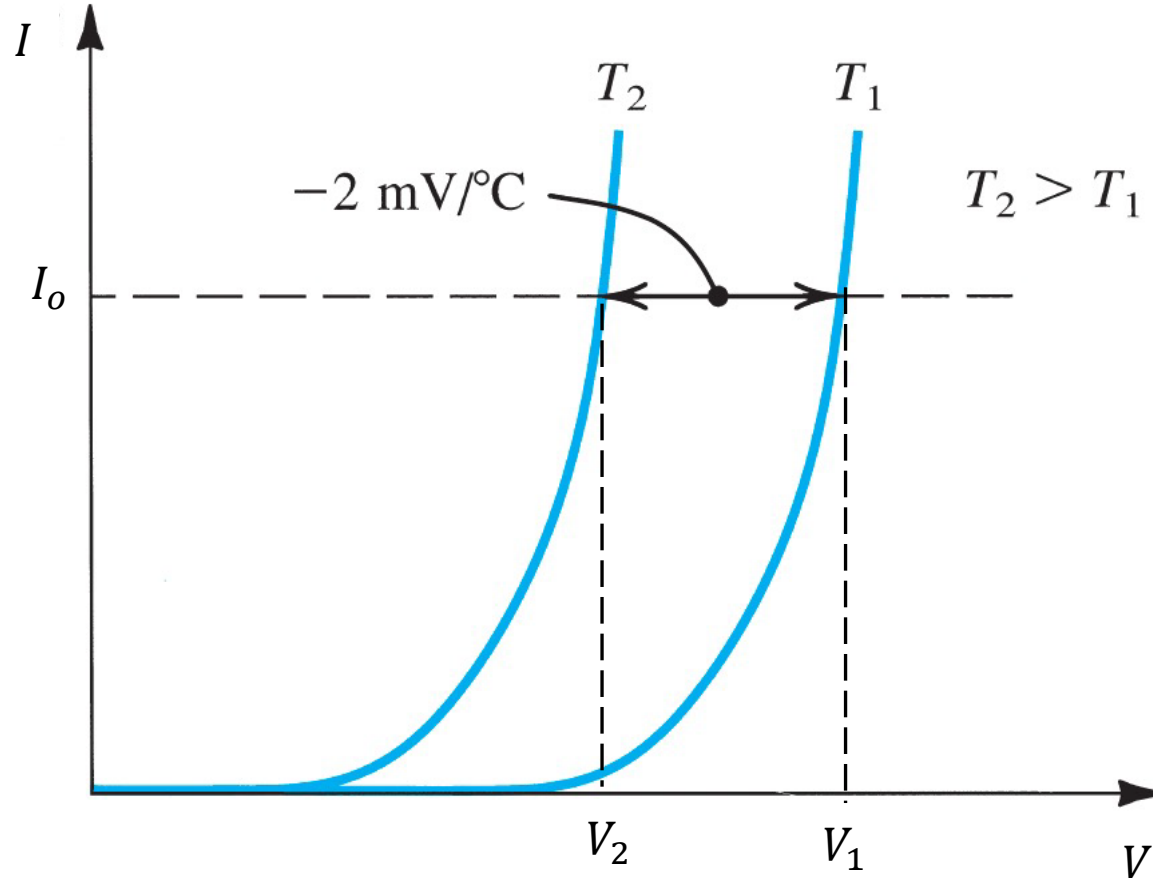
$q$ : the magnitude of electronic charge =  $1.6 \times 10^{-19}$  C

$I_S$  and  $V_T$  are temperature dependent.

$I_S$  doubles for every 5°C rise in temperature.  $V_T \approx 26 \text{ mV @ } 27^\circ \text{C}$

# PN junction-temperature coefficient

$$\text{Temperature coefficient} = \left. \frac{\Delta V}{\Delta T} \right|_{I=I_0} = \left. \frac{V_2 - V_1}{T_2 - T_1} \right|_{I=I_0}$$

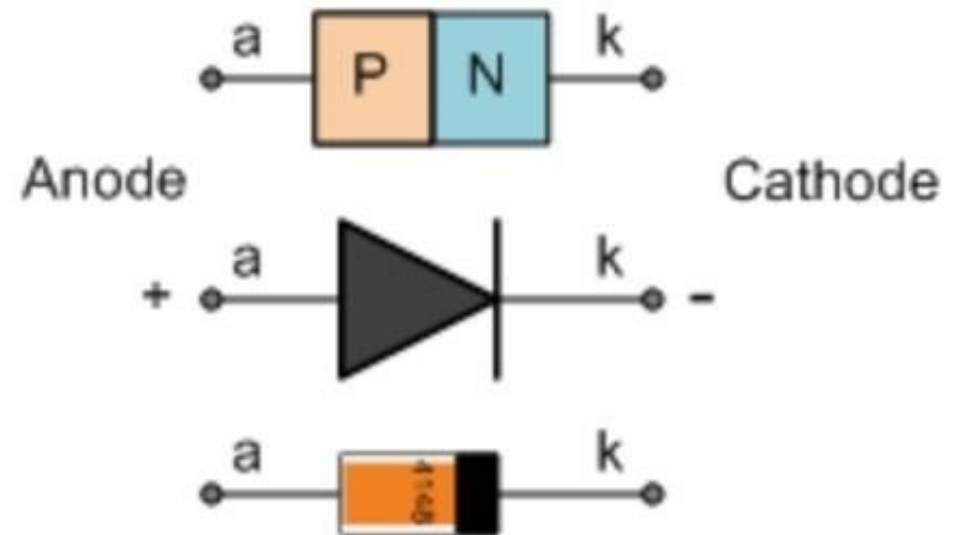
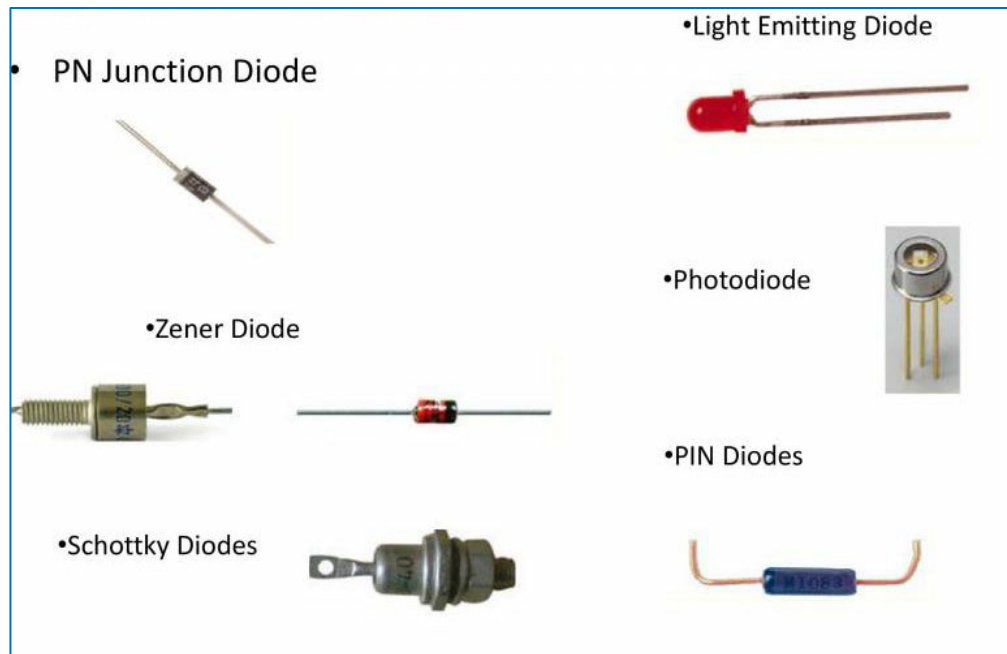


# Agenda

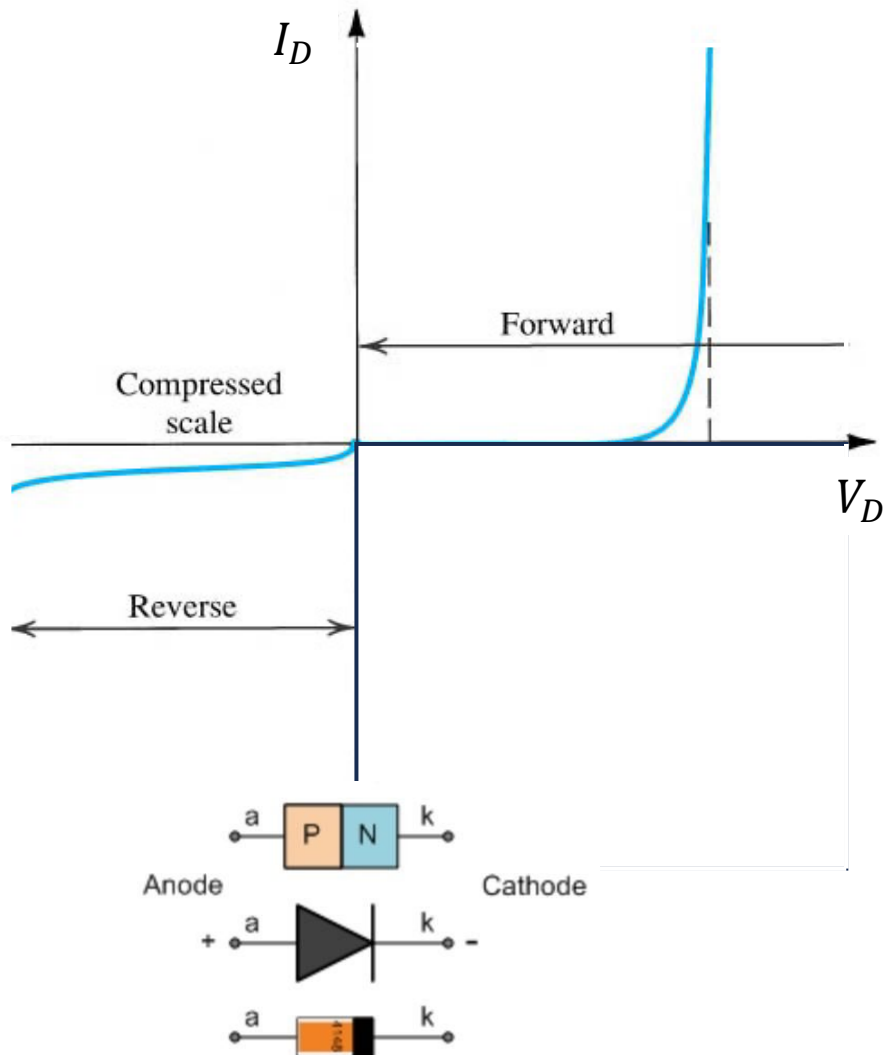
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# Diode

- A 2-terminal device 'passes' positive voltage & 'blocks' negative voltage
- A PN junction is a fundamental example of a diode.



# PN diode



$$I_D = I_s \left( e^{\frac{V_D}{nV_T}} - 1 \right)$$

- $I_s$  : reverse saturation current, given in datasheet
- $V_D$ : voltage across the diode
- $n$ : ideal factor, depending on the diode's construction,  $1 < n < 2$ ,  $n = 1$  for ideal diode
- $V_T$ : thermal voltage,  $V_T \approx 26 \text{ mV @ } 27^\circ\text{C}$

When a diode is forward-biased:

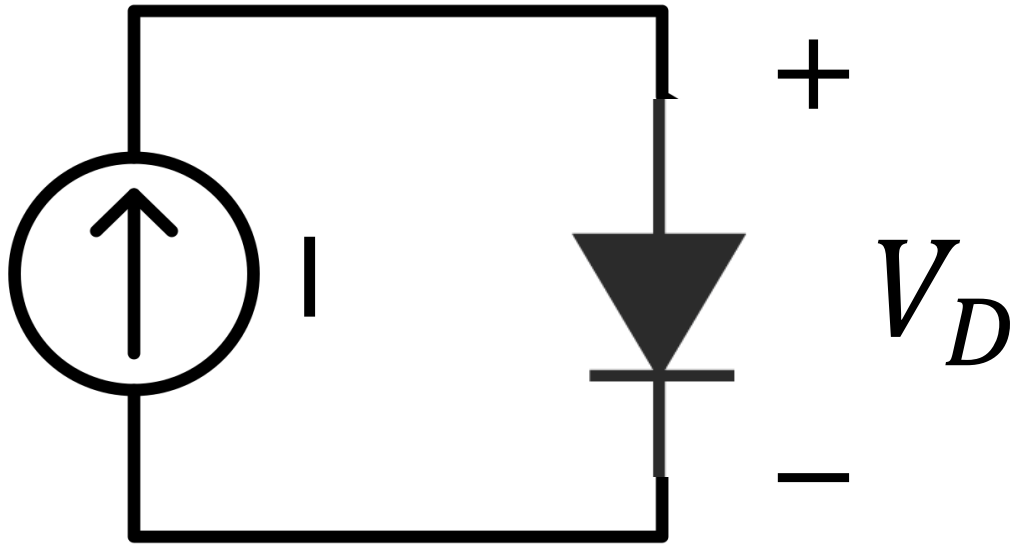
$$I_D \approx I_s e^{\frac{V_D}{V_T}}$$

- For  $V_D \gg V_T$  ( $V_D > 4V_T$  in practice),  $e^4 \approx 54.5$
- $n = 1$



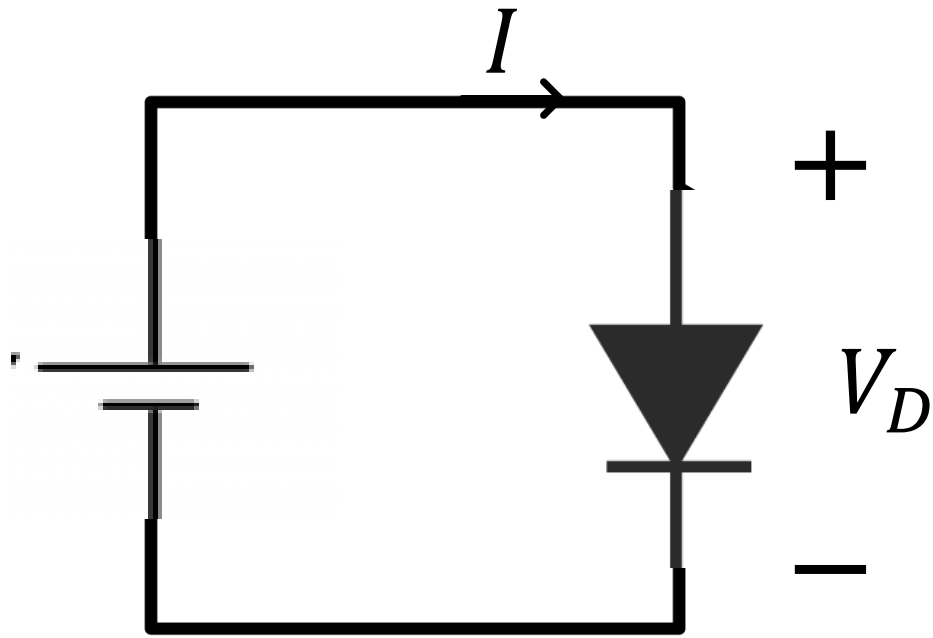
## Quiz: PN diode

$I_S = 10^{-16} \text{ A}$ ,  $V_T = 26 \text{ mV}$ , and  $I = 1 \text{ mA}$ ,  
 $V_D = ?$



$I_D \approx I_S e^{\frac{V_D}{V_T}}$  holds for both applying a voltage source or a current source.

# PN diode



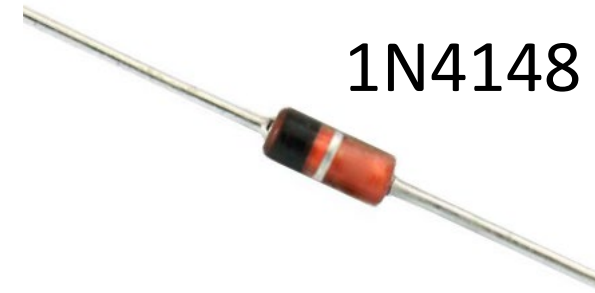
$$V_T \approx 26 \text{ mV @ } 27^\circ \text{C}$$

For  $I = I_1$ , we have  $V_D = V_{D1}$ .

If we want to achieve  $I = I_2 = 10I_1$ ,  
 $V_{D2} = V_{D1} + \Delta V$

$\Delta V = ?$

# Diode data sheet



1N4148

- ratings: What the manufacturer guarantees that it can withstand
- Characteristics: Properties

<b>ABSOLUTE MAXIMUM RATINGS</b> ( $T_{\text{amb}} = 25\text{ }^{\circ}\text{C}$ , unless otherwise specified)				
PARAMETER	TEST CONDITION	SYMBOL	VALUE	UNIT
Repetitive peak reverse voltage		$V_{\text{RRM}}$	100	V
Reverse voltage		$V_{\text{R}}$	75	V
Peak forward surge current	$t_{\text{p}} = 1\text{ }\mu\text{s}$	$I_{\text{FSM}}$	2	A
Repetitive peak forward current		$I_{\text{FRM}}$	500	mA
Forward continuous current		$I_{\text{F}}$	300	mA
Average forward current	$V_{\text{R}} = 0$	$I_{\text{F(AV)}}$	150	mA
Power dissipation	$l = 4\text{ mm}, T_{\text{L}} = 45\text{ }^{\circ}\text{C}$	$P_{\text{tot}}$	440	mW
	$l = 4\text{ mm}, T_{\text{L}} \leq 25\text{ }^{\circ}\text{C}$	$P_{\text{tot}}$	500	mW

$$I_{\text{D}}V_{\text{D}} < \text{power dissipation}$$

<b>THERMAL CHARACTERISTICS</b> ( $T_{\text{amb}} = 25\text{ }^{\circ}\text{C}$ , unless otherwise specified)				
PARAMETER	TEST CONDITION	SYMBOL	VALUE	UNIT
Thermal resistance junction to ambient air	$l = 4\text{ mm}, T_{\text{L}} = \text{constant}$	$R_{\text{thJA}}$	350	K/W
Junction temperature		$T_{\text{j}}$	175	$^{\circ}\text{C}$
Storage temperature range		$T_{\text{stg}}$	-65 to +150	$^{\circ}\text{C}$

# Diode data sheet

- Characteristics: Properties

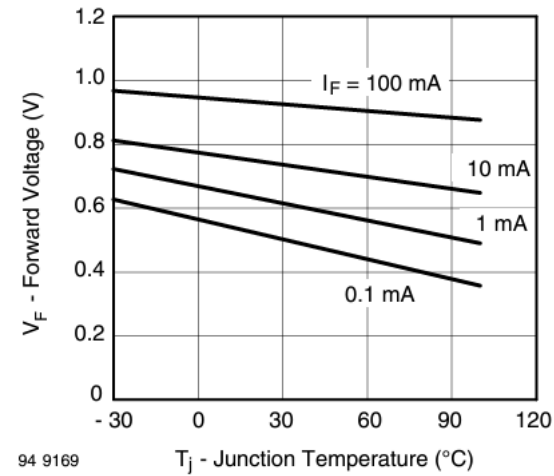


Fig. 1 - Forward Voltage vs. Junction Temperature

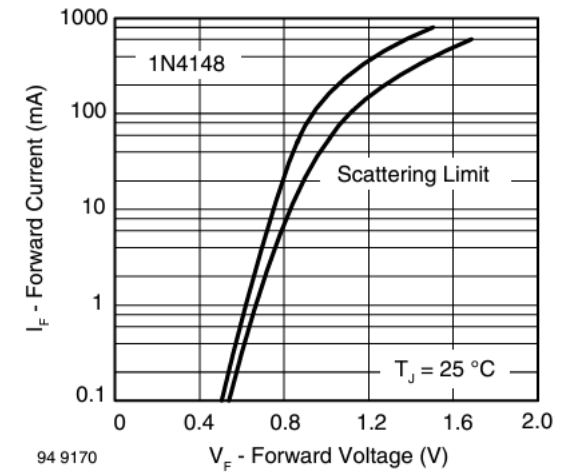


Fig. 2 - Forward Current vs. Forward Voltage

ELECTRICAL CHARACTERISTICS ( $T_{amb} = 25\text{ }^{\circ}\text{C}$ , unless otherwise specified)						
PARAMETER	TEST CONDITION	SYMBOL	MIN.	TYP.	MAX.	UNIT
Forward voltage	$I_F = 10\text{ mA}$	$V_F$			1	V
Reverse current	$V_R = 20\text{ V}$	$I_R$			25	nA
	$V_R = 20\text{ V}, T_J = 150\text{ }^{\circ}\text{C}$	$I_R$			50	$\mu\text{A}$
	$V_R = 75\text{ V}$	$I_R$			5	$\mu\text{A}$
Breakdown voltage	$I_R = 100\text{ }\mu\text{A}, t_p/T = 0.01,$ $t_p = 0.3\text{ ms}$	$V_{(BR)}$	100			V
Diode capacitance	$V_R = 0\text{ V}, f = 1\text{ MHz},$ $V_{HF} = 50\text{ mV}$	$C_D$			4	pF
Rectification efficiency	$V_{HF} = 2\text{ V}, f = 100\text{ MHz}$	$\eta_r$	45			%
Reverse recovery time	$I_F = I_R = 10\text{ mA},$ $i_R = 1\text{ mA}$	$t_{rr}$			8	ns
	$I_F = 10\text{ mA}, V_R = 6\text{ V},$ $i_R = 0.1 \times I_R, R_L = 100\text{ }\Omega$	$t_{rr}$			4	ns

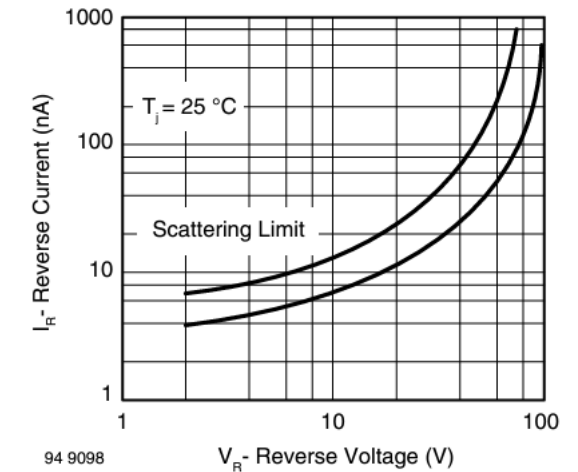
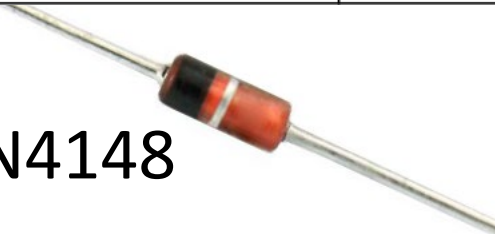


Fig. 3 - Reverse Current vs. Reverse Voltage

1N4148

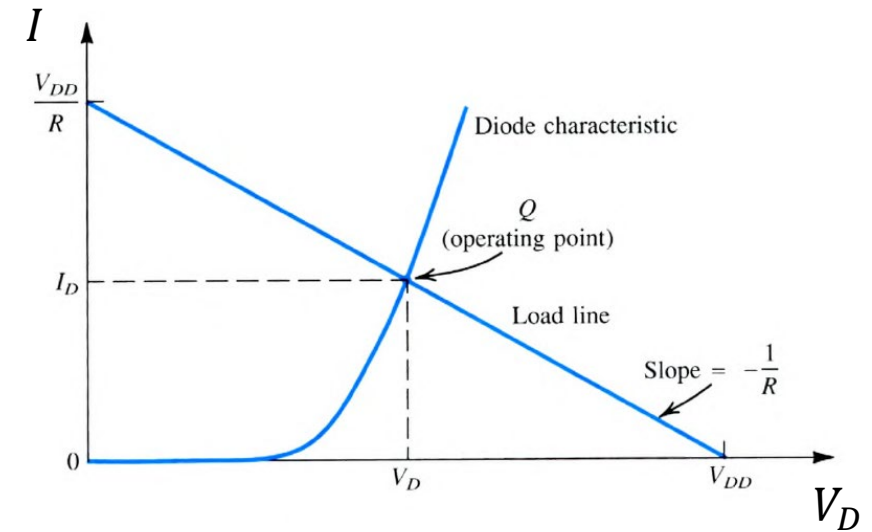
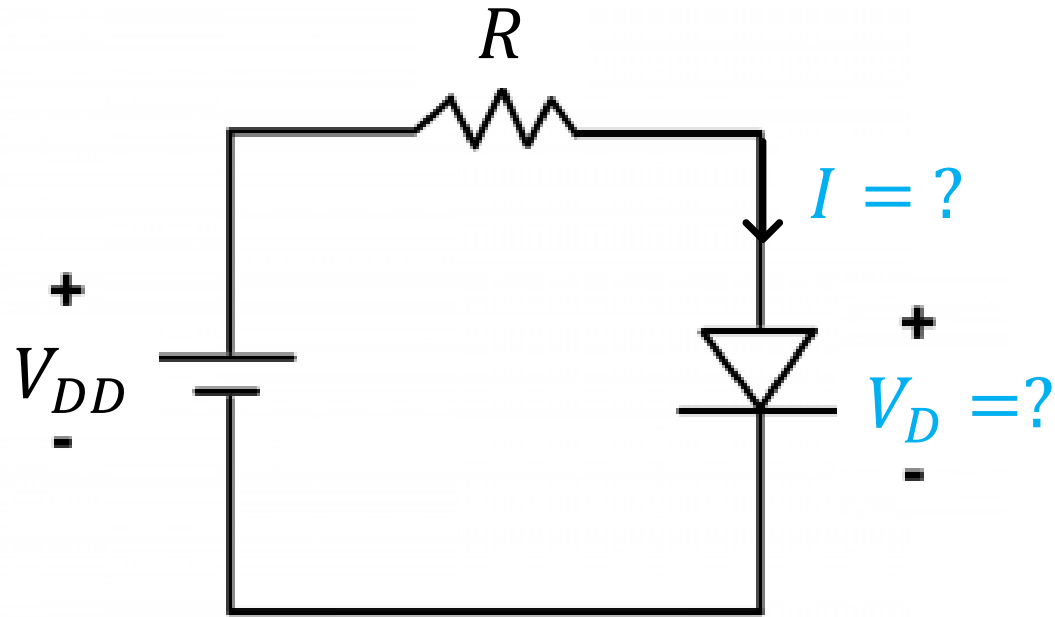


# LTspice simulation

- **Extract** of Spice parameters for diode
  - Some parameters are disabled by default
  - Default temperature 27°C= 300 K

Spice symbol	S & S symbol	Unit	Default value	1N4148 Motorola	Description
ICE	$I_{n_s}$	A	1e-14	2.52 n	Saturation current
N	n	-	1	1,752	Emission coefficient
RS	$R_s$	$\Omega$	0	0.568	Ohmic resistance
VJ	$V_0$	V	1		Built-in potential
CJO	$C_{j0}$	F	0	4 p.m	Zero-bias depletion cap.
M	m	-	0.5	0.4	Grading coefficient
TT	$\tau_T$	p	0	20 n	Transit time
BV	$V_{ZK}$	V	inf.		Breakdown voltage
IBV	$I_{n_{ZK}}$	A	reach		Reverse current @ $V_{ZK}$

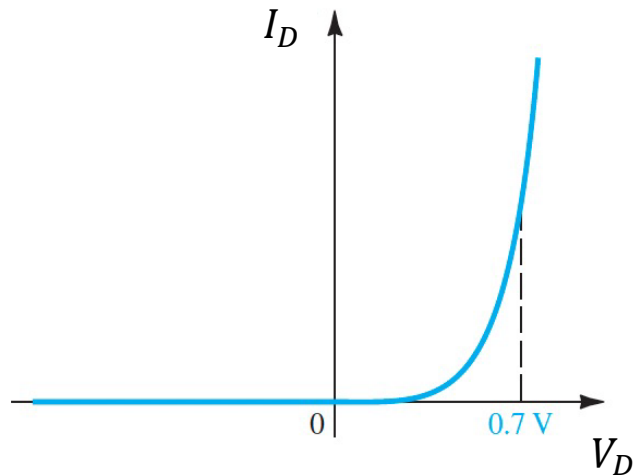
# PN diode



Can we solve the circuit by hand?

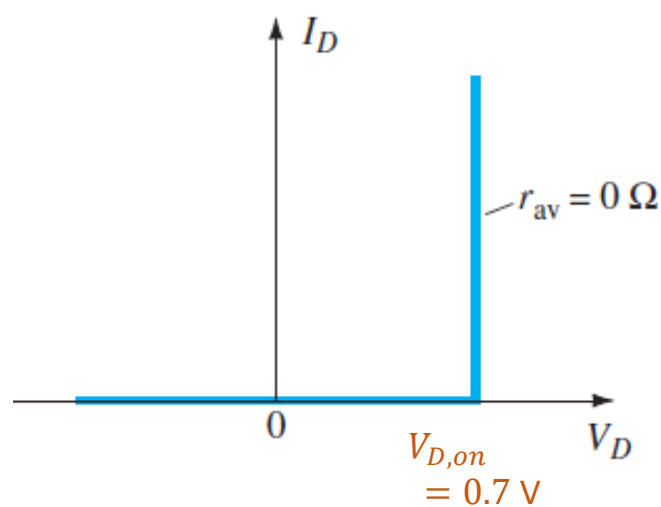
# PN diode models

Exponential model  
(usage rate = 10-20%)

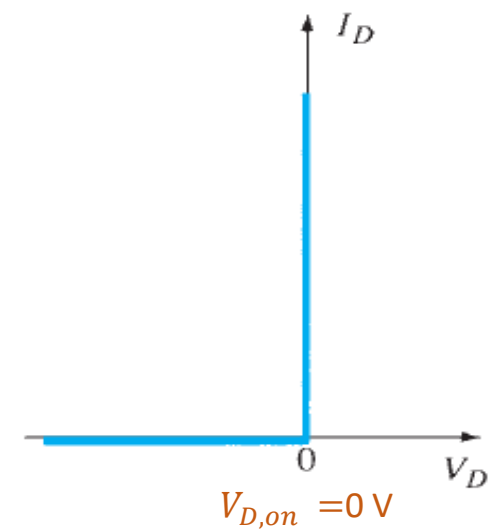


$$I_D \approx I_S e^{\frac{V_D}{V_T}}$$

Constant voltage drop model  
(usage rate = 70-80%)

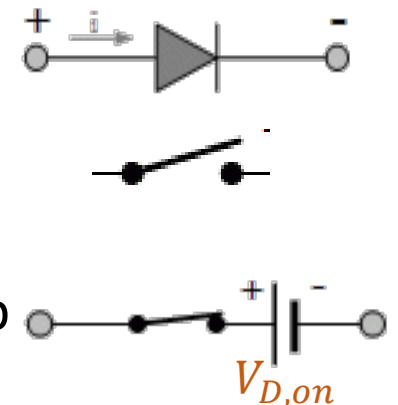


Ideal model  
(usage rate = 10-20%)

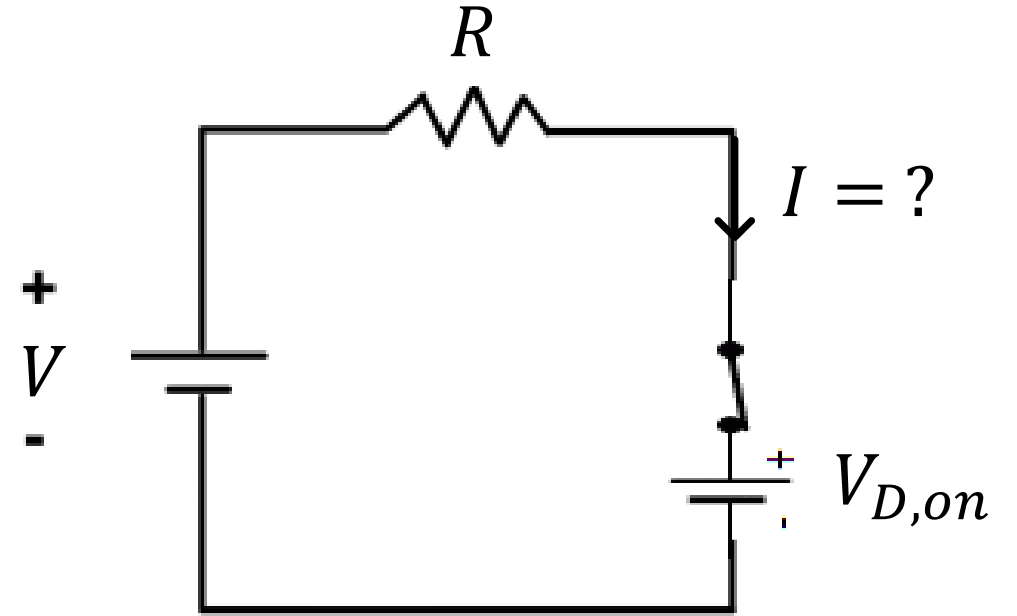
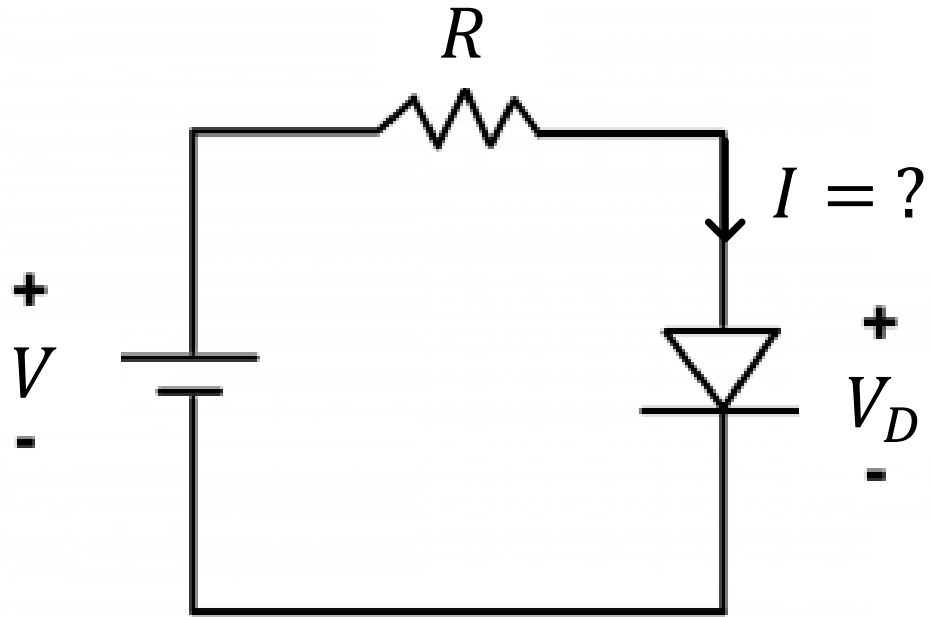


The diode has two states:

- $V_D < V_{D,on} \rightarrow$  diode is off  $\rightarrow$  open circuit
- $V_D \geq V_{D,on} \rightarrow$  diode is on  $\rightarrow$  a voltage drop



# PN diode circuit



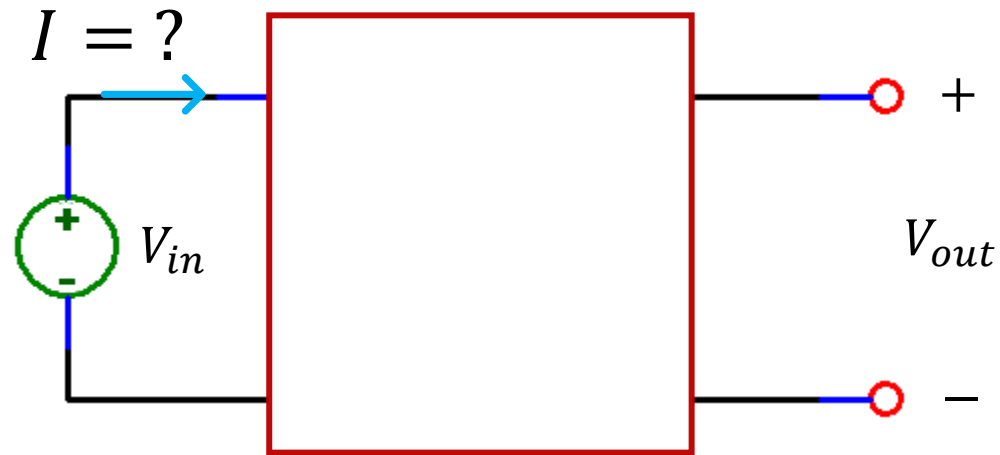
Assuming the constant voltage drop model,  
can we solve the circuit by hand?

$$I = \frac{V - V_{D,on}}{R}$$



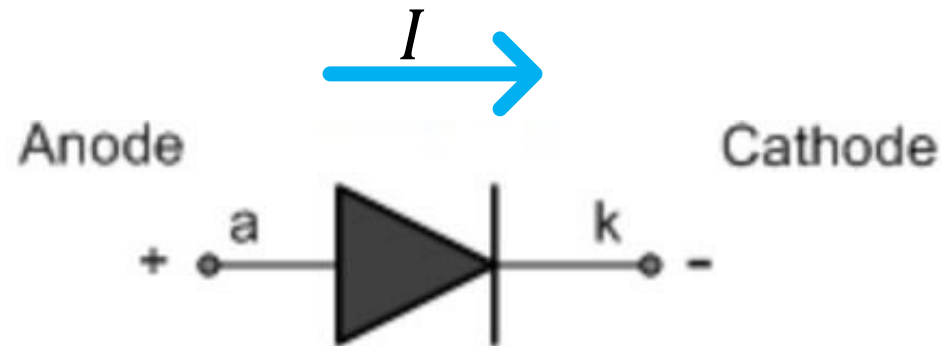
# Types of characteristics for circuits

- I-V characteristics
- Input-output characteristics
- Time response

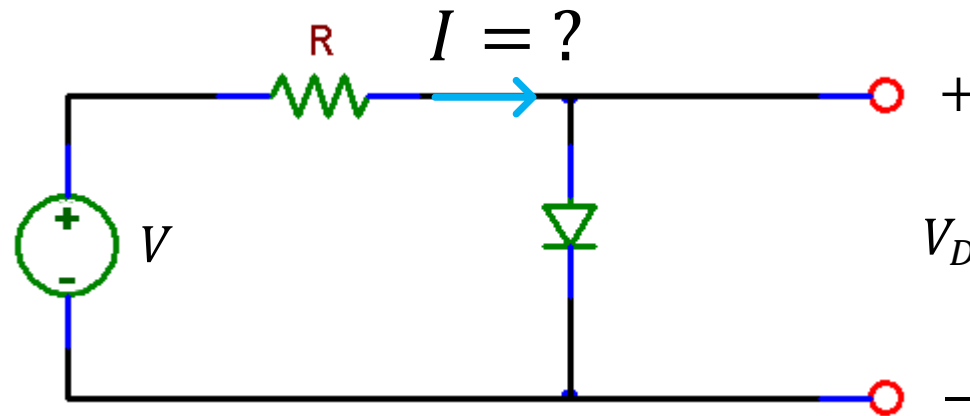


# Principle of diode circuit analysis

- Begin by assuming a certain state of diodes, i.e., on or off, check the final results against these assumptions.
- If a diode is about to turn on or off, it must sustain a voltage of  $V_{D,on}$ , but the current flowing through it is small, i.e., approximating 0 A
- If a diode is on and carries a current, the current must flow from the anode to the cathode, i.e., along the direction of the arrow.

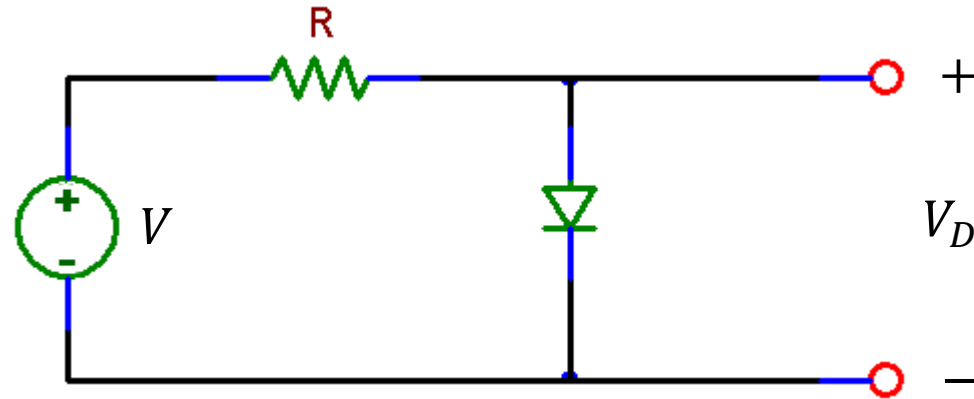


# PN diode circuit—I-V



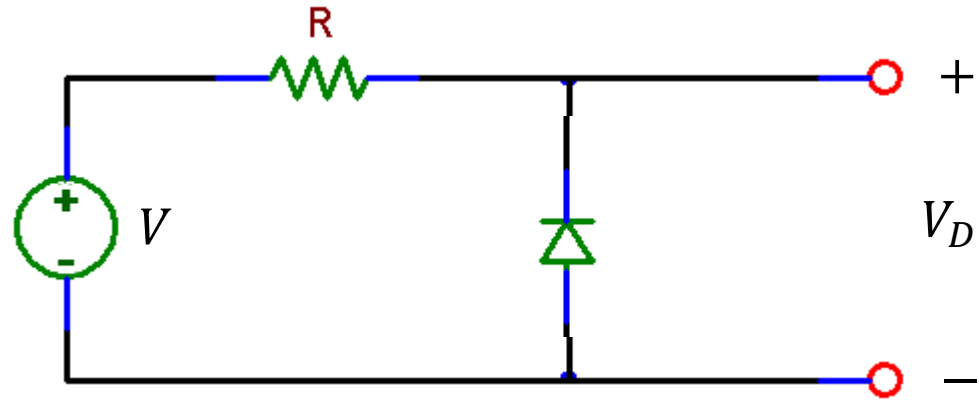
Assuming the constant voltage drop model, plot the I-V curve for the diode in reverse and forward bias regions.

# PN diode circuit – input-output



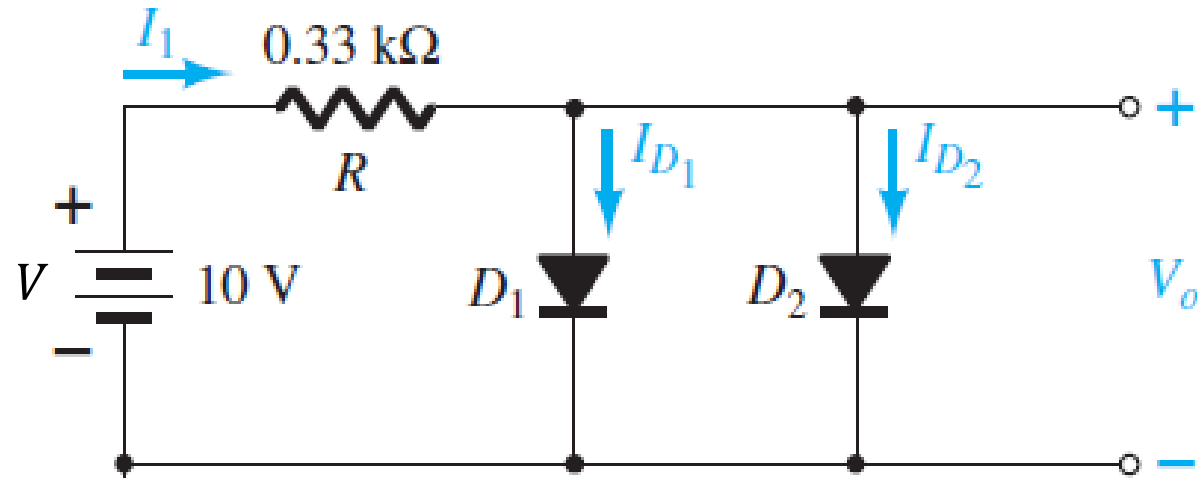
Assuming the constant voltage drop model, plot the  $V_D - V$  curve for the diode in reverse and forward bias regions.

# Quiz: PN diode circuit – input - output



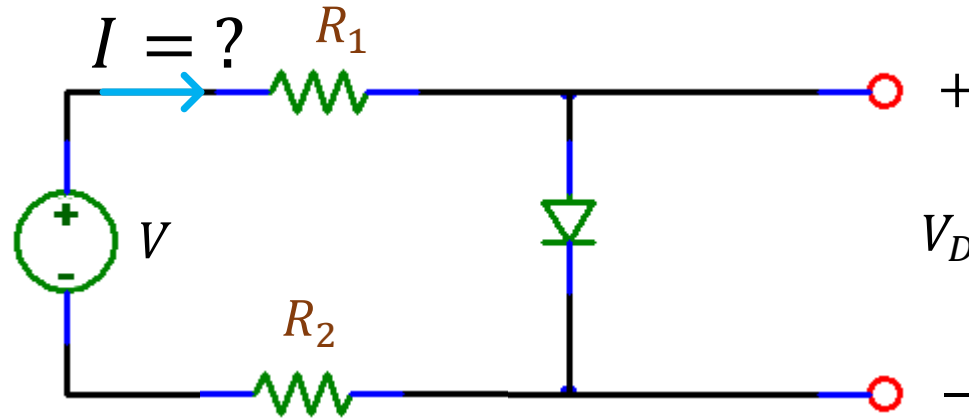
Assuming the constant voltage drop model and **flip the diode upside down**, plot the  $V_D - V$  curve for the diode in reverse and forward bias regions.

# Example



Assuming the constant voltage drop model and the diode in reverse and forward bias regions,  $I_1$ ,  $I_{D1}$ ,  $I_{D2}$  and  $V_o = ?$

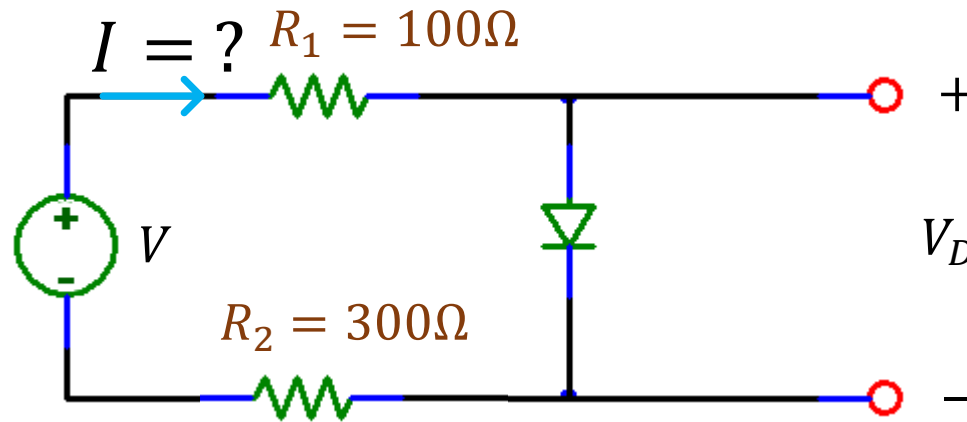
# PN diode circuit



Assuming the constant voltage drop model and the diode in reverse and forward bias regions,

- plot the I-V curve
- Plot the  $V_{R1}$ - $V$  curve
- Plot the  $V_D$ - $V$  curve
- Plot the  $V_{R2}$ - $V$  curve

# Quiz: PN diode circuit



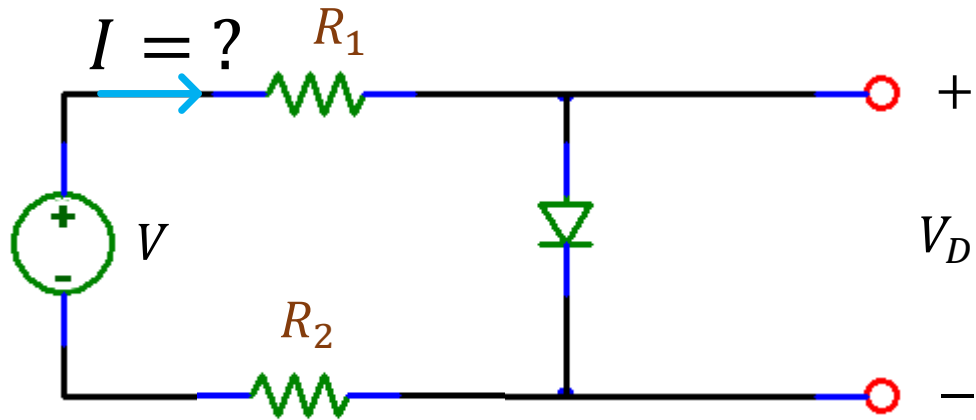
Assuming the constant voltage drop model and the diode in reverse and forward bias regions, the diode is on or off?  $I=?$   $V_{R1}=?$

$V_D=?$   $V_{R2}=?$

- When  $V = 0.5$  V
- When  $V = 0.7$  V
- When  $V = 2$  V



# PN diode circuit--LTspice



Assuming the constant voltage drop model and the diode in reverse and forward bias regions,

- plot the I-V curve
- Plot the  $V_{R1}$ - $V$  curve
- Plot the  $V_D$ - $V$  curve
- Plot the  $V_{R2}$ - $V$  curve

