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Side 316''

$$a) D_0 = 4N \left(\frac{d}{\lambda} \right) \quad D_0 = 20 \text{ dB} = 10^2 = 100$$

$$d = \frac{\lambda}{4}$$

$$100 = 4N \left(\frac{\frac{\lambda}{4}}{\lambda} \right) \Leftrightarrow N = \underline{\underline{100}}$$

$$b) L = 99 \cdot d = 99 \cdot \frac{\lambda}{4} = 24.75 \cdot \lambda$$

$$c) \text{HPBW} = 2 \cdot \cos^{-1} \left(1 - \frac{1.391 \cdot \lambda}{\pi N d} \right) = 2 \cdot \cos^{-1} \left(1 - \frac{1.391 \cdot \lambda}{\pi \cdot 100 \cdot \frac{\lambda}{4}} \right) = 2 \cdot \cos^{-1} \left(1 - \frac{5.564}{\pi \cdot 100} \right)$$

$$= 0.377 \text{ rad} = 21.6^\circ$$

d) -13 dB since it is almost a sinc function

$$e) \beta = \pm k d = \pm \frac{2\pi}{\lambda} \cdot \frac{\lambda}{4} = \pm \frac{\pi}{2} = \pm 90^\circ$$