

$$\Omega = \omega / \omega_d$$

7.2

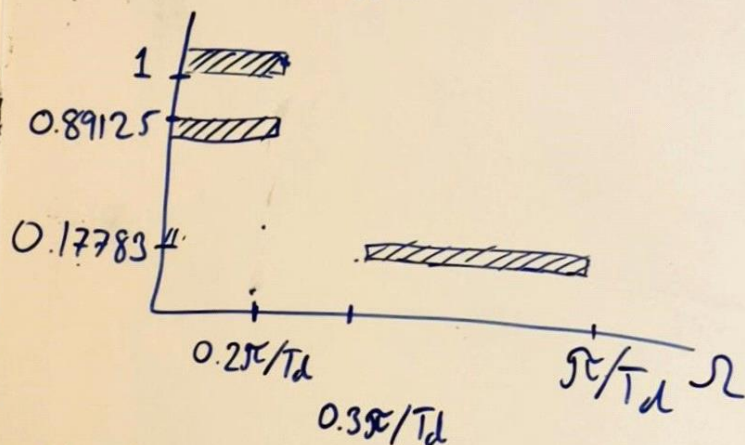
a)

$$0.89125 \leq |H(j\Omega)| \leq 1$$

$$|H(j\omega)| \leq 0.17783$$

$$0 \leq |\Omega| \leq 0.2\pi/T_d$$

$$0.3\pi/T_d \leq \pi/T_d$$



b) Butterworth Frequency response is monotonic

$$|H_c(j0.2\pi)|^2 = \frac{1}{1 + \left(\frac{0.2\pi}{\Omega_c T_d}\right)^{2N}} = (0.89125)^2$$

$$|H_c(j0.3\pi)|^2 = \frac{1}{1 + \left(\frac{0.3\pi}{\Omega_c T_d}\right)^{2N}} = (0.17783)^2$$

To get  $\Omega_c T_d = 0.704$ ,  $N = 5.88$

Round  $N$  up to 6 yields:  $\Omega_c T_d = 0.703$