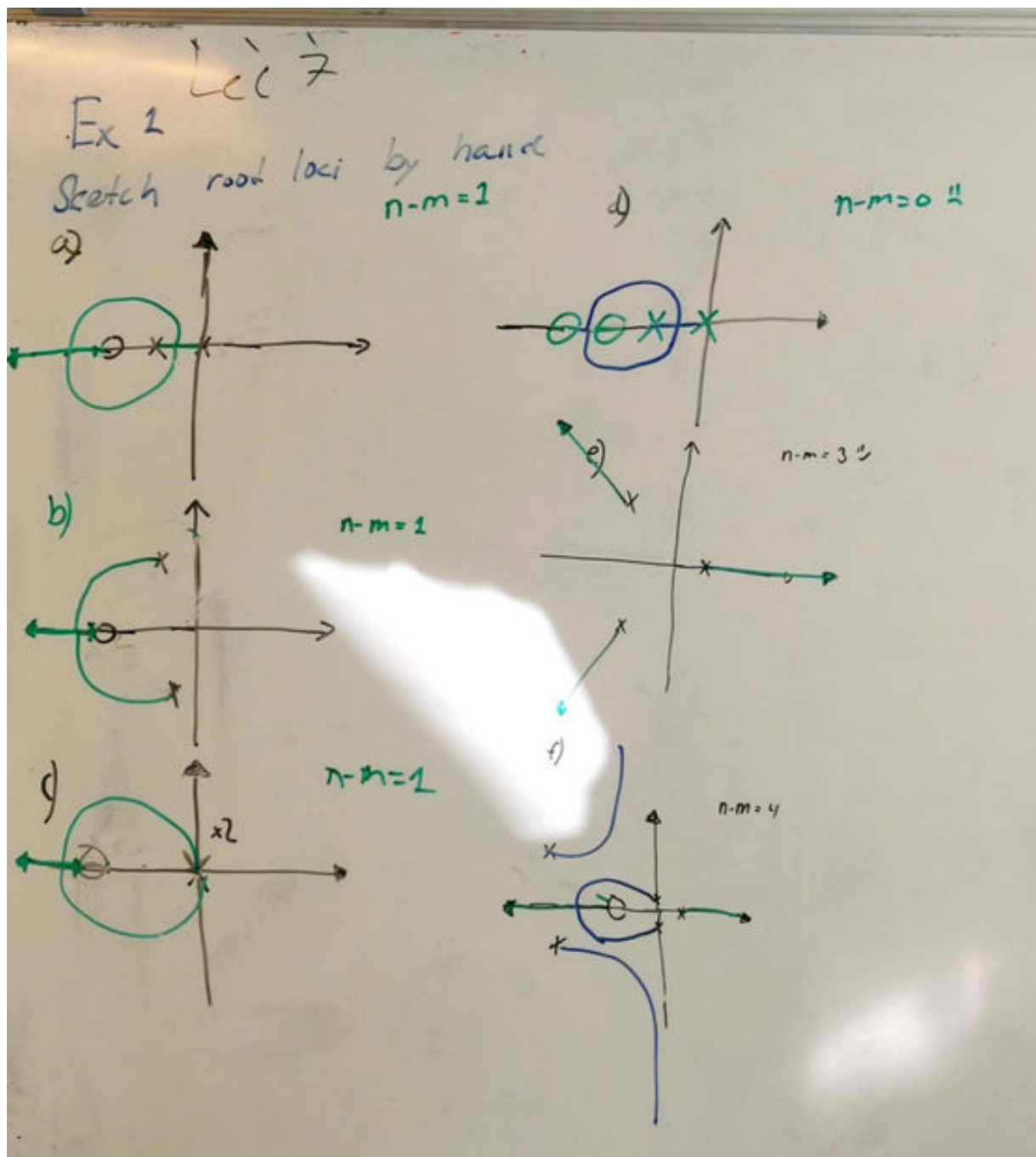


## Ex 1

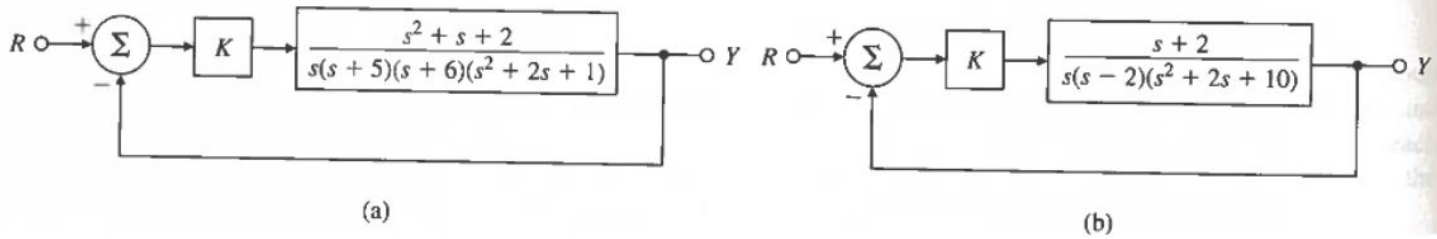


Konventionerne for rootlocus i hånden eller nærmere reglerne:

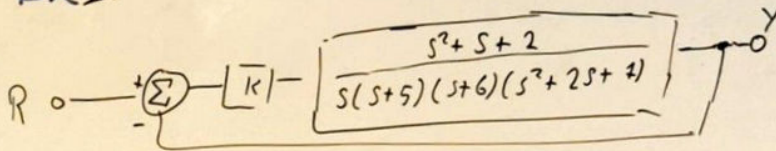
Se gennemgang på icloud for hvordan man tegner root locus.

## Ex 2

5.11 Use Routh's criterion to find the range of the gain  $K$  for which the systems in Fig. 5.53 are unstable, and use the root locus to confirm your calculations.



Ex 2 Lec 7



open loop:  $1 + D(s)G(s)H(s)$

$$D(s) = K$$

$$T(s) = 1 + K \frac{s^2 + s + 2}{s(s+5)(s+6)(s^2 + 2s + 1)}$$

$$\text{poly: } s^5 + 13s^4 + 53s^3 + (k+71)s^2 + (k+30)s + 2k$$

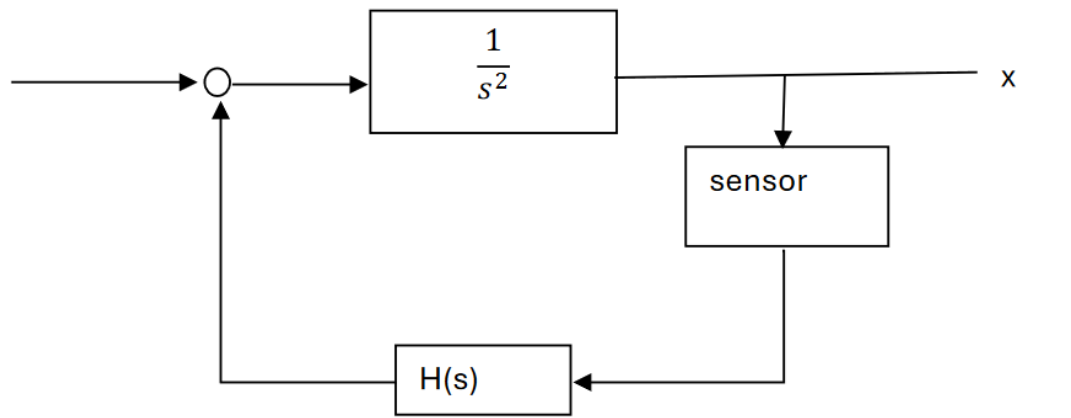
$$\begin{array}{l|lllll} s^5 & 1 & 53 & k+30 & 0 & \\ s^4 & 13 & (k+71) & 2k & 0 & \\ s^3 & 618-k & 11k+319 & 0 & 0 & \\ s^2 & c_1 & & & & \\ s^1 & & & & & \\ s^0 & & & & & \end{array}$$

$$b_1 = \frac{-(1 \cdot (k+71) - 13 \cdot 53)}{1} = 618 - k$$

$$b_2 = \frac{-(1 \cdot 2k - (13 \cdot (k+30)))}{1} = 11k + 319$$

$$c_1 = - \left( \frac{(13 \cdot (11k+319)) - ((618-k) \cdot (k+71))}{618-k} \right) = \frac{k^2 - 404k - 3923}{k-618}$$

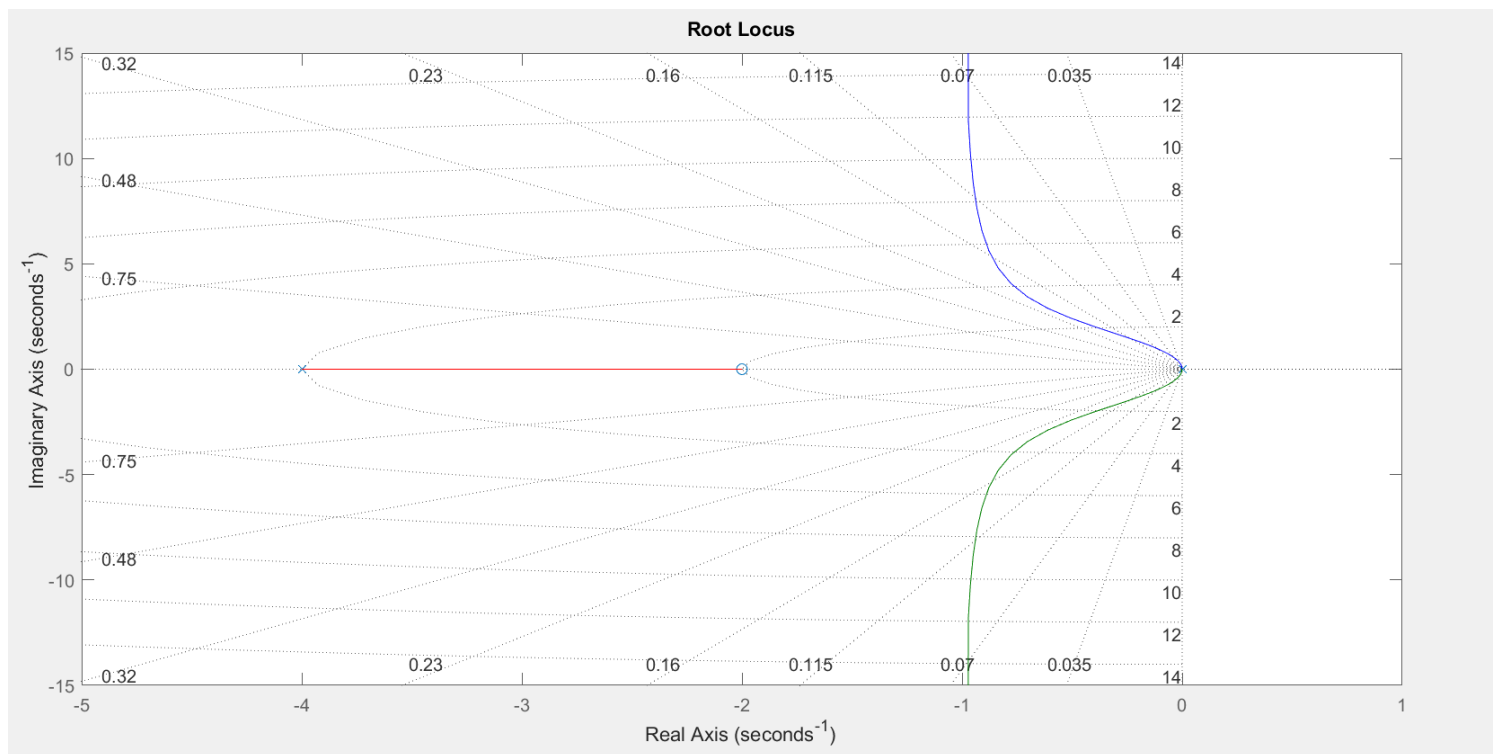
Ex 3



Show that if the sensor transferfunction =1, the lead compensator  $\Phi(s) = K \frac{s+2}{s+4}$  stabilizes the system

Use rootlocus and see that the system is stable.

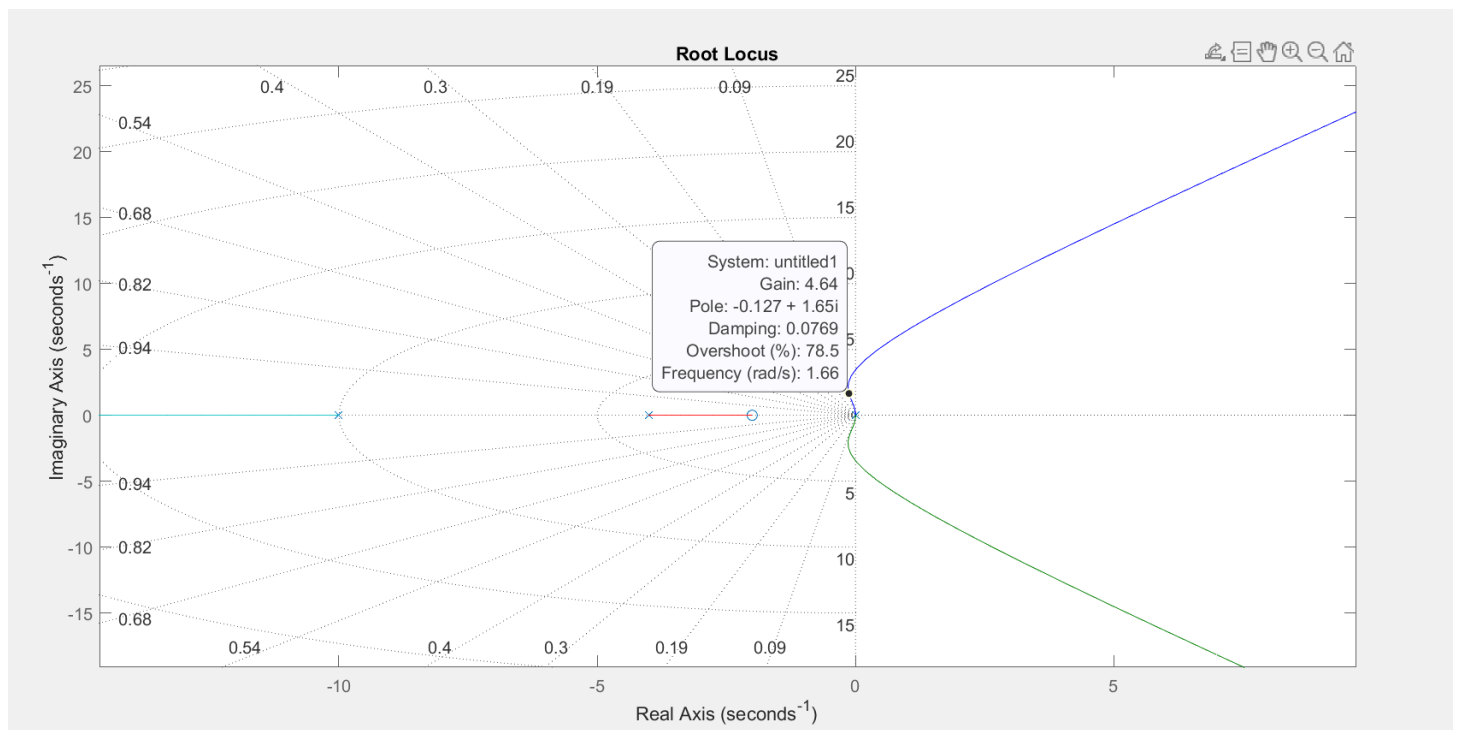
For  $H(s) = K \frac{s+2}{s+4}$



Assume that the sensor  $= \frac{1}{0.1s+1}$

Using the root locus, find a value for K that will give a maximum damping ration

For  $H(s) = \frac{1}{0.1s+1}$



Dette kan aflæses ud fra rootlocus hvoraf den maksimale damping kan findes ved en given K.

```
clear all
close
syms K
s = tf('s');
G = 1/s^2;
H = (s+2)/(s+4);
rlocus(G*H); %for 1 is stable since the root locus does not cross into the RHP of
the plot.
hold on
sen = 1/(0.1*s + 1);
% rlocus(sen*G*H);% for 2
sgrid
```