

transmitter ( $x_t$ )  
receiver ( $x_r$ )

$$x_t = (-2, -4)$$

$$\text{Power} = P(x) \propto \frac{1}{d^2} \quad d = \text{distance}$$

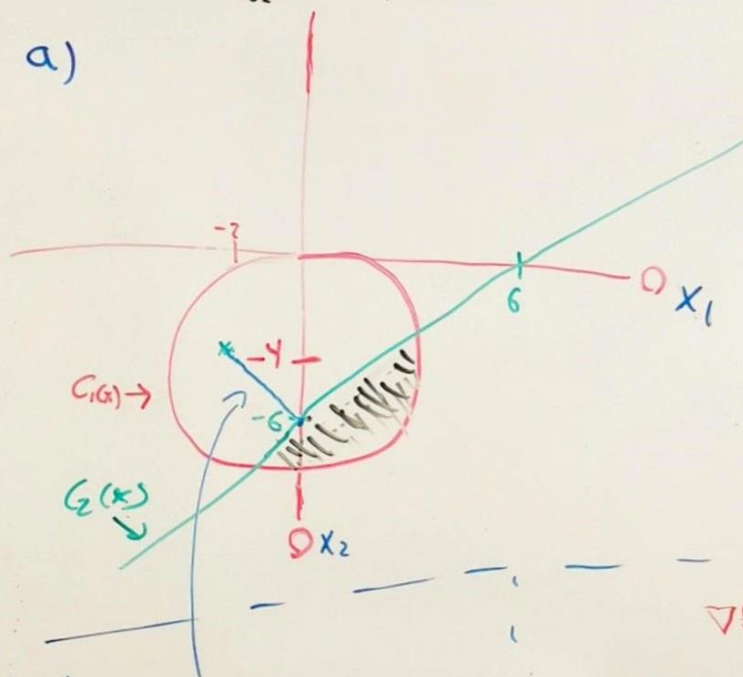
(max. this)

Constraints:

$$C_1(x) = -x_1^2 - (x_2 + 4)^2 + 16 \geq 0$$

$$C_2(x) = x_1 - x_2 - 6 \geq 0$$

a)



b) Cost function

$$f(x) = d^2 = |x_r - x_t|^2 = (x_{r,1} - (-2))^2 + (x_{r,2} - (-4))^2$$

$$\min |x_r - x_t|^2$$

s.t.

$$x_r \in \{x_r \in \mathbb{R}^2 \mid C_1(x_r), C_2(x_r)\}$$

d)

$$\nabla f(x_r) = \begin{pmatrix} 2(x_{r,1} + 2) \\ 2(x_{r,2} + 4) \end{pmatrix}$$

$$\nabla f(6, -6) = \begin{pmatrix} 4 \\ -4 \end{pmatrix}$$

$$\nabla f(x_r)^T d = (4 \ -4) \begin{pmatrix} d_1 \\ d_2 \end{pmatrix} = 4d_1 - 4d_2 \geq 0$$

since  $d_2 \leq d_1$

c) Solve graphically