Rapport Travaux Pratiques: Programmation par Contraintes

- TP 4:

Contraintes Logiques

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Dans ce T.P., nous allons utiliser la programmation par contraintes pour faire un planning pour organiser une régate, planning qui respecte certaines contraintes.

Question 4.1 Nous définissons ici un prédicat getData(?TailleEquipes, ?NbEquipes, ?CapaBateaux, ?NbBateaux, ?

```
Listing 1 - "getData"
```

```
getData(TailleEquipes, NbEquipes, CapaBateaux, NbBateaux, NbConf):-
2
             TailleEquipes = [](5,5,2,1),
3
            NbEquipes = 4,
4
            CapaBateaux = [](7,6,5),
5
            NbBateaux = 3,
6
            NbConf = 3.
8
   /* Tests
9
   [eclipse 7]: getData(TailleEq, NbEq, CapaBat, NbBat, NbConf).
10
11 TailleEq = [](5, 5, 2, 1)
12 \quad NbEq = 4
13 CapaBat = [](7, 6, 5)
14 \quad NbBat = 3
15 \quad NbConf = 3
16 Yes (0.00s cpu)
17 */
```

qui unifie les variables passées en paramètres avec les données du problème.

Question 4.2 Nous définissons ici un prédicat *defineVars(?T,+NbEquipes,+NbConf,+NbBateaux)* qui unifie T au tableau des variables et contraint le domaine des variables.

```
Listing 2 – "define Vars"
```

1 define Vars (T, NbEquipes, NbConf, NbBateaux):-

```
2
             dim(T, [NbEquipes, NbConf]),
3
             ( for (Ind1, 1, NbEquipes), param (T, NbBateaux, NbConf)
4
             do
5
                       ( for (Ind2, 1, NbConf), param (T, Ind1, NbBateaux)
6
                      do
7
                               T[Ind1, Ind2] #:: 1.. NbBateaux
8
                      )
9
             ).
10
    /* Tests
11
12
    [eclipse 8]: getData(TailleEq, NbEq, CapaBat, NbBat, NbConf), defineVars(T, NbEq,
        NbConf, NbBat).
13
    TailleEq = [](5, 5, 2, 1)
14
15
   NbEq = 4
   CapaBat = [](7, 6, 5)
16
   NbBat = 3
17
18
   NbConf = 3
   T = []([](\_419\{1 \dots 3\}, \_488\{1 \dots 3\}, \_557\{1 \dots 3\}), [](\_628\{1 \dots 3\}, \_697\{1 \dots 3\})]
19
        .. 3}, _766{1 .. 3}), [](_837{1 .. 3}, _906{1 .. 3}, _975{1 .. 3}), [](
        _1046{1 .. 3}, _1115{1 .. 3}, _1184{1 .. 3}))
20
    Yes (0.00s cpu)
21
    */
```

Question 4.3 Nous définissons ici un prédicat *getVarList(+T, ?L)* qui construit la liste L des variables contenues dans le tableau T. La liste des variables contient les variables de la première colonne suivies de celles de la seconde colonne, etc.

```
Listing 3 – "getVarList"
```

```
1
    getVarList(T,L):-
2
             dim(T, [NbEquipes, NbConf]),
3
             ( for (Indice1, 1, NbConf), fromto ([], In, Out, L), param (T, NbEquipes)
4
5
                       (for (Indice2, 1, NbEquipes), fromto ([], In2, Out2, L2), param (T,
                           Indice1)
6
                      do
7
                                Var is T[Indice2, Indice1],
8
                                append (In2, [Var], Out2)
9
                      ),
10
                      append (In, L2, Out)
11
             ) .
12
13
    /* Tests
14
                    getData(TailleEq, NbEq, CapaBat, NbBat, NbConf), defineVars(T, NbEq,
        NbConf, NbBat), getVarList(T, L).
15
    TailleEq = [](5, 5, 2, 1)
16
   NbEq = 4
17
18
    CapaBat = [](7, 6, 5)
19
   NbBat = 3
20 \quad NbConf = 3
```

```
21  T = []([](_484{1 ... 3}, _553{1 ... 3}, _622{1 ... 3}), [](_693{1 ... 3}, _762{1 ... 3}, _831{1 ... 3}), [](_902{1 ... 3}, _971{1 ... 3}, _1040{1 ... 3}), [](_1111{1 ... 3}, _1180{1 ... 3}, _1249{1 ... 3}))

22  L = [_484{1 ... 3}, _693{1 ... 3}, _902{1 ... 3}, _1111{1 ... 3}, _553{1 ... 3}, _762{1 ... 3}, _1140{1 ... 3}, _1180{1 ... 3}, _1180{1 ... 3}, _622{1 ... 3}, _831{1 ... 3}, _1040{1 ... 3}, _1249{1 ... 3}]

23  Yes (0.00s cpu)

24 */
```

Question 4.4 Nous définissons ici un prédicat *solve(?T)* qui résoud le problème des régates où seules les contraintes de domaines sont posées.

```
Listing 4 – "solve1"
```

```
solve1(T) :-
1
2
            getData(_TailleEquipes, NbEquipes, _CapaBateaux, NbBateaux, NbConf),
3
            define Vars (T, NbEquipes, NbConf, NbBateaux),
4
            getVarList(T,L),
5
            labeling (L).
6
7
   /* Tests
8
   [eclipse 10]: solve1(T).
   T = []([](1, 1, 1), [](1, 1, 1), [](1, 1, 1), [](1, 1, 1))
10
   Yes (0.00s cpu, solution 1, maybe more)?;
11
12
   T = []([](1, 1, 1), [](1, 1, 1), [](1, 1, 1), [](1, 1, 2))
13
   Yes (0.00s cpu, solution 2, maybe more)?;
14
15
   T = []([](1, 1, 1), [](1, 1, 1), [](1, 1, 1), [](1, 1, 3))
16
   Yes (0.00s cpu, solution 3, maybe more)?
17
```

Question 4.5 Nous définissons ici un prédicat *pasMemeBateaux*(+*T*,+*NbEquipes*,+*NbConf*) qui impose qu'une même équipe ne retourne pas deux fois sur le même bateau. On modifie ensuite le prédicat *solve* pour qu'il prenne en compte cette nouvelle contrainte.

Listing 5 – "pasMemeBateaux"

```
pasMemeBateaux (T, NbEquipes, NbConf):-
1
             dim(T, [NbEquipes, NbConf]),
3
             ( for (Indice1, 1, NbEquipes), param (T, NbConf)
4
5
                      (for (Indice2, 1, NbConf), fromto ([], In, Out, L), param (T, Indice1
6
                      do
7
                               Bat is T[Indice1, Indice2],
8
                               append(In,[Bat],Out)
9
10
                      alldifferent(L)
11
             ) .
12
```

```
13
   solve2(T) :-
            getData(_TailleEquipes, NbEquipes, _CapaBateaux, NbBateaux, NbConf),
14
15
            define Vars (T, NbEquipes, NbConf, NbBateaux),
16
            pasMemeBateaux (T, NbEquipes, NbConf),
17
            getVarList(T,L),
18
            labeling(L).
19
20
   /* Tests
   [eclipse 11]: solve2(T).
21
23
   T = []([](1, 2, 3), [](1, 2, 3), [](1, 2, 3), [](1, 2, 3))
24
   Yes (0.00s cpu, solution 1, maybe more)?;
25
   T = []([](1, 2, 3), [](1, 2, 3), [](1, 2, 3), [](1, 3, 2))
26
27
   Yes (0.00s cpu, solution 2, maybe more)?;
28
29
   T = []([](1, 2, 3), [](1, 2, 3), [](1, 3, 2), [](1, 2, 3))
30
   Yes (0.00s cpu, solution 3, maybe more)?
   */
```

Question 4.6 Nous définissons ici un prédicat *pasMemePartenaires*(+*T*,+*NbEquipes*,+*NbConf*) qui impose qu'une même équipe ne se retrouve pas deux fois avec la même équipe. On modifie une nouvelle fois le prédicat *solve* pour qu'il prenne en compte cette nouvelle contrainte.

Listing 6 – "pasMemePartenaires"

```
pasMemePartenaires (T, NbEquipes, NbConf):-
1
             dim(T,[NbEquipes,NbConf]),
2
3
             ( for (Equipe1, 1, NbEquipes), param (T, NbConf, NbEquipes)
4
5
                      Indice is Equipe1+1,
6
                      ( for (Equipe2, Indice, NbEquipes), param (T, Equipe1, NbConf)
7
8
9
                               ( for (Conf, 1, NbConf), param (T, Equipe 1, Equipe 2), from to
                                    (0, In, Out, Tot)
10
                               d٥
                                         Bateau1 is T[Equipe1, Conf],
11
12
                                         Bateau2 is T[Equipe2, Conf],
13
                                         #=(Bateau1, Bateau2, Ans),
                                         Out #= In + Ans
14
15
16
                               Tot #=< 1
17
                      )
18
             ) .
19
20
    solve3(T) :-
             getData(_TailleEquipes, NbEquipes, _CapaBateaux, NbBateaux, NbConf),
21
22
             define Vars (T, NbEquipes, NbConf, NbBateaux),
23
             pasMemeBateaux (T, NbEquipes, NbConf),
             pas Meme Partenaires (T, Nb Equipes, Nb Conf),
24
25
             getVarList(T,L),
26
             labeling(L).
```

```
27
28
   /* Tests
29
   [eclipse 12]: solve3(T).
30
31
   T = []([](1, 2, 3), [](1, 3, 2), [](2, 1, 3), [](2, 3, 1))
32
   Yes (0.00s cpu, solution 1, maybe more)?;
33
34
   T = []([](1, 2, 3), [](1, 3, 2), [](2, 3, 1), [](2, 1, 3))
35
   Yes (0.00s cpu, solution 2, maybe more)?;
   T = []([](1, 3, 2), [](1, 2, 3), [](2, 1, 3), [](2, 3, 1))
37
   Yes (0.00s cpu, solution 3, maybe more)?
38
39
   */
```

Question 4.7 Nous définissons ici un prédicat *capaBateaux*(+*T*,+*TailleEquipes*,+*NbEquipes*,+*CapaBateaux*,+*NbE* qui vérifie que les capacités des bateaux sont respectées lors de chaque confrontation. On modifie une nouvelle fois le prédicat *solve* pour qu'il prenne en compte cette nouvelle contrainte.

Listing 7 – "capaBateaux"

```
capaBateaux (T, TailleEquipes, NbEquipes, CapaBateaux, NbBateaux, NbConf):-
1
2
             dim(T, [NbEquipes, NbConf]),
3
             ( for (Bateau, 1, NbBateaux), param (T, NbEquipes, NbConf, CapaBateaux,
                 TailleEquipes)
4
             do
5
                      (for (Conf, 1, NbConf), param (T, NbEquipes, Bateau, CapaBateaux,
                          TailleEquipes)
6
                      do
7
                               ( for (Equipe, 1, NbEquipes), param (T, Bateau, Conf,
                                   TailleEquipes), fromto(0, In, Out, Total)
8
9
                                        BateauI is T[Equipe, Conf],
10
                                        #=(Bateau, BateauI, Cond),
11
                                        Inc #= TailleEquipes[Equipe] * Cond,
12
                                        Out \#= In + Inc
13
14
                               Capacite is CapaBateaux [Bateau],
15
                               Total #=< Capacite
16
                      )
17
             ) .
18
19
    solve4(T) :-
20
             getData (TailleEquipes, NbEquipes, CapaBateaux, NbBateaux, NbConf),
21
             define Vars (T, NbEquipes, NbConf, NbBateaux),
22
             pasMemeBateaux (T, NbEquipes, NbConf),
             pas Meme Partenaires (T, Nb Equipes, Nb Conf),
23
24
             capaBateaux (T, TailleEquipes, NbEquipes, CapaBateaux, NbBateaux, NbConf),
25
             getVarList(T,L),
26
             labeling(L).
27
28
   /* Tests
   [eclipse 13]: solve4(T).
30
```

```
31  T = []([](1, 2, 3), [](2, 3, 1), [](3, 1, 2), [](3, 2, 1))
32  Yes (0.01s cpu, solution 1, maybe more) ?;
33
34  T = []([](1, 3, 2), [](2, 1, 3), [](3, 2, 1), [](3, 1, 2))
35  Yes (0.01s cpu, solution 2, maybe more) ?;
36
37  T = []([](1, 2, 3), [](3, 1, 2), [](2, 3, 1), [](1, 3, 2))
38  Yes (0.01s cpu, solution 3, maybe more) ?
39 */
```

Question 4.8 On passe ici à un problème de taille réelle. On dispose dorénavant de 13 voiliers et de 29 équipes qui doivent effectuer la régate comportant 7 confrontations.

Le temps d'exécution étant relativement long, il nous a été proposé d'améliorer le labeling. Pour cela, nous avons mélanger la liste des varaibles obtenu après *getVarList*, en alternant simplement les grosses et les petites équipes. Le gain sur le temps d'exécution est relativement important, puisqu'il est quasiment de 10!

Listing 8 – "Problème de taille réelle et labeling"

```
getData2(TailleEquipes, NbEquipes, CapaBateaux, NbBateaux, NbConf):-
2
              TailleEquipes =
                  3
              NbEquipes = 29,
4
              CapaBateaux = [](10,10,9,8,8,8,8,8,8,7,6,4,4),
5
              NbBateaux = 13,
             NbConf = 7.
6
7
8
    solve5(T):-
9
              getData2 (TailleEq, NbEq, CapaBat, NbBat, NbConf),
10
              define Vars (T, NbEq, NbConf, NbBat),
11
              pasMemeBateaux (T, NbEq, NbConf),
12
              pas Meme Partenaires (T, NbEq, NbConf),
13
              capaBateaux (T, TailleEq, NbEq, CapaBat, NbBat, NbConf),
14
              getVarList(T,L),
15
              labeling(L).
16
17
    /* Tests
18
   [eclipse 14]: solve5(T).
19
  T = []([](1, 2, 3, 4, 5, 6, 7), [](2, 1, 4, 3, 6, 5, 8), [](3, 4, 1, 2, 7, 8, 7)]
        5), [](4, 3, 1, 5, 2, 7, 6), [](5, 6, 2, 1, 3, 4, 9), [](2, 3, 5, 1, 4, 9, 10), [](3, 1, 2, 6, 4, 10, 11), [](6, 5, 7, 2, 1, 3, 4), [](6, 7, 5, 8, 2, 1, 3), [](7, 5, 6, 8, 3, 2, 1), [](7, 8, 9, 6, 1, 11, 2), [](8, 7, 6, 9, 10, 12, 2), [](8, 9, 7, 10, 11, 1, 12), [](1, 4, 8, 3, 9, 7, 10),
        [](4, 2, 8, 10, 7, 3, 9), [](5, 8, 3, 11, 6, 9, 1), [](9, 6, 4, 5, 8, 11,
         13), [](9, 8, 10, 12, 13, 2, 11), [](9, 10, 8, 11, 12, 13, 2), [](9, 11,
         12, 13, 1, 10, 3), [](10, 9, 11, 7, 12, 3, 13), [](10, 11, 9, 12, 8, 1,
        4), [](10, 12, 13, 11, 9, 2, 3), [](11, 9, 10, 13, 8, 4, 5), [](11, 10,
        12, 9, 13, 5, 1), [](11, 12, 9, 7, 10, 13, 8), [](12, 10, 13, 7, 11, 9,
        4), [](12, 13, 11, 9, 8, 2, 6), [](13, 11, 10, 7, 9, 8, 1))
   Yes (55.23s cpu, solution 1, maybe more)?
22 */
```

```
23
24
   % Amelioration du labeling pour gagner du temps
25
26
   getLast([A],A,[]).
2.7
   getLast([A|R],B,[A|L]):= getLast(R,B,L).
28
29
   debutfin([A|R],A,L,B) := getLast(R,B,L).
30
   debutfin([A,B,C],A,[A,C,B],C).
31
32.
   melangListe([],[]).
33
   melangListe([A,B,C],[A,C,B]):-!.
34
   melangListe(L,[A,B|L2]) :- debutfin(L,A,L1,B), melangListe(L1,L2).
35
36
   getVarList2(T,L):-
37
           dim(T,[NbEquipes,NbConf]),
38
           ( for (Indice1, 1, NbConf), fromto ([], In, Out, L), param (T, NbEquipes)
39
           do
40
                   (for (Indice2, 1, NbEquipes), fromto ([], In2, Out2, L2), param (T,
                       Indice1)
41
                   do
42
                           Var is T[Indice2, Indice1],
43
                           append (In2, [Var], Out2)
44
45
                   melangListe(L2,L3),
46
                   append (In, L3, Out)
47
           ) .
48
49
   solve6(T):-
50
           getData2 (TailleEq, NbEq, CapaBat, NbBat, NbConf),
51
           define Vars (T, NbEq, NbConf, NbBat),
52
           pasMemeBateaux (T, NbEq, NbConf),
53
           pas Meme Partenaires (T, NbEq, NbConf),
54
           capaBateaux (T, TailleEq, NbEq, CapaBat, NbBat, NbConf),
55
           getVarList2(T,L),
           labeling (L).
56
57
58
   /* Tests
59
   [eclipse 15]: solve6(T).
60
   T = []([](1, 2, 3, 4, 5, 6, 7), [](2, 1, 4, 3, 6, 5, 8), [](3, 4, 1, 2, 8, 7, 7, 7)]
        9), [](4, 3, 5, 1, 2, 9, 10), [](5, 6, 2, 7, 1, 3, 4), [](6, 5, 7, 2, 1,
        4, 3), [](6, 7, 8, 5, 2, 1, 11), [](7, 5, 6, 8, 9, 1, 2), [](8, 9, 7, 1)
       10, 4, 11, 5), [](8, 10, 9, 6, 11, 3, 2), [](9, 8, 12, 13, 7, 2, 6),
       3,\ 8,\ 9,\ 4)\,,\ [](11,\ 12,\ 10,\ 7,\ 3,\ 13,\ 9)\,,\ [](13,\ 11,\ 10,\ 9,\ 6,\ 1,\ 5)\,,
       [](3, 2, 4, 1, 7, 11, 12), [](3, 1, 2, 6, 9, 10, 11), [](2, 4, 3, 1, 9, 8, 6), [](2, 3, 1, 6, 7, 4, 5), [](1, 3, 2, 5, 4, 7, 6))
   Yes (6.98s cpu, solution 1, maybe more)?;
62
```

```
64 T = []([](1, 2, 3, 4, 5, 6, 7), [](2, 1, 4, 3, 6, 5, 8), [](3, 4, 1, 2, 8, 7, 9), [](4, 3, 5, 1, 2, 9, 10), [](5, 6, 2, 7, 1, 3, 4), [](6, 5, 7, 2, 1, 4, 11), [](6, 7, 8, 5, 2, 1, 3), [](7, 5, 6, 8, 9, 1, 2), [](8, 9, 7, 10, 4, 11, 5), [](8, 10, 9, 6, 11, 3, 2), [](9, 8, 12, 13, 7, 2, 6), [](10, 9, 8, 11, 13, 12, 1), [](12, 13, 11, 9, 10, 8, 1), [](11, 10, 13, 3, 8, 9, 4), [](11, 12, 10, 7, 3, 13, 9), [](13, 11, 10, 9, 6, 1, 5), [](13, 8, 11, 12, 4, 10, 3), [](10, 11, 9, 8, 12, 2, 3), [](9, 11, 6, 12, 10, 5, 13), [](9, 7, 10, 11, 12, 8, 2), [](7, 8, 9, 10, 3, 4, 1), [](7, 6, 5, 9, 11, 2, 8), [](5, 7, 1, 8, 3, 10, 13), [](4, 1, 6, 5, 3, 2, 12), [](3, 2, 4, 1, 7, 11, 12), [](3, 1, 2, 6, 9, 10, 11), [](2, 4, 3, 1, 9, 8, 6), [](2, 3, 1, 6, 7, 4, 5), [](1, 3, 2, 5, 4, 7, 6))
65 Yes (7.31s cpu, solution 2, maybe more)?
```

1 Code Complet, avec l'ensemble des tests

```
Listing 9 - "TP4"
   :-lib(ic).
2
3
   % Q4.1
    getData(TailleEquipes, NbEquipes, CapaBateaux, NbBateaux, NbConf):-
             TailleEquipes = [](5,5,2,1),
             NbEquipes = 4,
6
             CapaBateaux = [](7,6,5),
7
8
             NbBateaux = 3,
9
             NbConf = 3.
10
11
   [eclipse 7]: getData(TailleEq, NbEq, CapaBat, NbBat, NbConf).
13
14
   TailleEq = [](5, 5, 2, 1)
15 \quad NbEq = 4
16 CapaBat = [](7, 6, 5)
   NbBat = 3
17
18 \quad NbConf = 3
19
    Yes (0.00s cpu)
20
21
22
   % Q4.2
23
    define Vars (T, NbEquipes, NbConf, NbBateaux):-
24
             dim(T,[NbEquipes, NbConf]),
25
             ( for (Ind1, 1, NbEquipes), param (T, NbBateaux, NbConf)
26
             do
27
                       ( for (Ind2, 1, NbConf), param (T, Ind1, NbBateaux)
28
                       do
29
                                T[Ind1, Ind2] #:: 1.. NbBateaux
30
                       )
31
             ) .
32
33
   /* Tests
    [eclipse 8]: getData(TailleEq, NbEq, CapaBat, NbBat, NbConf), defineVars(T, NbEq,
        NbConf , NbBat ) .
35
   TailleEq = [](5, 5, 2, 1)
36
37 \quad NbEq = 4
38 \quad CapaBat = [](7, 6, 5)
39 \quad NbBat = 3
40 \quad NbConf = 3
   T = []([](\_419\{1 \ \dots \ 3\}, \ \_488\{1 \ \dots \ 3\}, \ \_557\{1 \ \dots \ 3\}), \ [](\_628\{1 \ \dots \ 3\}, \ \_697\{1 \ \dots \ 3\})]
         .. 3}, _766{1 .. 3}), [](_837{1 .. 3}, _906{1 .. 3}, _975{1 .. 3}), [](
        _1046{1 .. 3}, _1115{1 .. 3}, _1184{1 .. 3}))
42
    Yes (0.00s cpu)
43
    */
44
45 % Q4.3
46 getVarList(T,L):-
```

```
47
              dim(T, [NbEquipes, NbConf]),
48
              ( for (Indice1, 1, NbConf), fromto ([], In, Out, L), param (T, NbEquipes)
49
              do
50
                         (for (Indice2, 1, NbEquipes), fromto ([], In2, Out2, L2), param (T,
                             Indice1)
51
                        do
52
                                  Var is T[Indice2, Indice1],
53
                                  append (In2, [Var], Out2)
54
                        ),
55
                        append (In, L2, Out)
56
              ) .
57
58
    /* Tests
59
    [eclipse 9]: getData(TailleEq, NbEq, CapaBat, NbBat, NbConf), defineVars(T, NbEq,
         NbConf, NbBat), getVarList(T, L).
60
    TailleEq = [](5, 5, 2, 1)
61
    NbEq = 4
62
63
    CapaBat = [](7, 6, 5)
   NbBat = 3
64
65
   NbConf = 3
   T = []([](\_484\{1 \ldots 3\}, \_553\{1 \ldots 3\}, \_622\{1 \ldots 3\}), [](\_693\{1 \ldots 3\}, \_762\{1 \ldots 3\})]
         \ldots 3}, _{831\{1} \ldots 3}), _{[](_{902\{1} \ldots 3}, _{_{971\{1}} \ldots 3}, _{_{1040\{1}} \ldots 3}), _{[](_{902\{1}
         _1111{1 .. 3}, _1180{1 .. 3}, _1249{1 .. 3}))
    L = \begin{bmatrix} -484\{1 \dots 3\}, -693\{1 \dots 3\}, -902\{1 \dots 3\}, -1111\{1 \dots 3\}, -553\{1 \dots 3\}, \\ -762\{1 \dots 3\}, -971\{1 \dots 3\}, -1180\{1 \dots 3\}, -622\{1 \dots 3\}, -831\{1 \dots 3\}, \end{bmatrix}
67
         _1040{1 .. 3}, _1249{1 .. 3}]
    Yes (0.00s cpu)
68
69
    */
70
71
   % Q4.4
72
73
    solve1(T) :-
              getData(_TailleEquipes, NbEquipes, _CapaBateaux, NbBateaux, NbConf),
74
75
              define Vars (T, NbEquipes, NbConf, NbBateaux),
76
              getVarList(T,L),
77
              labeling (L).
78
79
    /* Tests
80
    [eclipse 10]: solve1(T).
81
    T = []([](1, 1, 1), [](1, 1, 1), [](1, 1, 1), [](1, 1, 1))
82
83
    Yes (0.00s cpu, solution 1, maybe more)?;
84
85
    T = []([](1, 1, 1), [](1, 1, 1), [](1, 1, 1), [](1, 1, 2))
    Yes (0.00s cpu, solution 2, maybe more) ?;
86
87
88
    T = []([](1, 1, 1), [](1, 1, 1), [](1, 1, 1), [](1, 1, 3))
89
    Yes (0.00s cpu, solution 3, maybe more)?
90
    */
91
92
    % Q4.5
    pasMemeBateaux (T, NbEquipes, NbConf):-
```

```
94
             dim(T, [NbEquipes, NbConf]),
95
             ( for (Indice1, 1, NbEquipes), param (T, NbConf)
96
             do
97
                       (for (Indice2, 1, NbConf), fromto ([], In, Out, L), param (T, Indice1
98
                      do
                               Bat is T[Indice1, Indice2],
99
100
                               append(In,[Bat],Out)
101
                       ),
102
                       alldifferent(L)
103
              ) .
104
105
    solve2(T) :-
              getData(_TailleEquipes, NbEquipes, _CapaBateaux, NbBateaux, NbConf),
106
              define Vars (T, NbEquipes, NbConf, NbBateaux),
107
108
              pasMemeBateaux (T, NbEquipes, NbConf),
             getVarList(T,L),
109
110
              labeling(L).
111
    /* Tests
112
113
    [eclipse 11]: solve2(T).
115
    T = []([](1, 2, 3), [](1, 2, 3), [](1, 2, 3), [](1, 2, 3))
    Yes (0.00s cpu, solution 1, maybe more)?;
116
117
    T = []([](1, 2, 3), [](1, 2, 3), [](1, 2, 3), [](1, 3, 2))
118
    Yes (0.00s cpu, solution 2, maybe more)?;
119
120
121
    T = []([](1, 2, 3), [](1, 2, 3), [](1, 3, 2), [](1, 2, 3))
122
    Yes (0.00s cpu, solution 3, maybe more)?
123
124
125
    % Q4.6
126
    pasMemePartenaires (T, NbEquipes, NbConf):-
             dim(T,[NbEquipes,NbConf]),
127
              ( for (Equipe1, 1, NbEquipes), param (T, NbConf, NbEquipes)
128
129
             do
130
                      Indice is Equipe1+1,
131
                      ( for (Equipe2, Indice, NbEquipes), param (T, Equipe1, NbConf)
132
                      do
133
134
                               ( for (Conf, 1, NbConf), param (T, Equipe 1, Equipe 2), from to
                                   (0, In, Out, Tot)
135
                               do
136
                                        Bateaul is T[Equipe1, Conf],
                                        Bateau2 is T[Equipe2, Conf],
137
                                        #=(Bateau1, Bateau2, Ans),
138
                                        Out #= In + Ans
139
140
                               ),
                               Tot #=< 1
141
142
                      )
143
             ) .
144
```

```
145
    solve3(T) :-
             getData(_TailleEquipes, NbEquipes, _CapaBateaux, NbBateaux, NbConf),
146
147
             define Vars (T, NbEquipes, NbConf, NbBateaux),
148
             pasMemeBateaux (T, NbEquipes, NbConf),
149
             pas Meme Partenaires (T, Nb Equipes, Nb Conf),
150
             getVarList(T,L),
151
             labeling(L).
152
153
    /* Tests
154
    [eclipse 12]: solve3(T).
155
    T = []([](1, 2, 3), [](1, 3, 2), [](2, 1, 3), [](2, 3, 1))
156
    Yes (0.00s cpu, solution 1, maybe more)?;
157
158
159
    T = []([](1, 2, 3), [](1, 3, 2), [](2, 3, 1), [](2, 1, 3))
160
    Yes (0.00s cpu, solution 2, maybe more)?;
161
162
    T = []([](1, 3, 2), [](1, 2, 3), [](2, 1, 3), [](2, 3, 1))
163
    Yes (0.00s cpu, solution 3, maybe more)?
164
    */
165
166
    % Q4.7
167
    capaBateaux (T, TailleEquipes, NbEquipes, CapaBateaux, NbBateaux, NbConf):-
             dim(T, [NbEquipes, NbConf]),
168
             (for (Bateau, 1, NbBateaux), param (T, NbEquipes, NbConf, CapaBateaux,
169
                  TailleEquipes)
170
             do
171
                      (for (Conf, 1, NbConf), param (T, NbEquipes, Bateau, CapaBateaux,
                           TailleEquipes)
172
                      do
173
                               ( for (Equipe, 1, NbEquipes), param (T, Bateau, Conf,
                                   TailleEquipes), fromto(0, In, Out, Total)
174
                               do
175
                                        BateauI is T[Equipe, Conf],
                                        #=(Bateau, BateauI, Cond),
176
                                        Inc #= TailleEquipes[Equipe] * Cond,
177
                                        Out #= In + Inc
178
179
180
                               Capacite is CapaBateaux [Bateau],
181
                               Total #=< Capacite
182
                      )
183
             ).
184
185
    solve4(T) :-
186
             getData (TailleEquipes, NbEquipes, CapaBateaux, NbBateaux, NbConf),
187
             define Vars (T, NbEquipes, NbConf, NbBateaux),
             pasMemeBateaux (T, NbEquipes, NbConf),
188
189
             pas Meme Partenaires (T, Nb Equipes, Nb Conf),
190
             capaBateaux (T, TailleEquipes, NbEquipes, CapaBateaux, NbBateaux, NbConf),
191
             getVarList(T,L),
192
             labeling (L).
193
194
    /* Tests
```

```
195
    [eclipse 13]: solve4(T).
196
197
    T = []([](1, 2, 3), [](2, 3, 1), [](3, 1, 2), [](3, 2, 1))
198
    Yes (0.01s cpu, solution 1, maybe more)?;
199
200
    T = []([](1, 3, 2), [](2, 1, 3), [](3, 2, 1), [](3, 1, 2))
201
    Yes (0.01s cpu, solution 2, maybe more)?;
202
203
    T = []([](1, 2, 3), [](3, 1, 2), [](2, 3, 1), [](1, 3, 2))
204
    Yes (0.01s cpu, solution 3, maybe more)?
205
206
207
    % Q4.8
208
209
    getData2 (TailleEquipes, NbEquipes, CapaBateaux, NbBateaux, NbConf):-
210
             TailleEquipes =
                 211
             NbEquipes = 29,
212
             CapaBateaux = [](10,10,9,8,8,8,8,8,8,7,6,4,4),
213
             NbBateaux = 13,
             NbConf = 7.
214
215
216
    solve5(T):-
             getData2 (TailleEq, NbEq, CapaBat, NbBat, NbConf),
217
             define Vars (T, NbEq, NbConf, NbBat),
218
219
             pasMemeBateaux (T, NbEq, NbConf),
             pas Meme Partenaires (T, NbEq, NbConf),
220
221
             capaBateaux (T, TailleEq, NbEq, CapaBat, NbBat, NbConf),
222
             getVarList(T,L),
223
             labeling (L).
224
225
    /* Tests
226
    [eclipse 14]: solve5(T).
227
    T = []([](1,\ 2,\ 3,\ 4,\ 5,\ 6,\ 7)\,,\ [](2,\ 1,\ 4,\ 3,\ 6,\ 5,\ 8)\,,\ [](3,\ 4,\ 1,\ 2,\ 7,\ 8,
228
        5), [](4, 3, 1, 5, 2, 7, 6), [](5, 6, 2, 1, 3, 4, 9), [](2, 3, 5, 1, 4, 9, 10), [](3, 1, 2, 6, 4, 10, 11), [](6, 5, 7, 2, 1, 3, 4), [](6, 7, 5,
        8,\ 2,\ 1,\ 3), [](7, 5, 6, 8, 3, 2, 1), [](7, 8, 9, 6, 1, 11, 2), [](8, 7,
        6, 9, 10, 12, 2), [](8, 9, 7, 10, 11, 1, 12), [](1, 4, 8, 3, 9, 7, 10),
        13), [](9, 8, 10, 12, 13, 2, 11), [](9, 10, 8, 11, 12, 13, 2), [](9, 11, 12, 13, 2)
         12, 13, 1, 10, 3), [](10, 9, 11, 7, 12, 3, 13), [](10, 11, 9, 12, 8, 1,
        4), [](10, 12, 13, 11, 9, 2, 3), [](11, 9, 10, 13, 8, 4, 5), [](11, 10,
        12, 9, 13, 5, 1), [](11, 12, 9, 7, 10, 13, 8), [](12, 10, 13, 7, 11, 9,
        4), [](12, 13, 11, 9, 8, 2, 6), [](13, 11, 10, 7, 9, 8, 1))
229
    Yes (55.23s cpu, solution 1, maybe more)?
230
231
232
    % Amelioration du labeling pour gagner du temps
233
234
    getLast([A],A,[]).
235
    getLast([A|R],B,[A|L]):= getLast(R,B,L).
236
```

```
237
            debutfin([A|R],A,L,B) := getLast(R,B,L).
238
            debutfin([A,B,C],A,[A,C,B],C).
239
240
            melangListe([],[]).
241
            melangListe([A,B,C],[A,C,B]):-!.
242
            melangListe(L,[A,B|L2]) :- debutfin(L,A,L1,B), melangListe(L1,L2).
243
244
            getVarList2(T,L):-
245
                                   dim(T, [NbEquipes, NbConf]),
246
                                    ( for (Indice1, 1, NbConf), fromto ([], In, Out, L), param (T, NbEquipes)
247
248
                                                           (for (Indice2, 1, NbEquipes), fromto ([], In2, Out2, L2), param (T,
                                                                      Indice1)
249
                                                          do
250
                                                                                 Var is T[Indice2, Indice1],
251
                                                                                 append (In2, [Var], Out2)
252
253
                                                          melangListe(L2,L3),
254
                                                          append (In, L3, Out)
255
                                    ) .
256
257
            solve6(T):-
258
                                    getData2 (TailleEq, NbEq, CapaBat, NbBat, NbConf),
259
                                    define Vars (T, NbEq, NbConf, NbBat),
260
                                    pasMemeBateaux (T, NbEq, NbConf),
                                    pas Meme Partenaires (T, NbEq, NbConf),
261
262
                                    capaBateaux (T, TailleEq, NbEq, CapaBat, NbBat, NbConf),
263
                                    getVarList2(T,L),
264
                                    labeling (L).
265
266
            /* Tests
267
            [eclipse 15]: solve6(T).
268
           269
                          4, 3), [](6, 7, 8, 5, 2, 1, 11), [](7, 5, 6, 8, 9, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 1, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](8, 9, 7, 2), [](
                        10, 4, 11, 5), [](8, 10, 9, 6, 11, 3, 2), [](9, 8, 12, 13, 7, 2, 6),
                       3, 8, 9, 4), [](11, 12, 10, 7, 3, 13, 9), [](13, 11, 10, 9, 6, 1, 5),
                       6, 5, 9, 11, 2, 8), [](5, 7, 1, 8, 3, 10, 13), [](4, 1, 6, 5, 3, 2, 12),
                       [](3, 2, 4, 1, 7, 11, 12), [](3, 1, 2, 6, 9, 10, 11), [](2, 4, 3, 1, 9, 12)
                       8, 6), [](2, 3, 1, 6, 7, 4, 5), [](1, 3, 2, 5, 4, 7, 6))
270
           Yes (6.98s cpu, solution 1, maybe more)?;
2.71
272 \quad T = \ [\ ]([\ ](1\ ,\ 2\ ,\ 3\ ,\ 4\ ,\ 5\ ,\ 6\ ,\ 7\ )\ ,\ [\ ](2\ ,\ 1\ ,\ 4\ ,\ 3\ ,\ 6\ ,\ 5\ ,\ 8\ )\ ,\ [\ ](3\ ,\ 4\ ,\ 1\ ,\ 2\ ,\ 8\ ,\ 7\ ,\ 8\ ,\ 7\ ,\ 8\ )\ ]
                          9), [](4, 3, 5, 1, 2, 9, 10), [](5, 6, 2, 7, 1, 3, 4), [](6, 5, 7, 2, 1,
                          4, 11), [](6, 7, 8, 5, 2, 1, 3), [](7, 5, 6, 8, 9, 1, 2), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), [](8, 9, 7, 1), []
                       10, 4, 11, 5), [](8, 10, 9, 6, 11, 3, 2), [](9, 8, 12, 13, 7, 2, 6),
                       [\ ](10\,,\ 9,\ 8,\ 11,\ 13,\ 12,\ 1)\,,\ [\ ](12\,,\ 13,\ 11,\ 9,\ 10,\ 8,\ 1)\,,\ [\ ](11\,,\ 10,\ 13,\ 12,\ 1)\,,
                       3,\ 8,\ 9,\ 4)\,,\ [](11,\ 12,\ 10,\ 7,\ 3,\ 13,\ 9)\,,\ [](13,\ 11,\ 10,\ 9,\ 6,\ 1,\ 5)\,,
```

```
10, 5, 13), [](9, 7, 10, 11, 12, 8, 2), [](7, 8, 9, 10, 3, 4, 1), [](7, 6, 5, 9, 11, 2, 8), [](5, 7, 1, 8, 3, 10, 13), [](4, 1, 6, 5, 3, 2, 12), [](3, 2, 4, 1, 7, 11, 12), [](3, 1, 2, 6, 9, 10, 11), [](2, 4, 3, 1, 9, 8, 6), [](2, 3, 1, 6, 7, 4, 5), [](1, 3, 2, 5, 4, 7, 6))

273 Yes (7.31s cpu, solution 2, maybe more)?

274 */
```