

## Coding Assignment #1

### Question 1.

A) The bias and weight terms for  $x2y$  and  $y2x$  for variables  $\text{var1} = 1$ ,  $\text{var2} = 0.3$ ,  $\text{degree} = 45$  are:

$$w_{x2y} = 0.5244587225052052 \quad b_{x2y} = 0.005071660776465743$$

$$w_{y2x} = 0.5449400592153517 \quad b_{y2x} = 0.011800263839855787$$

B) Figure 1 shows the regression plots with  $\text{var2}$  equaling 0.8, 0.3, 0.1 (left to right) where  $\text{var1}$  and  $\text{degree}$  remain constant at 1 and 45 respectively.

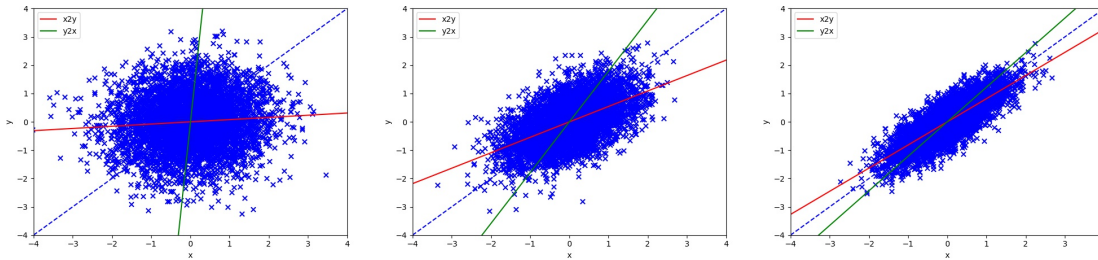


FIGURE 1. Regression plots: varied  $\text{var2}$ .

C) As  $\text{var2}$  moved from 0.8 down to 0.1 the data became less varied about the horizontal line rotated by 45 degrees. This led to both  $x2y$  and  $y2x$ , for smaller values of  $\text{var2}$ , to approach the dashed line that the data is mostly generated around. Also, the weights of both  $x2y$  and  $y2x$  increased as  $\text{var2}$  became smaller.

D) My experimental protocol to check the effects degree on the  $x2y$  and  $y2x$  regressions was to keep  $\text{var1}$  and  $\text{var2}$  constant as I chose degrees slightly higher and lower than the original degree of 45. This was to see how both regressions changed after crossing this original diagonal, where both  $x2y$  and  $y2x$  are equidistant to the data generation line (DGN). Then to check the effects as the degree moves further away from the original diagonal I chose a degree of 0.

Figure 2 shows the regression plots with degree equaling 60, 30, 0 (left to right) where  $\text{var1}$  and  $\text{var2}$  remain constant at 1 and 0.1 respectively.

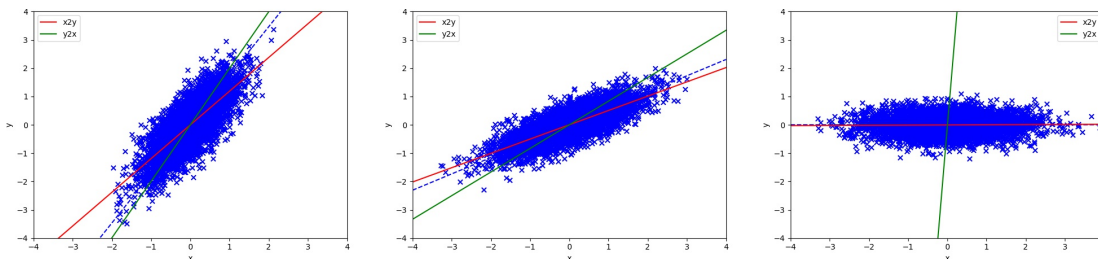


FIGURE 2. Regression plots: varied degree.

With this protocol, I was able to determine that as the degree approaches 0,  $x2y$  regression approaches the DGL and  $y2x$  regression approaches the  $\perp$ DGL. As the degree approaches 90, vice versa.

## Question 2.

- A) Mini-batch GD:  $\alpha = 0.001$ ,  $\text{batch\_size} = 10$ ,  $\text{MaxIter} = 100$   
 Epoch with best validation performance : epoch 100  
 Epoch 100 validation performance (risk) : 0.5462778014875631  
 Epoch 100 test performance (risk) : 0.5122943852532776

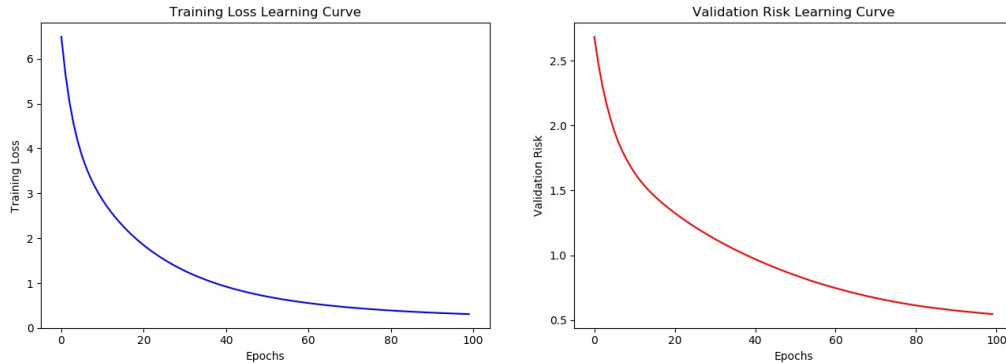


FIGURE 3. Training loss and validation risk learning curves.

- B) Mini-batch GD:  $\alpha = 0.001$ ,  $\text{batch\_size} = 10$ ,  $\text{MaxIter} = 100$ ,  $\text{decay} \in \{3, 1, 0.3, 0.1, 0.03, 0.01\}$   
 Epoch with best validation performance : epoch 98  
 Epoch 98 validation performance (risk) : 0.34793708487476305  
 Epoch 98 test performance (risk) : 0.3254641989474234

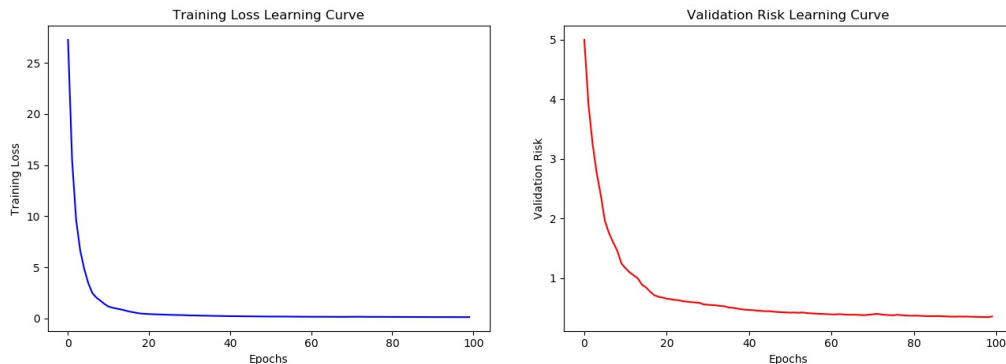


FIGURE 4. Training loss and validation risk learning curves.

- C) Do larger learning rates perform better than a smaller ones in terms of validation risk? We can investigate this relationship by plotting the learning curves of gradient descents with different learning rates. I chose learning rates 0.0001, 0.001, 0.01, and 0.1 to showcase the transition between fast and slow rates.

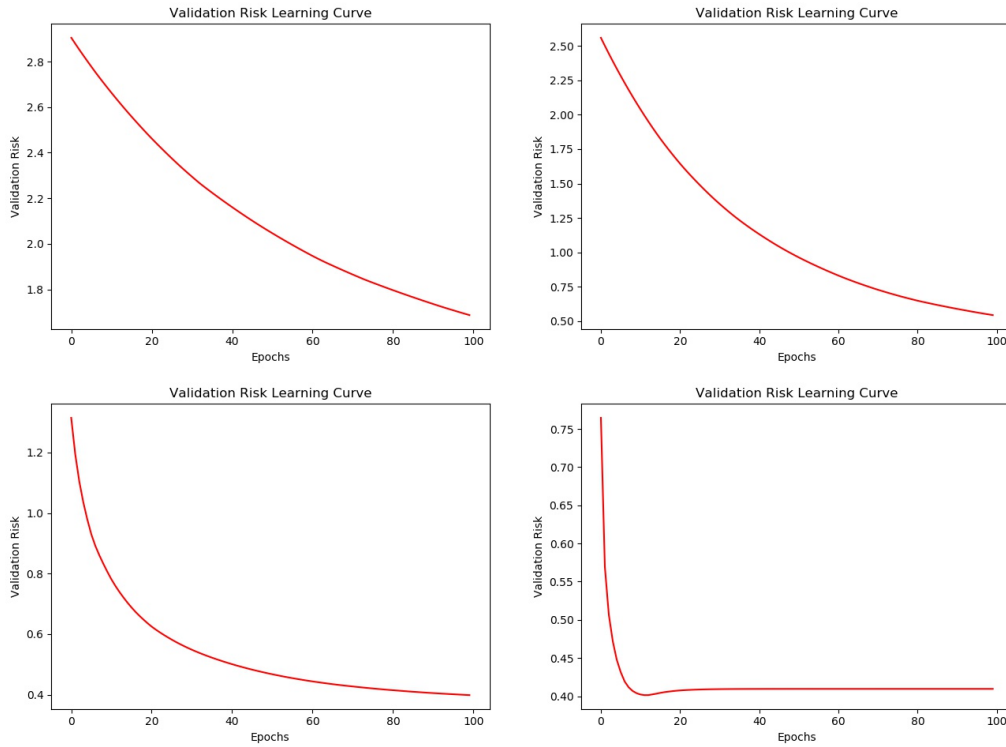


FIGURE 5. Validation risk learning curves: learning rates 0.0001, 0.001, 0.01, 0.1 from top left to bottom right.

From these plots we can see that the validation risk decreased quicker the larger the learning rate. Since we kept the number of iterations the same this resulted in the slower learning rates getting cut off before getting close to the optimum. However, with the largest learning rate we its lowest validation risk was on its 12th epoch and then did not decreasing any further as it oscillated around the optimum. As a result `learning_rate = 0.01` performed the best.

Based off of these results we can conclude that the best learning rate depends on the number of iterations; with more iterations smaller learning rates can more precisely approach the optimum than large ones, while with fewer iterations large learning rates descend quickly enough to be more effective than small ones.