

$$1. \quad \blacksquare L_1 = t(1, -1, 2) + (1, 1, 0)$$

$$\blacksquare L_2 = t(-1, 1, 0) + (2, 0, 2)$$

$$\exists t_1, t_2 \in \mathbb{R} : (t_1 + 1, -t_1 + 1, 2t_1) = (-t_2 + 2, t_2, 2)$$

$$\blacksquare t_1 + 1 = -t_2 + 2$$

$$\blacksquare -t_1 + 1 = t_2 \stackrel{*}{\Rightarrow} 0 = t_2$$

$$\blacksquare 2t_1 = 2 \Rightarrow \star : t_1 = 1$$

$$P = (2, 0, 2) : P \in L_1 \wedge P \in L_2$$

$\Rightarrow$  La intersección entre  $L_1$  y  $L_2$  es  $P$  ■

$$2. \quad \blacksquare P = (1, 1, 2) \in L_2 \wedge P_2 = (1, 1, 0) \in L_1 \wedge P_3(3, -1, 4) \in L_1$$

$$\blacksquare a = \overrightarrow{PP_2} = (0, 0, -2)$$

$$\blacksquare b = \overrightarrow{PP_3} = (2, -2, 2)$$

$$a \times b = \det \begin{pmatrix} i & j & k \\ 0 & 0 & -2 \\ 2 & -2 & 2 \end{pmatrix} = -4\hat{i} - 4\hat{j} - 0\hat{k}$$

$$\Pi : (-4, -4, 0) \cdot (x - 1, y - 1, z) = 0 \equiv \Pi : -4x + 4 - 4y + 4 = 0 \equiv \Pi : -4x - 4y = -8 \quad \Pi : x + y = 2$$