

1. $\int \int_D (2x + 1) dA, D : y = x^2 \wedge x + y = 2$

- $-2 \leq x \leq 1$
- $x^2 \leq y \leq 2 - x$

Tipo 1

$$\int_{-2}^1 \left(\int_{x^2}^{2-x} 2x + 1 dy \right) dx$$

- $\int_{x^2}^{2-x} 2x + 1 dy =$
 $2xy + y \Big|_{x^2}^{2-x} =$
 $2x(2-x) + (2-x) - 2x(x^2) - x^2 =$
 $4x - 2x^2 + 2 - x - 2x^3 - x^2 =$
 $2x^3 - 3x^2 + 3x + 2$
- $\int_{-2}^1 2x^3 - 3x^2 + 3x + 2 dx =$
 $\frac{x^4}{2} - x^3 + \frac{3x^2}{2} + 2x \Big|_{-2}^1 =$
 $\frac{1}{2} - 1 + \frac{3}{2} + 2 - 8 + 8 - 6 + 4 =$
 $2 - 1 + 2 - 6 + 4 = 1$

2. $\int \int_E x dV, E : z = e^{x^2}, z = -y, (x, y) \in R = [1, 2] \times [0, 2]$ en el plano xy

$$\int_1^2 \left(\int_0^2 \left(\int_{e^{x^2}}^{-y} x dz \right) dy \right) dx$$

- $\int_{e^{x^2}}^{-y} x dz =$
 $-xy - xe^{x^2}$
- $\int_0^2 -xy - xe^{x^2} dy =$
 $\frac{-xy^2}{2} - yxe^{x^2} \Big|_0^2 =$
 $-2x - 2xe^{x^2}$
- $\int_1^2 -2x - 2xe^{x^2} dx =$
 $-x^2 - e^{x^2} \Big|_1^2 =$
 $-4 - e^4 + 1 + e =$
 $-3 + e(-e^3 + 1)$