

$$f(x, y) = ye^{-xy}$$

$$f_x = -ye^{-xy}$$

$$f_y = -xye^{-xy} + e^{-xy}$$

$$P = (0, 2)$$

$$f_x \wedge f_y \text{ son continuas} \Rightarrow f \text{ derivable} \Rightarrow$$

$$D_u f(0, 2) = \nabla f(0, 2) \cdot u, \text{ con } \|u\| = 1$$

$$u = (a, b)$$

$$1 = (-2, -1) \cdot (a, b) \Leftrightarrow$$

$$-2a - b = 1 \Leftrightarrow$$

$$2a + b = -1$$

$$a = \frac{-1-b}{2} \quad b = -1 - 2a$$

$$1 = \sqrt{\frac{-1-b}{2}^2 + (-1 - 2a)^2} \Leftrightarrow$$

$$1 = \frac{1-2b-b^2}{4} + 1 - 4a + a^2$$

$$1 = \frac{1-2b-b^2}{4} + \frac{4-8a+4a^2}{4}$$

$$1 = \frac{5-2b-8a-b^2+4a^2}{4}$$