

$$f(1, 4) = z(1, 4) = 3(1) - 4 + 7 = 6$$

$$f_x(1, 4) = z_x(1, 4) = 3$$

$$f_y(1, 4) = z_y(1, 4) = -1$$

$$\begin{cases} x(s, t) = \cos(s)t^2 \\ y(s, t) = (s + 2t)^2 \end{cases}$$

$$\begin{cases} x_s(s, t) = -\sin(s)t^2 \\ x_t(s, t) = 2\cos(s)t \\ y_s(s, t) = 2(s + 2t) \\ y_t(s, t) = 4(s + 2t) \end{cases}$$

$$F(s, t) = f(x(s, t), y(s, t))$$

$$1. \quad \frac{\partial f}{\partial s} = \frac{\partial f}{\partial x} \cdot \frac{\partial x}{\partial s} + \frac{\partial f}{\partial y} \cdot \frac{\partial y}{\partial s} =$$

$$f_x(1, 4) \cdot x_s(0, -1) + f_y(1, 4) \cdot y_s(0, -1) =$$

$$3 \cdot 0 + (-1) \cdot 4 = -4$$

$$2. \quad \frac{\partial f}{\partial t} = \frac{\partial f}{\partial x} \cdot \frac{\partial x}{\partial t} + \frac{\partial f}{\partial y} \cdot \frac{\partial y}{\partial t} =$$

$$f_x(1, 4) \cdot x_t(0, -1) + f_y(1, 4) \cdot y_t(0, -1) =$$

$$3 \cdot (-2) + (-1) \cdot -8 = -6 + 8 = 2$$

$$z = \nabla F(0, -1) \cdot (s, t + 1) + F(0, -1) =$$

**$\nabla F(0, -1)$  ya lo calculamos antes**

$$\nabla F(s, t) = (-4, 2)$$

$$\Rightarrow z = (-4, 2) \cdot (s, t + 1) + f(1, 4)$$

$$\Rightarrow z = -4s + 2(t + 1) + 6$$