

1. $f(x, y) = x^3y^5 + 2x^4y$

- $f_x = 3x^2y^5 + 8x^3y$
- $f_{xx} = 6xy^5 + 24x^2y$
- $f_{xy} = 15x^2y^4 + 8x^3$
- $f_y = x^35y^4 + 2x^4$
- $f_{yy} = 20x^3y^3$
- $f_{yx} = 15x^2y^4 + 8x^3$

2. $f(x, y) = \sin^2(x + y)$

- $f_x = 2\sin(x + y)\cos(x + y)$
- $f_{xx} = -2\sin^2(x + y) + 2\cos^2(x + y)$
- $f_{xy} = -2\sin^2(x + y) + 2\cos^2(x + y)$
- $f_y = 2\sin(x + y)\cos(x + y)$
- $f_{yy} = -2\sin^2(x + y) + 2\cos^2(x + y)$
- $f_{yx} = -2\sin^2(x + y) + 2\cos^2(x + y)$

3. $f(x, y) = \sqrt{x^2 + y^2}$

- $f_x = \frac{x}{\sqrt{x^2 + y^2}}$
- $f_{xx} = \frac{y^2}{(x^2 + y^2)^{\frac{3}{2}}}$
- $f_{xy} = \frac{xy}{(x^2 + y^2)^{\frac{3}{2}}}$
- $f_y = \frac{y}{\sqrt{x^2 + y^2}}$
- $f_{yy} = \frac{x^2}{(x^2 + y^2)^{\frac{3}{2}}}$
- $f_{yx} = \frac{xy}{(x^2 + y^2)^{\frac{3}{2}}}$

4. $f(x, y) = \frac{xy}{x-y}$

- $f_x = \frac{y^2}{(x-y)^2}$
- $f_{xx} = \frac{-2y^2}{(x-y)^3}$
- $f_{xy} = \frac{-2yx}{(x-y)^3}$
- $f_y = \frac{x^2}{(x-y)^2}$
- $f_{yy} = \frac{2x^2}{(x-y)^3}$
- $f_{yx} = \frac{-2yx}{(x-y)^3}$