

$$\lim_{(x,y) \rightarrow (2,3)} y \sin(x \cdot y - 6) = 0$$

$$\|(x-2, y-3)\| < \delta \Rightarrow |y \cdot \sin(x \cdot y - 6)| < \epsilon$$

$$\blacksquare |x-2| \leq \|(x-2, y-3)\| < \delta$$

$$\blacksquare |y-3| \leq \|(x-2, y-3)\| < \delta$$

$$\begin{aligned} & |y \cdot \sin(x \cdot y - 6)| \equiv \\ & |((y-3) + 3) \cdot \sin(((x-2) + 2) \cdot ((y-3) + 3) - 6)| \equiv \\ & |((y-3) + 3) \cdot \sin((x-2)(y-3) + 3(x-2) + 2(y-3) + 6 - 6)| \equiv \\ & |((y-3) + 3) \cdot \sin((x-2)(y-3) + 3(x-2) + 2(y-3))| \equiv \\ & |(y-3) + 3| \cdot |\sin((x-2)(y-3) + 3(x-2) + 2(y-3))| \\ & (x, y) \rightarrow (2, 3) \Rightarrow (x-2)(y-3) + 3(x-2) + 2(y-3) \rightarrow 0 \\ & \star : x \rightarrow 0 \Rightarrow \sin(x) \leq x \\ & |(y-3) + 3| \cdot |\sin((x-2)(y-3) + 3(x-2) + 2(y-3))| \stackrel{\star}{\leq} \\ & |(y-3) + 3| \cdot |(x-2)(y-3) + 3(x-2) + 2(y-3)| \stackrel{DesTrian}{\leq} \\ & (|y-3| + 3) \cdot (|x-2| |y-3| + 3|x-2| + 2|y-3|) = \\ & (|y-3| + 3) \cdot (|x-2| |y-3| + 3|x-2| + 2|y-3|) < \\ & (\delta + 3) \cdot (\delta^2 + 5\delta) \stackrel{\delta \leq 1}{\leq} \\ & (\delta + 3) \cdot (6\delta) = \\ & 6\delta^2 + 18\delta \stackrel{\delta \leq 1}{\leq} \\ & 24\delta = \epsilon \Rightarrow \delta = \min(1, \frac{\epsilon}{24}) \end{aligned}$$