

1. $\int \int_D e^x y^3 dA$

$D =$

- $x = y^4$
- $x = 1$

\Rightarrow

- $0 \leq x \leq y^4$
- $0 \leq y \leq 1$

$\int_0^1 (\int_0^{y^4} e^x y^3 dx) dy$

- $\int_0^{y^4} e^x y^3 dx =$
 $e^{y^4} y^3 - y^3$
- $\int_0^1 e^{y^4} y^3 - y^3 dy =$
 $\int e^{y^4} y^3 dy$
 $u = y^4 \wedge du = 4y^3 dy \Rightarrow dy = \frac{du}{4y^3} \Rightarrow$
 $\int \frac{e^u}{4} du = \frac{1}{4} e^u + C = \frac{e^{y^4}}{4} + C \Rightarrow$
 $\int_0^1 e^{y^4} y^3 - y^3 dy \stackrel{Barrow}{=} \left. \frac{e^{y^4}}{4} - \frac{y^4}{4} \right|_0^1 =$
 $\frac{e}{4} - \frac{1}{4} - \frac{1}{4} = \frac{e-2}{4}$

2. ▪ $x + 2y = 2$ describe un plano
 $x = 0 \Rightarrow y = 1$
 $y = 0 \Rightarrow x = 2$
 Como se encuentra en el primer octante
 $D' =$
- $0 \leq x \leq 2 - 2y$
 - $0 \leq y \leq 1$
- $z = x^2 + y^2$ describe un paraboloide
 $0 \leq z \leq x^2 + y^2$

$\int_0^1 (\int_0^{2-2y} (\int_0^{x^2+y^2} 1 dz) dx) dy$

- $\int_0^{x^2+y^2} 1 dz = x^2 + y^2$
 - $\int_0^{2-2y} x^2 + y^2 dx \stackrel{Barrow}{=} \left. \frac{x^3}{3} + xy^2 \right|_0^{2-2y} =$
 $y^2 (-2y + 2) + \frac{(-2y+2)^3}{3}$
 - $\int_0^1 y^2 (-2y + 2) + \frac{(-2y+2)^3}{3} dy =$
 - $\int_0^1 y^2 (-2y + 2) dy =$
 $\int_0^1 -2y^3 + 2y^2 dy \stackrel{Barrow}{=} \left. -\frac{y^4}{2} + \frac{2y^3}{3} \right|_0^1 =$
 $-\frac{1}{2} + \frac{2}{3} = \frac{1}{6}$
 - $\int_0^1 \frac{(-2y+2)^3}{3} dy =$
 $\frac{1}{3} \int_0^1 -8y^3 + 24y^2 - 24y + 8 dy \stackrel{Barrow}{=} \left. \frac{1}{3} (-2y^4 + 8y^3 - 12y^2 + 8y) \right|_0^1 =$
 $\frac{1}{3} (-2 + 8 - 12 + 8) = \frac{2}{3}$
- $\int_0^1 y^2 (-2y + 2) + \frac{(-2y+2)^3}{3} dy = \frac{1}{6} + \frac{2}{3} = \frac{5}{6}$