

$$1. \ u = (3, -4), v = (5, 0)$$

$$P_u(v) = \frac{u \cdot v}{\|u\|^2} \cdot u = \frac{(3, -4) \cdot (5, 0)}{\|(3, -4)\|^2} \cdot (3, -4) =$$

$$\frac{15}{25} \cdot (3, -4) = \left(\frac{9}{5}, -\frac{12}{5}\right)$$

$$2. \ u = (1, 2), v = (-4, 1)$$

$$P_u(v) = \frac{u \cdot v}{\|u\|^2} \cdot u = \frac{(1, 2) \cdot (-4, 1)}{\|(1, 2)\|^2} \cdot (1, 2) =$$

$$-\frac{2}{5} \cdot (1, 2) = \left(-\frac{2}{5}, -\frac{4}{5}\right)$$

$$3. \ u = (3, 6, 2), v = (1, 2, 3)$$

$$P_u(v) = \frac{u \cdot v}{\|u\|^2} \cdot u = \frac{(3, 6, 2) \cdot (1, 2, 3)}{\|(3, 6, 2)\|^2} \cdot (3, 6, 2) =$$

$$\frac{3}{7} \cdot (3, 6, 2) = \left(\frac{9}{7}, \frac{18}{7}, \frac{6}{7}\right)$$