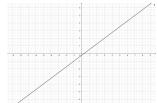
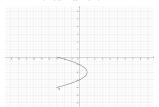
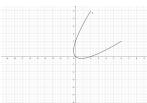
- 1. a)  $x = 3 4t \Rightarrow \star : \frac{-x+3}{4} = t$ 
  - $y = 2 3t \stackrel{\star}{\Rightarrow} y = 2 3(\frac{-x+3}{4}) \equiv y = \frac{3x}{4} \frac{1}{4}$



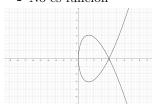
- b)  $= x = 1 t^2$ 
  - y = t 2
  - $-2 \le t \le 2$
  - No es función



- $c) \quad \bullet \quad x = t^2 + t$ 
  - $y = t^2 t$
  - $-2 \le t \le 2$
  - No es función

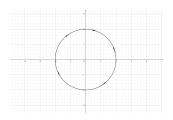


- $d) \quad \bullet \quad x = t^2$ 
  - $y = t^3 4t$
  - $-3 \le t \le 3$
  - No es función



- 2. a) r = 2
  - p = (0,0)
  - $x^2 + y^2 = 4$
  - $\begin{cases} x(t) = 2 \cdot \cos(t) \\ y(t) = 2 \cdot \sin(t) \\ 0 \le t < 2\pi \end{cases}$

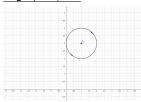
$\overline{t}$	x	y
$\frac{\pi}{2}$	0	2
$\frac{\pi}{3\pi}$	-2	0
$\frac{3\pi}{2}$	0	-2



- r=1
  - p = (1,3)
  - $(x-1)^2 + (y-3)^2 = 1$  $x(t) = 1 + \cos(t)$   $y(t) = 3 + \sin(t)$   $0 \le t < 2\pi$

$$\begin{cases} y(t) = 3 + \sin(t) \\ 0 \le t < 2\pi \end{cases}$$

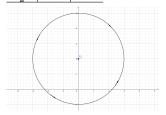
-		
t	x	y
$\frac{\pi}{2}$	1	4
$\bar{\pi}$	0	3
$\frac{3\pi}{2}$	1	2



- c)■ r = 3
  - p = (0, 2)
  - $(x)^2 + (y-2)^2 = 9$

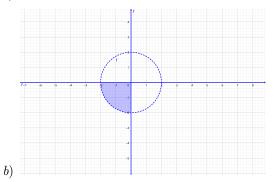
$$\begin{cases} x(t) = 3 \cdot \cos(t) \\ y(t) = 2 + 3\sin(t) \\ 0 \le t < 2\pi \end{cases}$$

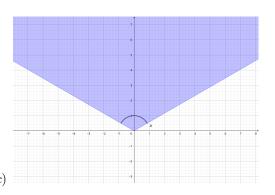
$\overline{t}$	x	y
$\frac{\pi}{2}$	0	5
$\pi$	-3	2
$\frac{3\pi}{2}$	0	-1





3. a)





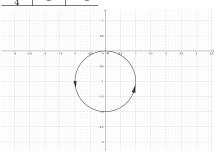
4. 
$$a$$
)  $\star : r = -2\sin(\theta)$ 

• 
$$x = \cos(\theta) * r \stackrel{\star}{\Rightarrow} x = \cos(\theta) \cdot (-2\sin(\theta))$$

• 
$$x = \sin(\theta) * r \stackrel{\star}{\Rightarrow} y = -2\sin^2(\theta)$$

$$\begin{cases} x(t) = -2 \cdot \cos(t) \sin(t) \\ y(t) = -2 \sin^2(\theta) \\ 0 \le t < \pi \end{cases}$$

t	x	y
$\frac{\pi}{4}$	-1	-1
$\frac{\frac{\pi}{4}}{\frac{\pi}{2}}$	0	-2
$\frac{2}{\pi}$ $\frac{3\pi}{}$	0	0
$\frac{3\pi}{4}$	1	-1



$$b) \quad \bullet \ \star : r = 1 - \cos(\theta)$$

• 
$$x = r \cdot \cos(\theta) \stackrel{\star}{\Rightarrow} x = \cos(\theta) - \cos^2(\theta)$$

• 
$$y = r \cdot \sin(\theta) \stackrel{\star}{\Rightarrow} y = \sin(\theta) - \sin(\theta) \cdot \cos(\theta)$$

$$r = \sqrt{x^2 + t^2} \stackrel{\star}{\Rightarrow}$$

$$r = \sqrt{x^2 + t^2} \Rightarrow \cos(\theta) = \frac{x}{\sqrt{x^2 + t^2}}$$

$$\sqrt{x^2 + t^2} = 1 - \cos(\theta) = \frac{x}{\sqrt{x^2 + y^2}}$$

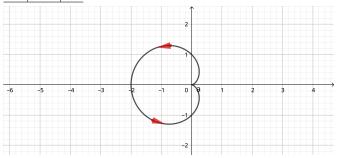
$$\sqrt{x^2 + t^2} = 1 - \frac{x}{\sqrt{x^2 + y^2}} \equiv$$

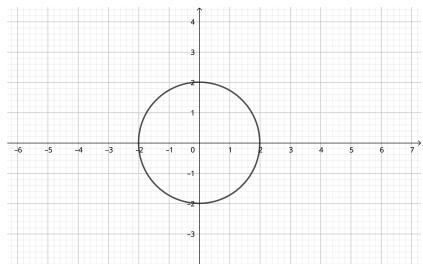
$$r^2 + y^2 = \sqrt{x^2 + y^2} - x$$

$$x^2 + y^2 = \sqrt{x^2 + y^2} - x$$

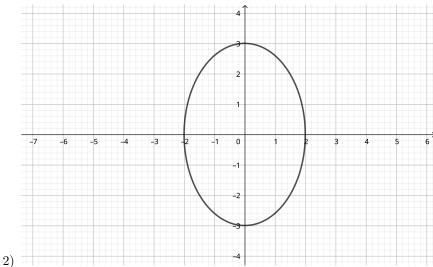
$$\begin{cases} x(\theta) = \cos(\theta) - \cos^2(\theta) \\ y(\theta) = \sin(\theta) - \sin(\theta) \cdot \cos(\theta) \\ 0 \le \theta < 2\pi \end{cases}$$

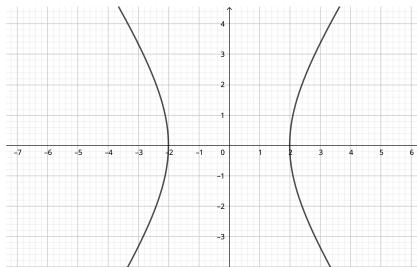
t	x	y
0	0	0
$\pi$	-2	0

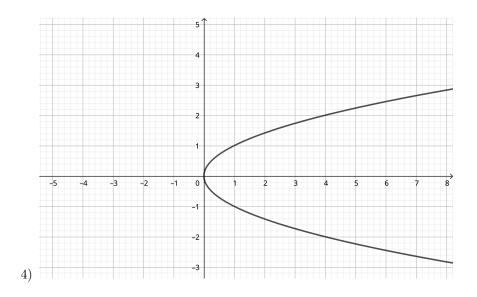




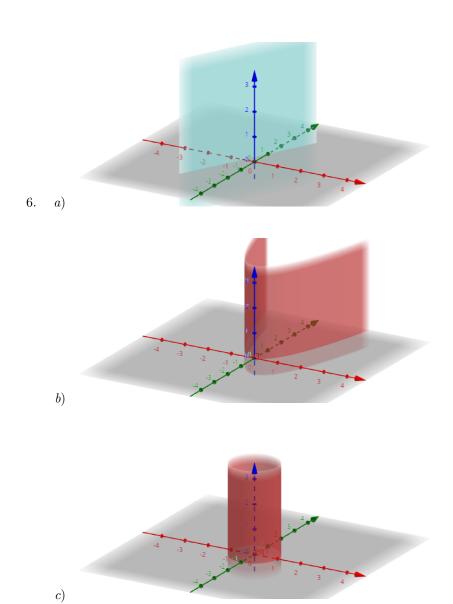
5. a) 1)  $\blacksquare$ 

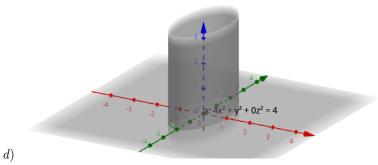






 $b)\,$  Son curvas de nivel, a mayor a mayor ancho, a mayor b mayor altura





7. a) 1) 
$$x^2 + \frac{y^2}{4} + \frac{z^2}{9} = 1$$

• 
$$\stackrel{z=-2}{\Rightarrow} x^2 + \frac{y^2}{9} + \frac{4}{9} = 1$$
 Una elipse  
•  $\stackrel{z=-1}{\Rightarrow} x^2 + \frac{y^2}{9} + \frac{1}{9} = 1$  Una elipse

• 
$$\stackrel{z=-1}{\Rightarrow} x^2 + \frac{y^2}{9} + \frac{1}{9} = 1$$
 Una elipse

• 
$$\stackrel{z=0}{\Rightarrow} x^2 + \frac{y^2}{9} = 1$$
 Circulo

• 
$$\stackrel{z=1}{\Rightarrow} x^2 + \frac{y^2}{9} + \frac{1}{9} = 1$$
 Una elipse

• 
$$\stackrel{z=2}{\Rightarrow} x^2 + \frac{y^2}{9} + \frac{4}{9} = 1$$
 Una elipse

• • 
$$\overset{y=-2}{\Rightarrow} x^2 + \frac{4}{9} + \frac{z^2}{9} = 1$$
 Una elipse  
•  $\overset{y=-1}{\Rightarrow} x^2 + \frac{1}{9} + \frac{z^2}{9} = 1$  Una elipse

• 
$$\stackrel{y=-1}{\Rightarrow} x^2 + \frac{1}{9} + \frac{z^2}{9} = 1$$
 Una elipse

• 
$$\stackrel{y=0}{\Rightarrow} x^2 + \frac{z^2}{9} = 1$$
 Circulo

• 
$$\stackrel{y=1}{\Rightarrow} x^2 + \frac{1}{9} + \frac{z^2}{9} = 1$$
 Una elipse

• 
$$\stackrel{y=2}{\Rightarrow} x^2 + \frac{4}{9} + \frac{z^2}{9} = 1$$
 Una elipse

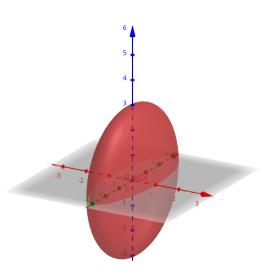
• • 
$$\stackrel{x=-2}{\Rightarrow} 4 + \frac{y^2}{9} + \frac{z^2}{9} = 1$$
 Circulo

• 
$$\stackrel{x=-1}{\Rightarrow} 1 + \frac{y^2}{9} + \frac{z^2}{9} = 1$$
 Circulo

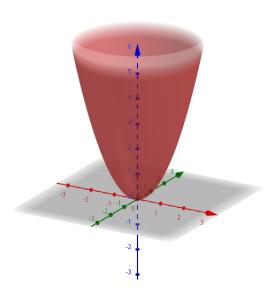
• 
$$\stackrel{x=0}{\Rightarrow} \frac{y^2}{9} + \frac{z^2}{9} = 1$$
 Circulo

• 
$$\stackrel{x=1}{\Rightarrow} 1 + \frac{y^2}{9} + \frac{z^2}{9} = 1$$
 Circulo

• 
$$\stackrel{x=2}{\Rightarrow} 4 + \frac{y^2}{9} + \frac{z^2}{9} = 1$$
 Circulo

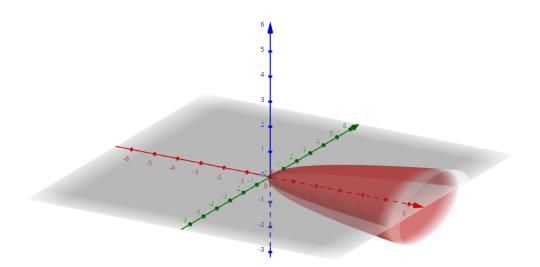


- 2)  $z = x^2 + y^2$ 
  - $\stackrel{z=0}{\Rightarrow} x^2 + y^2 = 0$  un punto
    - $\stackrel{z=1}{\Rightarrow} x^2 + y^2 = 1$  Un circulo con centro en (0,0) y radio 1
    - $\stackrel{z=2}{\Rightarrow} x^2 + y^2 = 2$  Un circulo con centro en (0,0) y radio  $\sqrt{(2)}$
  - - $\stackrel{y=-1}{\Rightarrow} x^2 + 1 = z$  Una parabola
    - $\stackrel{y=0}{\Rightarrow} x^2 + 0 = z$  Una parabola
    - $\overset{y=1}{\Rightarrow} x^2 + 1 = z$  Una parabola
    - $\stackrel{y=2}{\Rightarrow} x^2 + 4 = z$  Una parabola
  - •  $\stackrel{x=-2}{\Rightarrow} 4 + y^2 = z$  Una parabola
    - $\stackrel{x=-1}{\Rightarrow} 1 + y^2 = z$  Una parabola
    - $\stackrel{x=0}{\Rightarrow} 0 + y^2 = z$  Una parabola
    - $\stackrel{x=1}{\Rightarrow} 1 + y^2 = z$  Una parabola
    - $\stackrel{x=2}{\Rightarrow} 4 + y^2 = z$  Una parabola



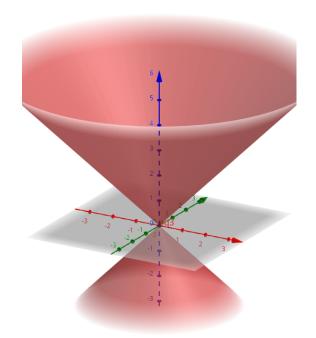
- 3)  $x = y^2 + 4z^2$ 
  - •  $\stackrel{z=-2}{\Rightarrow} x = y^2 + 16$  Una parabola
    - $\stackrel{z=-1}{\Rightarrow} x = y^2 + 4$  Una parabola
    - $\stackrel{z=0}{\Rightarrow} x = y^2 +$  Una parabola
    - $\stackrel{z=1}{\Rightarrow} x = y^2 + 4$  Una parabola
    - $\stackrel{z=2}{\Rightarrow} x = y^2 + 16$  Una parabola
  - •  $\stackrel{y=-2}{\Rightarrow} x = 4 + 4z^2$  Una parabola
    - $\overset{y=-1}{\Rightarrow} x = 1 + 4z^2$  Una parabola
    - $\stackrel{y=0}{\Rightarrow} x = 0 + 4z^2$  Una parabola
    - $\stackrel{y=1}{\Rightarrow} x = 1 + 4z^2$  Una parabola
    - $\stackrel{y=2}{\Rightarrow} x = 4 + 4z^2$  Una parabola
  - •  $\stackrel{x=0}{\Rightarrow} x = y^2 + 4z^2$  Un punto

- $\stackrel{x=1}{\Rightarrow} 1 = y^2 + 4z^2$  Una elipse
- $\stackrel{x=2}{\Rightarrow} 2 = y^2 + 4z^2$  Una elipse



4) 
$$z^2 = x^2 + y^2$$

- - $\stackrel{z=-1}{\Rightarrow} 1 = x^2 + y^2$  Un circulo con centro en (0,0) y radio 1
  - $\stackrel{z=0}{\Rightarrow} 0 = x^2 + y^2$  Un punto
  - $\overset{z=1}{\Rightarrow} 1 = x^2 + y^2$  Un circulo con centro en (0,0) y radio 1
  - $\stackrel{z=2}{\Rightarrow} 4 = x^2 + y^2$  Un circulo con centro en (0,0) y radio  $\sqrt(2)$
- $\bullet \bullet \overset{y=-2}{\Rightarrow} z^2 x^2 = 4 \text{ Hiperbola}$ 
  - $\stackrel{y=-1}{\Rightarrow} z^2 x^2 = 1$  Hiperbola
  - $\stackrel{y=0}{\Rightarrow} z^2 x^2 = 0$  Una X
  - $\stackrel{y=1}{\Rightarrow} z^2 x^2 = 1$  Hiperbola
  - $\stackrel{y=2}{\Rightarrow} z^2 x^2 = 4$  Hiperbola
- •  $\stackrel{x=-2}{\Rightarrow} z^2 y^2 = 4$  Hiperbola
  - $\stackrel{x=-1}{\Rightarrow} z^2 y^2 = 1$  Hiperbola
  - $\stackrel{x=0}{\Rightarrow} z^2 y^2 = 0$  Una x
  - $\stackrel{x=1}{\Rightarrow} z^2 y^2 = 1$  Hiperbola
  - $\stackrel{x=2}{\Rightarrow} z^2 y^2 = 4$  Hiperbola



$$5) \ x^2 = y^2 + 4z^2$$

• • 
$$\stackrel{z=-2}{\Rightarrow} x^2 = y^2 + 16$$
 Hiperbola

• 
$$\stackrel{z=-1}{\Rightarrow} x^2 = y^2 + 4$$
 Hiperbola

• 
$$\stackrel{z=0}{\Rightarrow} x^2 = y^2$$
 Un punto

• 
$$\stackrel{z=1}{\Rightarrow} x^2 = y^2 + 4$$
 Hiperbola

• 
$$\stackrel{z=2}{\Rightarrow} x^2 = y^2 + 16$$
 Hiperbola

$$\bullet \bullet \overset{y=-2}{\Rightarrow} x^2 = 4 + 4z^2 \text{ Hiperbola}$$

• 
$$\stackrel{y=-1}{\Rightarrow} x^2 = 1 + 4z^2$$
 Hiperbola

• 
$$\stackrel{y=0}{\Rightarrow} x^2 = 4z^2$$
 Una X

• 
$$\stackrel{y=1}{\Rightarrow} x^2 = 1 + 4z^2$$
 Hiperbola

• 
$$\stackrel{y=2}{\Rightarrow} x^2 = 4 + 4z^2$$
 Hiperbola

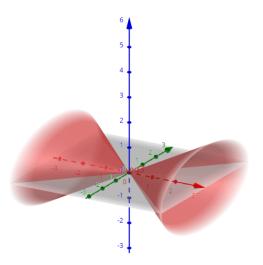
• • 
$$\stackrel{x=-2}{\Rightarrow} 4 = y^2 + 4z^2$$
 Un elipse

• 
$$\stackrel{x=-1}{\Rightarrow} 1 = y^2 + 4z^2$$
 Un elipse

• 
$$\stackrel{x=0}{\Rightarrow} 0 = y^2 + 4z^2$$
 Un punto

• 
$$\stackrel{x=1}{\Rightarrow} 1 = y^2 + 4z^2$$
 Un elipse

• 
$$\stackrel{x=2}{\Rightarrow} 4 = y^2 + 4z^2$$
 Un elipse



6) 
$$z = x^2 - y^2$$

• • 
$$\stackrel{z=-2}{\Rightarrow}$$
  $-2 = x^2 - y^2$  Hiperbola

• 
$$\stackrel{z=-1}{\Rightarrow} -1 = x^2 - y^2$$
 Hiperbola

• 
$$\stackrel{z=0}{\Rightarrow} y^2 = x^2$$
 Ejes de  $45^{\circ}$ 

• 
$$\stackrel{z=1}{\Rightarrow} 1 = x^2 - y^2$$
 Hiperbola

• 
$$\stackrel{z=2}{\Rightarrow} 2 = x^2 - y^2$$
 Hiperbola

• • 
$$\overset{y=-2}{\Rightarrow} z = x^2 - 4$$
 Parabola

• 
$$\stackrel{y=-1}{\Rightarrow} z = x^2 - 1$$
 Parabola

• 
$$\stackrel{y=0}{\Rightarrow} z = x^2 - 0$$
 Parabola

• 
$$\stackrel{y=1}{\Rightarrow} z = x^2 - 1$$
 Parabola

• 
$$\stackrel{y=2}{\Rightarrow} z = x^2 - 4$$
 Parabola

• • 
$$\stackrel{x=-2}{\Rightarrow} z = 4 - y^2$$
 Parabola

• 
$$\stackrel{x=-1}{\Rightarrow} z = 1 - y^2$$
 Parabola

• 
$$\stackrel{x=0}{\Rightarrow} z = 0 - y^2$$
 Parabola

• 
$$\stackrel{x=1}{\Rightarrow} z = 1 - y^2$$
 Parabola

• 
$$\stackrel{x=2}{\Rightarrow} z = 4 - y^2$$
 Parabola



7) 
$$x^2 + y^2 - z^2 = 1$$

• • 
$$\stackrel{z=-2}{\Rightarrow} x^2 + y^2 - 4 = 1$$
 Circulo

• 
$$\stackrel{z=-1}{\Rightarrow} x^2 + y^2 - 1 = 1$$
 Circulo

• 
$$\stackrel{z=0}{\Rightarrow} x^2 + y^2 - 0 = 1$$
 Circulo

• 
$$\stackrel{z=1}{\Rightarrow} x^2 + y^2 - 1 = 1$$
 Circulo

• 
$$\stackrel{z=2}{\Rightarrow} x^2 + y^2 - 4 = 1$$
 Circulo

• • 
$$\stackrel{y=-2}{\Rightarrow} x^2 + 4 - z^2 = 1$$
 Hiperbola

• 
$$\stackrel{y=-1}{\Rightarrow} x^2 + 1 - z^2 = 1$$
 Hiperbola

• 
$$\stackrel{y=0}{\Rightarrow} x^2 + 0 - z^2 = 1$$
 Hiperbola

• 
$$\stackrel{y=1}{\Rightarrow} x^2 + 1 - z^2 = 1$$
 Hiperbola

• 
$$\stackrel{y=2}{\Rightarrow} x^2 + 4 - z^2 = 1$$
 Hiperbola

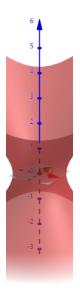
• • 
$$\stackrel{x=-2}{\Rightarrow} 4 + y^2 - z^2 = 1$$
 Hiperbola

• 
$$\stackrel{x=-1}{\Rightarrow} 1 + y^2 - z^2 = 1$$
 Hiperbola

• 
$$\stackrel{x=0}{\Rightarrow} 0 + y^2 - z^2 = 1$$
 Hiperbola

• 
$$\stackrel{x=1}{\Rightarrow} 1 + y^2 - z^2 = 1$$
 Hiperbola

• 
$$\stackrel{x=2}{\Rightarrow} 4 + y^2 - z^2 = 1$$
 Hiperbola



$$8) -x^2 - y^2 + z^2 = 1$$

• • 
$$\stackrel{z=-2}{\Rightarrow} -x^2 - y^2 + 4 = 1$$
 Circulo

• 
$$\stackrel{z=-1}{\Rightarrow} -x^2 - y^2 + 2 = 1$$
 Circulo

• 
$$\stackrel{z=0}{\Rightarrow} -x^2 - y^2 + 1 = 1$$
 Circulo

• 
$$\stackrel{z=1}{\Rightarrow} -x^2 - y^2 + 2 = 1$$
 Circulo

• 
$$\stackrel{z=2}{\Rightarrow} -x^2 - y^2 + 4 = 1$$
 Circulo

• • 
$$\stackrel{y=-2}{\Rightarrow} -x^2 - 4 + z^2 = 1$$
 Hiperbola

• 
$$\stackrel{y=-1}{\Rightarrow} -x^2 - 2 + z^2 = 1$$
 Hiperbola

• 
$$\stackrel{y=0}{\Rightarrow} -x^2 - 1 + z^2 = 1$$
 Hiperbola

• 
$$\stackrel{y=1}{\Rightarrow} -x^2 - 2 + z^2 = 1$$
 Hiperbola

• 
$$\stackrel{y=2}{\Rightarrow} -x^2 - 4 + z^2 = 1$$
 Hiperbola

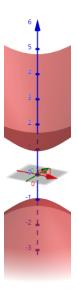
• • 
$$\stackrel{x=-2}{\Rightarrow} -4 - y^2 + z^2 = 1$$
 Hiperbola

• 
$$\stackrel{x=-1}{\Rightarrow}$$
  $-2 - y^2 + z^2 = 1$  Hiperbola

• 
$$\stackrel{x=0}{\Rightarrow} -1 - y^2 + z^2 = 1$$
 Hiperbola

• 
$$\stackrel{x=1}{\Rightarrow} -2 - y^2 + z^2 = 1$$
 Hiperbola

• 
$$\stackrel{x=2}{\Rightarrow}$$
  $-4 - y^2 + z^2 = 1$  Hiperbola



9) 
$$4x^2 + 9y^2 + z = 0$$

• • 
$$\stackrel{z=-2}{\Rightarrow} 4x^2 + 9y^2 + (-2) = 0$$
 Elipse

• 
$$\stackrel{z=-1}{\Rightarrow} 4x^2 + 9y^2 + (-1) = 0$$
 Elipse

• 
$$\stackrel{z=0}{\Rightarrow} 4x^2 + 9y^2 = 0$$
 Elipse

• 
$$\stackrel{z=1}{\Rightarrow} 4x^2 + 9y^2 + 1 = 0$$
 Elipse

• 
$$\stackrel{z=2}{\Rightarrow} 4x^2 + 9y^2 + 2 = 0$$
 Elipse

• • 
$$\stackrel{y=-2}{\Rightarrow} 4x^2 + 18 + z = 0$$
 Parabola

• 
$$\stackrel{y=-1}{\Rightarrow} 4x^2 + 9 + z = 0$$
 Parabola

• 
$$\stackrel{y=0}{\Rightarrow} 4x^2 + +z = 0$$
 Parabola

• 
$$\stackrel{y=1}{\Rightarrow} 4x^2 + 9 + z = 0$$
 Parabola

• 
$$\stackrel{y=2}{\Rightarrow} 4x^2 + 18 + z = 0$$
 Parabola

• • 
$$\stackrel{x=-2}{\Rightarrow}$$
 16 + 9 $y^2$  +  $z$  = 0 Parabola

• 
$$\stackrel{x=-1}{\Rightarrow} 4 + 9y^2 + z = 0$$
 Parabola

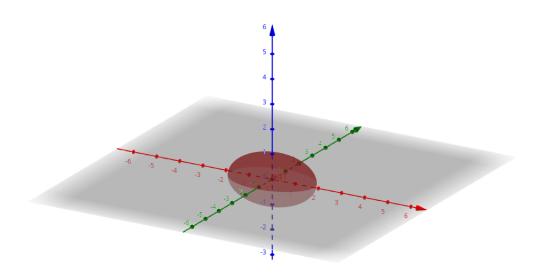
• 
$$\stackrel{x=0}{\Rightarrow} 9y^2 + z = 0$$
 Parabola

• 
$$\stackrel{x=1}{\Rightarrow} 4 + 9y^2 + z = 0$$
 Parabola

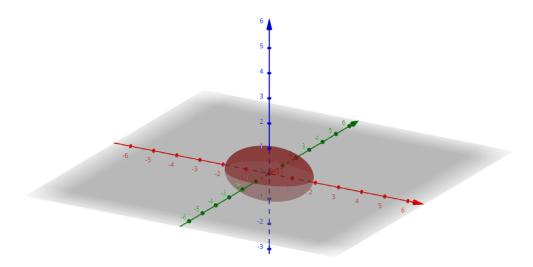
• 
$$\stackrel{x=2}{\Rightarrow}$$
 16 + 9 $y^2 + z = 0$  Parabola



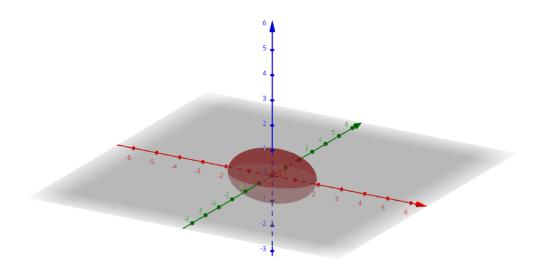
b) 1) 
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$$



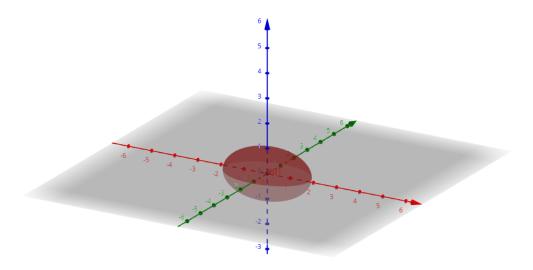
$$2) \ z = \frac{x^2}{a^2} + \frac{y^2}{b^2}$$



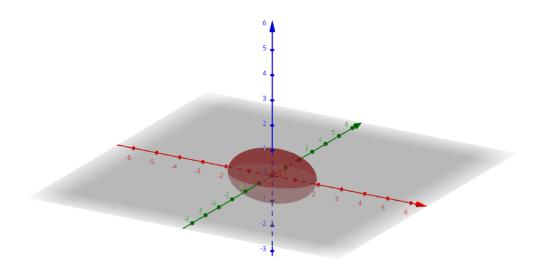
$$3) \ z^2 = \frac{x^2}{a^2} + \frac{y^2}{b^2}$$



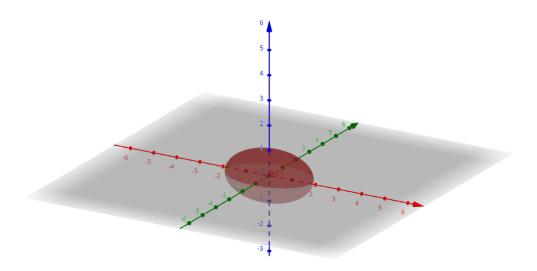
4) 
$$z = \frac{x^2}{a^2} - \frac{y^2}{b^2}$$



$$5) \ \frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{z^2}{c^2} = 1$$

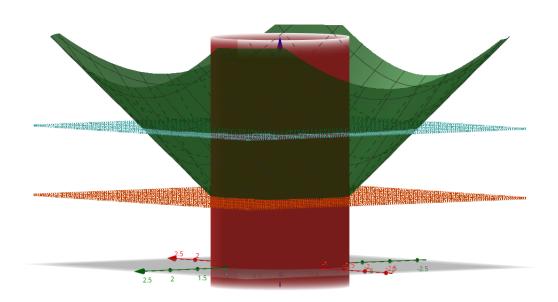


6) 
$$-\frac{x^2}{a^2} - \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$$



8.  $x^2 + y^2 = 1$  Un cilindro con centro en (0,0,0)

 $z=\sqrt(x^2+y^2)$ z es la distancia entre x e y, un paraboloide



9. a) 
$$r(t) = (\sqrt{4-t^2}, 5t+1, \ln(t+1))$$

a) 
$$r(t) = (\sqrt{4 - t^2}, 5t + 1, \ln(t + 1))$$
  
•  $f(t) = \sqrt{4 - t^2}$   
 $\Leftrightarrow 4 - t^2 \ge 0 \Leftrightarrow 4 \ge t^2 \Leftrightarrow \sqrt{4} \ge |t| \Leftrightarrow 2 \ge |t| \Leftrightarrow -2 \le t \le 2$   
 $\Rightarrow f: [-2, 2] \to \Re$ 

• 
$$g(t) = 5t + 1 \Rightarrow f: \Re \rightarrow \Re$$

$$h(t) = \ln(t+1) \\ \Leftrightarrow t+1 > 0 \Leftrightarrow t > -1$$

$$\Rightarrow h: ([-1,\infty+) \to \Re$$

b) 
$$r(t) = (4t, \frac{3t}{t-2}, e^t)$$

$$f(t) = 4t \Rightarrow f: \Re \to \Re$$

• 
$$g(t) = \frac{3t}{t-2} \Rightarrow f: \Re - \{2\} \rightarrow \Re$$

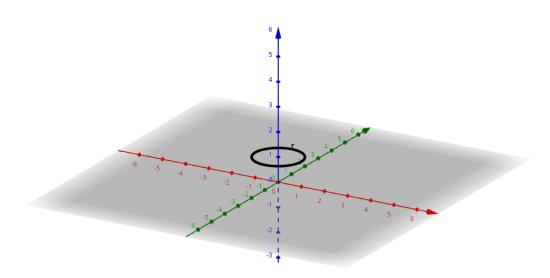
$$h(t) = e^t \Rightarrow \Re \to \Re$$

10. a) 
$$r(t) = (\cos(t), \sin(t), 1)$$

• 
$$f(t) = \cos(t) \Rightarrow f: \Re \rightarrow [-1, 1]$$

• 
$$g(t) = \sin(t) \Rightarrow f: \Re \rightarrow [-1, 1]$$

• 
$$h(t) = \cos(t) \Rightarrow f : \Re \to 1$$

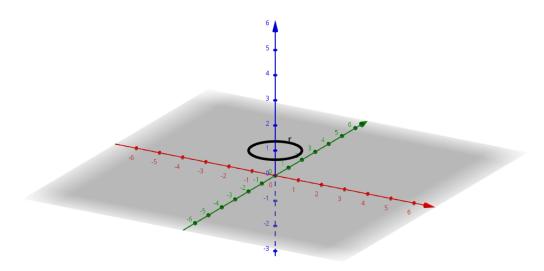


b) 
$$r(t) = (t, t^2, t - t^2)$$

$$f(t) = t \Rightarrow f: \Re \to [-1, 1]$$

$$\quad \bullet \ g(t) = t^2 \Rightarrow f: \Re \to [0, \infty +]$$

$$\bullet \ h(t) = t - t^2 \Rightarrow f: \Re \to [\infty -, \tfrac{1}{4}]$$

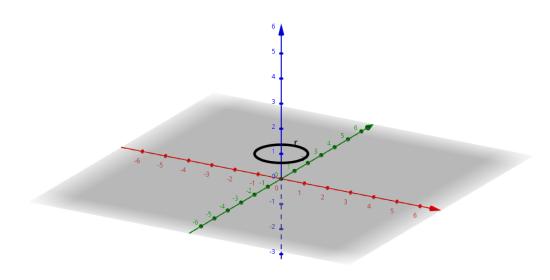


c) 
$$r(t) = (t^2 + t, t^2 - t, (t^2 - t)^2)$$

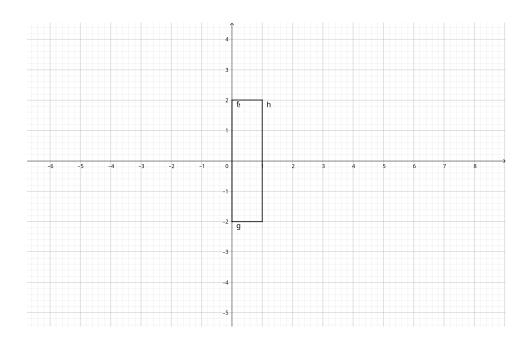
$$\quad \bullet \ f(t) = t^2 + t \Rightarrow f: \Re \to [-\tfrac{1}{4}, \infty +]$$

$$g(t) = t^2 - t \Rightarrow f: \Re \to \left[ -\frac{1}{4}, \infty + \right]$$

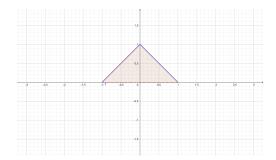
• 
$$h(t) = (t^2 - t)^2 \Rightarrow f : \Re \rightarrow [0, \infty +]$$



11. a) 
$$r(t) = \begin{cases} t(0; -4) + (0; 2)t \in [0, 1] \\ (t - 1)(1; 0) + (0; 2)t \in (1, 2) \\ (t - 2)(1; 0) + (0; -2)t \in [2, 3) \\ (t - 3)(0; -4) + (1; 2)t \in [2, 3] \end{cases}$$

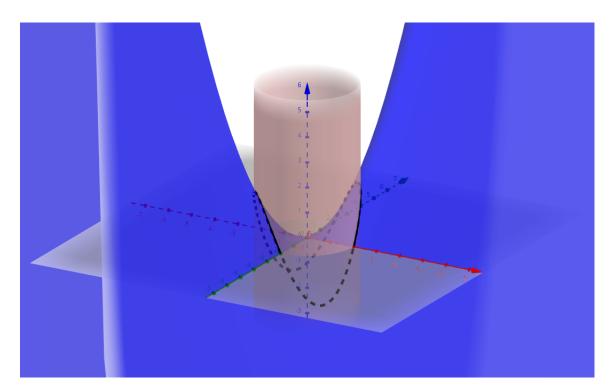


b) 
$$r(t) = \begin{cases} t(-2;0) + (1;0)t \in [0,1] \\ (t-1)(1;1) + (-1;0)t \in (1,2) \\ (t-2)(1;-1) + (0;1)t \in [2,3] \end{cases}$$



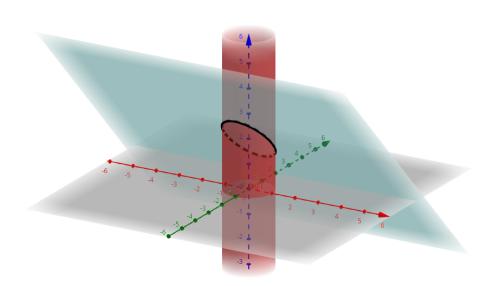
12. a) 
$$x^2 + y^2 = 4 \land z = x \cdot y$$

$$r(t) = \left\{ \begin{array}{l} x = 2\cos(t) \\ y = 2\sin(t) \\ z = 2\cos(t) \\ 0 \leq t \leq 2\pi \end{array} \right.$$



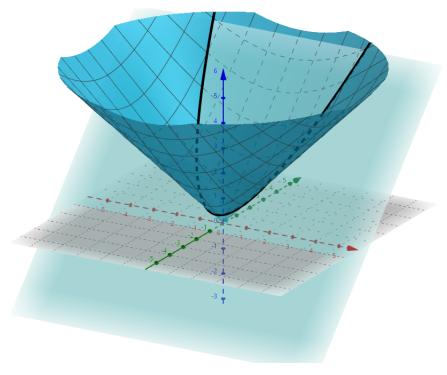
b) 
$$x^2 + y^2 = 1 \land y + z = 2$$

$$r(t) = \begin{cases} x = \cos(t) \\ y = \sin(t) \\ z = 2 - \sin(t) \\ 0 \le t \le 4\pi \end{cases}$$

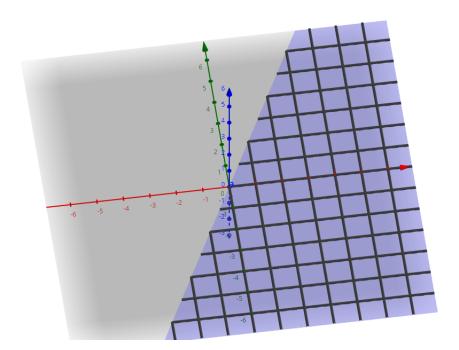


$$c) \ \ z = \sqrt{x^2 + y^2} \land z = 1 + y$$
 
$$1 + y = \sqrt{x^2 + y^2}$$
 
$$(1 + y)^2 = |x^2 + y^2|$$
 
$$y^2 + 2y + 1 = |x^2 + y^2|$$
 
$$y^2 + 2y + 1 = x^2 + y^2$$
 
$$y = \frac{x^2 - 1}{2}$$

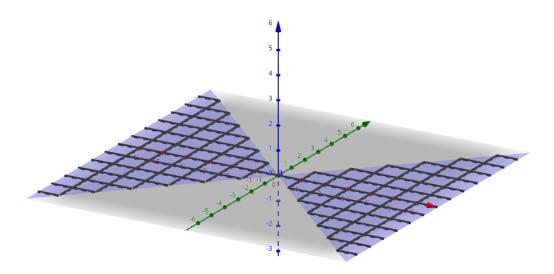
$$r(t) = \begin{cases} x = t \\ y = \frac{t^2 - 1}{2} \\ z = \frac{t^2 - 1}{2} + 1 \end{cases}$$



13. a) 
$$f(x,y) = \sqrt{2x - y}$$
  
 $\Leftrightarrow 2x - y \ge 0 \Leftrightarrow x \ge \frac{y}{2}$ 



$$b) \ f(x,y) = \sqrt{x^2 - y^2}$$
$$|x| \ge |y|$$



c) 
$$f(x, y, z) = ln(1 - x^2 - y^2 - z^2)$$
  
 $1 - x^2 - y^2 - z^2 \ge 0$ 

