

$$f(x, y) = x^2 + 4y^2 - 4xy + 2$$

$$\blacksquare f_x(x, y) = 2x + 4y^2 - 4y$$

$$x = 2(y - y^2)$$

$$(\frac{1}{2}, \frac{1}{2})$$

$$\blacksquare f_y(x, y) = 8y - 4x = 4(2y - x)$$

$$y = \frac{x}{2}$$

Ptos criticos: $\{(x, y) \in \mathbb{R}^2 : x = 2y\}$

$$H_f(x, \frac{x}{2}) = \begin{vmatrix} 2 & 8y - 4 \\ 8y - 4 & 8 \end{vmatrix} = 16 - 16(x - 1)^2 = 16(1 - (x^2 - 2x + 1)) =$$

$$16(-x^2 + 2x) = 16(x(-x + 2)) \Rightarrow$$

$$x = 0 \vee x = 2$$

$$x = -1 \Rightarrow < 0 \text{ pto silla}$$

$$x = 1 \Rightarrow > 0 \text{ minimo}$$

$$x = 3 \Rightarrow < 0 \text{ pto silla}$$