

$$1. \quad \blacksquare f(x, y) = x^3 y^4 + x^4 y^3$$

$$\blacksquare P = (1, 1)$$

$$\blacksquare \theta = \frac{\pi}{6}$$

$$\theta = \frac{\pi}{6} \equiv$$

$$x = \cos\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2}$$

$$y = \sin\left(\frac{\pi}{6}\right) = \frac{1}{2}$$

$$\Rightarrow \theta = \left(\frac{\sqrt{3}}{2}, \frac{1}{2}\right)$$

$$u = \frac{\theta}{\|\theta\|} = \left(\frac{\frac{\sqrt{3}}{2}}{\frac{\sqrt{10}}{2}}, \frac{\frac{1}{2}}{\frac{\sqrt{10}}{2}}\right) =$$

$$\left(\frac{\sqrt{3}}{\sqrt{10}}, \frac{1}{\sqrt{10}}\right)$$

$$f_x = 3x^2 y^4 + 4x^3 y^3$$

$$f_y = 4x^3 y^3 + 3x^4 y^2$$

$$f_x \wedge f_y \text{ son continua en todo } \mathbb{R}^2 \Rightarrow f \text{ es derivable} \Rightarrow$$

$$D_u f(1, 1) = \nabla f(1, 1) \cdot u$$

$$D_u f(1, 1) = (7, 7) \cdot \left(\frac{\sqrt{3}}{\sqrt{10}}, \frac{1}{\sqrt{10}}\right) = \frac{7\sqrt{3}}{\sqrt{10}} + \frac{7}{\sqrt{10}}$$

$$2. \quad \blacksquare f(x, y) = y e^{-x}$$

$$\blacksquare P = (0, 4)$$

$$\blacksquare \theta = \frac{2\pi}{3}$$

$$f_x = -y e^{-x}$$

$$f_y = e^{-x}$$

$$f_x \wedge f_y \text{ son continuas} \Rightarrow f \text{ es diferenciable en todo } \mathbb{R}^2 \Rightarrow$$

$$D_u f(0, 4) = \nabla f(0, 4) \cdot u$$

$$\theta = \left(\cos\left(\frac{2\pi}{3}\right), \sin\left(\frac{2\pi}{3}\right)\right) = \left(-\frac{1}{2}, \frac{\sqrt{3}}{2}\right)$$

$$u = \frac{\theta}{\|\theta\|} = \left(\frac{-1}{\sqrt{10}}, \frac{\sqrt{3}}{\sqrt{10}}\right)$$

$$D_u f(0, 4) = (-4, 1) \cdot \left(\frac{-1}{\sqrt{10}}, \frac{\sqrt{3}}{\sqrt{10}}\right) = \left(\frac{4}{\sqrt{10}}, \frac{\sqrt{3}}{\sqrt{10}}\right)$$