1.
$$f(x) = \frac{1}{1-x}$$

 $P_n(x) = 1 + x + x^2 + x^3 + x^4 + x^5 + \dots + x^n$

2.
$$f(x) = \cos(x)$$

$$P_n(x) = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!}..$$

3.
$$f(x) = \sin(x)$$

$$P_n(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!}..$$

4.
$$f(x) = e^{2x}$$

$$P_n(x) = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \frac{x^4}{4!} + \dots + \frac{x^n}{n!}$$

5.
$$f(x) = \frac{1}{(1-x)^2}$$

 $P_n(x) = 1 + 2x + 3x^2 + 4x^3 + 5x^4 + 6x^5 + \dots + (n+1)x^n$

6.
$$f(x) = \ln(1+x)$$

$$P_n(x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots + (-1)^{n+1} \frac{x^n}{n}$$