

$$f_x = \frac{2y}{\sqrt{x}} \quad f_y = 4\sqrt{x}$$

$$u = \frac{\nabla f(4,1)}{\|\nabla f(4,1)\|} =$$

$$\frac{(4,4)}{\sqrt{8}} = (\frac{2}{4}, \frac{2}{4})$$

$$D_u f(4,1) = (4,4) \cdot (\frac{2}{4}, \frac{2}{4}) = 4$$