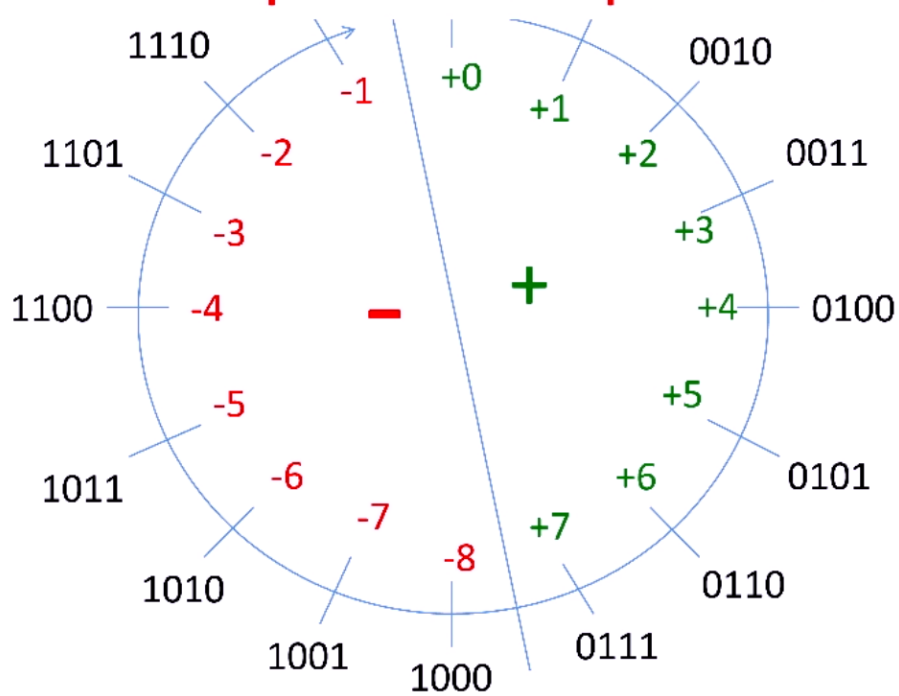


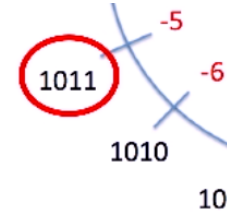
Two's Complement

- most significant bit is 1 if negative
- over/underflow as side effect



- subtraction equal to addition due to overflow

$$(+3) + (-5) = (-2)$$



$$\begin{array}{r}
 0011 \\
 + 1011 \\
 \hline
 1110
 \end{array}$$

- negation
 - flipping MSB
 - add 1

$$\begin{array}{rcl}
 -3: & 1 & 1 & 0 & 1 \\
 & \downarrow & \downarrow & \downarrow & \downarrow \\
 & 0 & 0 & 1 & 0 \\
 \text{Adding 1 makes the} & + & 0 & 0 & 0 & 1 \\
 \text{„two’s complement“} & & \hline
 +3: & 0 & 0 & 1 & 1
 \end{array}$$

Sign Extension

- required to add different sized numbers

Value A (16 bit): 7 (Binary: 00000000 00000111)

– Value B (8 bit): -1 (Binary: 11111111)

- fill up bits left of MSB with MSB

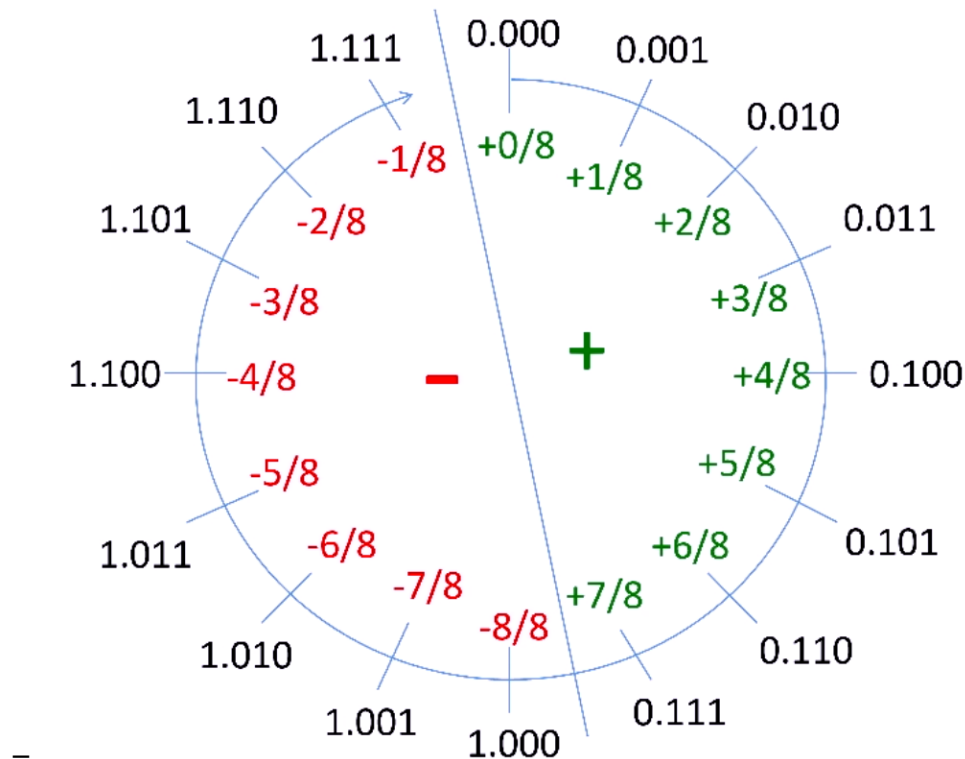
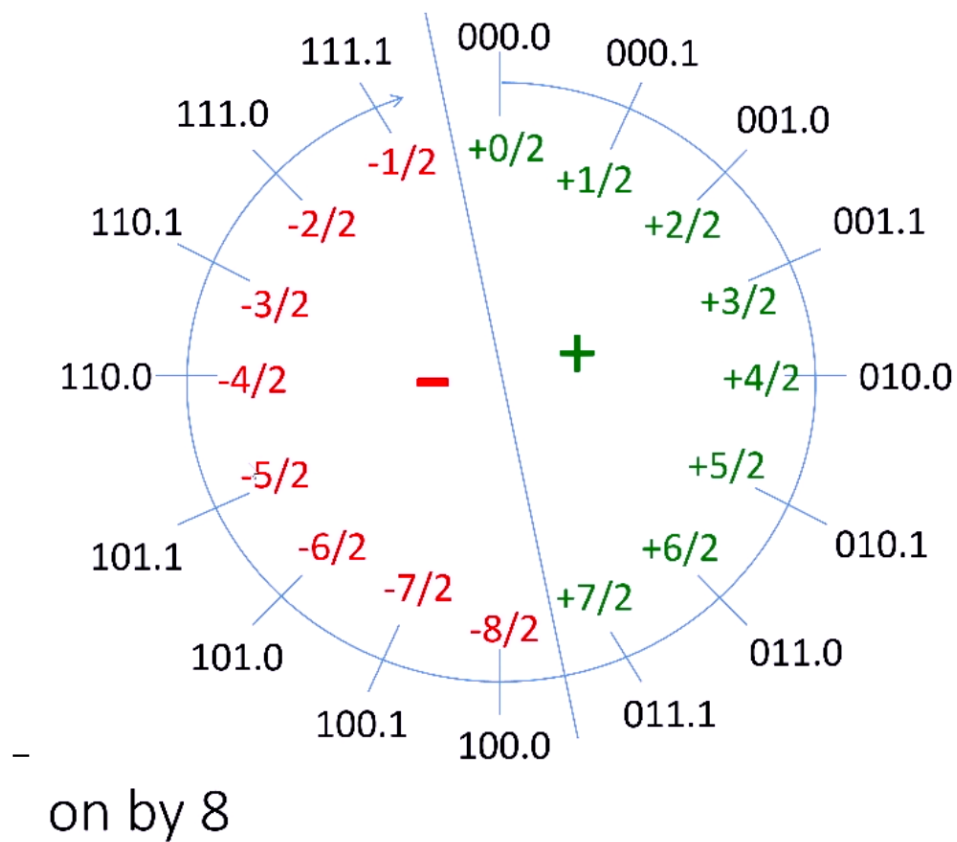
Value A (16 bit): 7 (Binary: 00000000 00000111)

Value B after sign extension (16 bit): -1 (Binary: 11111111 11111111)



Rational Numbers

- LSB represent fractions of 2



Multiplication and Division by the base

- multiplication by left shift
- division

- Arithmetic Shift Right
 - * shift right
 - * prior MSB as new MSB
- Logic Shift Right
 - * shift right
 - * 0 as new MSB