#### **Overview**

- written as A\* Algorithm
- [[Shortest Path Algorithms]] to find a single destination
- based on [[Breadth-First Search]] and [[Dijkstra's Algorithm]]
- informed
  - does not search uniformly
  - uses heuristics
  - prioritizes towards the direction of the goal

### **Heuristics**

**Def:** A heuristic is **consistent** if for every edge  $\{u, v\} \in E$  we have  $h(u) \le w(u, v) + h(v)$ 

- perfect heuristic
  - border line impossible
  - requires perfect knowledge lol
- overestimate
  - fast
  - not admissible
  - might not find path even if one exists

#### **A\*** Heuristics

- g(v)
  - distance from start to current vertex
- *h*(*u*)
  - distance from current vertex to end
    - \* "Luftlinie" as the crow flies
  - ignores obstacles which may block the path
  - underestimates the future cost
    - \* good characteristic
- therefore pretty efficient

## Comparison between A\* and Dijkstra's

• A\*

-									
				2+ 7?	3+ 6?	4+ 5?	5+ 4?	6+ 3?	6+ 1
_			2+ 7?	1	2	3	4	5	6
		2+ 7?	1		1	2	3	6	9
			2+ 7?	1	2	3	4	6+ 2?	
				2+ 7?	3+ 6?	4+ 5?	5+ 4?		

## • Dijkstra's

	7?	6	5	4	3	4	5	6	7?	
7?	6	5	4	3	2	3	4	5	6	7
6	5	4	3	2	1	2	3	4	5	6
5	4	3	2	1	0	1	2	3	6	7!
6	5	4	3	2	1	2	3	4	7?	
7?	6	5	4	3	2	3	4	5	6	7?
	7?	6	5	4	3	4	5	6	7?	

## Algorithm

Input: G(V,E,W) start point:  $\overline{S}$ , end point:  $\overline{t}$ Initialize S={s}, g(s)=0, g(V\N(s))= $\infty$ , g(v)=w(s,v), v∈ N(s)



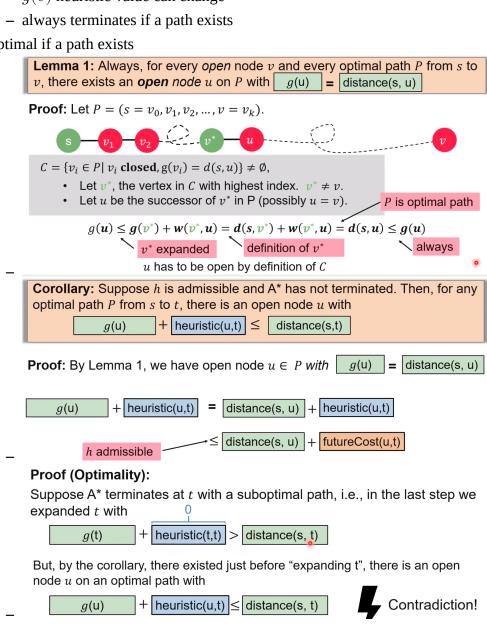
S: expanded/closed vertices  $V \setminus S$ : the open vertices g(v) + g(v) is the length of the best known (!) path from s to v

```
While t ∉ S do
u = \operatorname{argmin}_{u \in V \setminus S} \{g(u) + h(u, t)\}
                                                     g(v) is the length of the best
                                              h(u)
                                                     known (!) path from s to v
      For v s.t. {u, v}∈ E do
          temp=min{g(v),g(u)+w(u,v)}
                                                     h(u,t) is a heuristic guess for
          If temp < g(v) then:
                                                     the path from u to t.
               g(v) = temp
              S=S\setminus\{v\}
                                //does nothing if v \notin S
      S=S \cup \{u\}
                                    S might decrease!
```

red parts differ from [[Dijkstra's Algorithm]]

## **Properties**

- nodes may expand more than once
  - -g(v) heuristic value can change
- optimal if a path exists



- optimally efficient
  - with regards to the number of vertices expanded
- space as bottle neck

# g(v) + h(v) is stored for each visited v

**15-Puzzle:** Search space has a node for each configuration: 16!=20.922.789.888.000 vertices!

- motivation for memory bounded heuristic search
  - \* Iterative deepening A\*