Terminology

- threat
 - potential violation of security
- vulnerability
 - concrete flaw in the implementation
- exploit/attack
 - concrete attempt to violate the security

Passwords

- they suck:)
- can be based on what someone knows/has/is
- · password storage
 - plain passwords
 - * weak to eavesdropping (e.g. replay attack)
 - * vulnerable password table
 - hashed passwords
 - * still allows mass dictionary attacks
 - hashed passwords with salt
 - * no more parallel attacks
 - * no longer leaks users with identical password
- · weak authentication is susceptible to replay attacks
 - challenge-response
 - prove you know the secret without telling
 - e.g. TOTP

Authenticity using hash functions

3 Properties of Hash Functions:

- 1) Preimage restistance: T known, must be infeasible to find any message M that produces T (2t)
- 2) Second preimage resistance: M known, must be infeasible to find M' with same hash (2t)
- 3) Collision resistance: Must be infeasible to find two messages with the same hash $(2^{t/2})$
- birthday paradox
 - $-2^{t/2}$ messages => 2^{t-1} message pairs
 - collision probability for one pair is $\frac{1}{2^t} = 2^{-t}$
 - probability for at least one collision $\sim \frac{1}{2}$
- Compression function
 - hash function for fixed-size input
- MD-Hash
 - hash function for input of arbitrary size

- * iterates a compression function
- padding always applied so the input is a multiple of the block size
- hash=tag

MAC

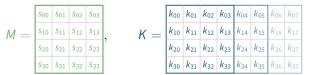
- hash function which uses symmetric key K (k-bits) to compute tag t (t-bits) for authentication of message M
- HMAC = hash based MAC
- application
 - * compute T for M
 - * send M and T
 - * receiver recomputes new tag T' on M
 - * receiver verifies T=T'
- unforgeability
 - * infeasible for attacker to forge any new valid pair (M,T) even if they can query tags for any other messages
- complexity
 - * Exhaustive key search takes $\sim 2^k$ offline trials
 - * Guessing the tag takes $\sim 2^t$ online trials
- Signatures
 - uses encryption instead of hashing
 - uses asymmetric private key K to encrypt message M to a signature S
 - send M and S
 - receiver decrypts S with public key to M' and verifies M=M'

Confidentiality using encryption

- block ciphers
 - bijective permutation E_K based on k-bit key K to encrypt n-bit message blocks M into n-bit cipher text blocks ${\bf C}$
 - inverse permutation ${\cal D}_K={\cal E}_K^{-1}$ for decryption
 - complexity
 - * 2^k possible keys(mappings)
 - * 2^n possible outputs for input
 - requirements
 - * pseudorandomness
 - unable to learn M from C (or vice-versa)
 - * key recovery security
 - unable to recover K given any arbitrary number of (M, C) pairs
- key-alternating using key schedule

- each round/iteration depends on different round key which has been derived from K
- e.g. AES
 - Block size n = 128 bits
 - Key size $k \in \{128, 192, 256\}$ bits \rightarrow ciphers AES-128, AES-192, AES-256
 - The 16-byte input block $M = s_{00} ||s_{10}||s_{20}||s_{30}||s_{01}|| \dots ||s_{33}|$ is written as a 4×4 matrix of bytes, the $\{16, 24, 32\}$ -byte key K as a $4 \times \{4, 6, 8\}$ matrix:

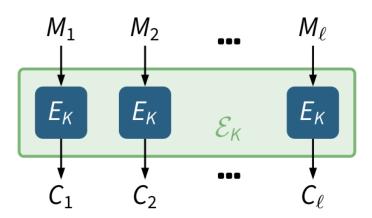
$$M = \begin{bmatrix} s_{00} & s_{01} & s_{02} & s_{03} \\ s_{10} & s_{11} & s_{12} & s_{13} \\ s_{20} & s_{21} & s_{22} & s_{23} \\ s_{30} & s_{31} & s_{32} & s_{33} \end{bmatrix},$$



- The state is initialized to M and updated in 10 rounds (for AES-128) or 12 rounds (AES-192) or 14 rounds (AES-256).
- * SubBytes
 - substitute using lookup table S-box with original byte as key
 - \bullet $b_{ij} = S[a_{ij}]$
- * ShiftRows
 - shift row i by i bytes to the left
 - $b_{ij} = a_{i(j+i\%4)}$
- * MixColumns
 - multiplication of each column with constant matrix M

$$(b_{0j},b_{1j},b_{2j},b_{3j})=M\cdot(a_{0j},a_{1j},a_{2j},a_{3j})$$

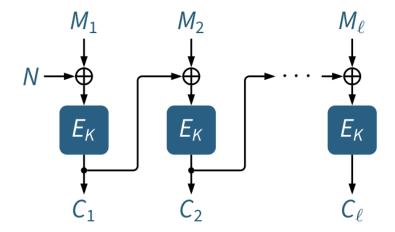
- * AddRoundKey
 - XOR with $k^{(r)}$
 - $b_{ij} = a_{ij} \oplus k^{(r)}$
- · regular encryption
 - does not provide authentication
 - ECB



 \triangle Patterns: Two identical blocks M_i , M_j get encrypted to the same C_i , C_i

 \triangle Context: Two identical messages M, M' get encrypted to the same C, C'

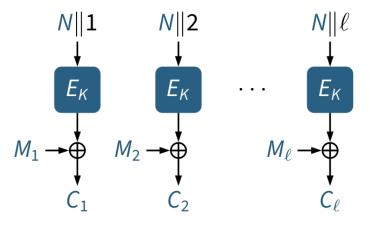
- CBC



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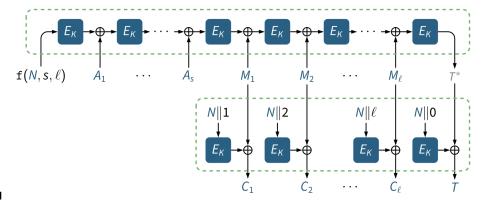
* C also depends on nonce and previous blocks

- CTR



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- * C also depends on nonce and block index
- Authenticated Encryption (with Associated Data)
 - * produces cipher text C and tag T for message M using symmetric key K, nonce N and associated data A (e.g. metadata or system parameters)
 - * some TLS 1.3 authenticated ciphers
 - ◆ AES-CCM (CTR using AES encryption with CBC-MAC authentication)



- ◆ AES-GCM (default)
- · Asymmetric encryption schemes
 - Preliminary maths
 - * Euler function for product n of 2 primes p, q

•
$$\varphi(n) = \varphi(pq) = (p-1)(q-1)$$

- * Euler theorem
 - a,n are coprime $\Leftrightarrow a^{\varphi(n)} \equiv 1 \pmod{n}$

Discrete Logarithm Problem

Given a prime number p, a generator $g \in \mathbb{Z}_p^*$, and an element $y \in \mathbb{Z}_p^*$, find the integer $x \in \{0, \dots, p-2\}$ such that $\underbrace{g \cdot g \cdots g}_{x \text{ times}} = g^x \equiv y \pmod{p}$.

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Integer Factorization Problem

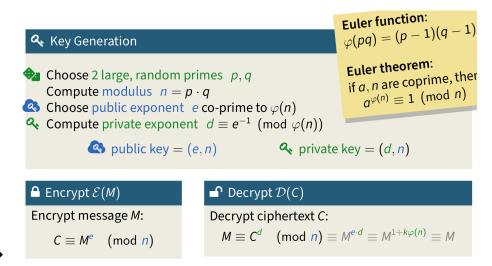
Given $n \in \mathbb{N}$, find primes p_i and exponents $e_i \in \mathbb{N}$ such that $n = p_1^{e_1} \cdot p_2^{e_2} \cdots p_k^{e_k}$

Diffie-Hellman Problem (DHP)

Given generator $\alpha \in \mathbb{Z}_p^*$ and $\alpha^a \pmod p$, $\alpha^b \pmod p$, find $K_{AB} = \alpha^{a \cdot b}$.

RSA Problem (RSAP)

- Given modulus n, exponent e, ciphertext C: find M such that $M^e \equiv C \pmod{n}$.
- Key exchange
 - * agree on shared symmetric key while communicating over insecure channel
 - * Diffie-Hellman
 - ullet public: large prime p and generator α
 - Alice chooses private key $a \in 2, ..., p-2$ and sends public key α^a to Bob
 - ullet Bob chooses private key $b\in 2,...,p-2$ and sends public key α^b to Alice
 - $\bullet \ K_{AB} \equiv (\alpha^b)^a \ (\text{mod } p) \equiv (\alpha^a)^b \ (\text{mod } p)$
- Asymmetric encryption
 - * uses private and public key
 - * RSA



- Square-and-Multiply b^e
 - $\blacksquare result := 1$
 - for each bit in e
 - $ightharpoonup result := result^2$
 - ▲ if bit is set
 - \bullet result := result * b
- ◆ textbook RSA is deterministic
 - use padding scheme
 Indistinguishability (under Adaptive Chosen-Ciphertext Attack)

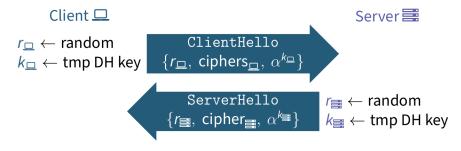
An attacker who knows the public key, chooses 2 messages M_0 , M_1 , and gets ciphertext C can not distinguish whether $C = E(M_0)$ or $C = E(M_1)$,

- even if they can ask for decryption of any $C^* \neq C$.
- e.g. RSAES-OAEP

Protocols

- problem with static asymmetric crypto
- no forward secrecy
 - if private key is leaked \Rightarrow all past communications compromised
- · no authenticity
 - no assurance with whom the key is exchanged
- Ephemeral Diffie-Helman DHE
 - Alice and Bob both have long term private/public key pair
 - execute regular DH over insecure channel
 - st both compute the same K_{AB}
 - send each other the signed transcript (all previous message) of the exchange
 - signed with long term private keys
 - send each other MAC-tag of transcript
 - * use K_{AB} to create tag

- throw away public/private keys a,b,α^a,α^b from DH
- Transport Layer Security TLS
 - Key exchange using DHE
 - * exchange ephemeral public DH key, randomness and list of preferred symmetric ciphers



- Authentication
 - * server sends certificate, signature over transcript and HMAC of transcript
 - signature using long term private key
 - HMAC using K_AB
 - * client sends HMAC of transcript back



- Sending application data
 - st send messages encrypted with new symmetric keys derived from K_{AB} with HKDF
 - ◆ HMAC-based key derivation function

Certificates + ties public key to an identity + X.509 standard contains + public key + identity information (e.g. name) + validity period + signature from a certificate authority CA + which issued the certificate

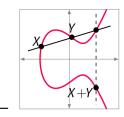
Miscellaneous

Kerckhoffs' Principle

A cryptosystem should be secure even if everything about the system, except the key, is public knowledge.

aka Shannon's Maxim: "The enemy knows the system" Opposite of "Security by obscurity"

- Elliptic Curve Cryptography ECC
 - An attractive alternative is the Elliptic Curve group, where each element is not an integer but a 2-dimensional point with two integer coordinates. The group operation is addition with special point addition formulas.



EC Discrete Logarithm Problem (ECDLP)

Given points P, Q on an elliptic curve with

$$Q = k \cdot P = \underbrace{P + P + \dots + P}_{k \text{ times}}$$

$$\text{wind } k$$

Find k.

- End-to-End Encryption
 - may require more security properties

Security properties: confidentiality, integrity, authentication, forward secrecy, post-compromise security, participant consistency, destination validation,

causality preservation, message unlinkability, message repudiation, participation repudiation, asynchronicity, ...

- Secure Multiparty Computation
 - multiple parties compute a result together without sharing their inputs
 - e.g. compute sum of consumed electricity without exposing each household's individual consumption
- Private Set Intersection
 - find intersection of two sets without sharing their content
 - e.g. tell new user which of their contacts also use Whatsapp without exposing all contacts to Whatsapp or all Whatsapp users to the new user
- RNG
 - nondeterministic hardware source
 - * generate random number from physical process
 - deterministic pseudorandomness
 - * PRNG generates random number (sequence) based on initial value
- Quantum Computing
 - new means of solving algorithms
 - Shor's algorithm solves IFP and DLP in polynomial time
 - breaks signatures (RSA) and key exchange (DH, ECC)
 - symmetric encryption is now slightly weaker
- Common crypto failures
 - using no/obsolete/backdoored/insufficient crypto
 - homebrew protocols
 - * combining secure primitives in an insecure manner

- improper key usage
- improper password storage
- bad RNG, low entropy
- reusing nonces

[[Kryptographie]]