Computational Intelligence 2023/2024 - Final Report

The aim of this report is to create a log-file to explain the work I did during the Computational Intelligence course.

LAB 1 - A*

- The goal of this lab is to solve the "Set Covering Problem" using the A* algorithm.
- Given a template of the problem, we need to build a new H function
- In the code, three different versions of the H function, have been developed
- You can see useful comments in the code

Solution

```
from random import random
from functools import reduce
from collections import namedtuple
from queue import PriorityQueue
from math import ceil
import numpy as np
PROBLEM SIZE = 15
NUM SETS = 25
SETS = tuple(
np.array([random() < 0.3 for _ in range(PROBLEM_SIZE)])</pre>
for _ in range(NUM_SETS)
State = namedtuple('State', ['taken', 'not_taken'])
def goal check(state):
    return np.all(reduce(
        np.logical_or,
        [SETS[i] for i in state.taken],
        np.array([False for _ in range(PROBLEM_SIZE)]),
    ))
def covered(state):
    return reduce(
        np.logical or,
        [SETS[i] for i in state.taken],
        np.array([False for _ in range(PROBLEM_SIZE)]),
    )
```

```
def g(state):
    return len(state.taken)
# number of positions to cover to reach the goal
def h1(state):
    return PROBLEM SIZE - sum(
        covered(state))
def h2(state):
    covered_tiles = sum(covered(state))
    if covered tiles == PROBLEM SIZE:
        return 0
    return 1 / covered tiles if covered tiles != 0 else 1
# We only considered the sets not taken,
# so as not to be influenced by the existence of large sets which have already
been taken
def h3(state):
    not taken sets = [s for i, s in enumerate(SETS) if i not in state.taken]
    largest_set_size = max(sum(s) for s in not_taken_sets) # select the larget
tiles (more number of true)
    missing size = PROBLEM SIZE - sum(covered(state)) # evaluates the number of
tiles that are not covered
    optimistic_estimate = ceil(missing_size / largest_set_size) # estimate the
number of set that are missing for the solution in a optimistic way
    # if the largest set is 5 and the missing size is 10 --> "maybe" 2 sets are
missing (optimistic assumption)
    return optimistic estimate
def f1(state):
    cost 1 = g(state)
    cost 2 = h1(state)
    return cost 1 + cost 2
# since h2 is a value between 0 and 1, we multiply it by 0.1 to make it more
significant
def f2(state):
    cost 1 = 0.1*g(state)
    cost_2 = h2(state)
    return cost_1 + cost_2
def f3(state):
    cost_1 = g(state)
    cost 2 = h3(state)
```

```
return cost_1 + cost_2
assert goal_check(
    State(set(range(NUM SETS)), set())
), "Problem not solvable"
# SOLUTION WITH H1
frontier = PriorityQueue()
state = State(set(), set(range(NUM SETS)))
frontier.put((f1(state), state))
counter = 0
_, current_state = frontier.get()
while not goal_check(current_state):
    counter += 1
    for action in current_state[1]:
        new_state = State(
            current_state.taken ^ {action},
            current_state.not_taken ^ {action},
        frontier.put((f1(new_state), new_state))
    _, current_state = frontier.get()
print(
    f"Solved in {counter:,} steps ({len(current_state.taken)} tiles)"
Result: "Solved in 3 steps (3 tiles)"
#SOLUTION WITH H2
frontier = PriorityQueue()
state = State(set(), set(range(NUM_SETS)))
frontier.put((f2(state), state))
counter = 0
_, current_state = frontier.get()
while not goal_check(current_state):
    counter += 1
    for action in current_state[1]:
        new_state = State(
            current_state.taken ^ {action},
            current_state.not_taken ^ {action},
        frontier.put((f2(new_state), new_state))
    _, current_state = frontier.get()
print(
    f"Solved in {counter:,} steps ({len(current_state.taken)} tiles)"
)
```

```
#SOLUTION WITH H3
frontier = PriorityQueue()
state = State(set(), set(range(NUM_SETS)))
frontier.put((f3(state), state))
counter = 0
_, current_state = frontier.get()
while not goal_check(current_state):
    counter += 1
    for action in current_state[1]:
        new_state = State(
            current_state.taken ^ {action},
            current_state.not_taken ^ {action},
        frontier.put((f3(new_state), new_state))
    _, current_state = frontier.get()
print(
    f"Solved in {counter:,} steps ({len(current_state.taken)} tiles)"
```

- *Collaborations*: Worked with Angelo Iannielli s317887
- Peer Reviews: Not requested for this Lab

Result: "Solved in 412 steps (3 tiles)"

Halloween Challenge - Set Covering

The aim of this challenge is to obtain the best results on a set covering problem with different algorithm, minimizing the number of calls to the fitness function

Two proposed solutions:

- Simulated Annealing: it is just an attempt but not properly working
- Tabu Search: results shown later

Solution

```
from itertools import product
import numpy as np
from scipy import sparse
from random import random, choice, randint, seed
from functools import reduce
from copy import copy
import math
import matplotlib.pyplot as plt
num_points = [100, 1_000, 5_000]
num sets = num points
density = [0.3, 0.7]
points = num points[1]
sets = num sets[1]
den = density[1]
iterations = 4000
def make_set_covering_problem(num_points, num_sets, density):
    """Returns a sparse array where rows are sets and columns are the covered
items"""
    seed(num_points * 2654435761 + num_sets + density)
    sets = sparse.lil_array((num_sets, num points), dtype=bool)
    for s, p in product(range(num sets), range(num points)):
        if random() < density:</pre>
            sets[s, p] = True
    for p in range(num_points):
        sets[randint(0, num sets - 1), p] = True
    return sets
SETS = make_set_covering_problem(points, sets, den)
```

```
Hill Climbing
# Taken from Giovanni Squillero's notebook on Github
def evaluate(state):
    cost = sum(state)
    valid = np.all(
        reduce(
            np.logical or,
            [SETS.getrow(i).toarray().flatten() for i, t in enumerate(state) if
t],
            np.array([False for _ in range(points)]),
        )
    )
    return valid, -cost if valid else 0
def tweak(state):
    new_state = copy(state)
    index = randint(0, sets - 1)
    new_state[index] = not new_state[index]
    return new_state
#current state = [choice([True, False]) for _ in range(sets)]
current_state = [choice([False]) for _ in range(sets)]
taken sets = []
iteration sets = []
for step in range(iterations):
    new_state = tweak(current_state)
    if evaluate(new state) >= evaluate(current state):
        current state = new state
        # print(current_state, evaluate(current_state))
        taken_sets.append(-evaluate(current_state)[1])
        iteration sets.append(step)
        print("Step: " + str(step) + " Current state: " +
str(evaluate(current state)))
print("Final state:", evaluate(current state))
plt.plot(iteration sets, taken sets)
plt.xlabel("Iterations")
plt.ylabel("Taken Sets")
plt.show()
Simulated Annealing
def acceptance_probability(current_solution, tweaked_solution, temp):
    x = -abs(current solution[1] - tweaked solution[1]) / temp
    return math.exp(x)
#current_state = [choice([True, False]) for _ in range(sets)]
```

current_state = [choice([False]) for _ in range(sets)]

```
temp_array = []
probability_array = []
taken_sets = []
iteration sets = []
for step in range(iterations):
    new state = tweak(current state)
    temp = iterations / (5 * step + 1)
    temp_array.append(temp)
    p = acceptance_probability(evaluate(current_state), evaluate(new_state), temp)
    probability array.append(p)
    if evaluate(new_state) >= evaluate(current_state) or random() < p:</pre>
        current state = new state
        # print(current state, evaluate(current state))
        taken_sets.append(-evaluate(current_state)[1])
        iteration_sets.append(step)
        print("Step: " + str(step) + " Current state: " +
str(evaluate(current_state)))
print("Final state:", evaluate(current_state))
plt.plot(iteration_sets, taken_sets)
plt.xlabel("Iterations")
plt.ylabel("Taken Sets")
plt.show()
plt.plot(range(iterations), temp array)
plt.xlabel("Iterazioni")
plt.ylabel("Temperature")
plt.show()
plt.plot(range(iterations), probability_array)
plt.xlabel("Iterations")
plt.ylabel("Acceptance Probability")
plt.show()
Tabu Search
temperature = 1000
cooling_rate = 0.8
taboo_list = []
temp_array = []
iteration_sets = []
probability_array = []
def find_greatest_set(x):
    return x.sum(axis=1).argmax()
def evaluate_2(state):
    cost = sum(state)
```

```
elem covered = reduce(
        np.logical_or,
        [SETS.getrow(i).toarray() for i, t in enumerate(state) if t],
        np.array([False for _ in range(points)]),
    )
    valid = np.all(elem_covered)
    num_elem_covered = np.count_nonzero(elem_covered)
    return valid, num_elem_covered, -cost
def tweak 2(state):
    new_state = copy(state)
    while new_state in taboo_list:
        index = randint(0, sets - 1)
        new state[index] = not new state[index]
    taboo_list.append(new_state)
    return new state
## Initialize the taboo list
taboo_list.clear()
## Find the set that cover the most num of elements and use it as starting point
current_solution = [False] * sets
current_solution[find_greatest_set(SETS)] = True
current_cost = evaluate_2(current_solution)
# Memorize that as the best solution for the moment
best_solution = [True] * sets
best_cost = (True, points, -sets)
# Insert the starting point into taboo list
taboo_list.append(current_solution)
for step in range(iterations):
    # Find a new possible solution
    new_state = tweak_2(current_solution)
    # print(new state)
    # Evaluate the cost
    new_cost = evaluate_2(new_state)
    print(new_cost)
    # Calculate deltaE using the number of taken elements
```

```
deltaE = - ( new_cost[1] - current_cost[1] )
print(deltaE)
if deltaE == 0:
    # Calculate deltaE using the number of taken sets
    deltaE = - ( new_cost[2] - current_cost[2] )
# The solution is better
if deltaE < 0:</pre>
    current_solution = new_state
    current_cost = new_cost
    if current_cost[2] > best_cost[2] and current_cost[0] == True:
        best solution = current solution
        best_cost = current_cost
else:
    probability = math.exp(-deltaE / temperature)
    probability_array.append(probability)
    if random() < probability:</pre>
            current_solution = new_state
            current_cost = new_cost
temperature *= cooling_rate
temp_array.append(temperature)
iteration_sets.append(step)
```

Results: (only for Tabu Search since it was the best)

size	density	Best result	Calls to solution	Total calls	
100	0.3	-7	504	1000	
1000	0.3	-15	991	1000	
5000	0.3	-21	545	1000	
100	0.7	-3	460	1000	
1000	0.7	-6	4	1000	
5000	0.7	-7	5	1000	

- *Collaborations*: Worked with Angelo Iannielli s317887
- Peer Reviews: Not requested for the challenge.

LAB 2 - NIM with ES

The goal of this lab is to write agents able to play [Nim], with an arbitrary number of rows and an upper bound k on the number of objects that can be removed in a turn (a.k.a., *subtraction game*).

The goal of the game is to **avoid** taking the last object.

- Task2.1: An agent using fixed rules based on *nim-sum* (i.e., an *expert system*)
- Task2.2: An agent using evolved rules using ES

Solution

```
import logging
from pprint import pprint, pformat
from typing import Callable
from collections import namedtuple
import random
from copy import deepcopy
import matplotlib.pyplot as plt
import random
import numpy as np
NUM ROWS = 5
K = None
NUM MATCHES = 200
\lambda = 20
\sigma = 0.1
GENERATION_SIZE = 500 // \lambda
random.seed(42)
Nimply = namedtuple("Nimply", "row, num objects")
class Nim:
    def __init__(self, num_rows: int, k: int = None) -> None:
        # Initialize the Nim object with given number of rows and an optional
maximum object limit
        self._rows = [
            i * 2 + 1 for i in range(num rows)
        # Create a list of odd numbers as row sizes
        self. k = k # Store the maximum object limit
    def __bool__(self):
        # Return True if there are objects remaining in the game, False otherwise
        return sum(self. rows) > 0
    def __str__(self):
        # Return a string representation of the object
        return "<" + " ".join(str(_) for _ in self._rows) + ">"
    @property
```

```
def rows(self) -> tuple:
        # Return the rows as a tuple
        return tuple(self. rows)
    def nimming(self, ply: Nimply) -> None:
        # Perform a nimming move by removing objects from a specified row
        row, num_objects = ply # Unpack the tuple
        assert (
            self._rows[row] >= num_objects
        ) # Check if the specified row has enough objects
            self. k is None or num objects <= self. k</pre>
        ) # Check if the number of objects is within the maximum limit
        self. rows[
            row
        ] -= num objects # Subtract the number of objects from the specified row
def pure random(state: Nim) -> Nimply:
    """A completely random move"""
    # Select a row that has at least one object remaining
    row = random.choice([r for r, c in enumerate(state.rows) if c > 0])
    # Randomly choose a number of objects to remove from the selected row
    num objects = random.randint(1, state.rows[row])
    # Create and return a Nimply object representing the chosen move
    return Nimply(row, num_objects)
def gabriele(state: Nim) -> Nimply:
    """Pick always the maximum possible number of the lowest row"""
    # Generate a list of possible moves
   possible moves = [(r, o) for r, c in enumerate(state.rows) for o in range(1, c
    # Select the move with the maximum number of objects from the lowest row
    return Nimply(*max(possible moves, key=lambda m: (-m[0], m[1])))
def nim_sum(state: Nim) -> int:
    tmp = np.array([tuple(int(x) for x in f"{c:032b}") for c in state.rows])
    xor = tmp.sum(axis=0) \% 2
    return int("".join(str(_) for _ in xor), base=2)
def analize(raw: Nim) -> dict:
    cooked = dict()
    cooked["possible_moves"] = dict()
    for ply in (Nimply(r, o) for r, c in enumerate(raw.rows) for o in range(1, c +
1)):
        tmp = deepcopy(raw)
        tmp.nimming(plv)
        cooked["possible_moves"][ply] = nim_sum(tmp)
    return cooked
```

```
def optimal(state: Nim) -> Nimply:
    analysis = analize(state)
    logging.debug(f"analysis:\n{pformat(analysis)}")
    spicy_moves = [ply for ply, ns in analysis["possible_moves"].items() if ns !=
0]
    if not spicy moves:
        spicy_moves = list(analysis["possible_moves"].keys())
    ply = random.choice(spicy_moves)
    return ply
def state info(state: Nim) -> dict:
    info = dict()
    info["possible_moves"] = [
        (r, o) for r, c in enumerate(state.rows) for o in range(1, c + 1)
    info["shortest row"] = min(
        (x for x in enumerate(state.rows) if x[1] > 0), key=lambda y: y[1]
    [0](
    info["longest_row"] = max((x for x in enumerate(state.rows)), key=lambda y:
y[1])[0]
    info["random row"] = random.choice([r for r, c in enumerate(state.rows) if c >
01)
```

Evolved Strategy

return info

In the evolved strategy we introduce 5 different kind of strategies (i.e. way to choose an action in the game)

- "shortest": chooses the shortest row and removes a random number of objects from it.
- "longest": chooses the longest row and removes a random number of objects from it.
- "random": chooses a random row and removes a random number of objects from it.
- "half_random": chooses a random row and removes half of the objects from it, rounded up.
- "one_random": chooses a random row and removes only one object from it.

An individual is a set of probabilities to choose one of the previous strategy. The algorithm selects the best individuals adapting the probabilities.

```
def evolved_strategy(genome) -> Callable:
    strategy_dict = {0: "shortest", 1: "longest", 2: "random", 3: "half_random",
4: "one_random"}

def adaptive(state: Nim) -> Nimply:
    data = state_info(state)

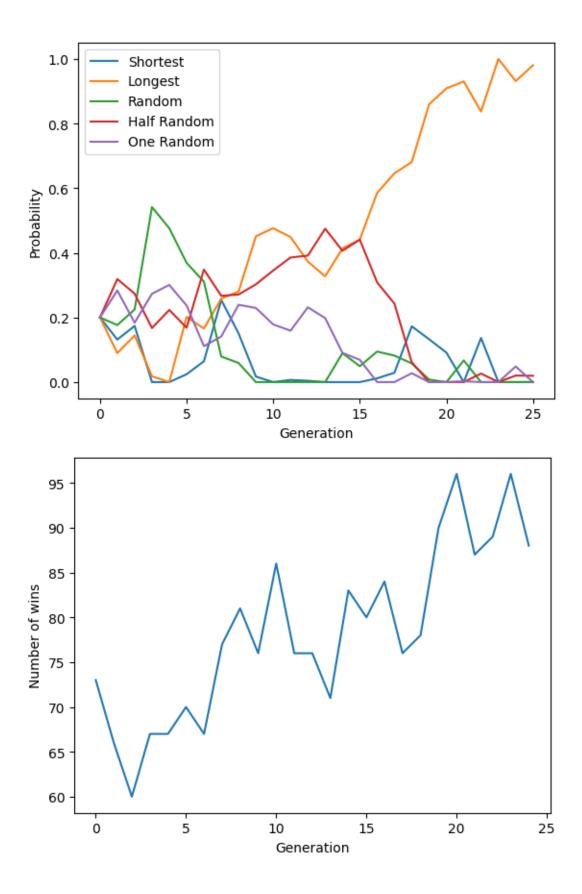
# select a strategy in a random way wheighed by the genome
```

```
selected_strategy = random.choices(range(len(genome)), weights=genome)[0]
        selected_strategy = strategy_dict[selected_strategy]
        if selected strategy == "shortest":
            ply = Nimply(
                data["shortest row"],
                random.randint(1, state.rows[data["shortest_row"]]),
            )
        elif selected strategy == "longest":
            ply = Nimply(
                data["longest row"], random.randint(1,
state.rows[data["longest_row"]])
        elif selected strategy == "random":
            ply = Nimply(
                data["random_row"], random.randint(1,
state.rows[data["random row"]])
        elif selected_strategy == "half_random":
            ply = Nimply(data["random row"], (state.rows[data["random row"]] // 2
+ 1))
        elif selected_strategy == "one_random":
            ply = Nimply(data["random row"], 1)
        # else:
        # ply = optimal(state)
        return ply
    return adaptive
The fitness function is evaluated as the percentage of victories of the individual against a player
that plays with the optimal strategy
# In the fitness function we play Nim for NUM MATCHES times where the player is:
# adaptive: for each move, choose a rule in a random way wheighed by the genome
# optimal: choose the optimal move
# Since "optimal" strategy is our upper bound, we can find the best individual
among population by comparing it with an individual that plays always with the
optimal solution
def fitness(adaptive: Callable) -> int:
    opponent = (adaptive, optimal)
    for _ in range(NUM_MATCHES):
        nim = Nim(NUM ROWS)
        player = 0
        while nim:
            ply = opponent[player](nim)
```

nim.nimming(ply) # perform the move

```
player ^= 1
        if player == 0:
            won += 1
    return won # return the number of matches won
def generate offsprings(offspring) -> list:
    output = []
    for _ in range(\lambda):
        new_offspring = [
            np.clip(val + np.random.normal(\emptyset, \sigma), \emptyset, 1) for val in offspring
        current_sum = sum(new_offspring)
# Normalize the sum to 1 if it is not already
        if current_sum != 1:
            scale factor = 1 / current sum
            # Apply scale factor to each value
            values = [val * scale_factor for val in new_offspring]
        else:
            values = new_offspring
        output.append(values)
    return output
(1,\lambda)-ES
current solution = (0.20, 0.20, 0.20, 0.20, 0.20)
choosen probability = list()
solutions list = list()
for n in range(GENERATION SIZE):
    # offspring <- select \lambda random points mutating the current solution
    # print("Starting probability for generation", n+1, "is:", current_solution)
    offsprings = generate offsprings(current solution)
    offsprings.append(current solution)
    # evaluate and select best
    evals = [
        (offspring, fitness(evolved_strategy(offspring))) for offspring in
offsprings
    evals.sort(key=lambda x: x[1], reverse=True)
    # pprint(evals)
```

```
current_solution = evals[0][0]
    choosen_probability.append(current_solution)
    solutions_list.append(evals[0][1])
    print(f"Best result for generation {n+1} is:", evals[0])
val = np.array([[0.20], [0.20], [0.20], [0.20]])
curve_names = ["Shortest", "Longest", "Random", "Half Random", "One Random"]
choosen_probability = np.array(choosen_probability)
for i in range(GENERATION SIZE):
    val = np.hstack((val, choosen probability[i].reshape(-1, 1)))
for i in range(5):
    plt.plot(range(GENERATION_SIZE + 1), val[i], label=curve_names[i])
plt.xlabel("Generation")
plt.ylabel("Probability")
plt.legend()
plt.show()
plt.plot(range(GENERATION_SIZE), solutions_list)
plt.xlabel("Generation")
plt.ylabel("Number of wins")
plt.show()
```



```
Adaptive (1,\lambda)-ES
current_solution = (0.20, 0.20, 0.20, 0.20, 0.20)
choosen_probability = list()
solutions list = list()
stats = [0, 0]
counter = 0
for n in range(GENERATION SIZE):
    print("Sigma for generation", n + 1, "is:", \sigma)
    offsprings = generate offsprings(current solution)
    offsprings.append(current solution)
    evals = [
        (offspring, fitness(evolved_strategy(offspring))) for offspring in
offsprings
    previous solution = evals[λ]
    for i in range(\lambda):
        if evals[i][1] > previous_solution[1]:
            counter += 1
    stats[1] += counter
    stats[0] += \lambda
    if (n + 1) \% 5 == 0:
        if stats[1] / stats[0] < 1 / 5:</pre>
            \sigma /= 1.1
        elif stats[1] / stats[0] > 1 / 5:
            \sigma *= 1.1
    evals.sort(key=lambda x: x[1], reverse=True)
    # pprint(evals)
    current_solution = evals[0][0]
    choosen_probability.append(current_solution)
    solutions list.append(evals[0][1])
    print(f"Best result for generation {n+1} is:", evals[0])
val = np.array([[0.20], [0.20], [0.20], [0.20], [0.20]])
curve_names = ["Shortest", "Longest", "Random", "Half Random", "One Random"]
choosen probability = np.array(choosen probability)
for i in range(GENERATION SIZE):
    val = np.hstack((val, choosen_probability[i].reshape(-1, 1)))
for i in range(5):
    plt.plot(range(GENERATION_SIZE + 1), val[i], label=curve_names[i])
```

```
plt.xlabel("Generation")
plt.ylabel("Probability")
plt.legend()
plt.show()
plt.plot(range(GENERATION_SIZE), solutions_list)
plt.xlabel("Generation")
plt.ylabel("Number of wins")
plt.show()
       1.0
      0.8
       0.6
 Probability
```

5

10

Generation

15

0.4

0.2

0.0

0

Shortest

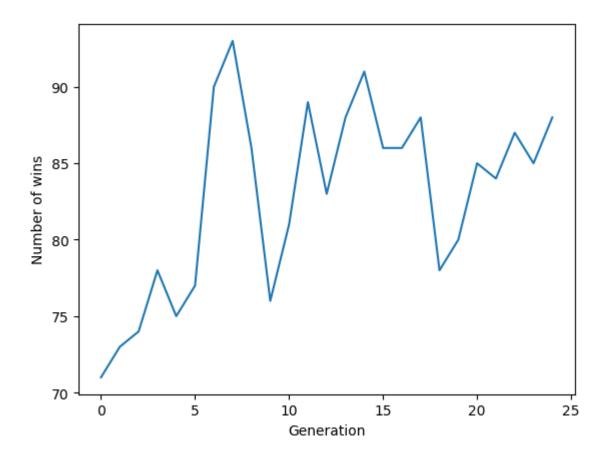
Longest Random

20

Half Random

One Random

25



- *Collaborations*: Worked with Angelo Iannielli s317887
- *Sources*: Functions "fitness", "state_info" and "evolved_strategy" have been inspired from Giovanni Squillero's repository on github nevertheless they have been modified and readapted.

Submittetd Reviews for LAB 2

R1:

USER: Donato Lanzillotti

Hi Donato, you've been randomly chosen on random.org for my review. I hope you find my comments helpful.

Your methodologies are similar to mine; it seems we're on the right way. I appreciate the idea of creating a new optimal function even though it wasn't required.

I noticed that you evaluate fitness by having an individual play against an opponent whose strategy changes with each move. While this makes results more robust, considering there's a proven optimal strategy for Nim, you could have had them play directly against the "optimal" strategy. This way, the algorithm learns to play against the best opponent and indirectly against all others.

Either way, it seems like you've done a good job. The code comments are helpful; perhaps you could have created a function that directly returns the move based on weights, avoiding if-else conditions in fitness. Anyway, the code is still clear.

Lastly, as a best practice, remember to always include labels in graphs for better readability.

Overall, great work! Feel free to comment on my code if you'd like.

R2:

USER: Michelangelo Caretto

Hi Michelangelo, I enjoyed your work and want to share some ideas. I'd like to congratulate with you for the README, it was very clear making it easy to understand the code. The game rules you designed are interesting and unconventional, good job. The variation of opponents and shifts when calculating fitness is a clever touch for more robust results. The range of weights is correct, but consider using real numbers from 0 onward to more easily evaluate the convergence of suboptimal strategies. Your implementation is good, but you could introduce a random choice based on the weights for strategy selection and maybe increment the number of games for each individual in order to avoid same fitness results for different individuals. I suggest adding intermediate outputs or a graph to visualize the evolution of the weights. Finally, label the graphs as a best practice for immediate understanding. I hope you find these suggestions useful. Good work!

Received Reviews

R1:

USER: Caretto Michelangelo s310178

Hello Nico, i'm going to review your work, hope you'll enjoy. I like a lot the way you wrote the code, because is so clean and readable and due to the graph i can easily understand how your "weight" structure works and which strategy is more strong in term of fitness. I would suggest you, when trying to create an agent playing a game to switch starting player every match too,otherwise your training will be only by one starting side. Talkink about the Es algortihm, you managed to find a solution in 25 Generation, due to the fact of "Optimal function" is not optimal, but in general we can not call an algortihm "ES" with this low number of Generation. Next time maybe with a little curiosity you could study the Nim problem more to make the optimal function stronger.... (less homework done and more curiosity) I would like to say that despite everything, I appreciated the work and the cleanliness. Thank you for your effort and attention to detail. Bye Bye Nico, Michelangelo.

R2:

USER: Samuele Vanini s318684

Overview The code is well-written and easy to follow. The strategies implemented seem reasonable and are easy to understand.

Areas for Improvement I have just a couple of considerations about what I feel is not completely right:

All the evolution strategies shown are in the realm of the single-state methods; from what I understood, we also had to implement evolution strategies with a population mu bigger than one. In "Adaptive $(1,\lambda)$ -ES" you are forcing the step size of sigma (dividing or multiplying it by 1.5); this is, in principle, wrong. We should not force a certain evolution using fixed parameters but let the algorithm find its way. If you want to balance exploration and exploitation, you can work on the selective pressure (in comma strategy, increase the number of lambda with respect to mu). Nim is an impartial game with a balanced state if and only if the nim-sum is 0, so you should alternate the player that does the first move during training. Take, for example, the match between 2 expert systems. The first player will always win if the game has an unbalanced initial state, even if the second player has the best strategy. This bias propagates in the training, introducing uncertainty during the fitness evaluation. Suggestions The number of generations, 25, is pretty low. The graph shows a fast convergence to 1 for the longest strategy. I would try to find new strategies to balance it. In "Adaptive $(1,\lambda)$ -ES" there is a sigma for all the probability; would have been good to see the effect of an adaptive sigma for each weight. It would have been interesting to see other evolution strategies like $(\mu + \lambda)$ or $(\mu/\rho + \lambda)$

R3:

USER: Donato Lanzillotti

PEER REVIEW Nim-Game POINT 1 The first point consisted of trying the different strategies and understand their performance. Running different games would have allowed you to realizing that the optimal strategy proposed was not totally correct (no 100% winning rate). Althought, changing it was not required.

POINT 2 About the ES, your idea was using the ES in order to find the most appropriate probabilities in choosing the shortest or the longest row. I noticed that you evaluate fitness by counting the number of winning games against a player that uses the optimal strategy. It is reasonable, but playing at the beginning just against a optimal player would not give you useful insight to move, since the winning rate would be always 0. This not the case since the optimal strategy proposed has not a winning rate equals to 100%. Thnaks to the graphs it is possible to appreciate the rate at which the probability goes to 0, it means choosing always the longest row.

Overall, it seems you have done a good job. The code is quite clear to understand but as a suggestions more commments will help into the comprehension.

LAB9

The aim of this lab is to Write a local-search algorithm (eg. an EA) able to solve the *Problem* instances 1, 2, 5, and 10 on a 1000-loci genomes, using a minimum number of fitness calls.

```
from random import choices
from random import random, randint, sample, uniform, seed
from copy import copy
from dataclasses import dataclass
import matplotlib.pyplot as plt

from tabulate import tabulate
import lab9_lib
```

BLACK-BOX PROBLEM with EA

- The goal of this implementation is to solve a problem with EA
- The goal is to maximize the fitness of an individual, how the fitness is evaluated is not known since it is a black-box problem
- An individual is has a genome of 1000 LOCI where a gene could be 0 or 1
- As additional information we know that an individual with all ones will have fitness equal 1, this information is additional and must not be used in the implementation since it can be considered cheating.
- We cannot use any method creating individuals, that gives an higher probability to have 1
 as a gene but the algorithm must favor the survival of individuals with more ones by itself.

```
OFFSPRING_SIZE = 80
POPULATION_SIZE = 40
MUTATION_PROBABILITY = .10
NUM_LOCI = 1000
PROBLEM = [1, 2, 5, 10]
seed(20)
```

Individual

- The individual is organized as a class where fitness is the fitness value of the individual and the genotype is a list of 1000 integers (0/1)
- The individual also has a function to perform the mutation and a functon to perform the xover
- The individual also show the roulette wheel selection that is a tecnique to choose a parent in the population

```
@dataclass
class Individual:
    fitness: tuple
    genotype: list[int]

# NOT USED
def tournament_selection(population, tournament_size):
```

```
# Randomly select individuals for the tournament
    tournament = sample(population, tournament_size)
    # Return the individual with the highest fitness
    return max(tournament, key=lambda ind: ind.fitness)
# Select a parent in a random way, giving more probability to individuals with
higher fitness
def roulette wheel selection(population):
    # Calculate the total fitness of the population (total numbers of the roulette
wheel)
    total fitness = sum(ind.fitness for ind in population)
    # Select a random value between 0 and the total fitness (select a random point
in the roulette wheel, like throwing the ball in a real roulette wheel)
    selection point = uniform(0, total fitness)
    # Go through the population and sum the fitness from 0, stop when the sum is
greater than the selection point
    # An individual with a higher fitness will have a higher probability that sum
will be greater than the selection point
    current sum = 0
    for ind in population:
        current_sum += ind.fitness
        if current_sum > selection_point:
            return ind
# Given the genome, select randomly a gene and switch is value
def mutate(ind: Individual) -> Individual:
    offspring = copy(ind)
    pos = randint(0, NUM LOCI - 1)
    if offspring.genotype[pos] == 1:
        offspring.genotype[pos] = 0
    else:
        offspring.genotype[pos] = 1
    offspring.fitness = None
    return offspring
# Give the genome of two individual, create a new offspring by removing a portion
of the genome from Ind1 and substituting it with the corresponding portion of Ind2
def n_cut_xover(ind1: Individual, ind2: Individual, n: int) -> Individual:
    # Generate n random cut points within the genotype range
    cut_points = sorted([randint(0, NUM_LOCI - 1) for _ in range(n)])
    # Initialize an empty offspring genotype
    offspring genotype = []
    # Alternate between parents for each segment
    for i in range(n + 1):
```

```
# Determine the start and end of the segment
start = cut_points[i - 1] if i > 0 else 0
end = cut_points[i] if i < n else NUM_LOCI

# Add the segment from the appropriate parent to the offspring genotype
if i % 2 == 0:
    offspring_genotype += ind1.genotype[start:end]
else:
    offspring_genotype += ind2.genotype[start:end]

# Create the offspring
offspring = Individual(fitness=None, genotype=offspring_genotype)
assert len(offspring.genotype) == NUM_LOCI
return offspring</pre>
```

Initial Population

- The initial population of size *POPULATON_SIZE* is created randomly with more probability to have a 0 then 1 in a locus
- For each individual in the initial population, we evaluate the fitness
- DISCLAIMER: creating an initial population with more zeros can be considered cheating because we know that these individuals will have a low value of fitness, by the way the intent of this choice is to appreciate how the algorithm increases the value of the fitness
- This choice also affects the number of fitness calls because the "plateau" will be reached with more generations
- Try the verision with uniform weights

EA-Algorithm

- Given the initial population, the algorithm select with a certain probability, to create a given number of offsprings using two different techniques (mutation,xover)
- The population is extended with the offsprings and than it's trimmed, letting survive only the best individuals

```
The algorithm is stopped when there are no improvements in the fitness (0.5\%) of
      variations in fitness in the last 600 generations) or if the value of the fitenss reachs 1
def evolutionary algorithm(fitness, population):
    generation = 0
    fitness history = []
    while True:
        offspring = []
        for _ in range(OFFSPRING_SIZE):
            if random() < MUTATION PROBABILITY:</pre>
                # mutation
                parent = roulette_wheel_selection(population)
                child = mutate(parent)
            else:
                # xover
                parent1 = roulette wheel selection(population)
                parent2 = roulette wheel selection(population)
                child = n_cut_xover(parent1, parent2, 6)
            offspring.append(child)
        for ind in offspring:
            ind.fitness = fitness(ind.genotype)
        population.extend(offspring) # add generated offspring to the population
        population.sort(key=lambda ind: ind.fitness, reverse=True) # sort the
population by fitness
        ind = population[0] # get the best individual
        population = population[:POPULATION SIZE] # keep only the best
POPULATION SIZE individuals
        current fitness = ind.fitness
        # Append the fitness to the history
        fitness history.append(current fitness)
        # Check termination condition
        if generation >= 600:
            recent_fitness_variation = max(fitness_history[-600:]) - min(
                fitness history[-600:]
            )
            if (
                recent_fitness_variation < 0.005 or current_fitness == 1</pre>
            ): # 0.5% variation or current_fitness is 1
                print(
                    f"Terminating at generation {generation} due to low fitness
variation or current_fitness reached 1."
```

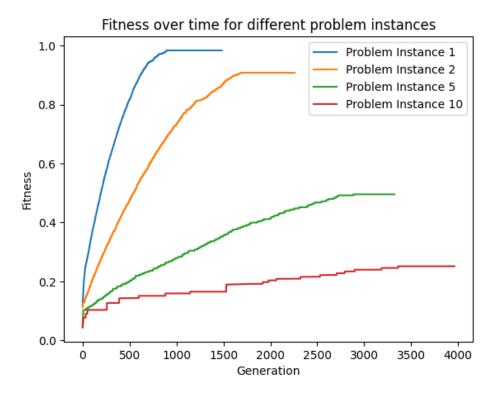
break

```
generation += 1
return fitness_history
```

Problem Results

• In this section the EA algorithm produces results for the different istances of the problem we have, showing results on a plot

```
problem instances = PROBLEM
fitness histories = []
call_history = []
for instance in problem instances:
    # Initialize your problem here with the current instance
    fitness = lab9 lib.make problem(instance)
    init population = generate init population(fitness)
    fitness_history = evolutionary_algorithm(fitness, init_population)
    # Append the fitness history of this run to the fitness_histories list
    fitness_histories.append(fitness_history)
    call history.append(fitness.calls)
# Plot the results
for i, fitness history in enumerate(fitness histories):
    plt.plot(fitness_history, label=f"Problem Instance {problem_instances[i]}")
plt.title("Fitness over time for different problem instances")
plt.xlabel("Generation")
plt.ylabel("Fitness")
plt.legend()
plt.show()
table data = []
for i, instance in enumerate(problem_instances):
    table_data.append([f"Problem Instance {instance}", f"{fitness_histories[i][-
1]:.2%}", call_history[i]])
table_headers = ["Problem Instance", "Final Fitness", "Fitness Calls"]
table = tabulate(table data, headers=table headers, tablefmt="pretty")
print(table)
```



+		+
Problem Instance 2 9 Problem Instance 5 4	98.40% 118680 90.80% 180840 9.54% 265800 5.13% 316920	

• *Collaborations*: No collaborations

Submittetd Reviews

R1:

USER: Lorenzo Calosso - s306041

Hi Lorenzo I am sending you my review, I hope you will appreciate it.

In general your work seems to me really well done and structured, I had no difficulties in reading your code thanks to the short texts you inserted before each section. I really appreciated the various comparisons you made using various techniques which led you to choose the best configuration.

Improvements You used the same number of individuals for both the offsprings and the initial population, this is not a mistake but usually there are more offsprings than population size. You can try changing these parameters to note any reduction in the number of fitness calls while maintaining the same performance. I recommend you to add a stop condition in case your fitness reaches 1 and also avoid entering a fixed number of generations, the stop criterion you used instead seems very correct to me. For comparison between the various configurations you used it would also be interesting to have graphs also to show the learning process of your algorithm Running my code the results obtained in the various instances of the problem were sometimes quite different due to the presence of random elements, since your code contains many random elements I suggest you reevaluate the choices you made by perhaps setting a fixed seed for the random functions.

R2:

USER: Michelangelo Caretto s310178

Hi Michelangelo I am writing you this review hoping you will enjoy it.

First of all I thank you for the readme you wrote which allowed me to understand your idea. Next time I suggest you to put markdown comments also before the various code sections so that it will be more understandable.

Your idea of using metrics other than fitness seems interesting and certainly from the results you have shown it allows you to reduce the number of fitness calls while still getting good results. I am not entirely sure that using other metrics besides fitness is "standard" procedure for an EA but after all this seems to work. The results obtained for the vanilla verison seem a bit low to me, I think the reason is that you imposed a fixed number of generations rather than letting the algorithm go. You could set an infinite loop that interrupts if the fitness value reaches 1 or if you don't notice any substantial improvement in the last x generations, this certainly increases the number of fitness calls but may also increase the result. Finally, I suggest you introduce some graphs to show the learning of the algorithm.

Received Reviews

R1:

USER: Lorenzo Calosso - s306041

Some considerations:

The code is well written and organized, the markdowns and the comments help to understand what you are doing The graph and the table at the end are a smart and nice way to present your results You obtained some good results on the first three instances with respect to the number of fitness calls done Some advice:

Try to combine also other techniques and see if the fitness improves; personally, I found out that, on this problem, techniques like Elitism, local-search mutation, inversion mutation or also the normal xover, combined together, give an improvement on the results. For what regard the final fitness of the instance 10, you could try to implement the self adaptive mutation rate instead of using a fixed one: in my case it has given a significant improvement

R2:

USER: Federico Buccellato s309075

Hello,

I have noticed that your solution faithfully follows the literature provided by the course. I find your code to be extremely well-organized and readable, and the comments significantly contribute to the understanding of the code. The evolutionary algorithm is structured effectively and appears correct. I particularly appreciated how you handle the possible termination in case of reaching the maximum fitness or constant fitness across generations.

Overall, your work is of high quality. The only suggestion I can give is to experiment with some different algorithms to assess how fitness behaves in alternative contexts.

Nevertheless, it is a job very well done!

LAB 10 - TicTacToe with RL

The aim of this lab is to solve a very simple game, using Reinforcement Learning Strategy

Tic-Tac-Toe with RL

- The game is played on a grid that's 3 squares by 3 squares.
- Players are "X" and "O".
- Players take turns putting their marks in empty squares.
- The first player to get 3 of her marks in a row (up, down, across, or diagonally) is the winner.
- When all 9 squares are full, the game is over. If no player has 3 marks in a row, the game ends in a tie.

Environment

- The grid is composed by a magic square [2, 7, 6, 9, 5, 1, 4, 3, 8]
- The idea of the magic square is that each row/column/diagonals sum up to 15

State

• The state is the set of positions taken by player "X" and player "O"

Action

• The action is the choice of a number inside the magic square

Reward

• The reward given to the agent is: 1 if the player wins the game, -1 if it loses and 0.5 if the game is a tie

Agent

• The agent is a player that uses the Q-Learning logic

```
import random
from collections import namedtuple
from itertools import combinations
from random import seed
import matplotlib.pyplot as plt
from tqdm import tqdm

Position = namedtuple("Position", ["x", "o"])
seed(40)
```

Game Class

- play_game(): create the logic of the game where "X" and "0" players take turns
- win(): checks if a players has completed a row/column/diagonal (sum to 15)
- board_full(): checks if all the positions have been setted in the board (the game is tie)
- print_board() && print_board_info(): pretty print of the game board

```
class TicTacToe:
    def __init__(self, playerX, playerO, human_game=False):
        self.board = [2, 7, 6, 9, 5, 1, 4, 3, 8]
        self.current_board = Position(set(), set())
        self.playerX, self.player0 = playerX, player0
        self.playerX turn = random.choice([True, False]) #randomLy choose who goes
first
        self.winner = None
        self.human game = human game
    def play game(self):
        self.playerX.start_game("X")
        self.playerO.start game("0")
        while True:
            player, char, other_player = (
                (self.playerX, "X", self.player0)
                if self.playerX turn
                else (self.player0, "0", self.playerX)
            )
            if self.human_game:
                print(f"Player {char} move")
                self.print board info()
            move = player.move(self.current board)
            moves = self.current board.x if self.playerX turn else
self.current_board.o
            moves.add(move)
            if self.human game:
                self.print board()
            if self.win(moves):
                player.reward(1, self.current_board)
                other player.reward(-1, self.current board)
                self.winner = char
                break
            if self.board_full(): # tie game
                player.reward(0.5, self.current board)
                other_player.reward(0.5, self.current_board)
                self.winner = None
                break
            other player.reward(∅, self.current board)
            self.playerX_turn = not self.playerX_turn
    def win(self, state):
        return any(sum(c) == 15 for c in combinations(state, 3))
```

```
def board full(self):
   player = self.playerX if self.playerX_turn else self.player0
   return player.available moves(self.current board) == set()
def print board(self):
    for r in range(3):
       print("----")
       for c in range(3):
           i = r * 3 + c
           char = " "
           if self.board[i] in self.current_board.x:
               char = "X"
           elif self.board[i] in self.current board.o:
               char = "0"
           print(f" | {char}", end=" ")
       print("|")
   print("----")
def print_board_info(self):
    for r in range(3):
       print("----")
       for c in range(3):
           i = r * 3 + c
           print(f" | {self.board[i]}", end=" ")
       print("|")
   print("----")
```

Player Class

- The player class is a generic class with some methods to implement the choosing action logic, available moves and also a reward function if needed
- Random Player class overrides the player class implementing a player that takes action randomly
- Q-Learining Player class overrides the player implementing a RL agent

```
class Player(object):
    def __init__(self):
        self.name = "human"

def start_game(self, char):
    print("\nNew game!")

def move(self, current_board):

    move = int(input("Your move? "))
    if move not in self.available_moves(current_board):
        print("Illegal move.")
        move = self.move(current_board)
```

```
return move
    def reward(self, value, current_board):
        print("{} rewarded: {}".format(self.name, value))
    def available moves(self, current board):
        available = set(range(1, 9 + 1)) - current_board.x - current_board.o
        return available
class RandomPlayer(Player):
    def init (self):
        self.name = "random"
    def reward(self, value, board):
        pass
    def start_game(self, char):
    def move(self, current board):
        available = self.available moves(current board)
        return random.choice(list(available))
class QLearningPlayer(Player):
    def __init__(self, epsilon=0.2, alpha=0.2, gamma=0.9):
        self.name = "Qlearner"
        self.q = {} # (state, action) keys: Q values
        self.epsilon = epsilon # e-greedy chance of random exploration
        self.alpha = alpha # Learning rate
        self.gamma = gamma # discount factor for future rewards
    def start game(self, char):
        self.last_state = (set(), set())
        self.last_action = None
    def getQ(self, state, action):
        # encourage exploration; "optimistic" 1.0 initial values
        if self.q.get((state, action)) is None:
            self.q[(state, action)] = 1.0
        return self.q.get((state, action))
    def move(self, current_board):
        self.last state = (
            tuple(current_board.x),
            tuple(current_board.o),
        ) # Convert Position to tuple
        possible actions = list(self.available moves(self.last state))
        if random.random() < self.epsilon:</pre>
```

```
self.last_action = random.choice(list(possible_actions))
            return self.last action
        qs = [self.getQ(self.last_state, a) for a in possible_actions]
        maxQ = max(qs)
        if qs.count(maxQ) > 1:
            # more than 1 best option; choose among them randomly
            best options = [i for i in range(len(possible actions)) if qs[i] ==
maxQ]
            i = random.choice(best_options)
        else:
            i = qs.index(maxQ)
        self.last_action = possible_actions[i]
        return possible actions[i]
    def reward(self, value, current_board):
        new state = (tuple(current board[0]), tuple(current board[1]))
        if self.last action:
            self.learn(
                self.last state,
                self.last_action,
                value,
                new state
            )
    def learn(self, state, action, reward, result state):
        prev = self.getQ(state, action)
        if self.available_moves(result_state) == set():
            self.q[(state, action)] = prev
            maxqnew = max([self.getQ(result state, a) for a in
self.available moves(result state)])
            self.q[(state, action)] = (1-self.alpha)*prev + self.alpha * (
                (reward + self.gamma * maxqnew)
            )
    def available_moves(self, current_board):
        available = set(range(1, 9 + 1)) - set(current_board[0]) -
set(current board[1])
        return available
Train
      Train the RL agent against a player
def trained_agent(p1, agent, num_games=200000):
    for _ in tqdm(range(0, num_games)):
        t = TicTacToe(p1, agent)
```

```
t.play_game()
return agent
```

Test

```
Test the trained agent against a player
agent = trained_agent(RandomPlayer(), QLearningPlayer())
p1 = RandomPlayer()
agent.epsilon = 0 # remove randomness from the trained agent
num_X = 0
num O = 0
num_ties = 0
for _ in range(100):
    t = TicTacToe(p1, agent)
    t.play_game()
    if t.winner == "X":
        num X += 1
    elif t.winner == "0":
        num 0 += 1
    else:
        num_ties += 1
print("X wins: " + str(num_X))
print("0 wins: " + str(num_0))
print("Ties: " + str(num_ties))
```

Learning process

- The agent is trained for different number of games values
- Higher the number of training games, higher the performance
- Run this part is time consuming (20min on my laptop)
 num_train_games_values = list(range(1, 200001, 1000))

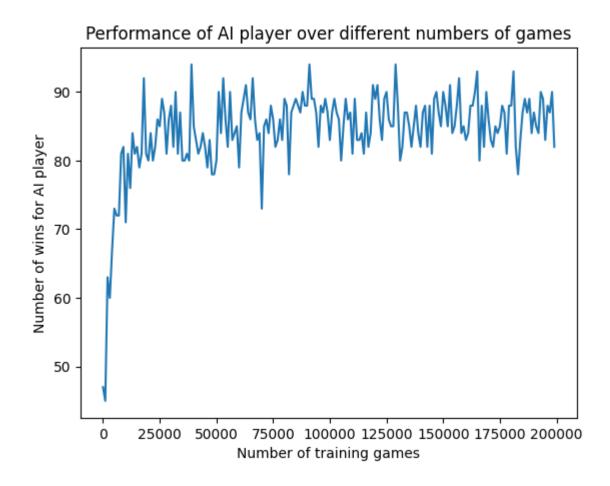
if t.winner == "0":

```
results = []
for num in tqdm(num_train_games_values):
    agent = trained_agent(RandomPlayer(), QLearningPlayer(), num)
    p1 = RandomPlayer()
    num_win = 0

for _ in range(100):
    t = TicTacToe(p1, agent)
    t.play_game()
```

```
num_win += 1
results.append(num_win)
```

```
plt.plot(num_train_games_values, results)
plt.xlabel('Number of training games')
plt.ylabel('Number of wins for AI player')
plt.title('Performance of AI player over different numbers of games')
plt.show()
```



Plays against Al

• Try to defeat the AI playing a game

```
human = Player()
t = TicTacToe(human, agent, human_game=True)
print("TIC TAC TOE")
t.print_board_info()
print("-----")

t.play_game()
print("Winner is: " + str(t.winner))
t.print_board()
```

• *Collaborations*: No collaborations

Submittetd Reviews

R1:

USER: Federico Buccellato s309075

Hi Federico here is my review for your work, I hope you will appreciate it.

First of all, your work seems well done to me and your extension of what we saw in class using Q-learning seems correct. I have some pointers for you to improve your work and make it better understandable. I would suggest you to divide your code into classes by perhaps creating a "game" class and a "player" class this allows for better organization and also better reading of the code. In the training phase you could add an additional "epsilon" parameter to encourage agent exploration by choosing a random action (greedy approach) The results look good to me, try to increase the number of matches to update the Q-Table you might have better results. To make the agent more robust, you could do training with different types of players, to be varied randomly during the various iterations just for this reason, creating a player class to be extended could be a good idea.

In conclusion your work seems well done, I only suggest you to improve a bit the organization of your code. Good work for the next projects!

R2

USER: Lorenzo Calosso - s306041

Hi Lorenzo here is my review for your work, I hope you will appreciate it.

I really congratulate you as your code is really easy to read and understand due to the use of the classes you created. The implementation of Q-Learning seems to me to be correct from a theoretical and also implementation point of view. I don't have many comments to make to you as the code is well written and very similar to my implementation and also the results obtained seem promising. To further improve your work you could create a "player" class to be extended with different types of players, "random", "minmax", "RL-agent" or other types of players with other strategies, so as to randomly vary the opponent during training making the final agent more robust. It would also be interesting to see the learning process of your agent as the number of iterations of training changes, so you can figure out the right tradeoff between the number of training iterations and the number of wins.

In conclusion, I again congratulate you on your work.

Received Reviews

R1

USER: Paul Raphael

Hello.

Your work is great and very well explained and displayed, the only thing lacking in my opinion is that you don't change the parameters alpha gamma and epsilon during training (maybe you did it on your own or I missed it) It could be interesting. Aside from that I couldn't find any issues good job and good luck for the exam!

R2

USER: Angelo Iannielli

Hello Nicolò,

I've conducted a review of your code and wanted to share my observations.

My 2 cents: Your code is well-structured and organized. I particularly appreciate the clear division into classes, managing both the game logic and player behaviors. This choice significantly enhances the readability and maintainability of the code.

The option to test the trained player in a match against a human player is very interesting. This feature makes your code interactive, providing an immediate test of the achieved results during training.

The integration of graphs at the end of the lab provides a comprehensive view of the learning process. This is a positive touch that offers a visual overview of the agent's performance throughout the training matches.

Recommended Adjustments: The start_game() function might be considered redundant as it merely prints a static string. You may want to evaluate whether it's essential to keep this function. The print statements during training could be shortened to enhance file readability. Consider reducing the length of the prints while retaining essential information. Future Developments: It could be interesting to explore varying the epsilon variable as the algorithm learns to play. This might help reduce randomness in the agent's moves and reduce exploration during the learning process. Additionally, it would be compelling to train the agent against players using different strategies. This could provide insights into how well the agent adapts to diverse playing styles. Overall, you've done an excellent job. Keep it up and consider the suggestions to further enhance your code

Quixo Project

ExtendedGame

Overview

The ExtendedGame class extends the functionality of a basic game represented by the Game class. It introduces additional functions that do not change the logic of the game but are useful to implement a player such as MinMaxPlayer.

Class Overview

ExtendedGame Methods:

- **possible_moves(self, playerId: int) -> tuple[tuple[int, int], Move]:** Returns a tuple of possible moves for a given player in the current state of the game
- create_new_state(self, from_pos: tuple[int, int], slide: Move, player_id: int) ->
 "ExtendedGame": Creates a new game state performing a move
- **_switch_player()** switch the current player after a move

Players

Overview

- RandomPlayer: A player that makes random moves.
- HumanPlayer: A player that allows a human to interactively make moves.
- MinMaxPlayer: An AI player using the Minimax algorithm with Alpha-Beta Pruning to make strategic moves.

Player Classes

- RandomPlayer This class represents a player that randomly selects moves on the game board. It is implemented with the make_move method, where it generates random positions and a random move direction.
- HumanPlayer This class represents a player that allows a human to interactively make moves. The make_move method prompts the user to input the position to move from and the direction to move.
- MinMaxPlayer This class represents an AI player using the Minimax algorithm with Alpha-Beta Pruning to make optimal moves. The make_move method implements the Minimax algorithm to evaluate possible moves and choose the best one. The evaluate method assigns scores to different game states, and the minmax method recursively explores possible moves while considering alpha-beta pruning for optimization.

MinMaxPlayer Configuration

The MinMaxPlayer class takes three parameters during instantiation:

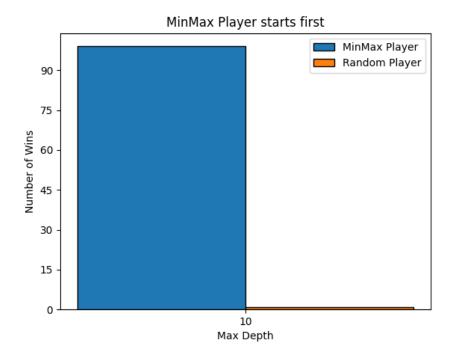
- game: The game object (an instance of ExtendedGame) on which the player will make moves.
- max_depth: The maximum depth to explore in the Minimax algorithm.

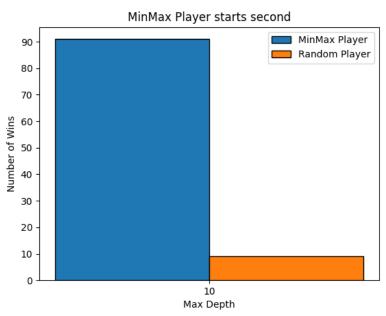
The agent is proposed with a **max_depth = 10** even if tests show that the agent as good results also with other lower even numbers.

Useful functions and Testing

In order to test the performance of the game some useful functions are provided.

- test_agent(num_games) to simply test the Minmax player against a RandomPlayer 100 times
- **test_agent_depths(num_games, max_depths)** to test the MinMaxPlayer performance against a RandomPlayer, playing 100 times as first player (simbol 0) and 100 times as second player (simbol 1)
- **plot_results(results, filename, title)** to print some histograms about results obtained with the previous function.
- **play_against_ai()** to play a real time game against the MinMaxPlayer.





```
class ExtendedGame(Game):
    def __init__(self):
        super().__init__()
    def possible moves(self, playerId: int) -> tuple[tuple[int, int], Move]:
        """Return a tuple of possible moves for a given player in a given state of
the game"""
        # Define the edges of the game grid
        perimeter = [0, 4]
        # Initialize an empty list to store possible moves
        possible moves = []
        # Get the current game board
        board = self.get board()
        # Iterate over the edges of the game grid
        for index in perimeter:
            # Iterate over the columns of the game grid
            for col in range(5):
                # If the current cell belongs to the current player or is empty
                if board[col][index] in {playerId, -1}:
                    # If we are not on the first column, we can move up
                    if col != 0:
                        possible moves.append(((index, col), Move.TOP))
                    # If we are not on the last column, we can move down
                        possible_moves.append(((index, col), Move.BOTTOM))
                    # If we are not on the first row, we can move left
                    if index != 0:
                        possible moves.append(((index, col), Move.LEFT))
                    # If we are not on the last row, we can move right
                    if index != 4:
                        possible_moves.append(((index, col), Move.RIGHT))
            # Iterate over the rows of the game grid
            for row in range(5):
                # If the current cell belongs to the current player or is empty
                if board[index][row] in {playerId, -1}:
                    # If we are not on the first column, we can move up
                    if index != 0:
                        possible moves.append(((row, index), Move.TOP))
                    # If we are not on the last column, we can move down
                    if index != 4:
                        possible moves.append(((row, index), Move.BOTTOM))
                    # If we are not on the first row, we can move left
                    if row != 0:
                        possible_moves.append(((row, index), Move.LEFT))
                    # If we are not on the last row, we can move right
                    if row != 4:
                        possible moves.append(((row, index), Move.RIGHT))
```

```
# Return the possible moves as a tuple
        return tuple(possible_moves)
    def create new state(
        self, from pos: tuple[int, int], slide: Move, player id: int
    ) -> "ExtendedGame":
        """Return a new game state after applying a move"""
        # Swap the position coordinates
        from pos = (from pos[1], from pos[0])
        # Create a new instance of the ExtendedGame
        new_game = ExtendedGame()
        new_game.current_player_idx = player_id
        # Copy the current game board to the new game
        new game. board = deepcopy(self. board)
        new_game._take(from_pos, player id)
        new game. slide(from pos, slide)
        new_game._switch_player()
        # Return the new game state
        return new game
    def _switch_player(self):
        self.current_player_idx = 1 - self.current_player_idx
class RandomPlayer(Player):
    def __init__(self) -> None:
        super().__init__()
        self.name = "RandomPlayer"
   def make_move(self, game: "ExtendedGame") -> tuple[tuple[int, int], Move]:
        from pos = (random.randint(0, 4), random.randint(0, 4))
        move = random.choice([Move.TOP, Move.BOTTOM, Move.LEFT, Move.RIGHT])
        return from pos, move
class HumanPlayer(Player):
    def __init__(self) -> None:
        super(). init ()
        self.name = "HumanPlayer"
    def make move(self, game: "ExtendedGame") -> tuple[tuple[int, int], Move]:
        # Get the current player
        player = game.get current player()
        # Get the list of possible moves
        possible_moves = game.possible_moves(player)
```

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print("BOARD:")
        game.print()
        # Print the list of possible moves
        print("Possible moves:")
        for move in possible_moves:
            print(f"From position {move[0]} move {move[1]}")
        # Ask the user for their move
        from pos = tuple(
            map(int, input("Enter the position to move from (row, col):
").split(","))
        move = Move[
            input("Enter the direction to move (TOP, BOTTOM, LEFT, RIGHT):
").upper()
        return from_pos, move
class MinMaxPlayer(Player):
    def __init__(self, game: "ExtendedGame", max_depth) -> None:
        super().__init__()
        self.name = "MinMaxPlayer"
        self.game = game
        self.max_depth = max_depth
        self.infinity = float("inf")
   def evaluate(self, game: "ExtendedGame") -> int:
        player = (
            1 - game.get_current_player()
        ) # restore the player of the prevoius state since create_new_state()
switch it.
        score = 0
        board = game.get_board()
        # Check rows
        for row in board:
            score += self.evaluate_line(row, player)
        # Check columns
        for col in board.T:
            score += self.evaluate_line(col, player)
        # Check main diagonal
        main diag = np.diagonal(board)
        score += self.evaluate_line(main_diag, player)
        # Check secondary diagonal
        secondary_diag = np.diagonal(np.fliplr(board))
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score += self.evaluate_line(secondary_diag, player)
        return score
    @staticmethod
    def evaluate_line(line: list[int], player_id: int) -> int:
        line score = 0
        # Count occurrences of player's symbol and opponent's symbol
        player_count = np.sum(line == player_id)
        opponent count = np.sum(line == 1 - player id)
        # Assign scores based on counts
        if player count > 0:
            line_score += 10**player_count
        if opponent_count > 0:
            line_score -= 10**opponent_count
        return line_score
    def minmax(
        self,
        game: "ExtendedGame",
        depth: int,
        alpha: float,
        beta: float,
        isMaximizingPlayer: bool,
    ) -> tuple[int, float, float]:
        # Base case: if we have reached the maximum depth or the game is over,
        # return the evaluation of the game state
        if depth == 0 or game.check winner() != -1:
            return self.evaluate(game), alpha, beta
        # Decrease the depth
        depth -= 1
        player = game.get_current_player()
        # If we are the maximizing player
        if isMaximizingPlayer:
            # Initialize the maximum evaluation to negative infinity
            bestVal = -self.infinity
            # Iterate over all possible moves
            for move in game.possible moves(player):
                # Create a new game state by making the move
                new_state = game.create_new_state(move[0], move[1], player)
                # Call minmax recursively on the new state
                value, alpha, beta = self.minmax(new state, depth, alpha, beta,
False)
```

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# Update the maximum evaluation
                bestVal = max(bestVal, value)
                # Update alpha
                alpha = max(alpha, value)
                # If beta is less than or equal to alpha, break the loop (alpha-
beta pruning)
                if alpha >= beta:
                    break
            # The result is the maximum evaluation, alpha and beta
            result = bestVal, alpha, beta
        # If we are the minimizing player
        else:
            # Initialize the minimum evaluation to positive infinity
            bestVal = self.infinity
            # Iterate over all possible moves
            for move in game.possible moves(player):
                # Create a new game state by making the move
                new state = game.create new state(move[0], move[1], player)
                # Call minmax recursively on the new state
                value, alpha, beta = self.minmax(new_state, depth, alpha, beta,
True)
                # Update the minimum evaluation
                bestVal = min(bestVal, value)
                # Update beta
                beta = min(beta, value)
                # If beta is less than or equal to alpha, break the loop (alpha-
beta pruning)
                if alpha >= beta:
                    break
            # The result is the minimum evaluation, alpha and beta
            result = bestVal, alpha, beta
        return result
    def make_move(self, game: "ExtendedGame") -> tuple[tuple[int, int], Move]:
        # Initialize the best move to None and the best evaluation to negative
infinity
        bestMove = None
        bestVal = -self.infinity
        # Get the current player, it will be the index of the MinmaxPlayer
        player = self.game.get_current_player()
        # Get the list of possible moves for MinmaxPlayer
        possible_moves = list(game.possible_moves(player))
        # Iterate over all possible moves
        for move in possible moves:
            # Create a new game state by making the move
            new_state = self.game.create_new_state(move[0], move[1], False)
```

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# Early return if a move is a winning move for MinmaxPlayer
            if new_state.check_winner() == player:
                bestMove = move
                break
            # Call the Minimax function on the new state to get the evaluation of
the state
            value = self.minmax(
                new_state, self.max_depth, -self.infinity, self.infinity, False
            [0]
            # If the evaluation of the state is greater than the best evaluation,
update the best evaluation and the best move
            if value > bestVal:
                bestVal = value
                bestMove = move
        return bestMove
def test agent(num games: int) -> None:
    count 0 = 0
    count 1 = 0
    for _ in range(num_games):
        game = ExtendedGame()
        player1 = MinMaxPlayer(game, 10)
        player2 = RandomPlayer()
        winner = game.play(player1, player2)
        if winner == 0:
            count 0 += 1
        else:
            count 1 += 1
        print(f"{player1.name} win {count 0} matches")
        print(f"{player2.name} win {count_1} matches")
def test_agent_depths(num_games: int, max_depths: list[int]) -> None:
    results_when_first = []
    results_when_second = []
    for max_depth in tqdm(max_depths, desc="Testing depths"):
        wins when first = 0
        losses_when_first = 0
        wins when second = 0
        losses_when_second = 0
```

```
for in tqdm(range(num games), desc="Testing games"):
            # MinMaxPlayer starts first
            game = ExtendedGame()
            player1 = MinMaxPlayer(game, max_depth)
            player2 = RandomPlayer()
            winner = game.play(player1, player2)
            if winner == 0:
                wins when first += 1
                losses_when_first += 1
            # MinMaxPlayer starts second
            game = ExtendedGame()
            player1 = RandomPlayer()
            player2 = MinMaxPlayer(game, max depth)
            winner = game.play(player1, player2)
            if winner == 1:
                wins_when_second += 1
            else:
                losses_when_second += 1
        results when first.append((max depth, wins when first, losses when first))
        results_when_second.append((max_depth, wins_when_second,
losses when second))
    return results_when_first, results_when_second
def plot_results(
    results: list[tuple[int, int, int]], filename: str, title: str
) -> None:
    depths, wins_0, wins_1 = zip(*results)
    width = 0.35 # the width of the bars
    fig, ax = plt.subplots()
    ax.bar(
        [d - width / 2 for d in depths],
        wins_0,
        width,
        label="MinMax Player",
        edgecolor="black",
    ax.bar(
        [d + width / 2 for d in depths],
        wins_1,
        width,
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label="Random Player",
        edgecolor="black",
    )
    ax.set_title(title)
    ax.set_xlabel("Max Depth")
    ax.set_ylabel("Number of Wins")
    ax.set_xticks(depths)
    ax.yaxis.set_major_locator(
        MaxNLocator(integer=True)
    ) # Set y-axis to display only integers
    ax.legend()
    plt.savefig(filename)
    plt.show()
def play_against_ai() -> None:
   game = ExtendedGame()
    player1 = MinMaxPlayer(game, 10)
    player2 = HumanPlayer()
   winner = game.play(player1, player2)
    if winner == 0:
        print(f"{player1.name} wins!")
    else:
        print(f"{player2.name} wins!")
if __name__ == "__main__":
   test_agent(100)
    # results_first, results_second = test_agent_depths(
         100, [10]
    # )
    # plot_results(results_first, "results_first.png", "MinMax Player starts
    # plot_results(results_second, "results_second.png", "MinMax Player starts
second")
   # play_against_ai()
```